## Scaling Definitions

Proposed Scaling Definitions (May 2021 update)

## 1) Consensus (Old)

Define
$T_{R}=3000$ bytes ; Reference Transaction weight. Note: $T_{R}$ must be greater than $T_{2} . T_{2}$ equals the weight in bytes of a 2 input and 2 output transaction.
$Z_{M}=300000$ bytes ; Minimum penalty free zone.
$M_{B}=$ Block weight in bytes.
$\mathrm{M}_{\mathrm{L}}=$ the median over the last 100000 blocks of max((min $\left.\left(M_{B}, 1.4 M_{L}\right), Z_{M}\right)$; recursive calculation for $M_{L}$ with $M_{L}$ starting at $M_{\llcorner }$of previous 100001 block (currently $=Z_{M}$ ); Long Term Median
$Z_{M}$; Penalty free zone.
$M_{S}=$ the median over the last 100 blocks of $\max \left(M_{B}, Z_{M}\right)$; Effective short term median.
$M_{N}=\min \left(M_{S}, 50 M_{L}\right) ;$ Median for Penalty calculation.
$\mathrm{R}_{\text {Base }}=$ Block Reward.
$0<\mathrm{M}_{\mathrm{B}} \leq 2 \mathrm{M}_{\mathrm{N}}$; Requirement for valid block.
$B=M_{B} / M_{N}-1$ where $-1<B \leq 1$
$P_{B}=R_{\text {Base }} B^{2}$ for $B>0$; Monero applies a penalty $P_{B}$, to increase the block weight by $B$.
$P_{B}=0$ for $B \leq 0$
$\mathrm{dP}_{\mathrm{B}} / \mathrm{dB}=2 \mathrm{R}_{\text {Base }} \mathrm{B}$

1) Consensus (New)

Define
$T_{R}=3000$ bytes ; Reference Transaction weight. Note: $T_{R}$ must be greater than $T_{2} . T_{2}$ equals the weight in bytes of a 2 input and 2 output transaction.
$Z_{M}=300000$ bytes ; Minimum penalty free zone.
$M_{B}=$ Block weight in bytes .
$M_{L}=$ The median over the last 100000 blocks of max((min ( $\mathrm{M}_{\mathrm{B}}, 2 \mathrm{M}_{\mathrm{L}}$ ), $\mathrm{Z}_{\mathrm{M}}, \mathrm{M}_{\mathrm{L}} / 2$ ) ; recursive calculation for $\mathrm{M}_{\mathrm{L}}$ with $\mathrm{M}_{\mathrm{L}}$ starting at $\mathrm{M}_{\mathrm{L}}$ of previous 100001 block (currently $=\mathrm{Z}_{\mathrm{M}}$ ); Long term median
$M_{L}$; Penalty free zone. This is now dynamic.
$M_{S}=$ the median over the last 100 blocks of $\max \left(M_{B}, M_{L}\right)$; Effective short term median.
$M_{N}=\min \left(M_{S}, 50 M_{L}\right) ;$ Median for Penalty calculation.
$\mathrm{R}_{\text {Base }}=$ Block Reward.
$0<\mathrm{M}_{\mathrm{B}} \leq 2 \mathrm{M}_{\mathrm{N}}$; Requirement for valid block.
$B=M_{B} / M_{N}-1$ where $-1<B \leq 1$
$P_{B}=R_{\text {Base }} B^{2}$ for $B>0$; Monero applies a penalty $P_{B}$, to increase the block weight by $B$.
$P_{B}=0$ for $B \leq 0$
$d P_{B} / d B=2 R_{\text {Base }} B$

## 2a) Minimum Fee For Node Relay (Old)

We add a, penalty attracting, transaction $T$ with a size of $T$ to a block of weight $M_{B}$

Define
$B_{T}=T_{T} / M_{N}$
$P_{B T}=R_{\text {Base }}\left(B+B_{T}\right)^{2}=R_{\text {base }}\left(B^{2}+2 B B_{T}+B_{T}{ }^{2}\right)$; The new penalty, where $B+B_{T}>0$
$P_{T}=P_{B T}-P_{B}=R_{\text {Base }}\left(2 B B_{T}+B_{T}{ }^{2}\right)$; Increase in penalty from adding transaction $T$
$F_{T}=R_{\text {Base }}\left(2 B B_{T}+B_{T}{ }^{2}\right)$; The additional fee required to overcome the increase in penalty $P_{T}$

For the case $B=0$ this reduces to $F_{T}=R_{\text {Base }} B_{T}{ }^{2}$
$M_{F}=\min \left(M_{N}, M_{L}\right) ;$ Median for minimum fee calculation

To calculate the minimum fee we consider a transaction of weight $T_{R}$ at the start of the penalty, $B=0$ with $M_{N}=Z_{M}$. $20 \%$ of the fee required to pay the penalty incurred is the minimum fee.
$B_{R}=T_{R} / Z_{M}$
$F_{R}=R_{B_{B a s e}} B_{R}{ }^{2}$; Fee required to pay the penalty incurred
$f_{R}=R_{\text {Base }} B_{R} / M_{F}$; Fee required to pay the penalty incurred fee per byte for at $M_{F}=Z_{M}$ scaled with $M_{F}$
$f_{I}=0.2 f_{R}$; Minimum fee per byte

## Examples:

$T_{R}=3000$ bytes, $R_{\text {Base }}=1.2$ XMR, $\mathrm{Z}_{\mathrm{M}}=300000$ bytes
$\mathrm{M}_{\mathrm{N}}=300000$ bytes, $\mathrm{M}_{\mathrm{L}}=300000$ bytes
$f_{l}=0.2 * R_{\text {base }} B_{R} / M_{F}=8.00 \mathrm{nXMR} /$ byte ,
$\mathrm{M}_{\mathrm{N}}=1425000$ bytes, $\mathrm{M}_{\mathrm{L}}=1425000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.2 * \mathrm{R}_{\text {base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{F}}=1.68 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{N}}=1500000$ bytes, $\mathrm{M}_{\mathrm{L}}=1500000$ bytes
$\mathrm{f}_{\mathrm{l}}=0.2 * \mathrm{R}_{\text {base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{F}}=1.60 \mathrm{nXMR} /$ byte
$T_{R}=3000$ bytes, $R_{\text {Base }}=0.6$ XMR, $Z_{M}=300000$ bytes
$\mathrm{M}_{\mathrm{N}}=300000$ bytes, $\mathrm{M}_{\mathrm{L}}=300000$ bytes
$\mathrm{f}_{\mathrm{l}}=0.2 * \mathrm{R}_{\text {base }} B_{\mathrm{R}} / \mathrm{M}_{\mathrm{F}}=4.00 \mathrm{nXMR} /$ byte ,
$M_{N}=1425000$ bytes, $M_{L}=1425000$ bytes
$f_{l}=0.2 * R_{\text {base }} B_{R} / M_{F}=0.84 \mathrm{nXMR} /$ byte
$M_{N}=1500000$ bytes, $M_{L}=1500000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.2 * \mathrm{R}_{\text {base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{F}}=0.80 \mathrm{nXMR} /$ byte

## 2a) Minimum Fee For Node Relay (New)

$T_{T}$ We add a, penalty attracting, transaction $T$ with a size of $T_{T}$ to a block of weight $M_{B}$

Define
$B_{T}=T_{T} / M_{N}$
$P_{B T}=R_{\text {Base }}\left(B+B_{T}\right)^{2}=R_{\text {base }}\left(B^{2}+2 B B_{T}+B_{T}^{2}\right)$; The new penalty, where $B+B_{T}>0$
$P_{T}=P_{B T}-P_{B}=R_{\text {Base }}\left(2 B B_{T}+B_{T}^{2}\right)$; Increase in penalty from adding transaction $T$
$F_{T}=R_{\text {Base }}\left(2 B B_{T}+B_{T}{ }^{2}\right)$; The additional fee required to overcome the increase in penalty $P_{T}$

For the case $B=0$ this reduces to $F_{T}=R_{\text {Base }} B_{T}{ }^{2}$
$M_{F}=\min \left(M_{N}, M_{L}\right)\left(=M_{L}\right.$ if the proposed consensus change is implemented) ; Median for minimum fee calculation

To calculate the minimum fee we consider a transaction of weight $T_{R}$ at the start of the penalty, $B=0$ with $M_{N}=M_{F}$ $95 \%$ of the fee required to pay the penalty incurred is the minimum fee.
$B_{R L}=T_{R} / M_{F}$; Note change $M_{F}$ instead of $Z_{M}$
$F_{R}=R_{\text {Base }} B_{R L}{ }^{2}$; Fee required to pay the penalty incurred
$f_{R}=R_{\text {Base }} B_{R L} / M_{F}$; Fee required to pay the penalty incurred per byte for a given $M_{F}$
$f_{l}=0.95 f_{R}$; Minimum fee per byte

## Examples:

$T_{R}=3000$ bytes, $R_{\text {Base }}=1.2$ XMR, $\mathrm{Z}_{\mathrm{M}}=300000$ bytes
$M_{N}=300000$ bytes, $M_{L}=300000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95 * \mathrm{R}_{\text {base }} B_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=38.0 \mathrm{nXMR} /$ byte
$M_{N}=1425000$ bytes, $M_{L}=1425000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95 *_{\text {base }} \mathrm{B}_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=1.68 \mathrm{nXMR} /$ byte
$M_{N}=1500000$ bytes, $M_{L}=1500000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95$ * $_{\text {base }} B_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=1.52 \mathrm{nXMR} /$ byte
$T_{R}=3000$ bytes, $R_{\text {Base }}=0.6 \mathrm{XMR}, \mathrm{Z}_{\mathrm{M}}=300000$ bytes
$\mathrm{M}_{\mathrm{N}}=300000$ bytes, $\mathrm{M}_{\mathrm{L}}=300000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95{ }^{*} \mathrm{R}_{\text {base }} \mathrm{B}_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=19.0 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{N}}=1425000$ bytes, $\mathrm{M}_{\mathrm{L}}=1425000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95 *_{\text {base }} \mathrm{B}_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=0.84 \mathrm{nXMR} /$ byte
$M_{N}=1500000$ bytes, $M_{L}=1500000$ bytes
$\mathrm{f}_{\mathrm{I}}=0.95 *_{\text {base }} \mathrm{B}_{\mathrm{RL}} / \mathrm{M}_{\mathrm{F}}=0.76 \mathrm{nXMR} /$ byte

## 2b) Wallet Fees (Old)

For the calculation of wallet fees we assume that the next 10 blocks have, no transactions other than the coinbase transaction, the empty blocks, We then calculate $\mathrm{M}_{\mathrm{sw}}$ by following the calculation of $\mathrm{M}_{\mathrm{s}}$ at this future point. We use the previous 10000 blocks and the future 10 empty blocks.

Define
$\mathrm{M}_{\mathrm{Bw}}=$ Block weight in bytes for past and current real and future empty blocks
$Z_{M}$; Penalty free zone for wallet fees
$\mathrm{M}_{\mathrm{sw}}=$ the median over the "last" 100 blocks of $\max \left(\mathrm{M}_{\mathrm{Bw}}\right.$, $Z_{M}$ ) ;
$\mathrm{M}_{\mathrm{Nw}}=\min \left(\mathrm{M}_{\mathrm{sw}}, 50 \mathrm{M}_{\mathrm{L}}\right)$
$M_{F W}=\min \left(M_{N W}, M_{L}\right) ;$ Median for wallet fee calculation
$B_{R}=T_{R} / Z_{M}$

## 2b) Wallet Fees (New)

For the calculation of wallet fees we assume that the next 10 blocks have no transactions, other than the coinbase transaction, the empty blocks, We then calculate $\mathrm{M}_{\mathrm{Lw}}$ and $M_{s w}$ by following the calculation of $M_{L}$ and $M_{S}$ at this future point. We use the previous 99990 blocks and the future 10 empty blocks ( 100000 blocks) for $M_{\llcorner }$and the previous 90 blocks and future 10 blocks (100 blocks) for $\mathrm{M}_{\mathrm{s}}$

Define
$\mathrm{M}_{\mathrm{BW}}=\mathrm{M}_{\mathrm{B}}$ for the last 99990 blocks
$M_{B W}=0$ for the future 10 blocks; $A$ value of 0 bytes can be used for the empty blocks for the purposes of calculating $\mathrm{M}_{\mathrm{Lw}}$ and $\mathrm{M}_{\mathrm{sw}}$
$\mathrm{M}_{\mathrm{Lw}}=$ The median over the last 99990 blocks and future 10 blocks (100000 blocks) of $\max \left(\left(\min \left(\mathrm{M}_{\mathrm{Bw}}, 2 \mathrm{M}_{\mathrm{L}}\right), \mathrm{Z}_{\mathrm{M}}\right.\right.$,
$\left.M_{L} / 2\right)$; The current value of $M_{L}$ from consensus is used; Effective long term median for wallet fees
$M_{L w}$; Penalty free zone for wallet fees
$\mathrm{M}_{\mathrm{sw}}=$ the median over the last 90 blocks and future 10 blocks (100 blocks) of $\max \left(\mathrm{M}_{\mathrm{BW}}, \mathrm{M}_{\mathrm{Lw}}\right)$; Effective short term median for wallet fees
$\mathrm{M}_{\mathrm{Nw}}=\min \left(\mathrm{M}_{\mathrm{sw}}, 50 \mathrm{M}_{\mathrm{Lw}}\right)$
$\mathrm{M}_{\mathrm{FW}}=\min \left(\mathrm{M}_{\mathrm{NW}}, \mathrm{M}_{\mathrm{Lw}}\right)\left(=\mathrm{M}_{\mathrm{Lw}}\right.$ if the proposed consensus change is implemented) ; Median for wallet fee calculation
$B_{R L W}=T_{R} / M_{F W} ;$ Used for the low and normal fees
$B_{R}=T_{R} / Z_{M} ;$ Used for the medium and high fees
$F_{N}=R_{B a s e} B_{R}{ }^{2}$; Normal Transaction fee at minimum fee and $F_{L}=R_{\text {Base }} B_{R L w}{ }^{2}$; Low transaction fee for reference minimum $M_{\text {FW }}=Z_{M}$ transaction
$f_{N}=R_{\text {Base }} B_{R} / M_{\text {Fw }}$; Normal Transaction fee per byte for a given $\mathrm{M}_{\mathrm{Fw}}$
$f_{L}=R_{\text {Base }} B_{R L W} / M_{F W}$; Low transaction fee per byte for a given $\mathrm{M}_{\mathrm{FW}}$
$f_{N}=4 f_{L} ;$ Normal transaction fee per byte for a given $M_{F w}$
$f_{M}=16 R_{\text {Base }} B_{R} / M_{F w}$;Medium Transaction fee per byte for a given $\mathrm{M}_{\mathrm{FW}}$
$f_{P}=2 R_{\text {Base }} / M_{N W}=2 f_{N} M_{F W} /\left(B_{R} M_{N W}\right)$; Maximum Penalty $(B=1) f_{P}=2 R_{B a s e} / M_{N W}=f_{M} M_{F W} /\left(8 B_{R} M_{N W}\right) ;$ Maximum Penalty ( $B=1$ ) Transaction fee per byte for a given $\mathrm{M}_{\mathrm{Nw}}$
$f_{H}=f_{P}$; Highest Transaction fee per byte.

Transaction fee per byte for a given $\mathrm{M}_{\mathrm{Nw}}$
$f_{H}=4 f_{M} \max \left(1, M_{F w} /\left(32 B_{R} M_{N w}\right)\right)$; High Transaction fee per byte

## Wallet Fee Examples

$T_{R}=3000$ bytes, $R_{\text {Base }}=0.6$ XMR, $\mathrm{Z}_{\mathrm{M}}=300000$ bytes
$M_{N W}=300000$ bytes, $M_{L}=300000$ bytes
$\mathrm{f}_{\mathrm{N}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{Fw}}=20.0 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{L}}=0.2 \mathrm{f}_{\mathrm{N}}=4.00 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=5 \mathrm{f}_{\mathrm{N}}=100 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=2 \mathrm{f}_{\mathrm{N}} \mathrm{M}_{\mathrm{FW}} /\left(\mathrm{B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=4000 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{H}}=\mathrm{f}_{\mathrm{P}}=4000 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{NW}}=15000000$ bytes, $\mathrm{M}_{\mathrm{L}}=300000$ bytes
$\mathrm{f}_{\mathrm{N}}=\mathrm{R}_{\mathrm{Base}} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=20.0 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{L}}=0.2 \mathrm{f}_{\mathrm{N}}=4.00 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=5 \mathrm{f}_{\mathrm{N}}=100 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=2 \mathrm{f}_{\mathrm{N}} \mathrm{M}_{\mathrm{FW}} /\left(\mathrm{B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=80 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{H}}=\mathrm{f}_{\mathrm{P}}=80 \mathrm{nXMR} /$ byte
$M_{N W}=1425000$ bytes, $M_{L}=1425000$ bytes
$\mathrm{f}_{\mathrm{N}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=4.21 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{L}}=0.2 \mathrm{f}_{\mathrm{N}}=0.842 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=5 \mathrm{f}_{\mathrm{N}}=21.1 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=2 \mathrm{f}_{\mathrm{N}} \mathrm{M}_{\mathrm{FW}} /\left(\mathrm{B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=842 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{H}}=\mathrm{f}_{\mathrm{P}}=842 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{NW}}=1500000$ bytes, $\mathrm{M}_{\mathrm{L}}=1500000$ bytes
$\mathrm{f}_{\mathrm{N}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=4.00 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{L}}=0.2 \mathrm{f}_{\mathrm{N}}=0.80 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=5 \mathrm{f}_{\mathrm{N}}=20 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=2 \mathrm{f}_{\mathrm{N}} \mathrm{M}_{\mathrm{FW}} /\left(\mathrm{B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=800 \mathrm{nXMR} /$ byte $\mathrm{f}_{\mathrm{H}}=\mathrm{f}_{\mathrm{P}}=800 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{Nw}}=75000000$ bytes, $\mathrm{M}_{\mathrm{L}}=1500000$ bytes
$\mathrm{f}_{\mathrm{N}}=\mathrm{R}_{\text {Base }} B_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=4.00 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{L}}=0.2 \mathrm{f}_{\mathrm{N}}=0.80 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=5 \mathrm{f}_{\mathrm{N}}=20 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=2 \mathrm{f}_{\mathrm{N}} \mathrm{M}_{\mathrm{FW}} /\left(\mathrm{B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=16 \mathrm{nXMR} /$ byte $\mathrm{f}_{\mathrm{H}}=\mathrm{f}_{\mathrm{P}}=16 \mathrm{nXMR} /$ byte

## Wallet Fee Examples

$\mathrm{T}_{\mathrm{RW}}=3000$ bytes, $\mathrm{R}_{\text {Base }}=0.6 \mathrm{XMR}, \mathrm{Z}_{\mathrm{M}}=300000$ bytes
$\mathrm{M}_{\mathrm{NW}}=300000$ bytes, $\mathrm{M}_{\mathrm{Lw}}=300000$ bytes
$\mathrm{f}_{\mathrm{L}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{RLW}} / \mathrm{M}_{\mathrm{FW}}=20.0 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{N}}=4 \mathrm{f}_{\mathrm{L}}=80 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=16 \mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=320 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{P}}=2 \mathrm{R}_{\text {Base }} / \mathrm{M}_{\mathrm{NW}}=\mathrm{f}_{\mathrm{M}} \mathrm{M}_{\mathrm{FW}} /\left(8 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)=4000 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{H}}=4 \mathrm{f}_{\mathrm{M}} \max \left(1, \mathrm{M}_{\mathrm{Fw}} /\left(32 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{Nw}}\right)\right)=4000 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{NW}}=15000000$ bytes, $\mathrm{M}_{\mathrm{LW}}=300000$ bytes
$\mathrm{f}_{\mathrm{L}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{RLW}} / \mathrm{M}_{\mathrm{FW}}=20.0 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{N}}=4 \mathrm{f}_{\mathrm{L}}=80 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=16 \mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{R}} / \mathrm{M}_{\mathrm{Fw}}=320 \mathrm{nXMR} /$ byte
$f_{P}=2 R_{\text {Base }} / M_{N W}=f_{M} M_{F W} /\left(8 B_{R} M_{N W}\right)=80 n X M R /$ byte
$\mathrm{f}_{\mathrm{H}}=4 \mathrm{f}_{\mathrm{M}} \max \left(1, \mathrm{M}_{\mathrm{FW}} /\left(32 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)\right)=1280 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{NW}}=1425000$ bytes, $\mathrm{M}_{\mathrm{Lw}}=1425000$ bytes
$\mathrm{f}_{\mathrm{L}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{RLW}} / \mathrm{M}_{\mathrm{FW}}=0.886 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{N}}=4 \mathrm{f}_{\mathrm{L}}=3.55 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=16 \mathrm{R}_{\text {Base }} B_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=67.4 \mathrm{nXMR} /$ byte
$f_{P}=2 R_{\text {Base }} / M_{N W}=f_{M} M_{F W} /\left(8 B_{R} M_{N w}\right)=842 n X M R /$ byte
$\mathrm{f}_{\mathrm{H}}=4 \mathrm{f}_{\mathrm{M}} \max \left(1, \mathrm{M}_{\mathrm{Fw}} /\left(32 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{Nw}}\right)\right)=842 \mathrm{nXMR} /$ byte
$M_{N W}=1500000$ bytes, $M_{\mathrm{Lw}}=1500000$ bytes
$\mathrm{f}_{\mathrm{L}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{RLW}} / \mathrm{M}_{\mathrm{FW}}=0.800 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{N}}=4 \mathrm{f}_{\mathrm{L}}=3.20 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=16 \mathrm{R}_{\text {Base }} B_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=64.0 \mathrm{nXMR} /$ byte
$f_{P}=2 R_{\text {Base }} / M_{N W}=f_{M} M_{F W} /\left(8 B_{R} M_{N W}\right)=800 n X M R /$ byte
$\mathrm{f}_{\mathrm{H}}=4 \mathrm{f}_{\mathrm{M}} \max \left(1, \mathrm{M}_{\mathrm{Fw}} /\left(32 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{NW}}\right)\right)=800 \mathrm{nXMR} /$ byte
$\mathrm{M}_{\mathrm{NW}}=75000000$ bytes, $\mathrm{M}_{\mathrm{LW}}=1500000$ bytes
$\mathrm{f}_{\mathrm{L}}=\mathrm{R}_{\text {Base }} \mathrm{B}_{\mathrm{RLW}} / \mathrm{M}_{\mathrm{FW}}=0.800 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{N}}=4 \mathrm{f}_{\mathrm{L}}=3.20 \mathrm{nXMR} /$ byte
$\mathrm{f}_{\mathrm{M}}=16 \mathrm{R}_{\text {Base }} B_{\mathrm{R}} / \mathrm{M}_{\mathrm{FW}}=64.0 \mathrm{nXMR} /$ byte
$f_{P}=2 R_{\text {Base }} / M_{N W}=f_{M} M_{F W} /\left(8 B_{R} M_{N W}\right)=16 n X M R /$ byte
$\mathrm{f}_{\mathrm{H}}=4 \mathrm{f}_{\mathrm{M}} \max \left(1, \mathrm{M}_{\mathrm{FW}} /\left(32 \mathrm{~B}_{\mathrm{R}} \mathrm{M}_{\mathrm{Nw}}\right)\right)=256 \mathrm{nXMR} /$ byte
The difference is that the low fee always allows for scaling of the reference transaction, and is the lowest fee that allows for scaling of the reference transaction. Before the lowest fee that allowed for scaling of the reference transaction was the normal fee which was higher than the minimum required for scaling above 300000 bytes.

## 3) Reference transaction, $T_{R}$, Minimum <br> penalty free zone, $Z_{M}$, and Median calculation after a fork.

Note: I am not recommending that we reduce $T_{R}$ from the current 3000 bytes until, at least, we finalize the transaction size for Triptych or another replacement for CLSAG, if Triptych is not used. This is to reduce the impact on fees overall. For example: A reduction in fees followed by an increase in fees or the need to increase $Z_{M}$ more than would be necessary.
$\mathrm{T}_{2 \mathrm{C}}=$ Weight in bytes of a 2 input and 2 output transaction for the current Monero version rounded up to the nearest 100 bytes. $\mathrm{T}_{2 \mathrm{P}}=$ Weight in bytes of a 2 input and 2 output transaction for the previous Monero version rounded up to the nearest 100 bytes. If a future Monero fork does not permit a 2 input and 2 output transaction then the permitted transaction in both versions with the lowest number of inputs and outputs greater than or equal to 2 is used instead.

## Calculation of $T_{R}$

$T_{R P}=T_{R}$ of previous Monero version
$T_{R C}$ of current Monero version is set as follows: $T_{R C} \geq T_{2 C}$
Recommendation (See: Note) $\mathrm{T}_{\mathrm{RC}}=\max \left(\mathrm{T}_{2 \mathrm{C}}, \mathrm{T}_{\mathrm{RP}}\right)$
$T_{R}=T_{R C}(=3000$ bytes for BP+ fork if ring size <26)

## Calculation of $Z_{M}$

$Z_{M P}=Z_{M}$ of previous Monero version
$Z_{M C}=\max \left(Z_{M P}, Z_{M P} T_{R C} / T_{R P}\right)$
$Z_{M}=Z_{\text {MC }}$ ( $=300000$ bytes if $T_{R}=3000$ bytes)
Calculation of $M_{L}, M_{s}, M_{L w}$ and $M_{s w}$ where $M_{L}>Z_{M}$, or would be under (ii), and where blocks from a previous Monero version are included in a calculation after the fork.
(i) For $\mathrm{T}_{2 \mathrm{C}} \leq \mathrm{T}_{2 \mathrm{P}}$
$M_{L}, M_{s}, M_{L w}$ and $M_{s w}$ are calculated in the usual way with no reduction is size applied to the pre fork blocks
(ii) For $T_{2 c}>T_{2 P}$

When blocks of previous Monero are included in a calculation after the fork version $\mathrm{M}_{\mathrm{B}}$ for the pre fork blocks is replaced by $M_{B C}$, where $M_{B C}=M_{B} T_{2 C} / T_{2 P}$. The current value of $Z_{M}$ is used, and the starting median for $M_{L}$ and $M_{L w}$ may also need to be adjusted. This needs to be looked at for each specific fork case. There may be a one time increase in $\mathrm{M}_{\mathrm{L}}, \mathrm{M}_{\mathrm{s}}, \mathrm{M}_{\mathrm{Lw}}$ or $\mathrm{M}_{\mathrm{sw}}$ at the fork.

## 4) Wallet Fee Rounding

Wallet fees, $f_{N}, f_{L}, f_{M}$, and $f_{H}$ are rounded up to the desired number of significant digits in the significant

## Wallet Fee Rounding Examples

Three significant digits
27810 Rounded to : 27900
$37.94 \quad$ Rounded to : 38.0
$0.5555 \quad$ Rounded to : 0.556
0.002342 Rounded to : 0.00235

Two significant digits
27810 Rounded to : 28000
$37.94 \quad$ Rounded to : 38
0.5555 Rounded to : 0.56
0.002342 Rounded to : 0.0024

