

Problem 1:

Kruskal

edges:

$$AB = 2$$

$$CD = 3$$

$$FE = 4$$

$$CG = 5$$

$$GD = 6$$

$$GE = 7$$

$$AF = 8$$

$$FB = 9$$

$$BG = 10$$

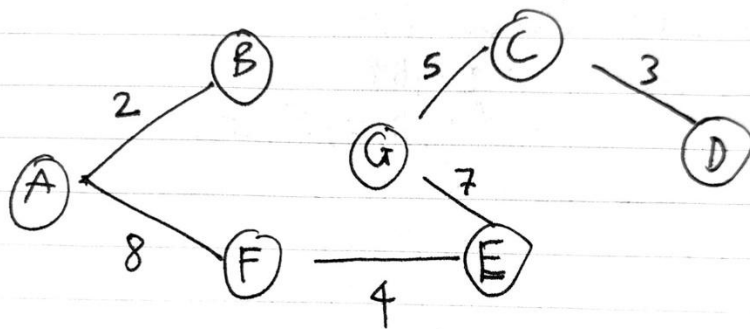
$$BC = 11$$

$$ED = 12$$

$$FG = 13$$

edge	decision	MST
AB	take	{AB}
CD	take	{AB, CD}
FE	take	{AB, CD, FE}
CG	take	{AB, CD, FE, CG}
GD	no	{AB, CD, FE, CG}
GE	take	{AB, CD, FE, CG, GE}
AF	take	{AB, CD, FE, CG, GE, AF}

We have $|V| = 7 \Rightarrow$ MST must have $|V| - 1$ edge, we stop here because we have 6 edges in MST



Prin

Thứ
Ngày

No.

we take source $S = \{A\}$
other vertices $V = \{B, C, D, E, F, G\}$

- smallest edge from $\{A\}$
is AB, then $S = \{A, B\}$

$V = \{C, D, E, F, G\}$

- smallest edge from $\{A, B\}$

is AF, then $S = \{A, B, F\}$

$V = \{C, D, E, G\}$

- and so we have FE then $S = \{A, B, F, E\}$

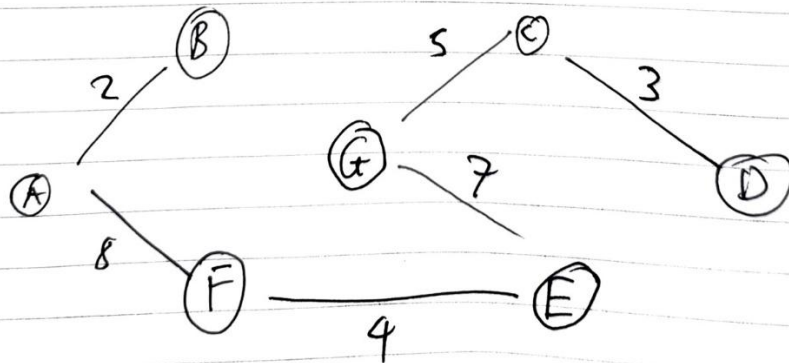
$V = \{C, D, G\}$

- then we have EG then $S = \{A, B, F, E, G\}$

$V = \{C, D\}$

- then GC then $S = \{A, B, F, E, G, C\}$

finally : CD then $S = \{A, B, F, E, G, C, D\}$



Problem 2:

2,

when we start, let consider path value, start at A

(1), (2), (3), (4), (5)

0 ∞ ∞ ∞ ∞

first loop

$$1 \rightarrow 2 = 6 < \infty \Rightarrow (2) = 6$$

$$1 \rightarrow 4 = 7 < \infty \Rightarrow (4) = 7$$

$$2 \rightarrow 3 = 6 + 5 = 11 < \infty \Rightarrow (3) = 11$$

$$2 \rightarrow 4 = 6 + 8 = 14 > (4) \Rightarrow \text{no change}$$

$$2 \rightarrow 5 = 6 - 4 = 2 < \infty \Rightarrow (5) = 2$$

$$3 \rightarrow 2 = 11 - 2 = 9 > (2) \Rightarrow \text{no change}$$

$$4 \rightarrow 3 = 7 - 3 = 4 < (3) \Rightarrow (3) = 4$$

$$4 \rightarrow 5 = 7 + 9 = 16 > (5) \Rightarrow \text{no change}$$

$$5 \rightarrow 1 = 2 + 2 = 4 > (1) \Rightarrow \text{no change}$$

$$5 \rightarrow 3 = 2 + 7 = 9 > (3) \Rightarrow \text{no change}$$

then after first loop:

(1), (2), (3), (4), (5)

0 6 4 7 2

2nd loop

$$1 \rightarrow 2 = 0 + 6 = (2) \Rightarrow \text{no}$$

$$1 \rightarrow 4 = 0 + 7 = (4) \Rightarrow \text{no}$$

$$2 \rightarrow 3 = 6 + 5 > (3) \Rightarrow \text{no}$$

$$2 \rightarrow 4 = 6 + 8 > (4) \Rightarrow \text{no}$$

$$2 \rightarrow 5 = 6 - 4 = (5) \Rightarrow \text{no}$$

$$3 \rightarrow 2 = 4 - 2 = 2 < (2) \Rightarrow (2) = 2$$

$$4 \rightarrow 3 = 7 - 3 = (3) \Rightarrow \text{no}$$

$$4 \rightarrow 5 = 7 + 9 = 16 > (5) \Rightarrow \text{no}$$

$$5 \rightarrow 1 = 2 + 2 > (1) \Rightarrow \text{no}$$

$$5 \rightarrow 3 = 2 + 7 > (3) \Rightarrow \text{no}$$

(1), (2), (3), (4), (5)

0 2 4 7 2

3rd	4th
1 : 0	1 : 0
2 : 2	2 : 2
3 : 4	3 : 4
4 : 7	4 : 7
5 : -2	5 : -2

Problem 3:

3, vertices: A, B, C, D, E, F, G		
Start : A : 0	take A:	A : 0
B : ∞		B : ∞
C : ∞		C : 1 A
D : ∞		D : 2 A
E : ∞		E : ∞
F : ∞		F : ∞
G : ∞		G : ∞
take C:	A : 0	take D:
B : 3	C	A : 0
C : 1	A	B : 3 C
D : 2	A	C : 1 A
E : 4	C	D : 2 A
F : ∞		E : 4 C
G : ∞		F : ∞
		G : 3 D
take G:	A : 0	take B:
B : 3	C	A : 0
C : 1	A	B : 3 C
D : 2	A	C : 1 A
E : 4	C	D : 2 A
F : 4	G	E : 4 C
G : 3	D	F : 4 G
		G : 3 D

choose E :	A : 0		finally F :	A : 0
	B : 3	C		B : 3
	C : 1	A		C : 1
	D : 2	A		D : 2
	E : 4	C		E : 4
	F : 4	G		F : 4
	G : 3	D		G : 3

stop here because this is our destination

F: 4 $\Rightarrow$ shortest path from A to F is

A $\rightarrow$ D $\rightarrow$ G $\rightarrow$ F

Problem 4:

4, BFS:

$Q = [A]$

$visited = \{A\}$

take A, add B, C, D

$Q = [B, C, D]$

$visited = \{A, B, C, D\}$

take B, add E, F

$Q = [C, D, E, F]$

$visited = \{A, B, C, D, E, F\}$

take C, no add, $Q = [D, E, F]$

take D, no add, $Q = [E, F]$

take E, no add, $Q = [F]$

take F, no add, $Q = \emptyset$

$A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F$

DFS:

$Stack = [A]$

pop A, push D, C, B, $stack = [D, C, B]$

pop B, push F, E, $stack = [D, C, F, E]$

pop E, no push, $stack = [D, C, F]$

pop F, ———, $stack = [D, C]$

pop C, ———, $stack = [D]$

pop D, ———, $stack = \emptyset$

so $A \rightarrow B \rightarrow E \rightarrow F \rightarrow C \rightarrow D$

Problem 5:

Pseudocode:

rod-cutting-wCost(price, n, c)

create array $dp[0..n]$

$dp[0] = 0$

```
for j = 1 to n
  best = price[j]
  for i = 1 to j - 1
    best = max(best, price[i] + dp[j - i] - c)
  dp[j] = best
return dp[n]
```

This problem is more complicated than the original problem which is just cutting rod, because when we cut now we have to think whether cost < revenue or not.

We set `best = price[j]` because maybe no cut is better than cut, because cut may make cost > revenue.