



polyDB.org

A Database for Discrete Geometric Objects

## Database for collections of discrete geometric objects

▷ **aims:**

- ▷ unified access to collections of discrete geometric data
  - ▷ data with information on authors and references
  - ▷ stable references into data
  
  - ▷ no restriction on specific data/format of data
  - ▷ access not bound to specific software
  
  - ▷ allow simple experimentation with the data
- ▷ project started in June 2013 as extension to *polymake*
- ▷ web frontend: [polyDB.org](http://polyDB.org)



- ▷ *polyDB* is based on MongoDB
  - ▷ NoSQL database
  - ▷ JSON/BSON documents in *collections*
  - ▷ own MongoDB query language
- ▷ drivers/APIs for
  - ▷ PHP, Perl, Python, ...
  - ▷ C/C++, Julia...
- ▷ license
  - ▷ MongoDB: Server Side Public License (based on GPLv3)
  - ▷ Official drivers: Apache License v2.0
- ▷ *polyDB* vs. databases
  - ▷ review/QA via some publication
  - ▷ no computations in database
  - ▷ only data collection

# *polyDB*: Access

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- ▷ web frontend [polyDB.org](https://polydb.org)
- ▷ Rest API
  - ▷ Base URI: [polydb.org/rest/current/<endpoint>](https://polydb.org/rest/current/<endpoint>)  
[db.polymake.org/rest/current/id/Matroids.Small/n12r3\\_27395519](https://db.polymake.org/rest/current/id/Matroids.Small/n12r3_27395519)
  - ▷ Documentation: [polydb.org/rest/api/0.2](https://polydb.org/rest/api/0.2)
- ▷ *polymake* [polymake.org](https://polymake.org)
  - ▷ initial application
- ▷ OSCAR (using *Polymake.jl*) [docs.oscar-system.org/stable](https://docs.oscar-system.org/stable)  
[github.com/oscar-system/Polymake.jl](https://github.com/oscar-system/Polymake.jl)
- ▷ python or sage: *pypolydb* (in progress) [github.com/apaffenholz/pypolydb](https://github.com/apaffenholz/pypolydb)
- ▷ Julia: *PolyDB.jl* (in progress) [github.com/apaffenholz/PolyDB.jl](https://github.com/apaffenholz/PolyDB.jl)
- ▷ anything else with MongoDB driver [mongodb.com/docs/drivers](https://mongodb.com/docs/drivers)
  
- ▷ Queries in
  - ▷ MongoDB query language
  - ▷ some convenience functions

# polyDB Data Format

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- ▶ data for each collection has two parts
  - (1) data in form for efficient search
  - (2) format document defining
    - ▶ data format for each entry in collection
    - ▶ mathematical types of entries
- ▶ data in JSON
- ▶ format/types as JSON schema
- ▶ math/CAS interpretation via namespaces
  - ▶ e.g. software that can deserialize the format
  - ▶ possibly mixing namespaces/reading subsets

```
{
  "_id" : "6_40",
  "_ns" : {
    "polymake" : [
      "https://polymake.org",
      "4.3.2"
    ]
  },
  "_type" : "polytope::Polytope<Rational>",
  "VERTICES" : [
    [ "1", "0", "0", "0" ],
    [ "1", "1", "0", "0" ],
    [ "1", "0", "1", "0" ],
    [ "1", "0", "2", "3" ],
    [ "1", "3", "-1", "-2" ]
  ],
  "REFLEXIVE" : false,
  "N_LATTICE_POINTS" : 6,
  "EHRHART_POLYNOMIAL" : [
    { "1": "4/3", "0": "1", "2": "2", "3": "5/3" }
  ],
  "SMOOTH" : false,
  "NORMAL" : false,
  "SIMPLE" : false,
  "VERY_AMPLE" : false,
  "F_VECTOR" : [ 5, 9, 6 ],
  [...]
}
```

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# polyDB Data Format

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- ▶ ensure lossless storage/retrieval
  - ▶ keep exact mathematical types based on implementation in some CAS
  - ▶ data documents are not self contained
    - ▶ needs both data and schema
  - ▶ normalize data
    - dense/sparse formats
- ▶ versioning
  - handle changes in format/serialization
  - data maintenance: update format
- ▶ allow fast retrieval in a CAS
  - ▶ access to deserializer
  - ▶ JSON transformation

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  },
  "_type" : "polytope::Polytope<Rational>",
  "VERTICES" : [
    [ "1", "0", "0", "0" ],
    [ "1", "1", "0", "0" ],
    [ "1", "0", "1", "0" ],
    [ "1", "0", "2", "3" ],
    [ "1", "3", "-1", "-2" ]
  ],
  "REFLEXIVE" : false,
  "N_LATTICE_POINTS" : 6,
  "EHRHART_POLYNOMIAL" : [
    { "1": "4/3", "0": "1", "2": "2", "3": "5/3" }
  ],
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# *polyDB* Data Format

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  "VERTICES" : [
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    ["1", "1", "0", "0"],
    ["1", "0", "1", "0"],
    ["1", "0", "2", "3"],
    ["1", "3", "-1", "-2"]
  ],
  "REFLEXIVE" : false,
  "N_LATTICE_POINTS" : 6,
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    {"1": "4/3", "0": "1", "2": "2", "3": "5/3"}
  ],
  "SMOOTH" : false,
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  "SIMPLE" : false,
  "VERY_AMPLE" : false,
  "F_VECTOR" : [5,9,6],
  [...]
}
```

---

```
{
  "type" : "object",
  "$schema" : "http://json-schema.org/draft-07/schema#",
  "additionalProperties" : false
  "required" : [ ... ]
  "properties" : { ... },
  "definitions" : { ... },
}
```

---

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  "_id" : "6_40",
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    ["1", "0", "1", "0"],
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  ],
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  "F_VECTOR" : [5,9,6],
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}
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{
  "type" : "object",
  "$schema" : "http://json-schema.org/draft-07/schema#",
  "additionalProperties" : false
  "required" : [ ... ]
  "properties" : { ... },
  "definitions" : { ... },
}

"properties" : {
  "_id" : {
    "$ref" : "https://polymake.org/schemas/data.json#/definitions/obj_id"
  },
  "_type" : {
    "const" : "polytope::Polytope<Rational>"
  },
  "_ns" : {
    "additionalProperties" : false,
    "type" : "object",
    "properties" : {
      "polymake" : {
        "items" : [{"const" : "https://polymake.org"}, {"const" : "4.3.2"}],
        "additionalItems" : false,
        "type" : "array"
      }
    }
  }
}
[...]
```

---



# *polyDB* Data Format

---

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{
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    "polymake" : [
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    ]
  },
  "_type" : "polytope::Polytope<Rational>",
  "VERTICES" : [
    ["1", "0", "0", "0"],
    ["1", "1", "0", "0"],
    ["1", "0", "1", "0"],
    ["1", "0", "2", "3"],
    ["1", "3", "-1", "-2"]
  ],
  "REFLEXIVE" : false,
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    {"1": "4/3", "0": "1", "2": "2", "3": "5/3"}
  ],
  "SMOOTH" : false,
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  "VERY_AMPLE" : false,
  "F_VECTOR" : [5,9,6],
  [...]
}
```

---

```
{
  "type" : "object",
  "$schema" : "http://json-schema.org/draft-07/schema#",
  "additionalProperties" : false
  "required" : [ ... ]
  "properties" : { ... },
  "definitions" : { ... },
}
```

---

```
"required" : {
  "_ns",
  "_type",
  "VERTICES",
  "SIMPLICIAL",
  "EHRHART_POLYNOMIAL",
  "REFLEXIVE",
  "F_VECTOR",
  [...]
}
```

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  ],
  "REFLEXIVE" : false,
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    {"1": "4/3", "0": "1", "2": "2", "3": "5/3"}
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  "F_VECTOR" : [5, 9, 6],
  [...]
}
```

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```
{
  "type" : "object",
  "$schema" : "http://json-schema.org/draft-07/schema#",
  "additionalProperties" : false
  "required" : [ ... ]
  "properties" : { ... },
  "definitions" : { ... },
}

"properties" : {
  "AFFINE_HULL" : {
    "$ref" : "#/definitions/common-Matrix-Rational-NonSymmetric"
  },
  "REFLEXIVE" : {
    "$ref" : "#/definitions/common-Bool"
  },
  "EHRHART_POLYNOMIAL" : {
    "$ref" : "#/definitions/common-UniPolynomial-Rational-Int"
  },
  "N_LATTICE_POINTS" : {
    "$ref" : "#/definitions/common-Int"
  },
  "F_VECTOR" : {
    "$ref" : "#/definitions/common-Vector-Int"
  }
}
[...]
```

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  "type" : "object",
  "$schema" : "http://json-schema.org/draft-07/schema#",
  "additionalProperties" : false
  "required" : [ ... ]
  "properties" : { ... },
  "definitions" : { ... },
}

"definitions" : {
  "common-Int" : { "type" : "integer" },
  "common-Vector-Rational" : {
    "type" : "array",
    "items" : { "$ref" : "#/definitions/common-Rational" }
  }
  "common-Rational" : {
    "type" : "string",
    "pattern" : "^-?(\\d+(/\\d+)?)|inf$"
  },
  "common-Bool" : { "type" : "boolean" },
  [...]
}
```

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# Some use cases

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## ▷ 2024

- ▷ Nill, *Unimodular polytopes and a new Heller-type bound on totally unimodular matrices via Seymour's decomposition theorem*, 2024, arxiv:2405.13431
- ▷ Amendola, Oldekop, *Likelihood Geometry of Reflexive Polytopes*, 2024 arxiv:2311.13572
- ▷ Joswig, Kastner, Lorenz, *Confirmable workflows in Oscar*, 2024, arxiv:2404.06241

## ▷ 2023

- ▷ Corey, et al, *Quantum automorphisms of matroids*, 2023, arxiv:2312.13464
- ▷ Berglund et al., *New CalabiYau Manifolds from Genetic Algorithms*, 2023 arxiv:2306.06159

## ▷ 2022

- ▷ Fieker, Hofmann, Joswig, *Computing Galois groups of Ehrhart polynomials in OSCAR*, 2022, arxiv:2203.10287
- ▷ Cueto, Markwig, *Combinatorics and real lifts of bitangents to tropical quartic curves*, 2022, arxiv:2004.10891
- ▷ Geiger et al., *Self-dual matroids from canonical curves*, 2022, arxiv:2212.05910

## ▷ 2021

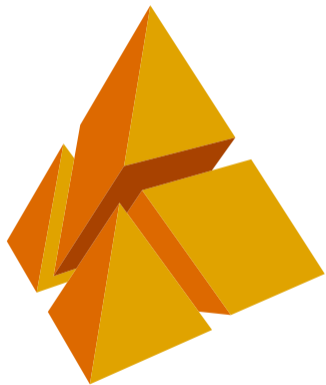
- ▷ Geiger, Panizzut, *Computing tropical bitangents to smooth quartic curves in polymake*, 2021, arxiv:2112.04447

## ▷ 2020

- ▷ Morrison, Tewari, *Convex lattice polygons with all lattice points visible*, arxiv:2005.04180

## ▷ 2019

- ▷ Joswig, Panizzut, Sturmfels, *The Schläfli Fan*, 2019, arxiv:1905.11951



polyDB.org