

Full Differentiable TDDFT Code for Neural Network XC Functional, and Attention Based Hamiltonian Learning Model

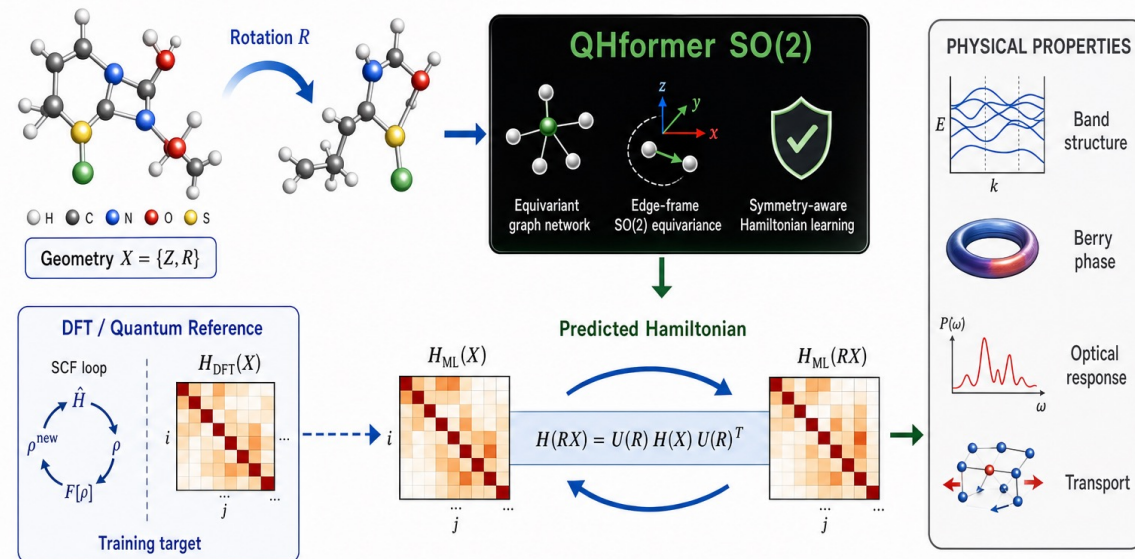
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University of Chinese Academy of Sciences



GradTDDFT
AI-native differentiable TDDFT in JAX



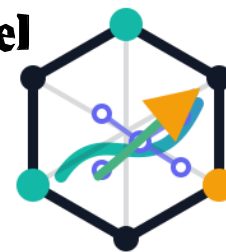
Full Differentiable TDDFT Code for Neural Network XC Functional

Qhformer_V2-A Sparsity Attention Hamiltonian Learning Model

DL-TDDFT – A Code for Accelerating TDDFT

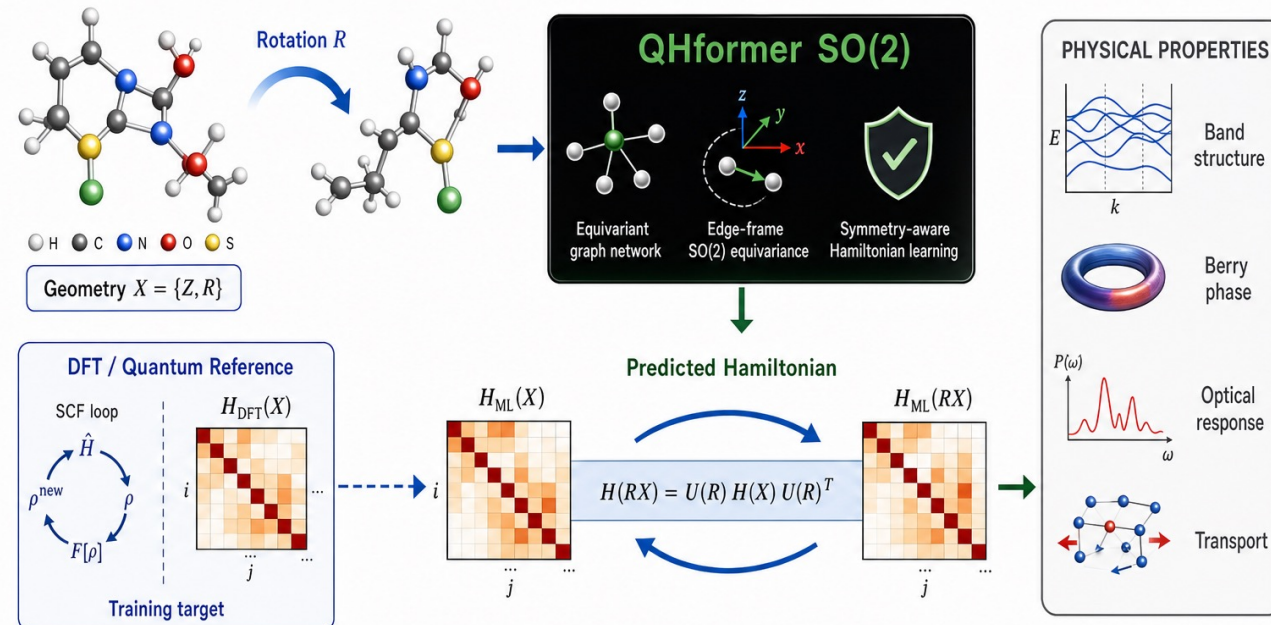
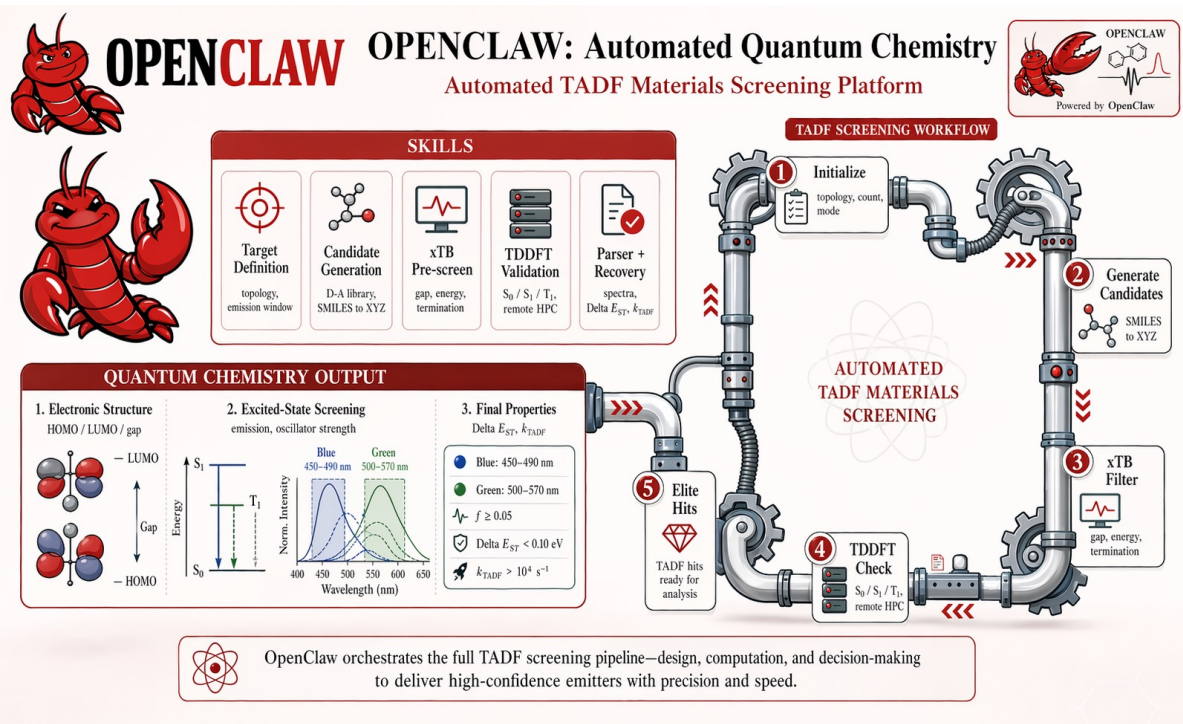
Quantum Chemistry with OpenClaw, Hermes – Automatic

Materials Calculation Skills and Agents Team for Researching



GradTDDFT

AI-native differentiable TDDFT in JAX



■ Background – Neural Network Training and Automatic Differentiable Program

● Basic Theory of Differentiation

• Analytical Differentiation

Derived purely by hand based on the derivative formula, then coding

• Numerical Differentiation

$$f'(x_i) \approx \frac{f(x_i) - f(x_i - \Delta)}{\Delta}$$

Difference approximates derivatives

• Symbolic Differentiation

Manual differentiation coding is implemented based on certain recursive relationships

• Automatic Differentiation

Based on the chain rule for derivative of composite functions, operators propagate gradients step by step on the computation graph

● Basic Theory of Automatic Differentiation

Think of the function $y = (f_k^\circ f_{k-1}^\circ f_{k-2}^\circ \dots f_1^\circ f_0^\circ)(x)$ and the derivation on $x = x_0$ of y

• Forward Mode

$$x_0 = x \text{ and } x_1 = f_0(x_0) \ x_2 = f_1(x_1) \dots x_{i+1} = f_i(x_i)$$

$$x'_0 = 1$$

$$x'_{i+1} = f'_i(x_i)x'_i$$

$$y' = x'_{i+1}$$

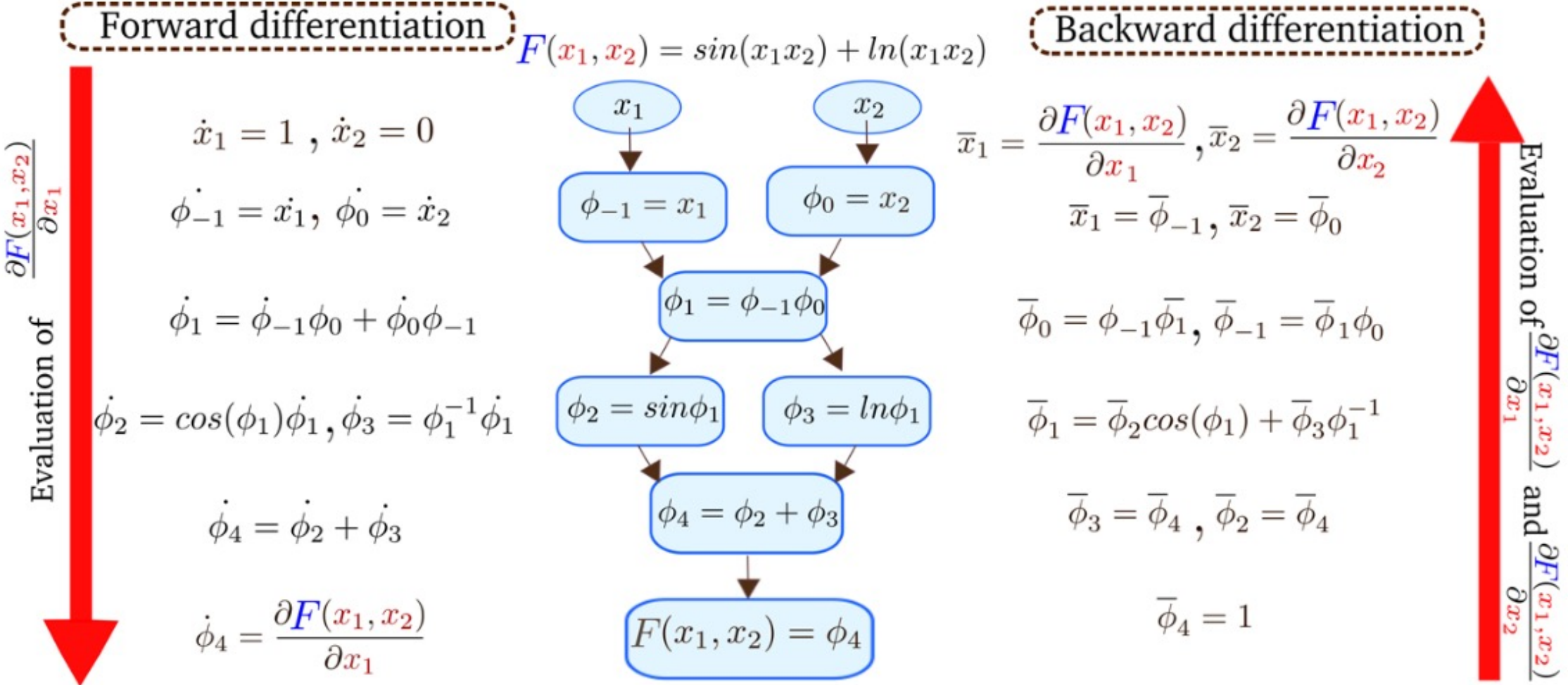
• Backward Mode

$$\bar{x}_{k+1} = 1$$

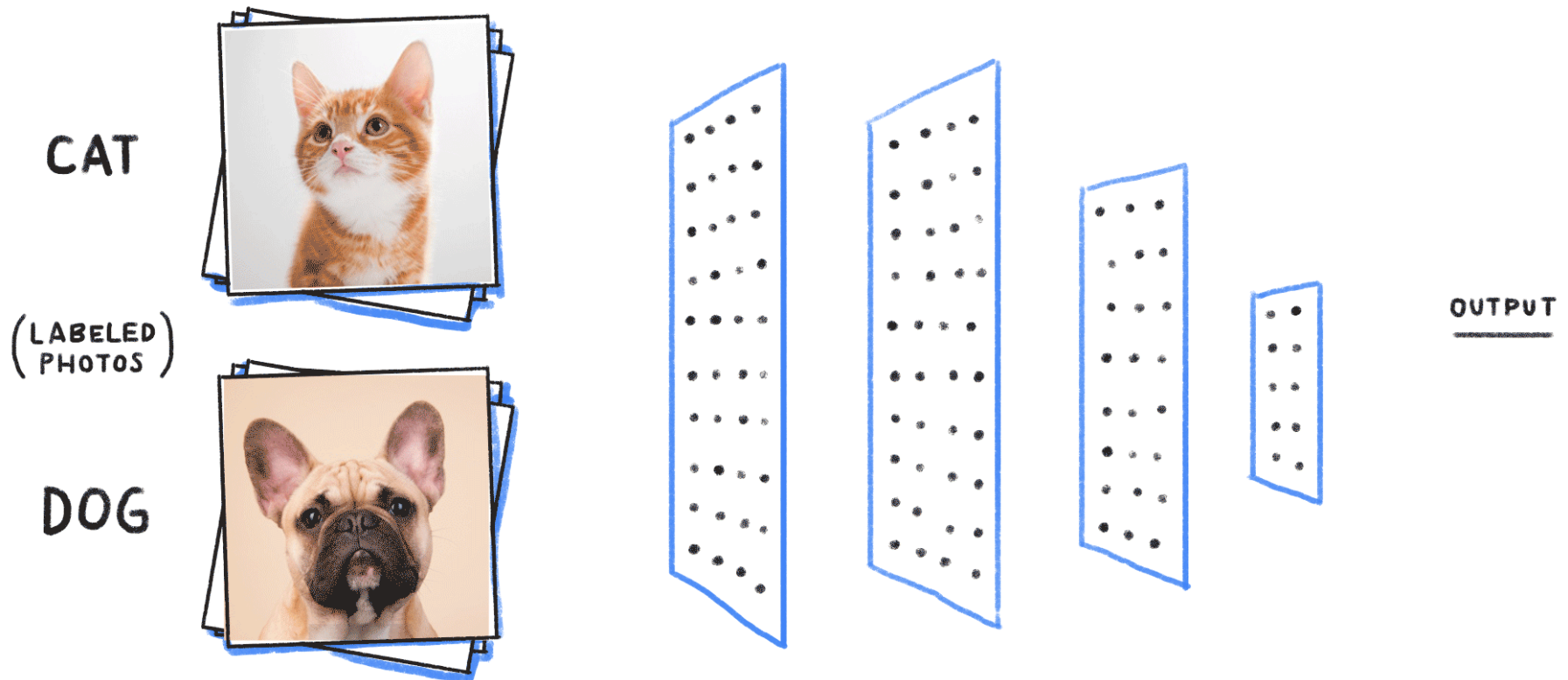
$$\bar{x}_i = \bar{x}_{i+1} \cdot f'_i(x_i) \text{ with } i = k, k-1, \dots, 1, 0$$

$$\bar{x}_0 = y'$$

Background – Neural Network Training and Automatic Differentiable Program



■ Background – Neural Network Training and Automatic Differentiable Program



← Loss Backward

Background – Neural Network Training and Automatic Differentiable Program

● Neural Network Forward Mode

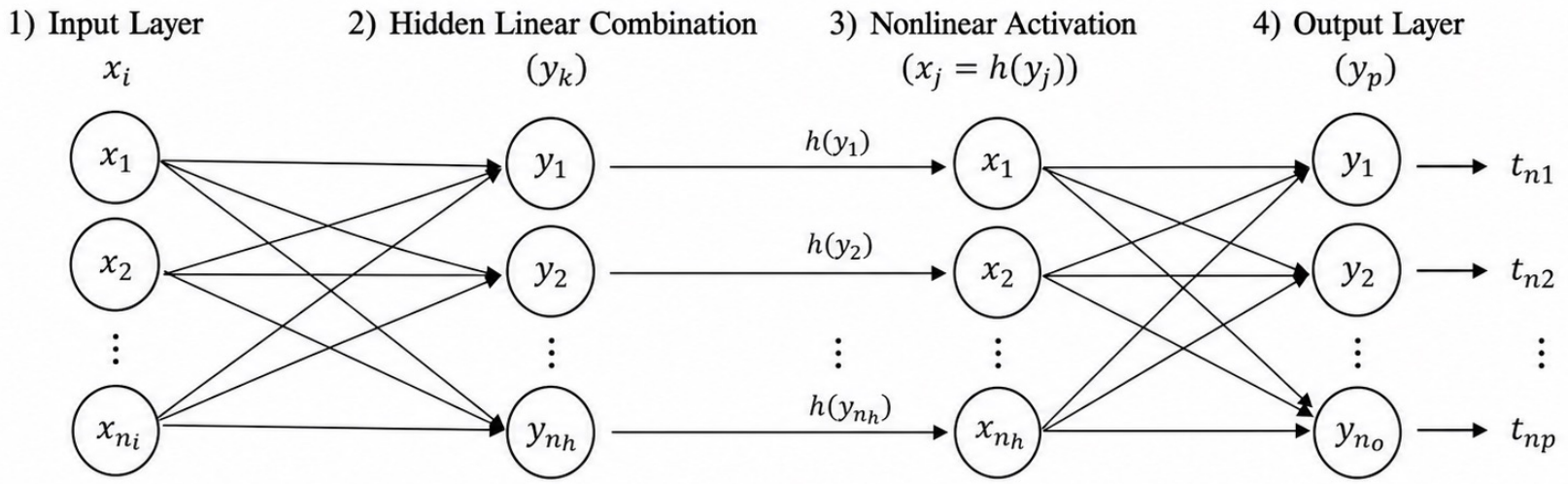
Single-Layer Network

$$y_k = \sum_i \omega_{ki} x_i \quad x_j = h(y_k)$$

$$y_p = \sum_j \omega_{pj} x_j$$

With Loss Function

$$L_n = \frac{1}{2} \sum_p (y_{np} - t_{nk})^2$$

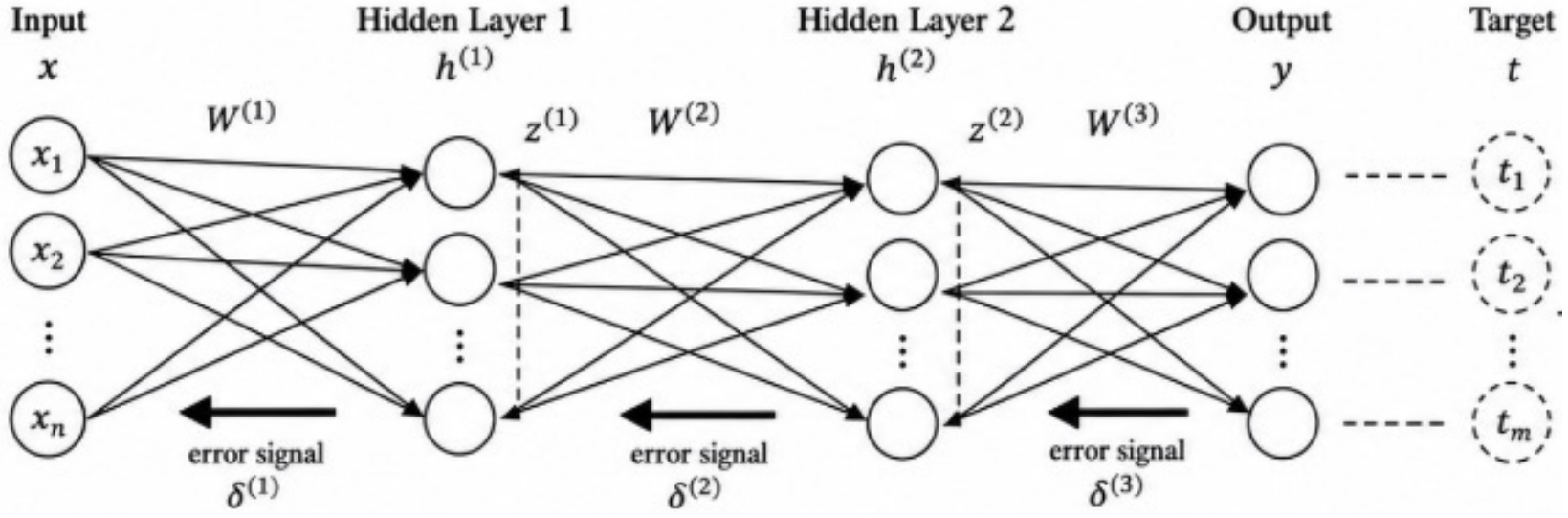


● Neural Network Backward Mode

$$\frac{\partial L_n}{\partial \omega_{ki}} = \frac{\partial L_n}{\partial y_k} \frac{\partial y_k}{\partial \omega_{ki}} = \delta_k x_i$$

$$\delta_k = \frac{\partial L_n}{\partial y_k} = \sum_p \frac{\partial L_n}{\partial y_p} \frac{\partial y_p}{\partial y_k}$$

$$\sum_p \frac{\partial L_n}{\partial y_p} \frac{\partial y_p}{\partial x_j} \frac{\partial x_j}{\partial y_k} = h'(y_k) \sum_p \delta_p \omega_{pj}$$



■ Background – Neural Network Training and Automatic Differentiable Program

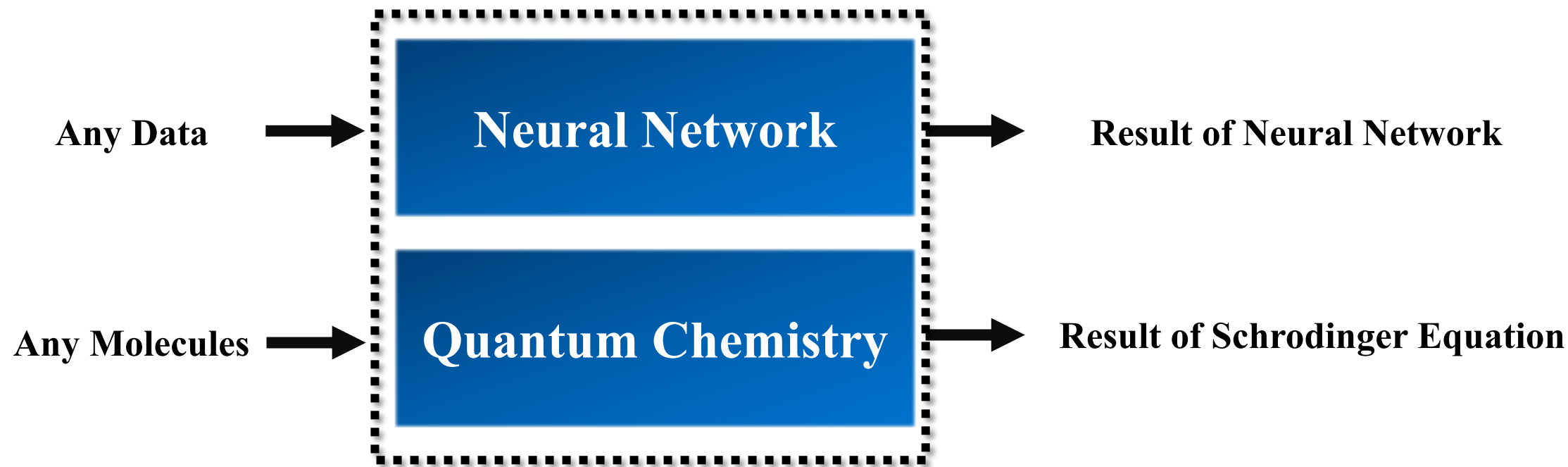
自动微分与量子化学--搞一个可微分的SCF程序



Yuan

中国科学院大学 物理学博士在读

Post-Ken 等 40 人赞同了该文章 >



zhuanlan.zhihu.com/p/2037550749622735901

■ Background – SIE and TDDFT

$$v_{ext}(\mathbf{x}, \{\mathbf{R}\}) \Leftrightarrow \rho(\mathbf{x}) \Leftrightarrow \{\psi_i(\mathbf{x})\}$$

$$\left[-\frac{1}{2} \nabla^2 + v_{ext}(\mathbf{x}, \{\mathbf{R}\}) + v_H(\mathbf{x}) + v_{xc}(\mathbf{x}) \right] \psi_i(\mathbf{x}) = \varepsilon_i \psi_i(\mathbf{x})$$



Runge-Gross Theorem

$$v_{ext}(\mathbf{x}, \{\mathbf{R}\}, t) + \mathbf{C}(t) \Leftrightarrow \rho(\mathbf{x}, t) \Leftrightarrow \{\psi_i(\mathbf{x}, t) e^{-i\alpha(t)}\}$$

$$\left[-\frac{1}{2} \nabla^2 + v_{ext}(\mathbf{x}, \{\mathbf{R}\}, t) + v_H(\mathbf{x}, t) + v_{xc}(\mathbf{x}, t) \right] \psi_i(\mathbf{x}, t) = i \frac{\partial}{\partial t} \psi_i(\mathbf{x}, t)$$



Linear-Response – Adiabatic Approximation

$$F_{aa}^{(0)} x_{ai} - x_{ai} F_{ii}^{(0)} + \sum_{bj} \left(\frac{\partial F_{ai}}{\partial P_{bj}} x_{bj} + \frac{\partial F_{ai}}{\partial P_{jb}} y_{bj} \right) P_{ii}^{(0)} = \omega x_{ia}$$

$$F_{aa}^{(0)} y_{ai} - y_{ai} F_{ii}^{(0)} - \sum_{bj} P_{ii}^{(0)} \left(\frac{\partial F_{ia}}{\partial P_{bj}} x_{bj} + \frac{\partial F_{ia}}{\partial P_{jb}} y_{bj} \right) = \omega x_{ia}$$

$$F_{aa}^{(0)} = \int d\mathbf{r} \psi_a^*(\mathbf{x}, t) \left\{ -\frac{1}{2} \nabla^2 + v_{ext}(\mathbf{x}, \{\mathbf{R}\}, t) + v_H(\mathbf{x}, t) + v_{xc}(\mathbf{x}, t) \right\} \psi_a(\mathbf{x}, t)$$

$$F_{ia} = \int d\mathbf{r} \psi_i^*(\mathbf{x}, t) \left\{ -\frac{1}{2} \nabla^2 + v_{ext}(\mathbf{x}, \{\mathbf{R}\}, t) + v_H(\mathbf{x}, t) + v_{xc}(\mathbf{x}, t) \right\} \psi_a(\mathbf{x}, t) + g_{ai}(\omega) + \Delta F_{ia}^{(0)}$$

The Time-Dependent of XC Functional Vanished !

Casida-TDDFT

$$\begin{pmatrix} A & B \\ B^* & A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

$$\psi_{ex} = \sum_{ai} x_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$

$$\psi_{di} = \sum_{ai} y_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$

TDA-TDDFT

$$AX = \omega X$$

$$\psi_{ex} = \sum_{ai} x_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$

Background – SIE and TDDFT

A, B Matrix and Response Kernel

$$A = \delta_{ij}\delta_{ab}(\varepsilon_a - \varepsilon_i) +$$

$$\int d\mathbf{r} \int d\mathbf{r}' \phi_i(\mathbf{r}) \phi_a^*(\mathbf{r}) \left\{ \frac{1}{|\mathbf{r} - \mathbf{r}'|} + f_{xc} \right\} \phi_b^*(\mathbf{r}') \phi_j(\mathbf{r}')$$

$$B = \int d\mathbf{r} \int d\mathbf{r}' \phi_i(\mathbf{r}) \phi_a^*(\mathbf{r}) \left\{ \frac{1}{|\mathbf{r} - \mathbf{r}'|} + f_{xc} \right\} \phi_b^*(\mathbf{r}') \phi_j(\mathbf{r}')$$

$$f_{xc}[\rho] = \frac{\delta^2 E_{xc}[\rho]}{\delta\rho(\mathbf{r})\delta\rho(\mathbf{r}')}$$

TDA-TDDFT

$$AX = \omega X$$

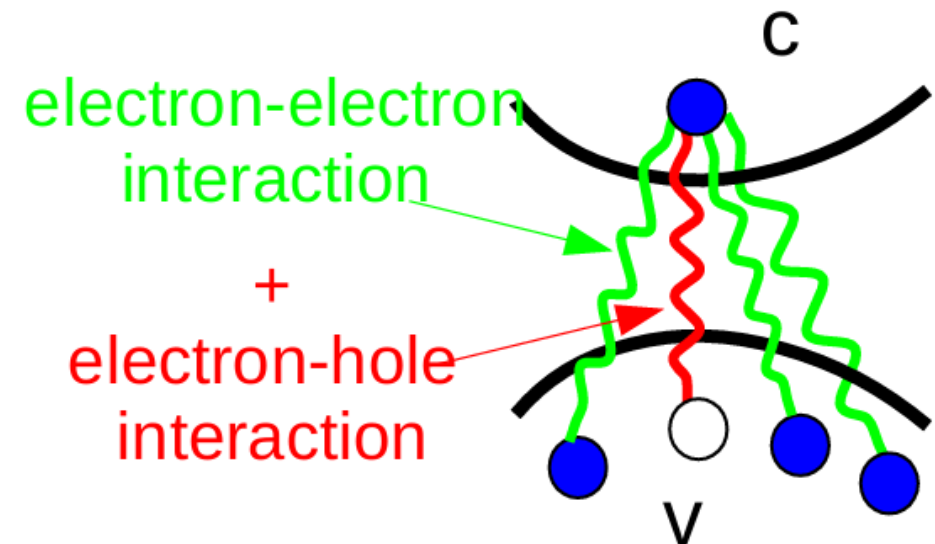
$$\psi_{ex} = \sum_{ai} x_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$

Casida-TDDFT

$$\begin{pmatrix} A & B \\ B^* & A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

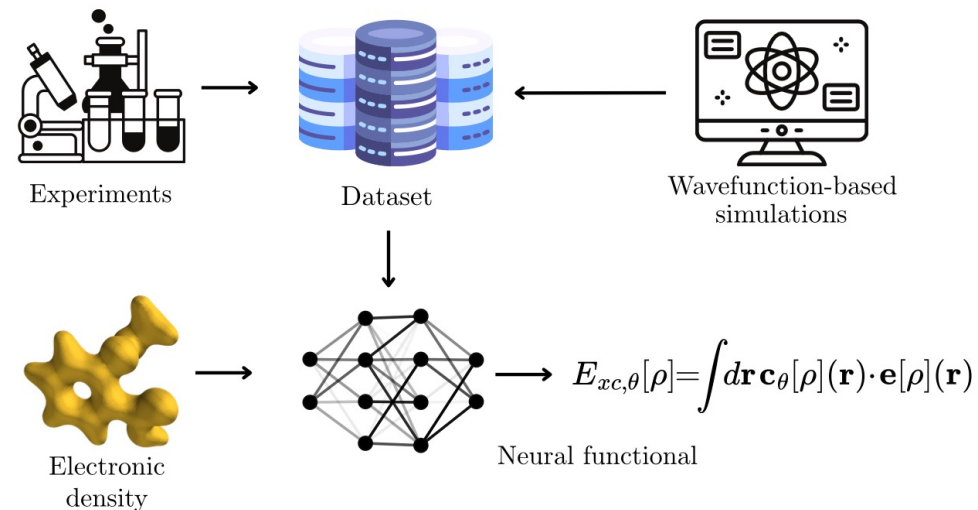
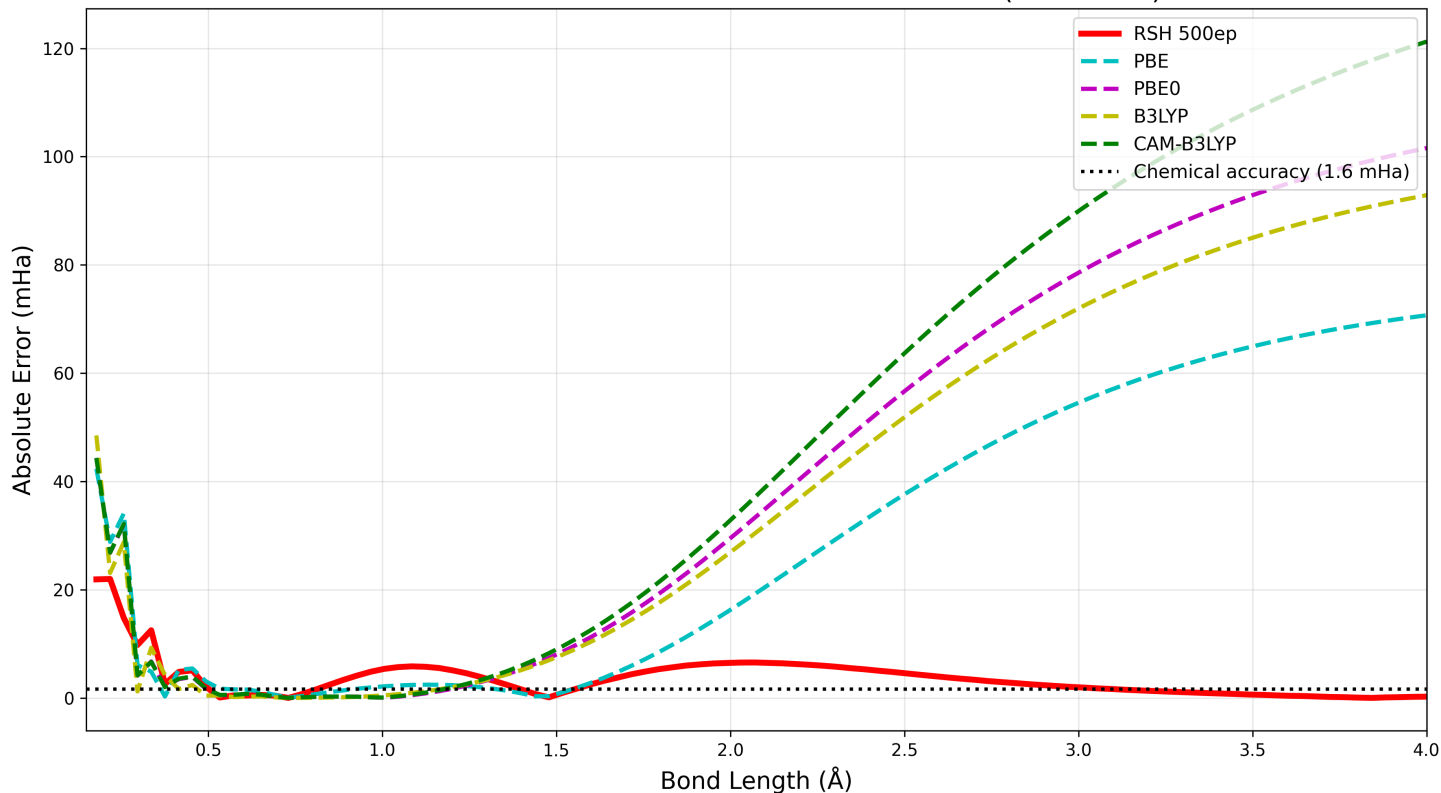
$$\psi_{ex} = \sum_{ai} x_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$

$$\psi_{di} = \sum_{ai} y_{ai} \hat{a}_a^+ \hat{a}_i \psi_{gr}$$



GradTDDFT – GradDFT for Ground State

H2 Dissociation Curve - Functional Errors vs FCI ($r \geq 0.15 \text{ \AA}$)



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Coefficient Functions

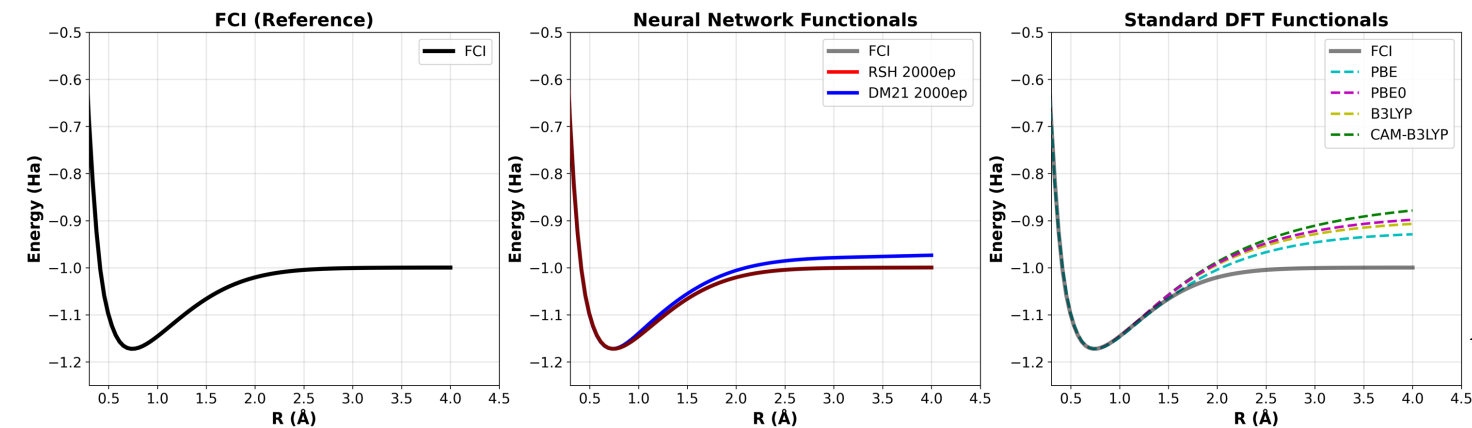
$$c_\theta[\rho](\mathbf{r}) = (c_{1,\theta}[\rho](\mathbf{r}), c_{2,\theta}[\rho](\mathbf{r}) \dots c_{k,\theta}[\rho](\mathbf{r}))$$

Energy Densities

$$e[\rho](\mathbf{r}) = (e_1[\rho](\mathbf{r}), e_2[\rho](\mathbf{r}) \dots e_k[\rho](\mathbf{r}))$$

Loss Function

$$L = \frac{1}{N^2} \sum_i (E_{pre} - E_{true})^2 + \frac{1}{N^2} \sum_i (\rho_{pre} - \rho_{true})^2$$



■ GradTDDFT – Response Kernel with Automatic Differentiation

- Total XC Energy

$$E_{xc}^{\theta}[\rho(\mathbf{r})] = \int d\mathbf{r} e_{xc}^{\theta}[\rho(\mathbf{r})]$$

- XC Energy on grid $e_{xc}^{\theta}[\rho(\mathbf{r})]$

- XC Potential on Grid

$$v_{xc}^{\theta}[\rho(\mathbf{r})] = \frac{\partial e_{xc}^{\theta}[\rho(\mathbf{r})]}{\partial \rho(\mathbf{r})}$$

$$f_{xc}^{\theta}[\rho(\mathbf{r})] = \frac{\partial^2 e_{xc}^{\theta}[\rho(\mathbf{r})]}{\partial \rho^2(\mathbf{r})}$$

- Calculated by jax

`jax.grad()/jax.hessian()`

$$e_{xc}^{\theta}[\rho(\mathbf{r})] \longrightarrow v_{xc}^{\theta}[\rho(\mathbf{r})] \longrightarrow f_{xc}^{\theta}[\rho(\mathbf{r})]$$

```
```python
def point_energy(variables: Array) -> Array:
 rho_point = jnp.maximum(variables[0],
density_floor_value)
 if kind_norm == "LDA":
 grad_point = jnp.zeros((3,),
dtype=variables.dtype)
 tau_point = jnp.asarray(0.0,
dtype=variables.dtype)
 elif kind_norm == "GGA":
 grad_point = variables[1:4]
 tau_point = jnp.asarray(0.0,
dtype=variables.dtype)
 elif kind_norm == "MGGA":
 grad_point = variables[1:4]
 tau_point = jnp.maximum(variables[4], 0.0)
 ...
 return eval_xc_energy_density(spec_norm, features)

return jax.jit(jax.vmap(jax.hessian(point_energy)))
```
```

■ GradTDDFT – Response Kernel with Automatic Differentiation

- LDA

$$E_{xc}[\rho(\mathbf{r})] = \int d\mathbf{r} e_{xc}[\rho(\mathbf{r})]$$

$$f_{xc}[\rho(\mathbf{r})] = \frac{\partial^2 e_{xc}}{\partial \rho^2}$$

- GGA

$$E_{xc} = \int d\mathbf{r} e_{xc}[\rho(\mathbf{r}), \nabla\rho(\mathbf{r})]$$

$$\delta E_{xc} = \int d\mathbf{r} \delta e_{xc}[\rho(\mathbf{r}), \nabla\rho(\mathbf{r})] = \int d\mathbf{r} \frac{\partial e_{xc}}{\partial \rho} \delta\rho + \frac{\partial \nabla e_{xc}}{\partial \nabla\rho} \delta\nabla\rho$$

$$\delta^2 E_{xc} = \int d\mathbf{r} \sum_{\mu\nu} \frac{\partial^2 e_{xc}}{\partial u_\nu \partial u_\mu} \delta u_\nu \delta u_\mu$$

- Meta-GGA

$$E_{xc} = \int d\mathbf{r} e_{xc}[\rho(\mathbf{r}), \nabla\rho(\mathbf{r}), \tau] \quad \tau = -\frac{1}{2} \sum_i |\nabla\psi|^2$$

$$f_{xc} = \frac{\partial^2 e_{xc}}{\partial u_\nu \partial u_\mu} \quad u_\mu = [\rho(\mathbf{r}), \nabla\rho(\mathbf{r}), \tau]$$



■ GradTDDFT– Response Kernel with Automatic Differentiation

- HF Exchange Kernel

$$E_x^{HF} = \int d\mathbf{r} c_x^{hf}[\rho(\mathbf{r})] e_x^{hf}[\phi(\mathbf{r})]$$

$$e_x^{hf}[\phi] = -\frac{1}{2} \sum_{pq} \phi_p^*(\mathbf{r}) \phi_q(\mathbf{r}) \int d\mathbf{r}' \frac{\phi_i^*(\mathbf{r}') \phi_j(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

In A matrix of Casida equation

$$K_{ai,bj} = -\alpha_{eff}(ij|ab) \quad \text{with} \quad \alpha_{eff} = \frac{\int c_x^{hf}[\rho(\mathbf{r})] \rho(\mathbf{r}) d\mathbf{r}}{\int \rho(\mathbf{r}) d\mathbf{r}}$$

- PT2 kernel

$$E_c^{PT2} = \sum_{ia,jb} \frac{(ai|jb)[2(ai|jb) - (ib|ja)]}{\epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b} \rightarrow \int d\mathbf{r} c_c^{pt2}[\rho] e_c^{pt2}[\phi(\mathbf{r})]$$

$$e_c^{PT2} = \sum_{ia,jb} \rho_{ai} V_{jb}(\mathbf{r}) \frac{[2(ai|jb) - (ib|ja)]}{\epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b}$$

$$f_{xc}^{pt2} = \frac{\partial^2 c_c^{pt2}[\rho]}{\partial u_\nu \partial u_\mu} e_c^{pt2}[\phi(\mathbf{r})] + \frac{\partial^2 e_c^{pt2}[\phi(\mathbf{r})]}{\partial u_\nu \partial u_\mu} c_c^{pt2}[\rho]$$



■ GradTDDFT– Response Kernel with Automatic Differentiation

● Approximated PT2 kernel For Double Hybrid XC Functional In TDDFT

$$E_c^{PT2} = \sum_{ia,jb} \frac{(ai|jb)[2(ai|jb) - (ib|ja)]}{\epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b} \rightarrow \int d\mathbf{r} c_c^{pt2}[\rho] e_c^{pt2}[\phi(\mathbf{r})]$$

$$e_c^{PT2} = \sum_{ia,jb} \rho_{ai} V_{jb}(\mathbf{r}) \frac{[2(ai|jb) - (ib|ja)]}{\epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b}$$

$$f_{xc}^{pt2} = \frac{\partial^2 c_c^{pt2}[\rho]}{\partial u_\nu \partial u_\mu} e_c^{pt2}[\phi(\mathbf{r})] + \frac{\partial^2 e_c^{pt2}[\phi(\mathbf{r})]}{\partial u_\nu \partial u_\mu} c_c^{pt2}[\rho] = \frac{\partial^2 c_c^{pt2}[\rho]}{\partial u_\nu \partial u_\mu} e_c^{pt2}[\phi(\mathbf{r})] \rightarrow \text{Fixed Local PT2 Feature}$$

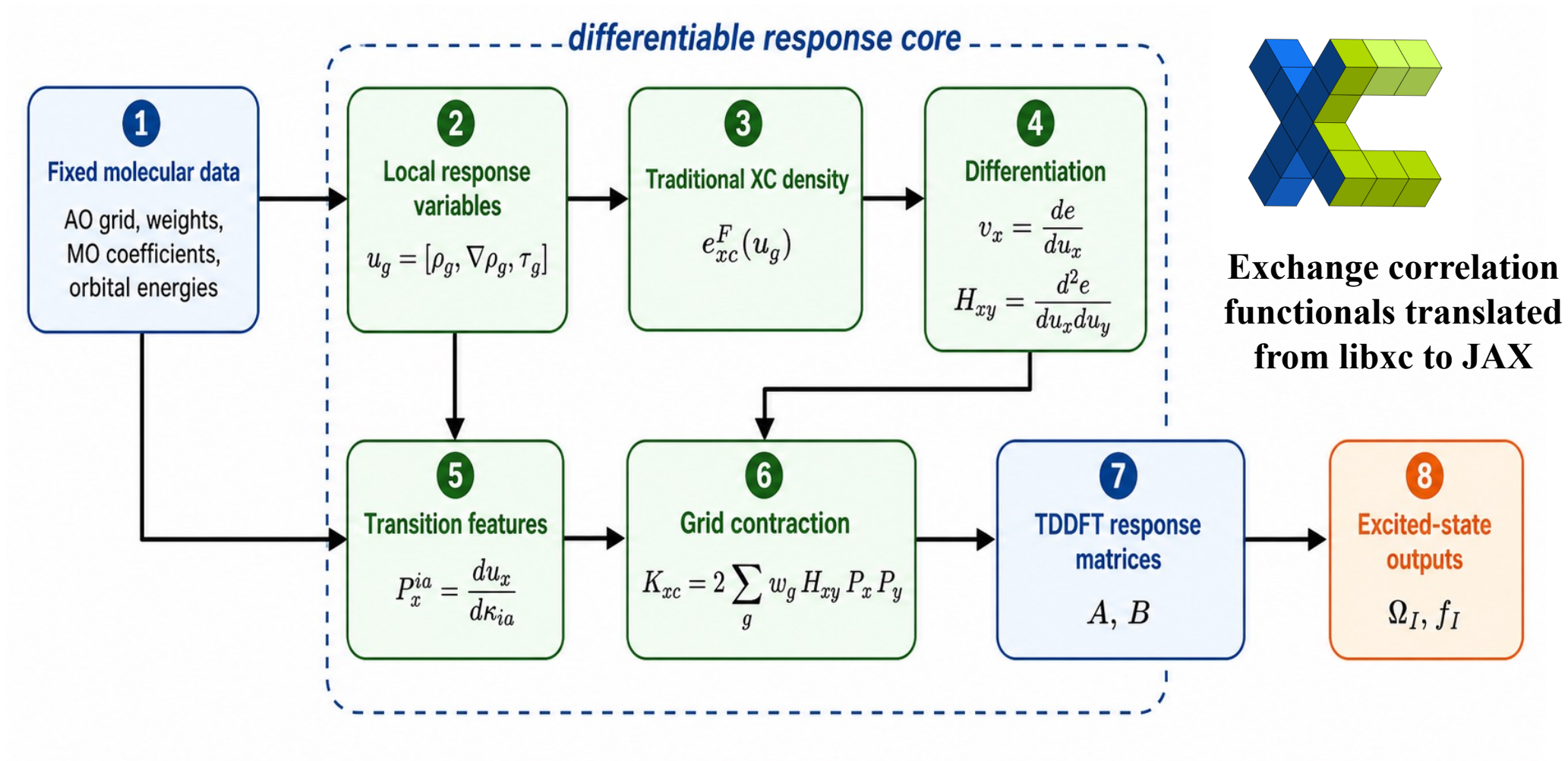
● CIS(D) For Double Hybrid XC Functional In TDDFT

$$\begin{pmatrix} A & B \\ B^* & A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} \quad \text{With } B = X + Y$$

$$\omega_{PT2} = \omega + a_c^\theta \Delta^{PT2} \quad a_c^\theta = \frac{\int c_c^{pt2}[\rho] \rho(\mathbf{r}) d\mathbf{r}}{\int \rho(\mathbf{r}) d\mathbf{r}}$$

$$\Delta^{PT2} = -\frac{1}{4} \sum_{ijab} \frac{U_{ijab}^I}{\epsilon_a + \epsilon_b - \epsilon_j - \epsilon_i - \omega} \quad U_{ijab}^I = \sum_c (ab|cj) B_{ic} - (ab|ci) B_{jc} + \sum_k (ka|ij) B_{kb} - (kb|ij) B_{ka}$$

■ GradTDDFT – Differentiable TDDFT Kernel



[Github.com/STOKES-DOT/GradTDDFT](https://github.com/STOKES-DOT/GradTDDFT)

■ GradTDDFT – Differentiable TDDFT Kernel

Excitation-energy and oscillator-strength agreement

| Molecule | TDA
MAE(Ω) / eV | TDA
MAE(f) | TDDFT
MAE(Ω) / eV | TDDFT
MAE(f) |
|----------|-----------------------------|---------------|-------------------------------|-----------------|
| H2O | 1.31e-11 | 8.37e-09 | 2.97e-11 | 1.76e-08 |
| CO | 3.62e-13 | 7.22e-09 | 6.84e-12 | 2.82e-08 |
| N2 | 5.86e-14 | 1.86e-22 | 3.72e-13 | 3.26e-22 |
| C2H4 | 1.09e-11 | 3.13e-09 | 1.72e-13 | 9.22e-10 |
| CH2O | 1.97e-12 | 8.04e-10 | 8.25e-13 | 3.11e-10 |
| C6H6 | 2.87e-10 | 5.89e-12 | 6.98e-11 | 1.29e-07 |

Excitation-energy and oscillator-strength agreement

| Molecule | TDA
MAE(Ω) / eV | TDA
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MAE(f) |
|----------|-----------------------------|---------------|-------------------------------|-----------------|
| H2O | 1.31e-11 | 8.37e-09 | 2.97e-11 | 1.76e-08 |
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| CH2O | 1.97e-12 | 8.04e-10 | 8.25e-13 | 3.11e-10 |
| C6H6 | 2.87e-10 | 5.89e-12 | 6.98e-11 | 1.29e-07 |

■ GradTDDFT – Training Modes in Neural Network XC Functional

- Ground State

Coefficient Functions

$$c_\theta[\rho](\mathbf{r}) = (c_{1,\theta}[\rho](\mathbf{r}), c_{2,\theta}[\rho](\mathbf{r}) \dots c_{k,\theta}[\rho](\mathbf{r}))$$

Energy Densities

$$e[\rho](\mathbf{r}) = (e_1[\rho](\mathbf{r}), e_2[\rho](\mathbf{r}) \dots e_k[\rho](\mathbf{r}))$$

Loss Function

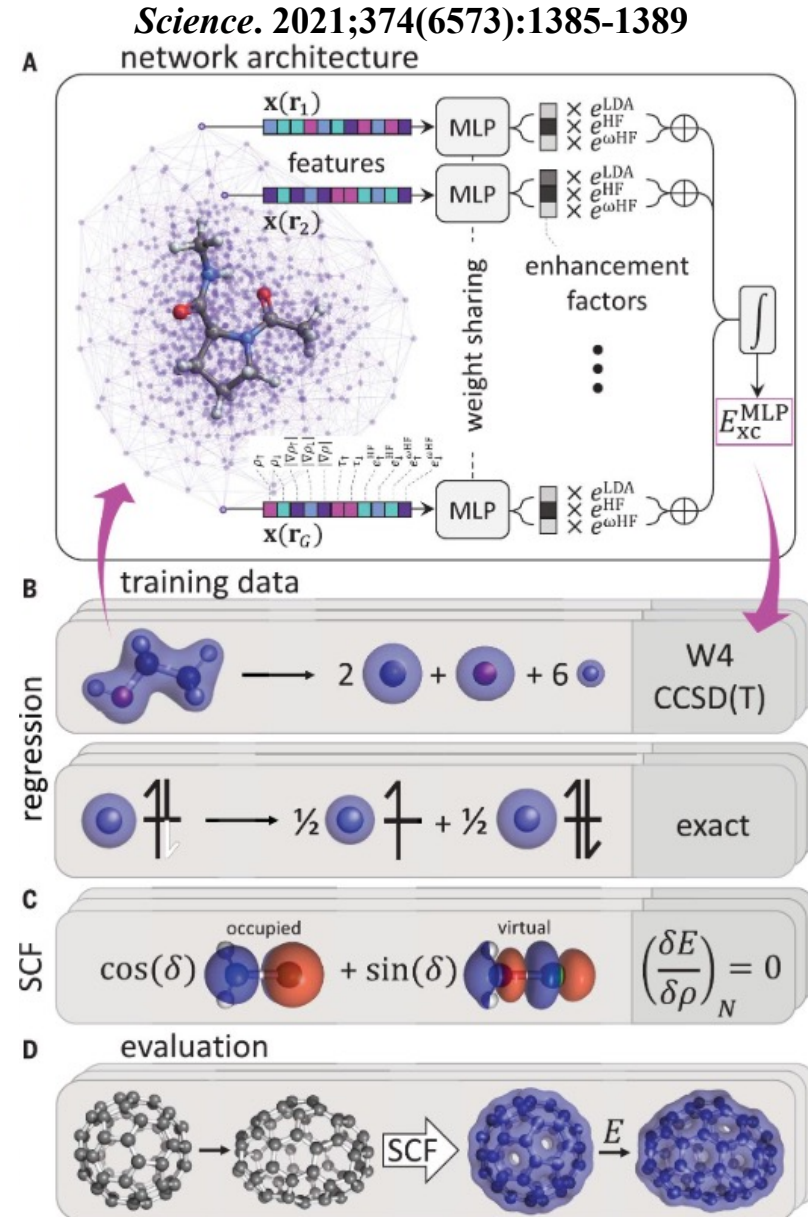
$$L = \frac{1}{N^2} \sum_i (E_{pre} - E_{true})^2 + \frac{1}{N^2} \sum_i (\rho_{pre} - \rho_{true})^2$$

- Excited State

jax.grad(XC)/jax.hessian(XC) on Grids

$$c_\theta[\rho](\mathbf{r}) e_{xc}^\theta[\rho(\mathbf{r})] \longrightarrow v_{xc}^\theta[\rho(\mathbf{r})] \longrightarrow f_{xc}^\theta[\rho(\mathbf{r})]$$

$$L = \frac{1}{N^2} \sum_i (E_{pre} - E_{true})^2 + \frac{1}{N} \sum_i (E_{pre} - E_{true})$$



■ GradTDDFT – Training Modes in Neural Network XC Functional

- Fixed-Density Mode

$$D_\theta = D_{ref}$$

$$L = L(\theta, D) \Big|_{D=D_{ref}}$$

$$\nabla_\theta L = \partial_\theta L(\theta, D) \Big|_{D=D_{ref}} \quad \text{with } \partial_\theta D = 0$$

- Explicit SCF Differential Mode

$$L = L(\theta, D_\theta) \quad \text{with } D_\theta = T_{SCF}^\theta(D_0)$$

$$\nabla_\theta L = \partial_\theta L(\theta, D_\theta) + \partial_{D_\theta} L(\theta, D_\theta) \cdot \partial_\theta D_\theta$$

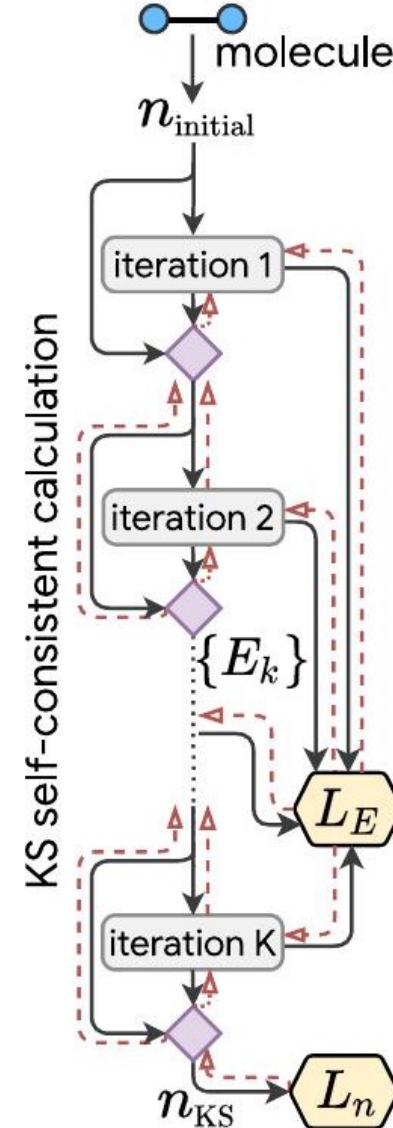
$$\text{with } \partial_\theta D_\theta = \sum_{K-1} [\prod_{s=t+1}^{K-1} \partial_D T_{SCF}^\theta(D^s)] \partial_\theta T_{SCF}^\theta(D^t)$$

- Implicit SCF Differential Mode

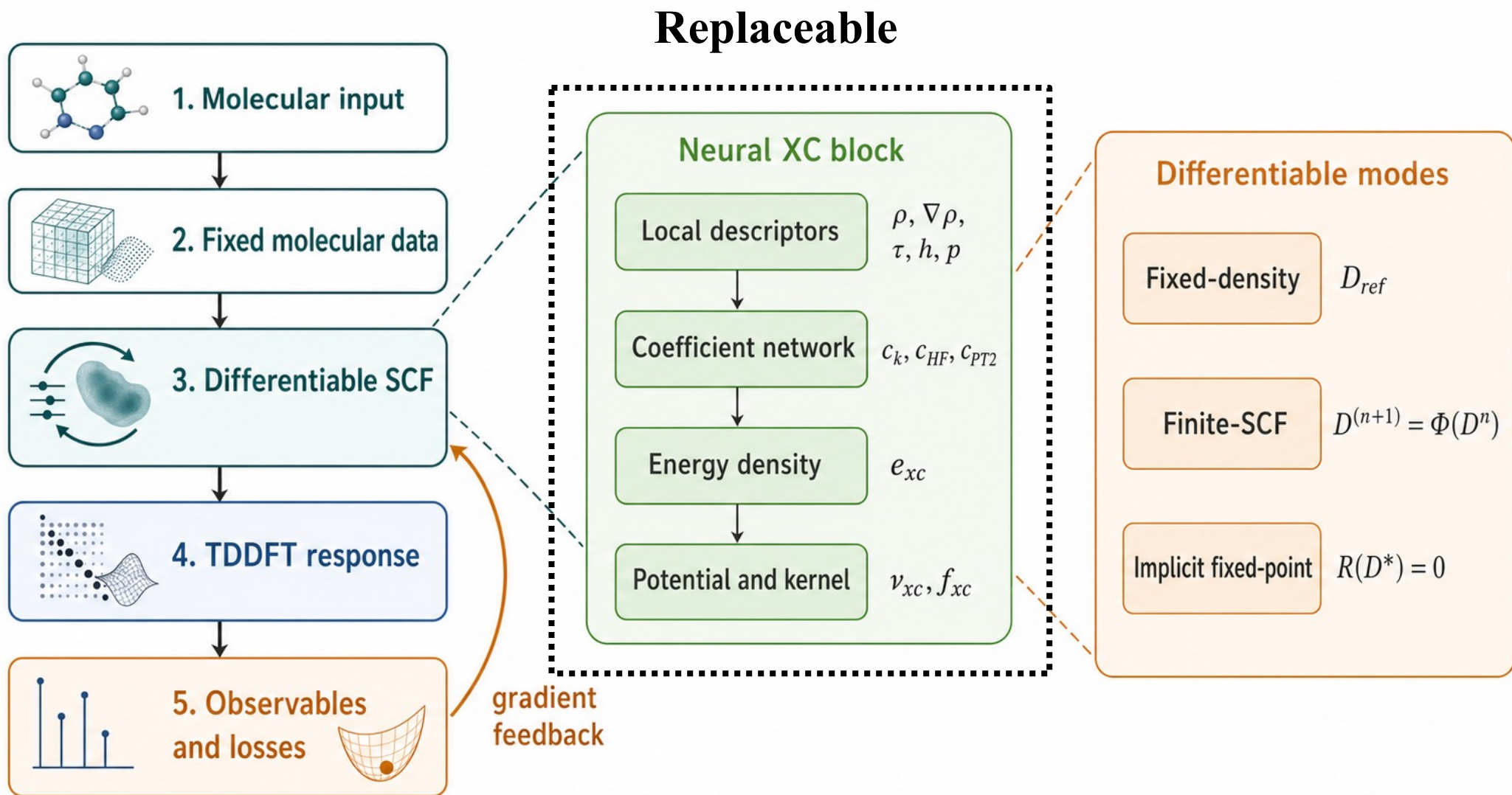
$$L = L(\theta, D_\theta) \quad \text{with } D_\theta = T_{SCF}^K(D_0)$$

$$R(D_\theta, \theta) = F_\theta(D_\theta)D_\theta S - SD_\theta F_\theta(D_\theta) = 0$$

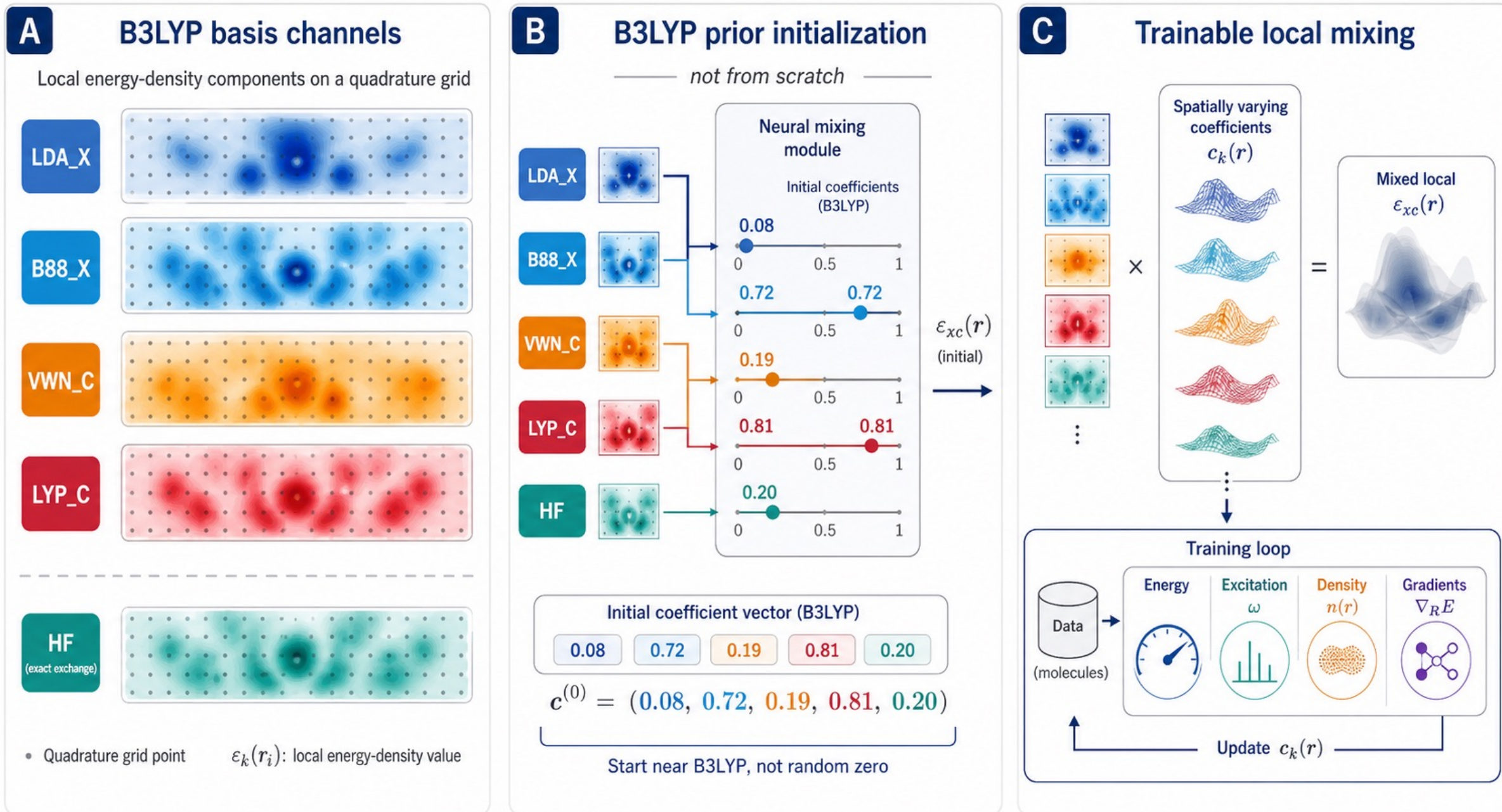
$$\nabla_\theta L = \partial_\theta L(\theta, D_\theta) + \partial_{\rho_\theta} L(\theta, D_\theta) \frac{\partial_\theta R}{\partial_{D_\theta} R}$$



■ GradTDDFT – Training Modes in Neural Network XC Functional



■ GradTDDFT – Training Modes in Neural Network XC Functional



■ GradTDDFT – Training Modes in Neural Network XC Functional

- Implicit SCF for H_2^+ Ground State with def2-SVP, grid level = 2

- N-electron system

$$v_{\text{eff}}(\mathbf{r}, \mathbf{R}) = v_{\text{ext}}(\mathbf{R}) + \int d\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + v_{\text{xc}}(\mathbf{r})$$

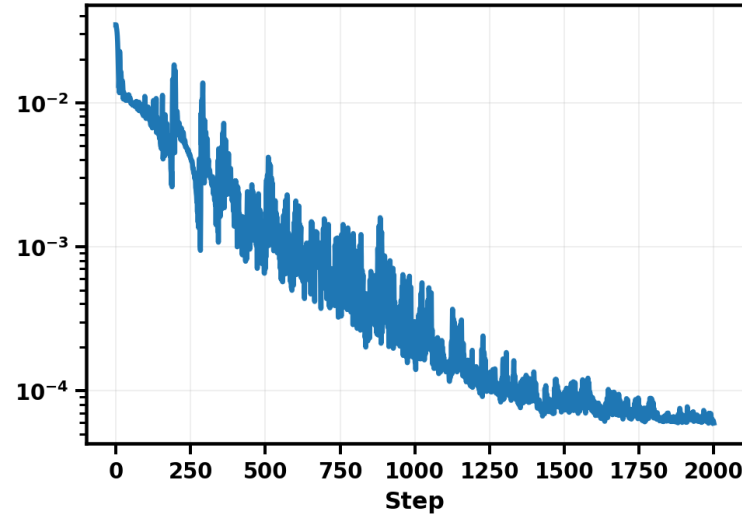
- One-electron system ($|\mathbf{r}| \rightarrow \infty$)

$$v_{\text{eff}}(\mathbf{r}, \mathbf{R}) = v_{\text{ext}}(\mathbf{R}) + \frac{1}{|\mathbf{r}|} + v_{\text{xc}}(\mathbf{r})$$

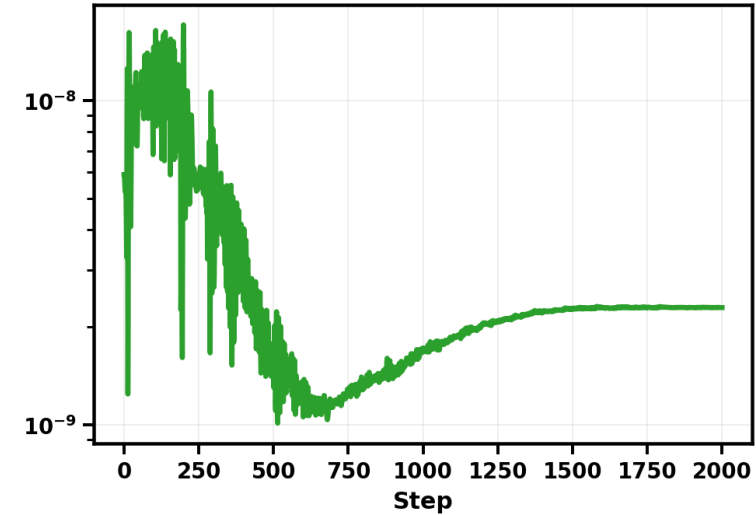
- Loss Function

$$L = \frac{1}{N} \sum |E_{\text{NN}} - E_{\text{FCI}}| + \frac{1}{N^2} \sum (E_{\text{NN}} - E_{\text{FCI}})^2 + \frac{1}{N^2} \sum (\rho_{\text{NN}} - \rho_{\text{FCI}})^2$$

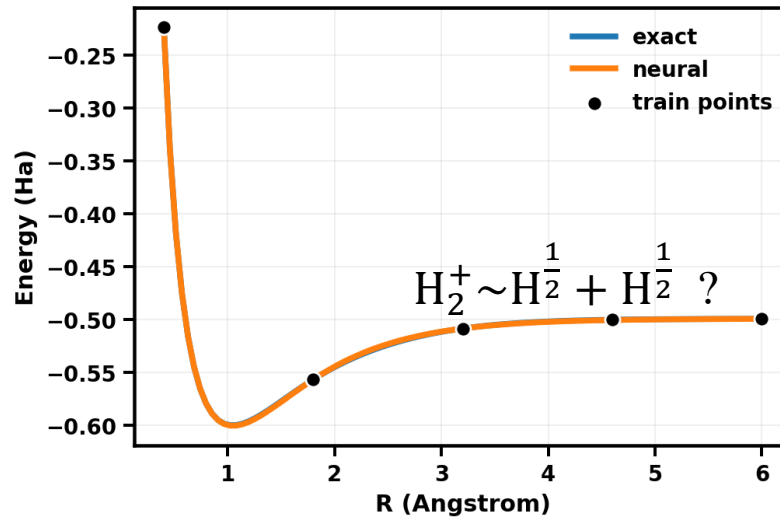
Training Total Loss



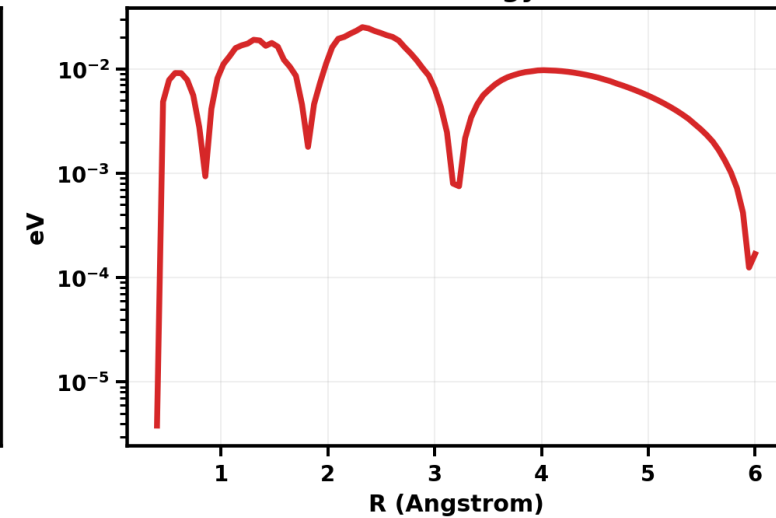
Density Constraint Penalty



Ground-State Curve



Absolute Energy Error



■ GradTDDFT – Training Modes in Neural Network XC Functional

- Implicit SCF for H₂ Ground State with def2-SVP, grid level = 2

- **Static Correlation Error**

σ_g^2 Binding Orbital

σ_u^2 Antibinding Orbital

- **MCSCF**

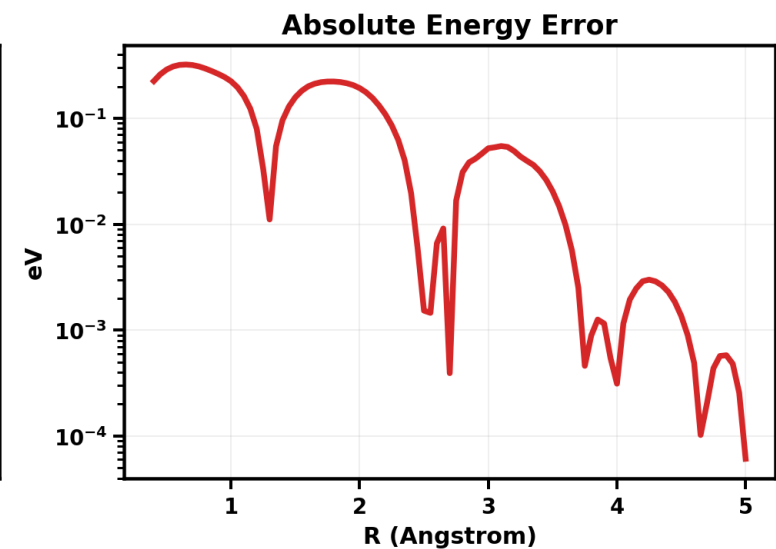
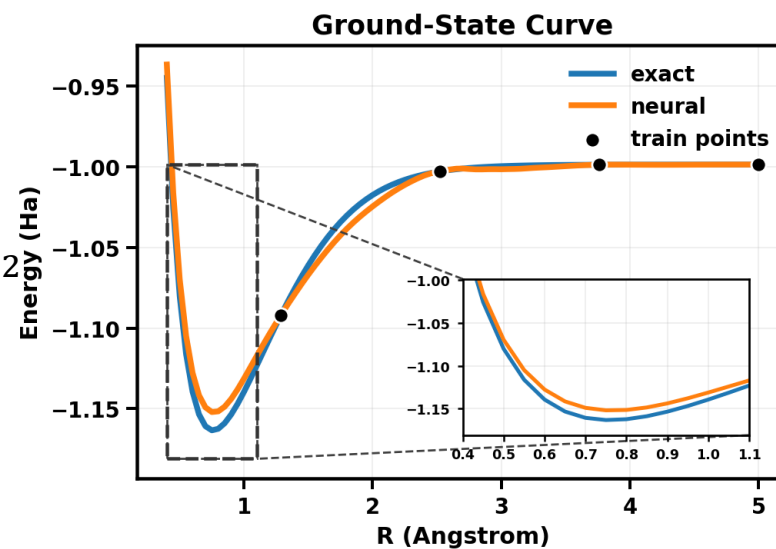
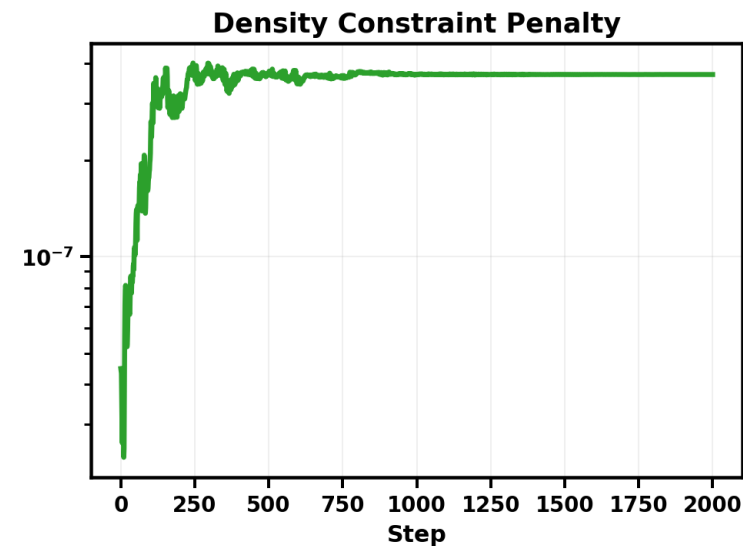
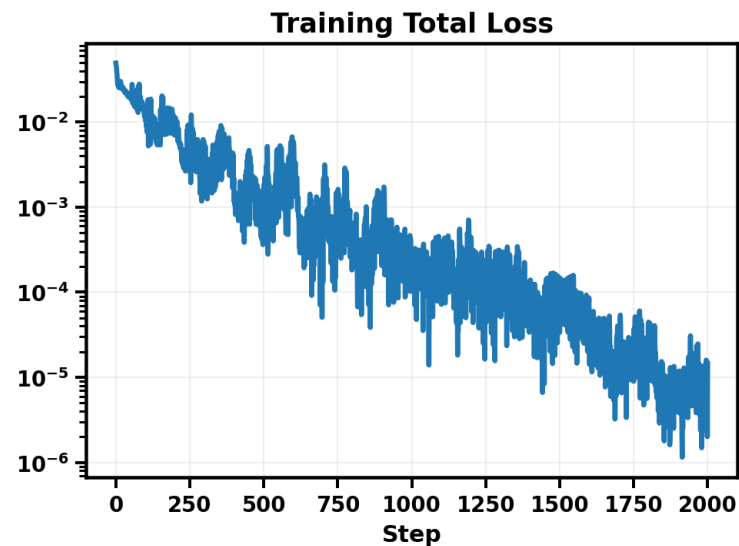
$$\psi = c_u \phi(\sigma_g^2) + c_u \phi(\sigma_u^2)$$

- **Hartree-Fock**

$$\psi_1 = \phi(\sigma_g^2) \quad \psi_2 = \phi(\sigma_u^2)$$

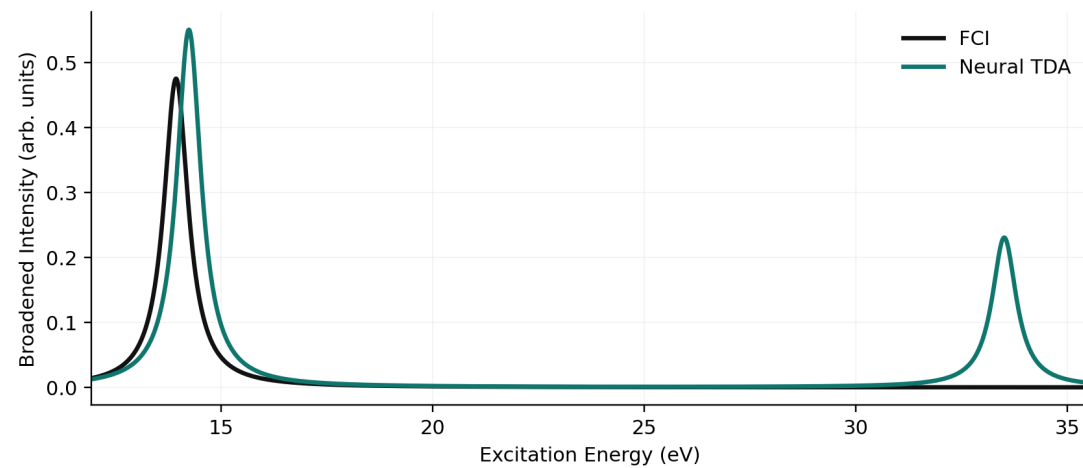
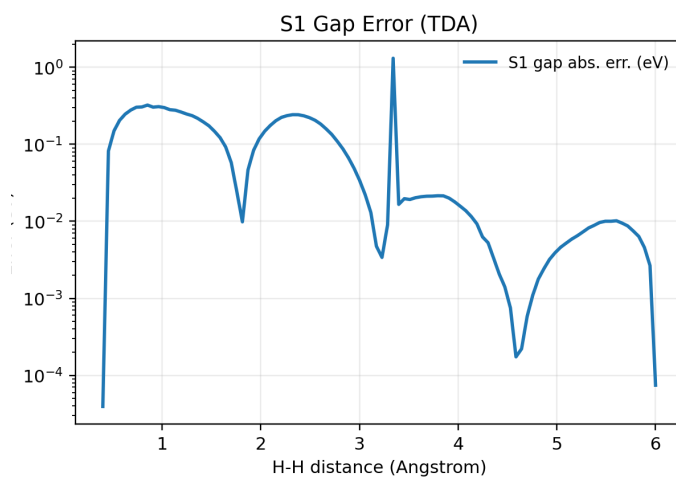
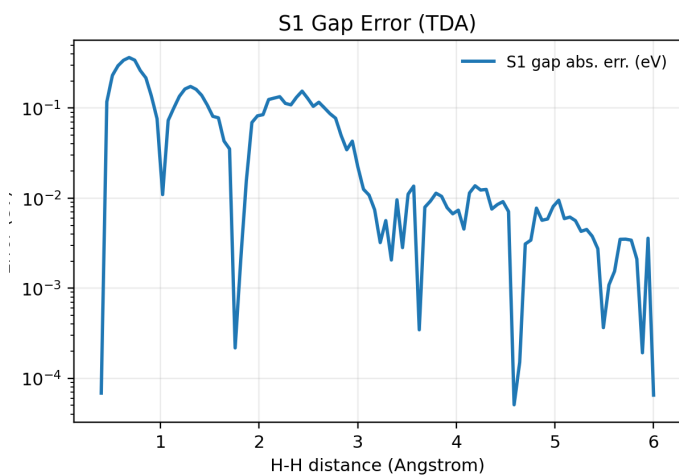
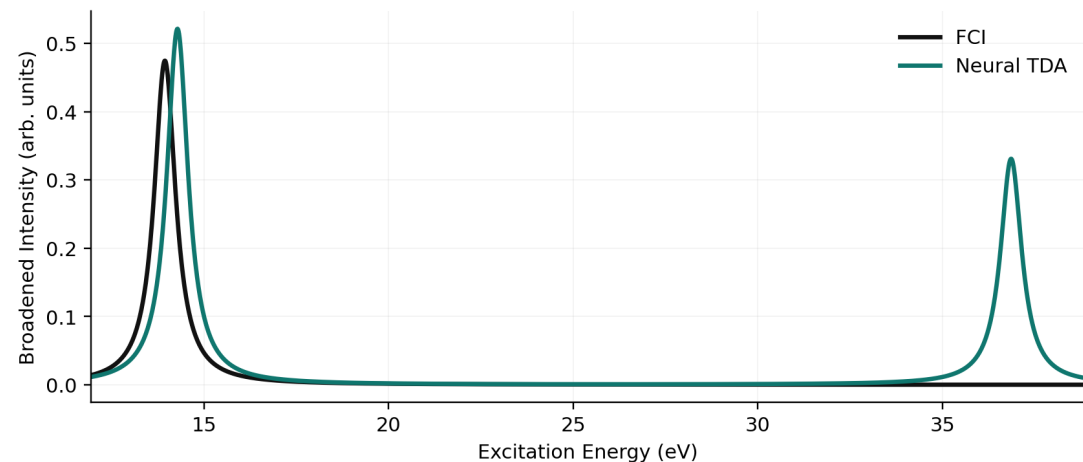
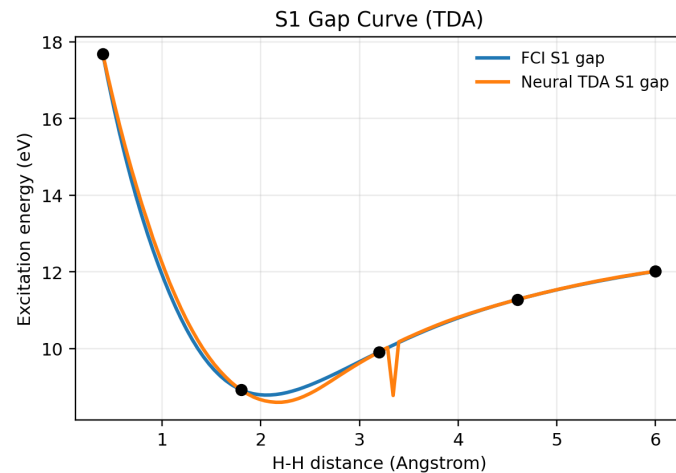
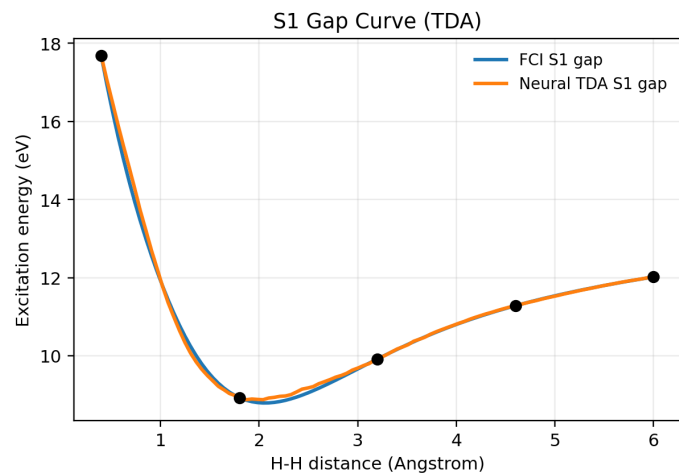
- **Loss Function**

$$L = \frac{1}{N} \sum |E_{NN} - E_{FCI}| + \frac{1}{N^2} \sum (E_{NN} - E_{FCI})^2 + \frac{1}{N^2} \sum (\rho_{NN} - \rho_{FCI})^2$$



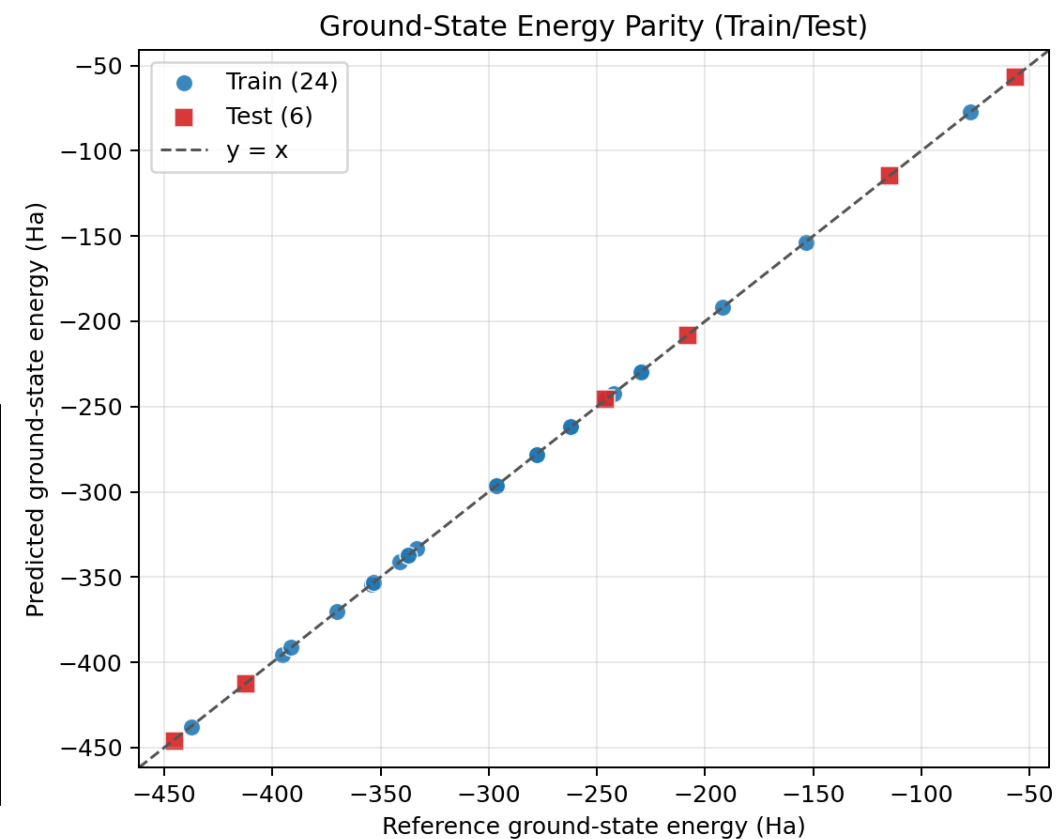
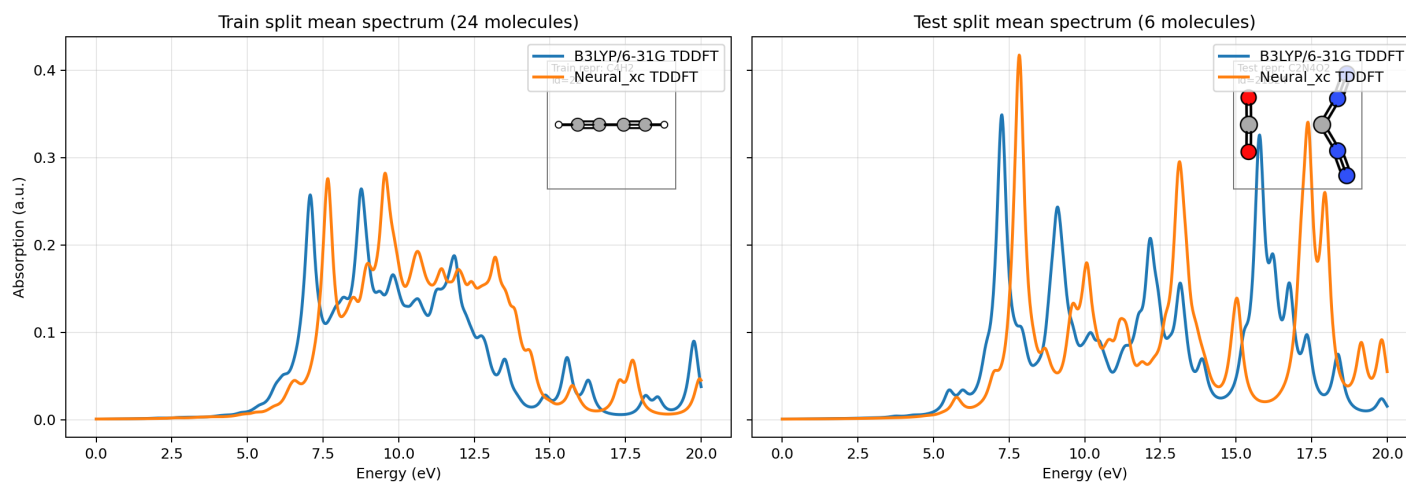
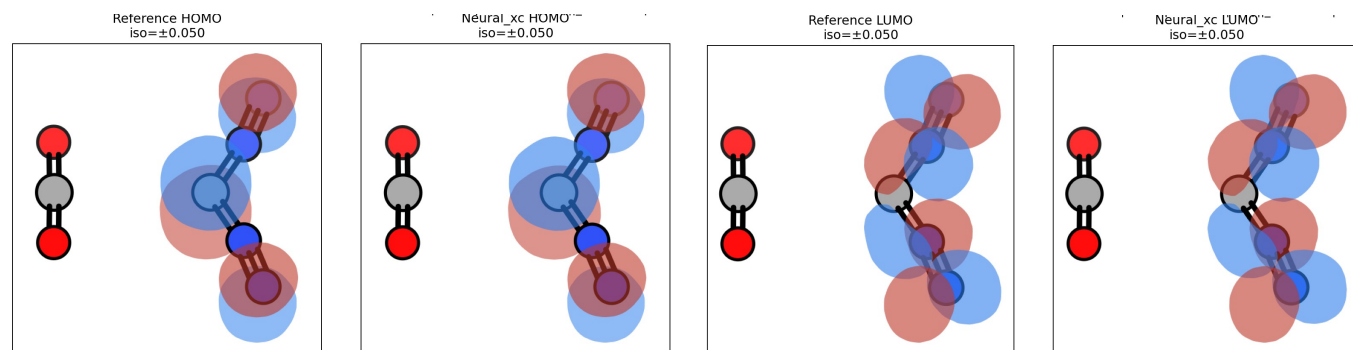
■ GradTDDFT – Training Modes in Neural Network XC Functional

- Implicit SCF +Explicit TDA for S_1 of H_2 with def2-SVP, grid level = 2



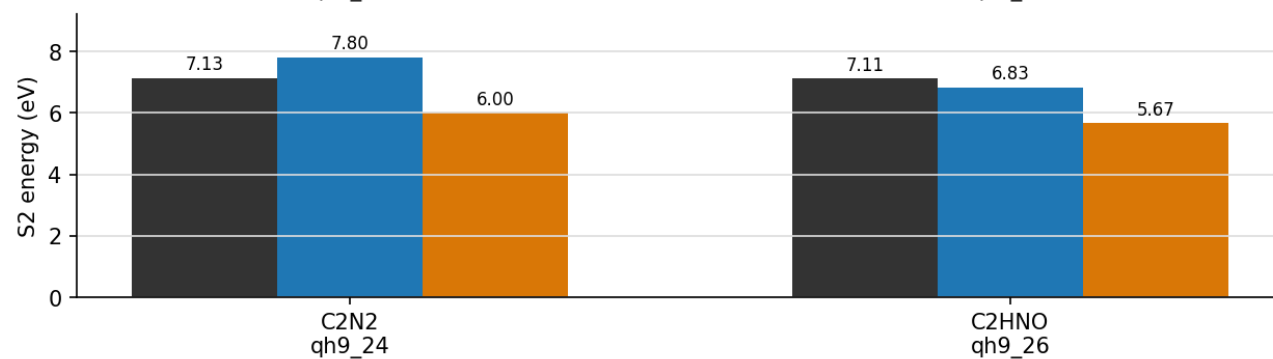
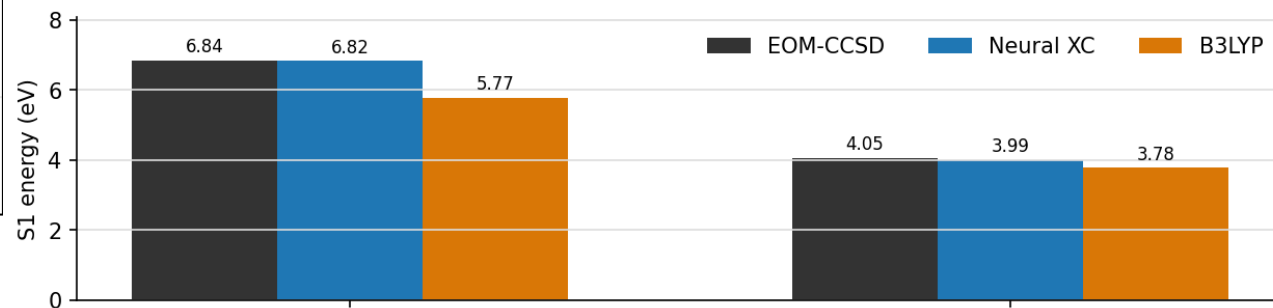
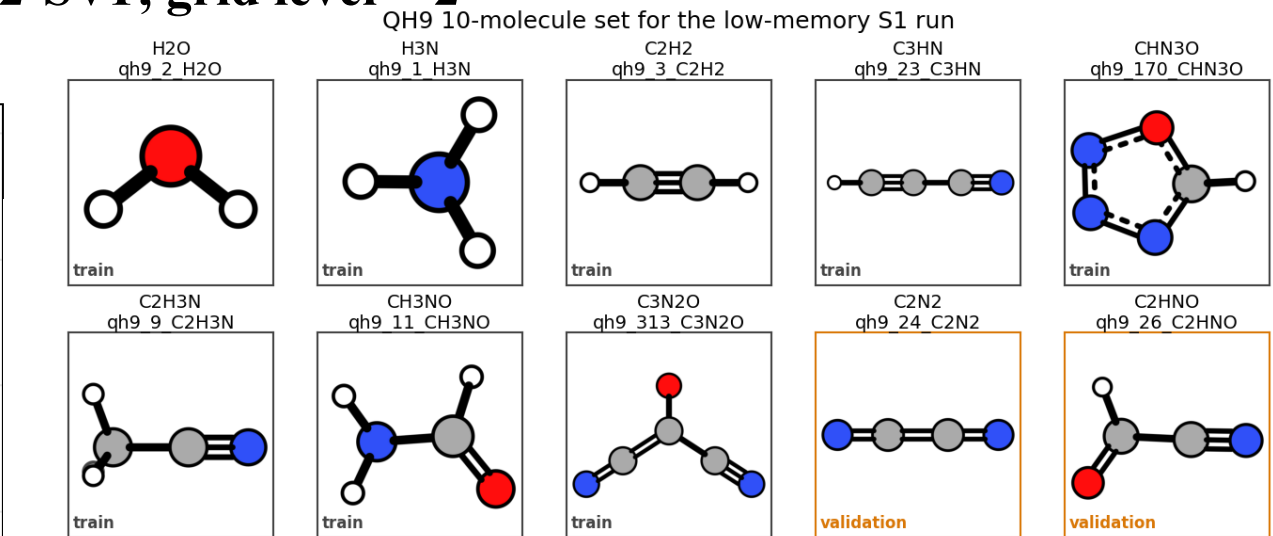
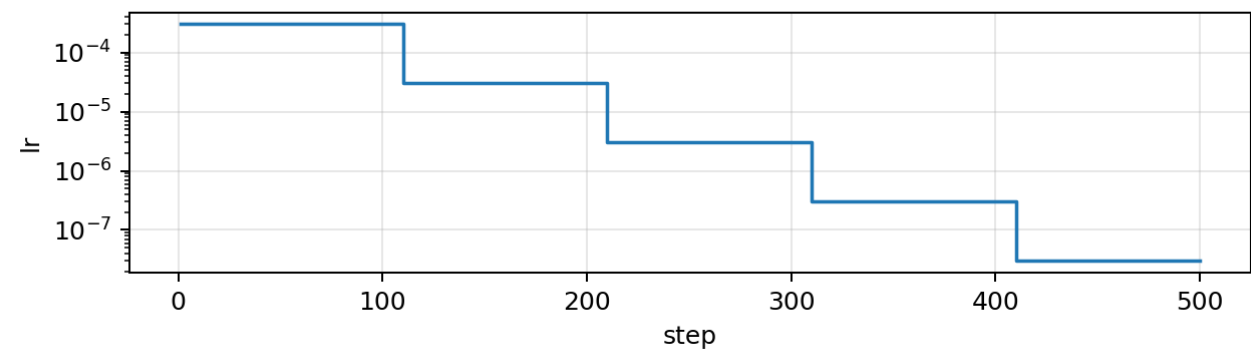
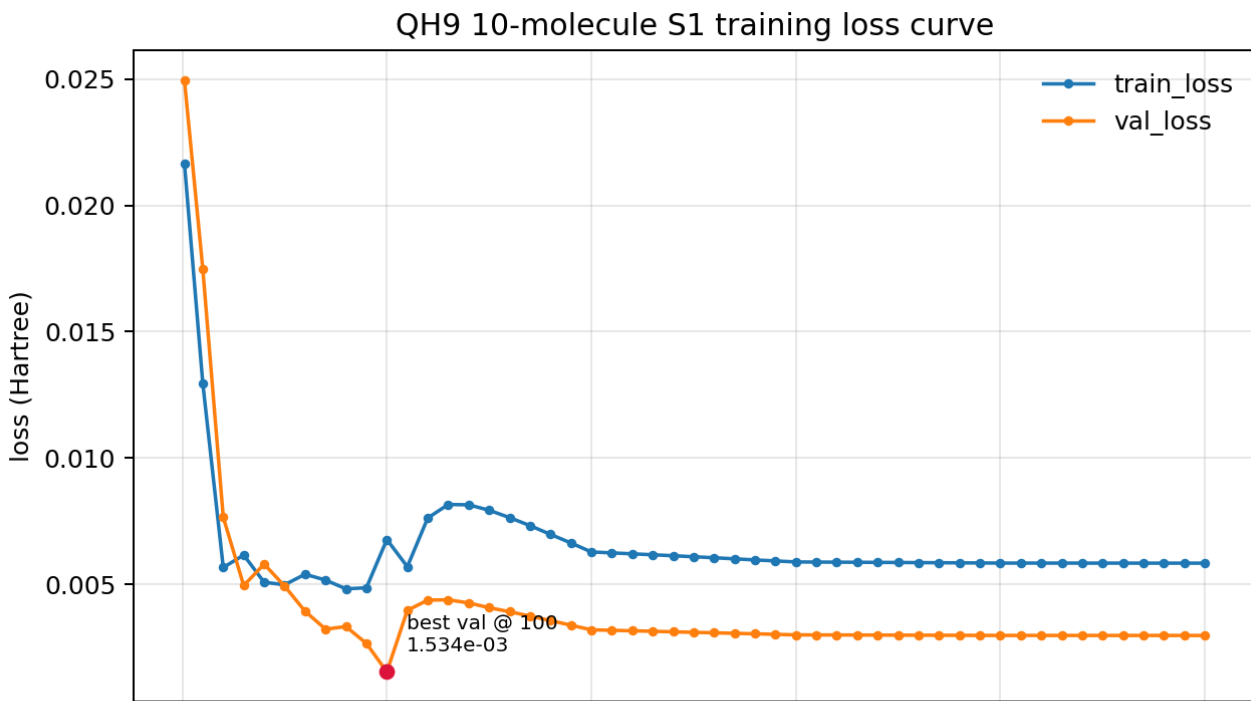
■ GradTDDFT – Training Modes in Neural Network XC Functional

● Fixed Density for Ground State-QM9



■ GradTDDFT – Training Modes in Neural Network XC Functional

- Implicit SCF +Explicit TDA for S_1 of QM9 with def2-SVP, grid level = 2



TD-GradDFT – Failure of Full Absorption Spectrum Calculation

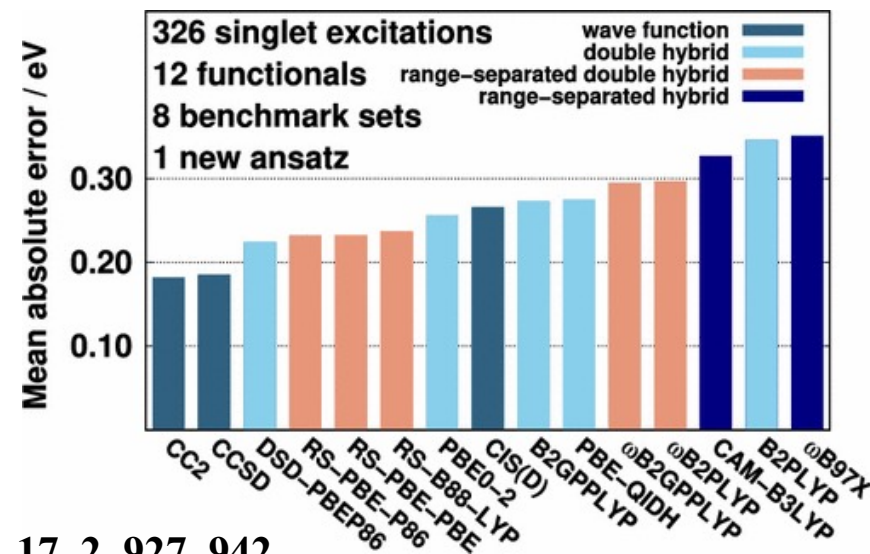
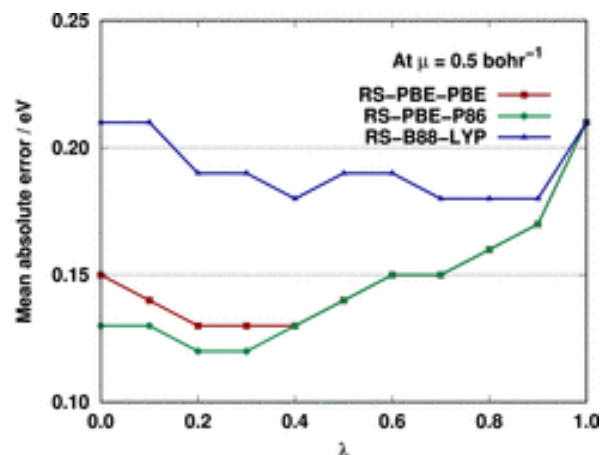
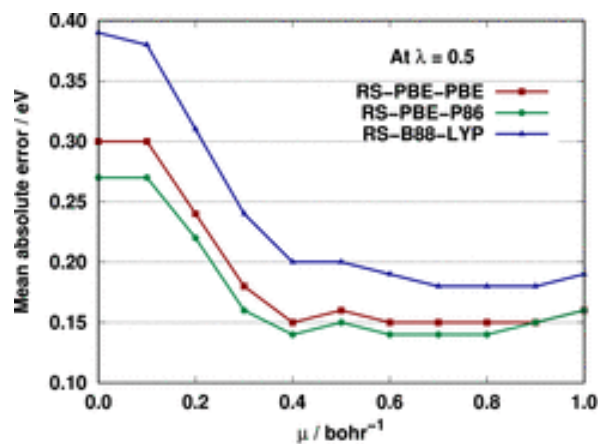
- TDDFT is not a rigorous theorem for excited state wave function

$$\psi_{ex}^{CIS} = \phi_0 + \sum_{ai} x_{ai} \phi_a^i$$

$$\psi_{ex}^{FCI} = \phi_0 + \sum_{ai} c_{ai} \phi_a^i + \sum_{aibj} c_{aibj} \phi_{ab}^{ij} + \sum_{aibjck} c_{aibjck} \phi_{abc}^{ijk} + \dots$$

- No Ground Truth has a good performance both on ground state and excited state for complex electron configuration

But !



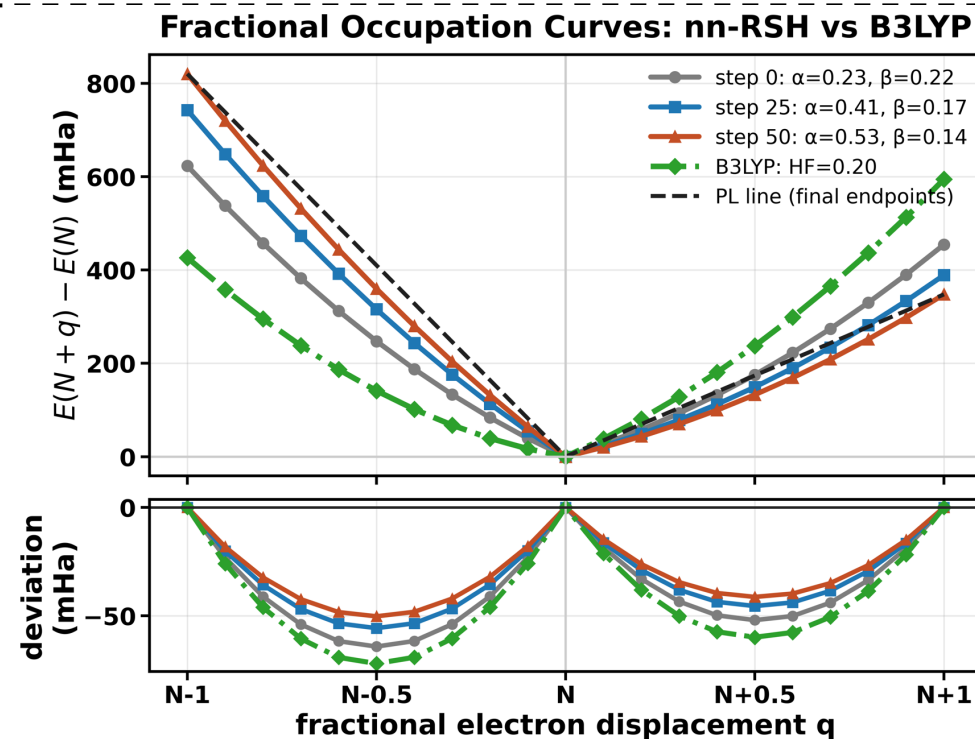
■ GradTDDFT – Functional and Outlook

● Functional

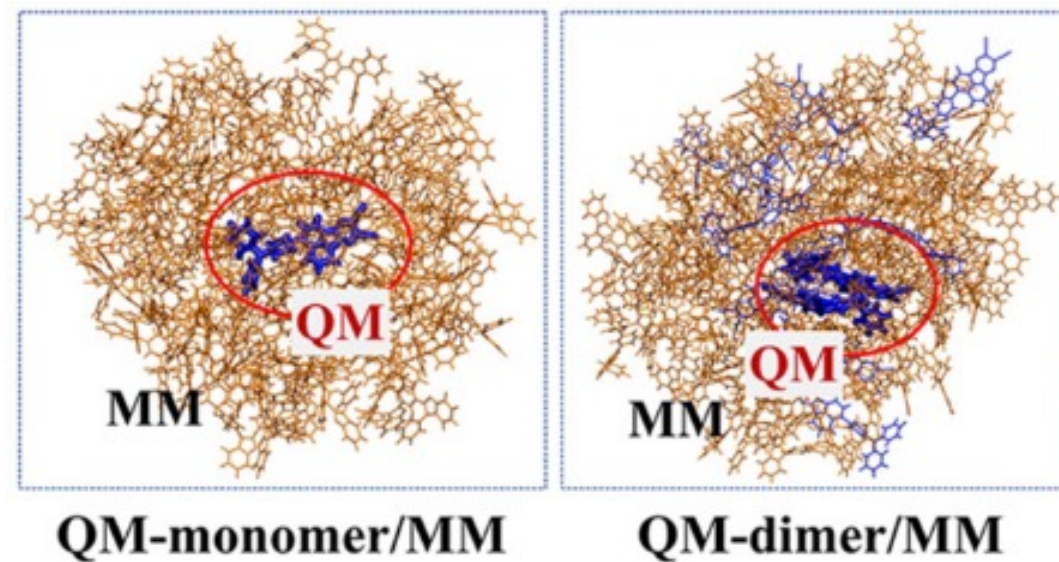
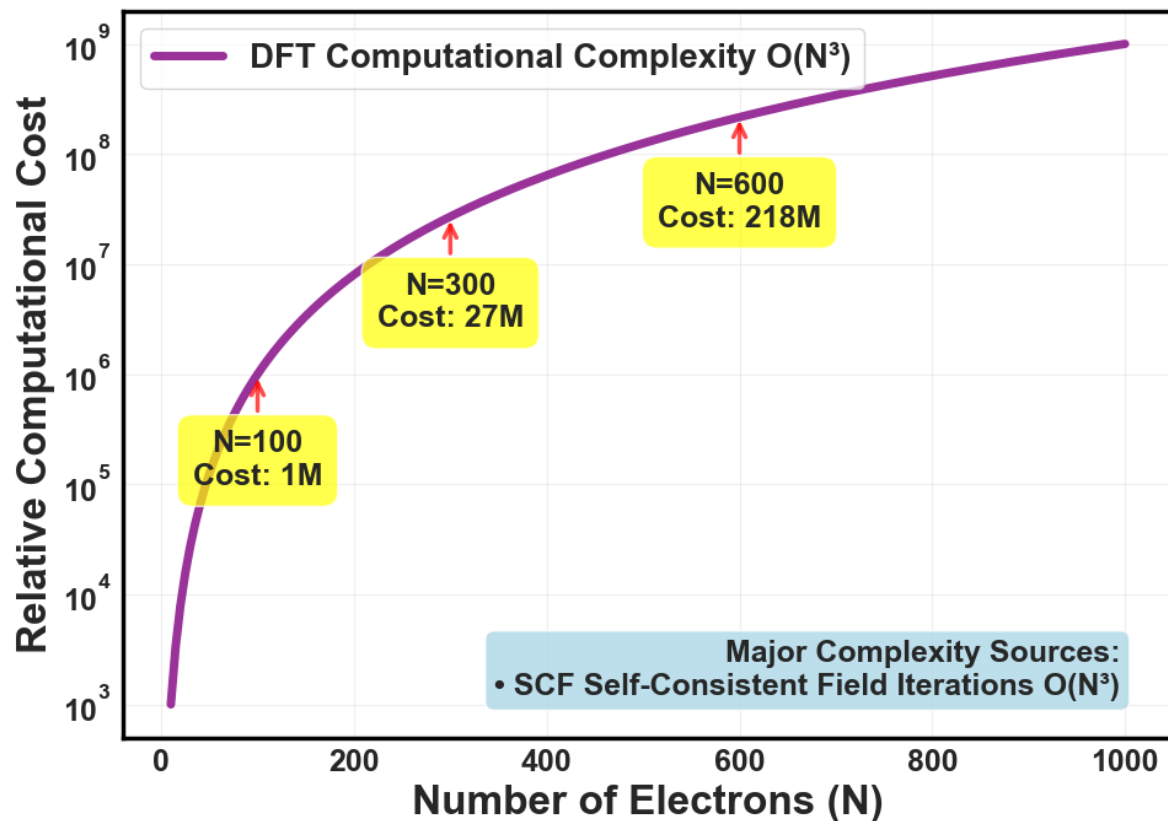
- Differential SCF code with three modes and differential LR-TDDFT code
- HF and PT2 local energy density hybrid and CIS(D) based TDDFT for Double Hybrid Functional
- GPU/CPU Integral Modules for DFT/TD-DFT
- General XC Functional Library based on JAX-XC and General Base Set Library form PySCF
- Fractional charge evaluation and differential unrestricted SCF code

● Outlook

- Lower GPU Memory Usage for Large Systems!(Hard For Most Differentiable DFT)
- Automatic Differentiation for Geometry Optimization and Response Properties of molecules
- General Neural Network Designing, Training, Evaluating Framework for Quantum Chemistry-GradSCF



■ Equivariance in Neural Network – Covariance in DFT Hamiltonian



Phys Chem Chem Phys. 2024;26(26):18418-18425

■ Equivariance in Neural Network – Covariance in DFT Hamiltonian

Kohn-Sham Density Functional Theory

$$v_{ext}(\mathbf{x}, \{\mathbf{R}\}) \Leftrightarrow \rho(\mathbf{x}) \Leftrightarrow \{\psi_i(\mathbf{x})\}$$

$$\hat{H} = \hat{H}_0 + \hat{V} \quad \rho(\mathbf{x}) = \sum_i^N \psi_i^*(\mathbf{x})\psi_i(\mathbf{x})$$

$$\rho(\mathbf{x}, \mathbf{x}') = \sum_i^N \psi_i^*(\mathbf{x})\psi_i(\mathbf{x}')$$

$$\left[-\frac{1}{2}\nabla^2 + v_{ext}(\mathbf{x}, \{\mathbf{R}\}) + v_H(\mathbf{x}) + v_{xc}(\mathbf{x}) \right] \psi_i(\mathbf{x}) = \varepsilon_i \psi_i(\mathbf{x})$$



Phys. Rev. B 136, 864 (1964).

Atomic Basis Function

Hamiltonian Matrix in Atomic Basis Function

$$\psi_i(\mathbf{x}) = \sum_a C_{ai} \chi_a(\mathbf{x}) \quad HC = \varepsilon SC$$

$$H = H_{ij} = \sum_{ab} C_{ai}^* C_{bj} \chi_i^*(\mathbf{x}) \hat{H} \chi_j(\mathbf{x})$$

Equivariance in Atomic Basis Function

$$\chi_j(\mathbf{x}) = R_{nl}(r) Y_{ml}(\theta)$$

$$Y_{ml}(\theta') = \sum_{m'=-l}^l D_{m'm}^l Y_{m'l}(\theta)$$

$$\chi_j(\mathbf{R} \cdot \mathbf{x}) = \mathbf{D}(\mathbf{R}) \chi_j(\mathbf{x})$$



Covariance in DFT Hamiltonian Matrix

$$H' = H'_{ij} = \sum_{ab} C_{ai}^* C_{bj} \chi_i^*(\mathbf{R} \cdot \mathbf{x}) \hat{H} \chi_j(\mathbf{R} \cdot \mathbf{x})$$

$$H' = \mathbf{D}^T(\mathbf{R}) \mathbf{H} \mathbf{D}(\mathbf{R})$$

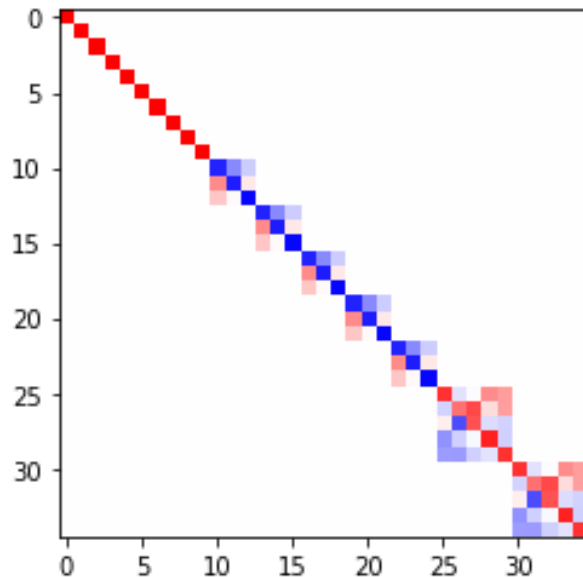
■ Equivariance in Neural Network – Rotation Matrix in Winger-D Representation

Rotation Matrix in Euler Representation

$$\mathcal{M}(\alpha, \beta, \gamma) = \mathcal{R}_z(\alpha)\mathcal{R}_x(\beta)\mathcal{R}_z(\gamma)$$

$$\begin{matrix} \cos \alpha \cos \gamma - \cos \beta \sin \alpha \sin \gamma & -\cos \beta \cos \gamma \sin \alpha - \cos \alpha \sin \gamma & \sin \alpha \sin \beta \\ = \cos \gamma \sin \alpha + \cos \alpha \cos \beta \sin \gamma & \cos \alpha \cos \beta \cos \gamma - \sin \alpha \sin \gamma & -\cos \alpha \sin \beta \\ \sin \beta \sin \gamma & \cos \gamma \sin \beta & \cos \beta \end{matrix}$$

Rotation Matrix in Winger-D Representation



Irreducible representation

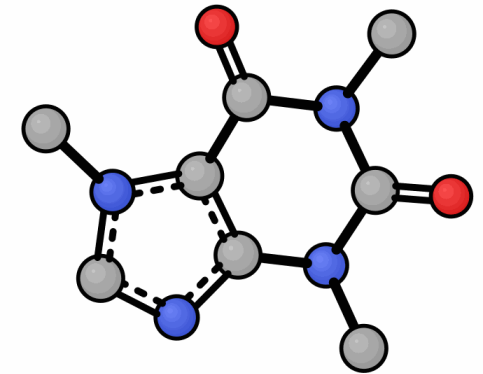
$$10x0e + 5x1o + 2x2e$$



10 Even Scalars, 5 Odd Vectors, 2 Even Second-Order Tensors



$$D^l = 10D^0 \oplus 5D^1 \oplus 2D^3$$



■ Equivariance in Neural Network – Tensor Field Network

● Tensor Product in SO(3) Representation-Wigner-Eckert Theorem

$$v_1^{l_1} \otimes v_1^{l_2} = \sum_{m_1=-l_1}^{l_1} \sum_{m_2=-l_2}^{l_2} C_{l_1, m_1, l_2, m_2}^{l_3, m_3} v_{1, m_1}^{l_1} v_{2, m_2}^{l_2}$$

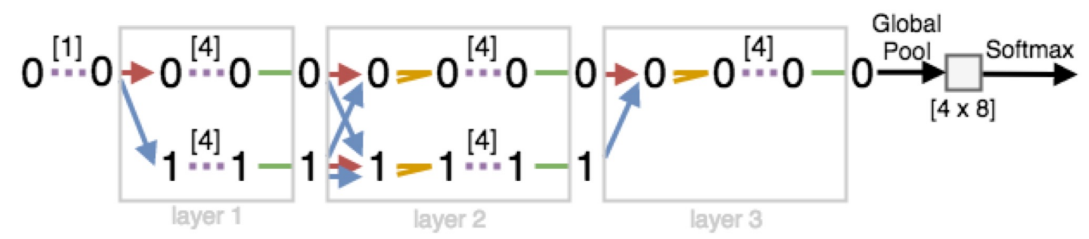
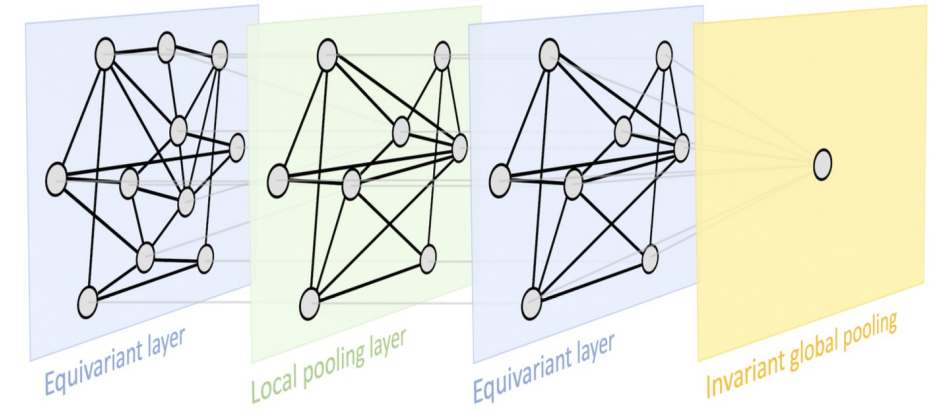
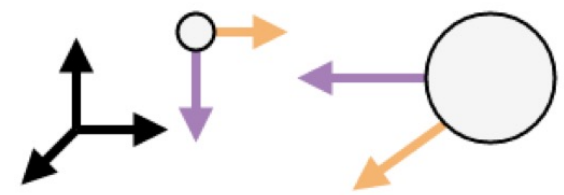
$$v_1^{l_1} \otimes v_1^{l_2} = v^{|l_1-l_2|} \oplus v^{|l_1-l_2|+1} \oplus v^{|l_1-l_2|+2} \oplus \dots \oplus v^{|l_1+l_2|}$$

● Message Passing in TFN

$$f_i' = \frac{1}{\sqrt{Z}} \sum_{N_i} f_j \otimes h(\|\vec{x}_{ij}\|) Y\left(\frac{\vec{x}_{ij}}{\|\vec{x}_{ij}\|}\right)$$

$$V_{acm}^{(l)} = \{0: [[\mathbf{m0}], [\mathbf{m1}]], 1: [[\mathbf{v0x}, \mathbf{v0y}, \mathbf{v0z}], [\mathbf{a0x}, \mathbf{a0y}, \mathbf{a0z}], [\mathbf{v1x}, \mathbf{v1y}, \mathbf{v1z}], [\mathbf{a1x}, \mathbf{a1y}, \mathbf{a1z}]]\}$$

l : dictionary key, l
 [] point index, a
 [] channel index, c
 [] representation index, m

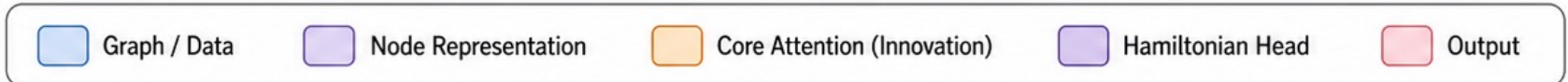
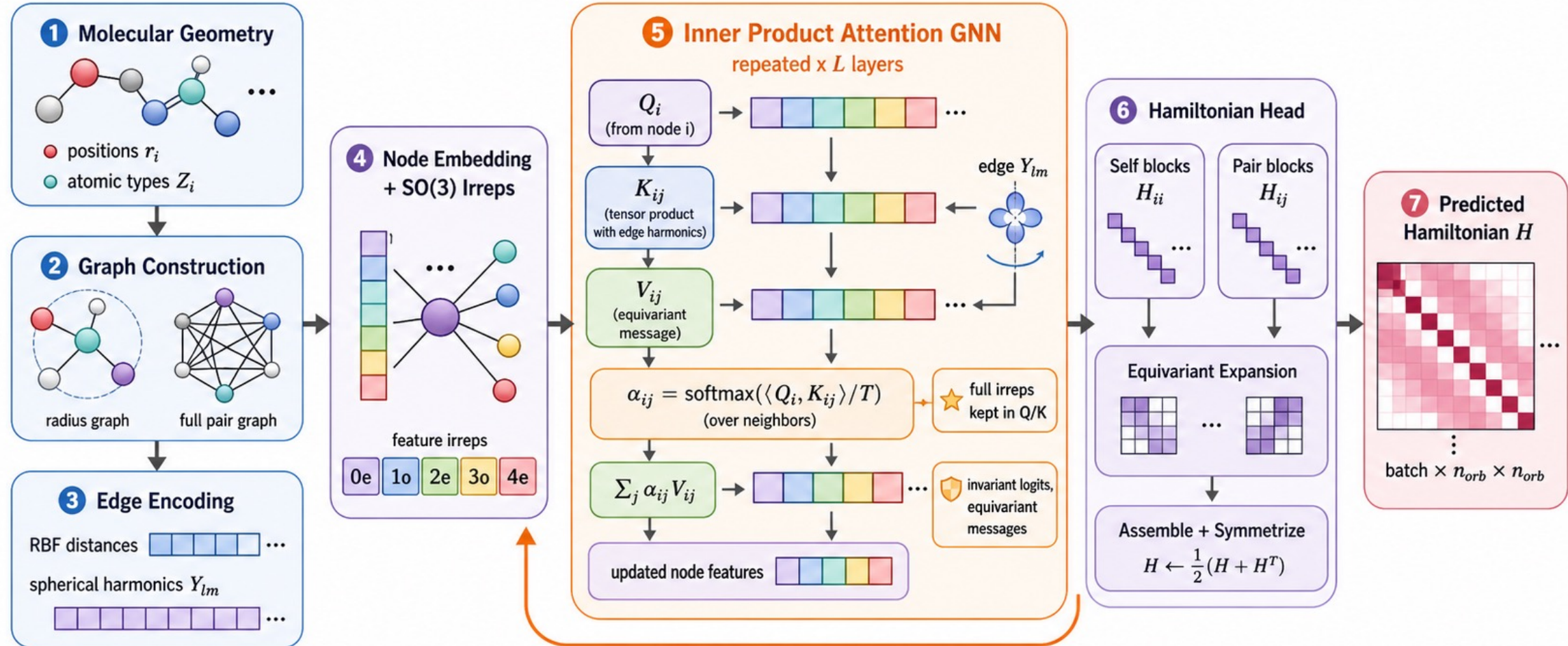


Key
 → L=0 Convolution → Self-interaction → Concatenation
 → L=1 Convolution → Nonlinearity → Fully Connected

■ Equivariance in Neural Network – Basic Architecture of QHformer

QHformer Model Architecture

SO(3)-Equivariant Hamiltonian Prediction with Inner Product Attention



■ Equivariance in Neural Network – Basic Architecture of QHformer

InnerProduct Attention Mechanism

$$q_i = \text{Linear}(x_i)$$

$$k_j = \text{TP}(x_j, Y(r_{ij}))$$

$$\text{IP}(q_i, k_j) = \sum_l \sum_m q_i^{(l,m)} \cdot k_j^{(l,m)}$$

$$v_j = \text{TP}(x_j, Y(r_{ij}))$$

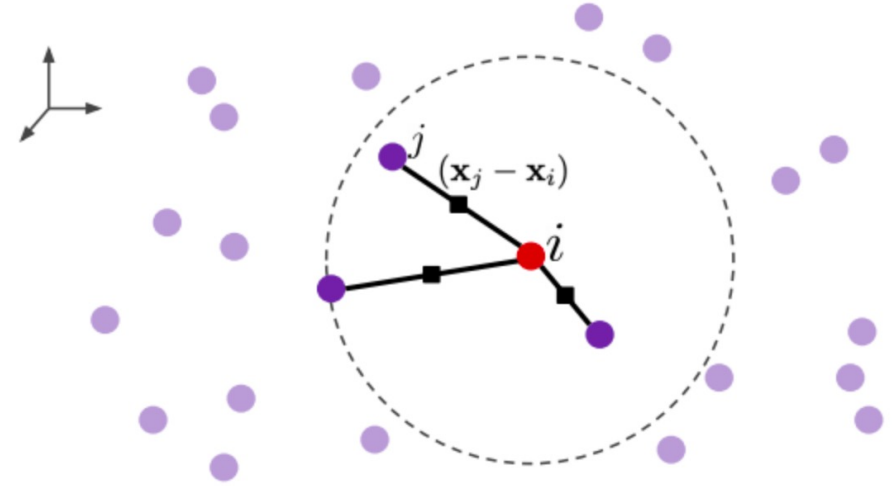
$$\alpha_{ij} = \text{softmax}(\text{IP}(q_i, k_j) / \sqrt{d})$$

Aggregate Message with Invariance Attention Score

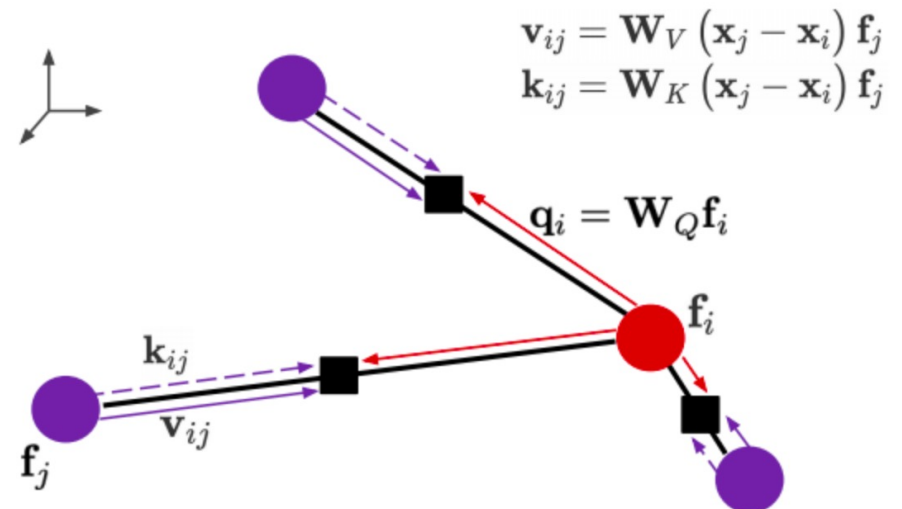
$$m_i = \sum_{j \in N(i)} \alpha_{ij} \cdot v_{ij}$$

$$x'_i = x_i + W_{\text{out}} \cdot m_i$$

Step 1: Get nearest neighbours and relative positions

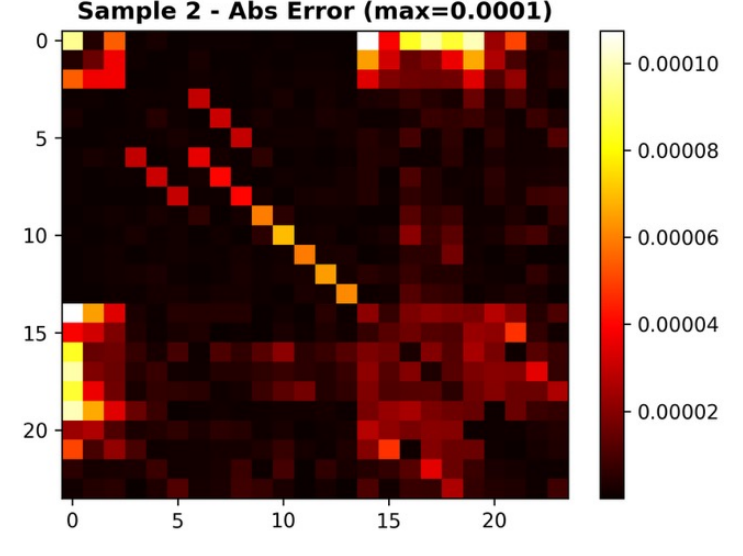
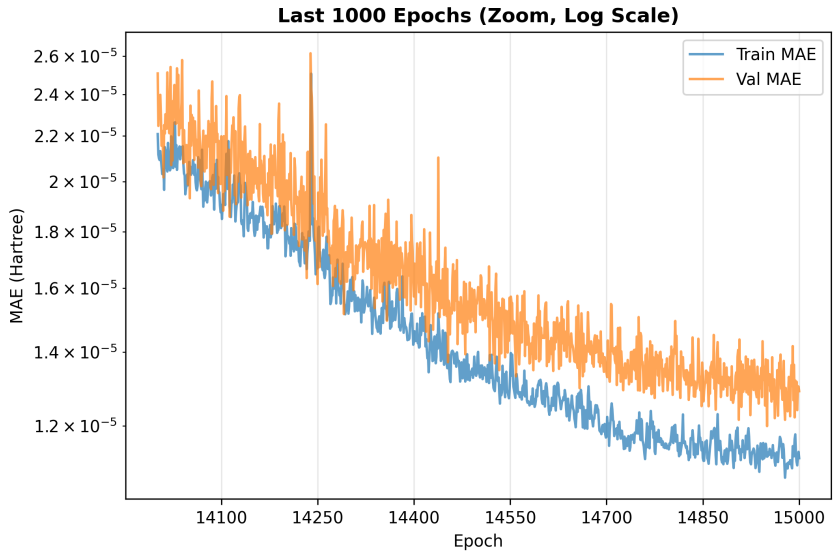
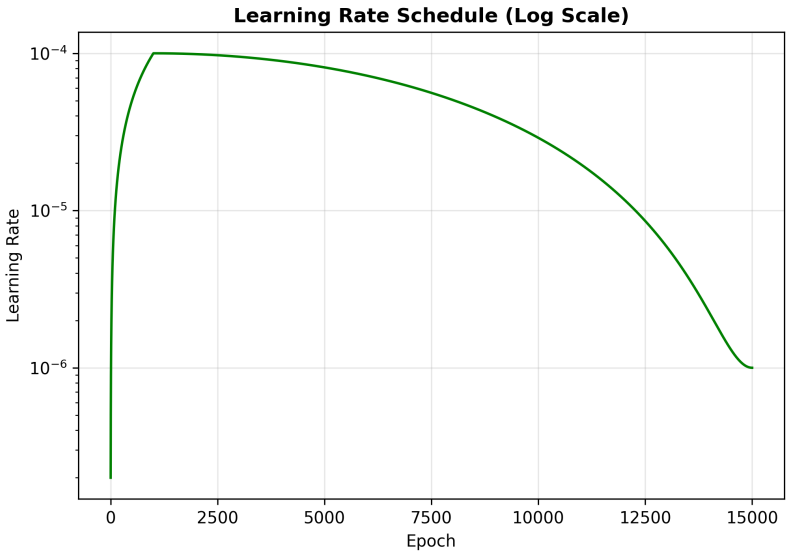
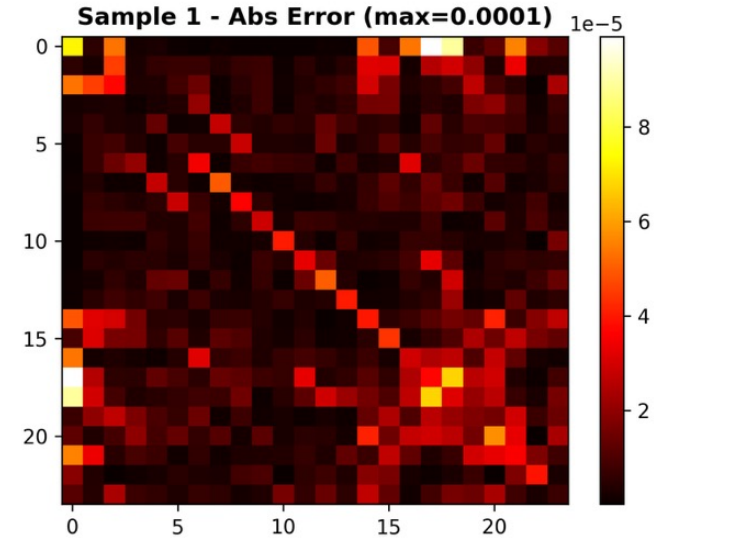
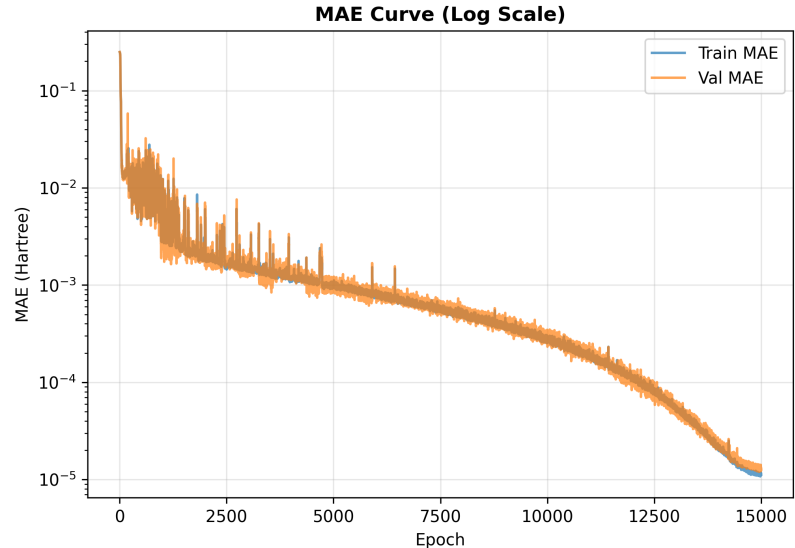
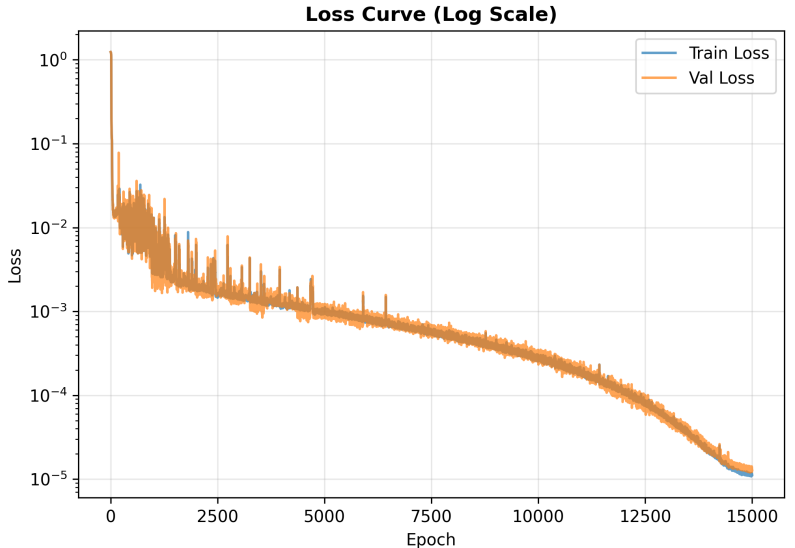


Step 3: Propagate queries, keys, and values to edges



■ Equivariance in Neural Network – Basic Architecture of QHformer

Training Progress - 100% Data



■ Equivariance in Neural Network – SO(2) Convolution Core in DeepTB-E3

SO(3) Convolution Filter

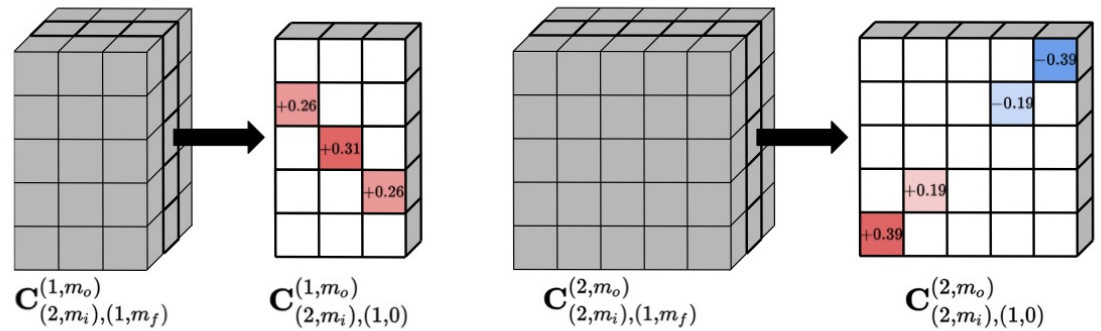
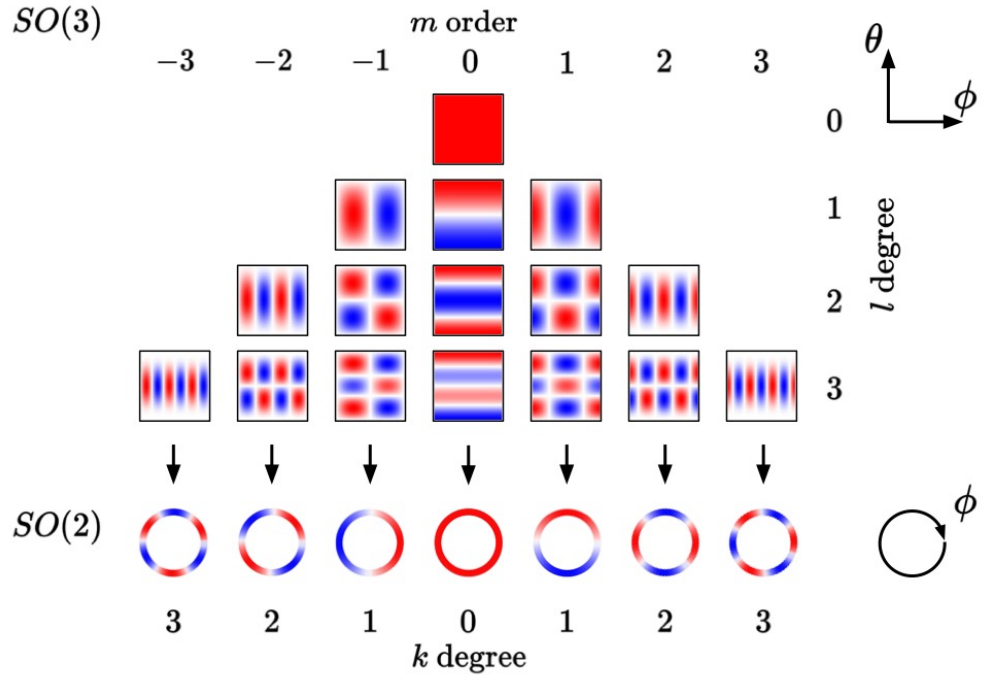
$$F_m^{lin^{lf}}(\mathbf{r}_{ij}) = R^{lin^{lf}}(|\mathbf{r}_{ij}|) Y_m^{lf} \left(\frac{\mathbf{r}_{ij}}{|\mathbf{r}_{ij}|} \right)$$



SO(2) Convolution Filter

$$F_m^{lin^{lf}}(\mathbf{r}_{ij}) = R^{lin^{lf}}(|\mathbf{r}_{ij}|) Y_m^{lf} \left(\frac{\mathbf{r}_{ij}}{|\mathbf{r}_{ij}|} \right)$$

$$= D^{-1}(\mathbf{R}) R^{lin^{lf}}(|\mathbf{r}_{ij}|) Y_m^{lf} \left(\mathbf{R} \cdot \frac{\mathbf{r}_{ij}}{|\mathbf{r}_{ij}|} \right)$$



■ Equivariant Neural Network – SO(2) Attention Mechanism in SE(3)-GAT

- **Inner-Product Attention Mechanism**

$$q_i = \text{Linear}(x_i)$$

$$k_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

$$v_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

$$\text{IP}(q_i, k_j) = \sum_l \sum_m q_i^{(l,m)} \cdot k_j^{(l,m)}$$

$$\alpha_{ij} = \text{softmax}(\text{IP}(q_i, k_j) / \sqrt{d})$$

- **Message Passing**

$$m_i = \sum_{j \in N(i)} \alpha_{ij} \cdot v_{ij}$$

$$x'_i = x_i + W_{\text{out}} \cdot m_i$$

- **SE(3) Head Splitting Strategy**

$$q_i^l \in \mathbb{R}^{M_l \times (2l+1)}$$



$$q_i^{l,h} \in \mathbb{R}^{\left(\frac{M_l}{H}\right) \times (2l+1)}, h = 0, 1, 2, 3 \dots H$$

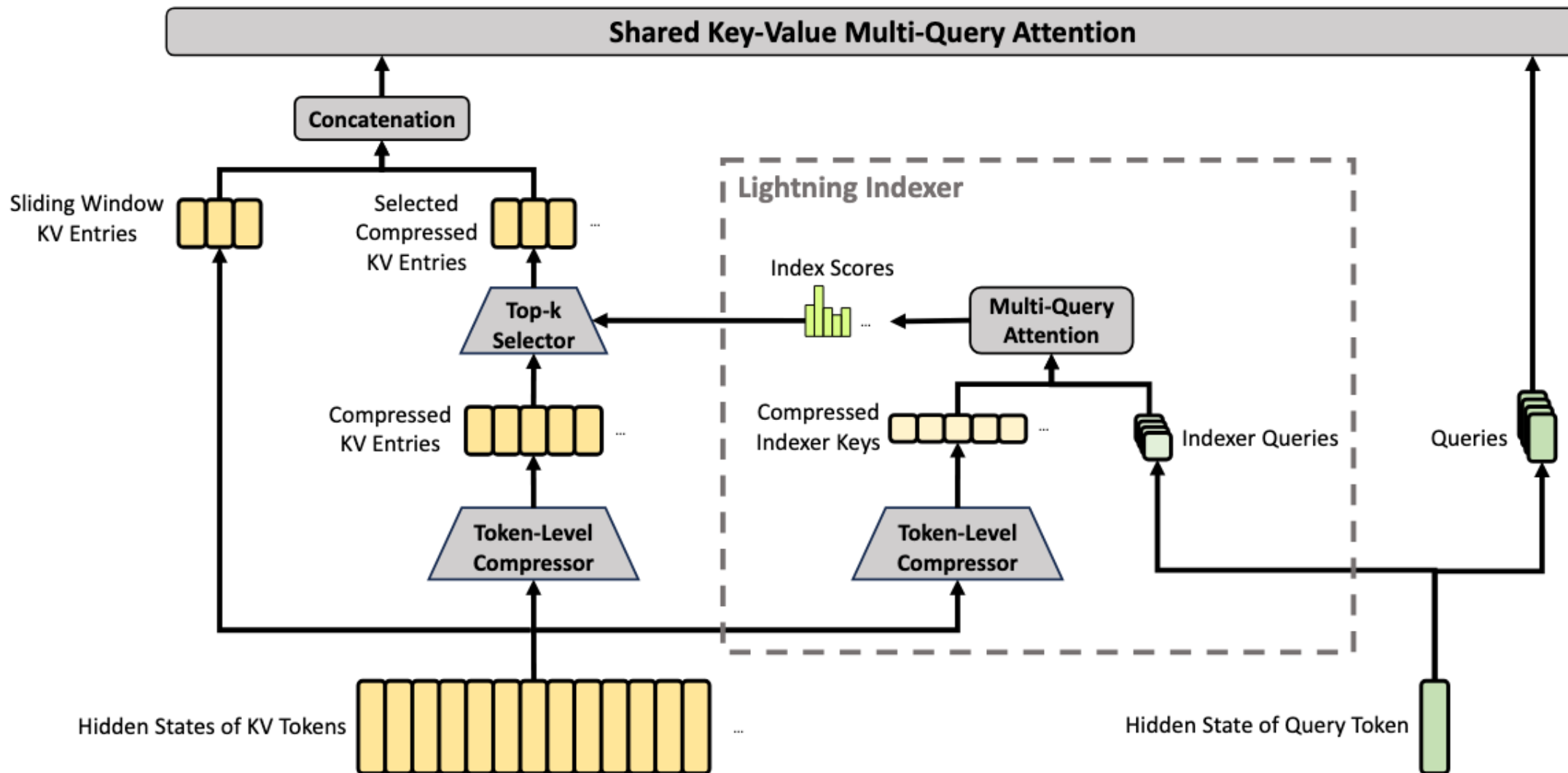
- **SO(2)-Attention Mechanism**

$$v_j = \text{SO2Conv}(x_j, r_{ij}, w_{ij}) = D^{-1}(\mathbf{R}) x_j Y_m^{lf} \left(\mathbf{R} \cdot \frac{\mathbf{r}_{ij}}{|\mathbf{r}_{ij}|} \right) w_{ij}$$

$$k_j = \text{SO2Conv}(x_j, r_{ij}, w_{ij}) = D^{-1}(\mathbf{R}) x_j Y_m^{lf} \left(\mathbf{R} \cdot \frac{\mathbf{r}_{ij}}{|\mathbf{r}_{ij}|} \right) w_{ij}$$

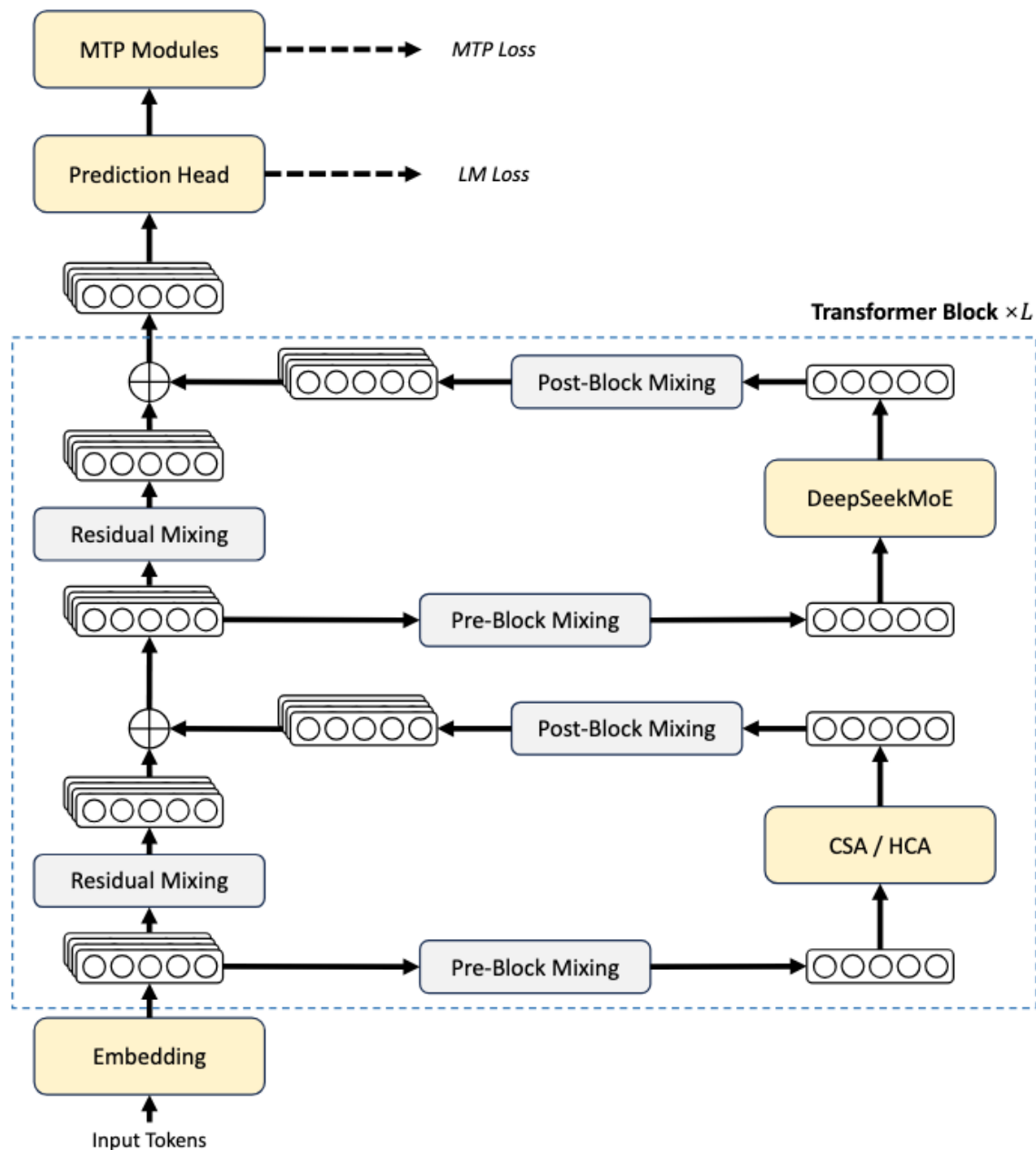
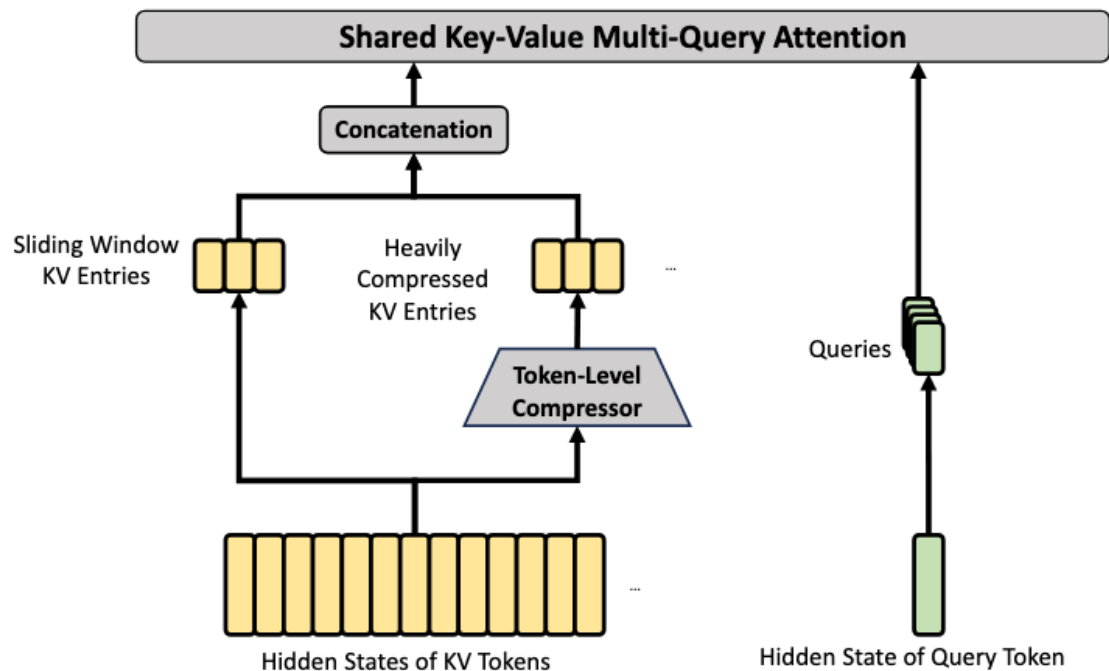
■ Equivariant Neural Network – Hybrid Attention Mode Inspired by DeepSeek V4 Pro

Compressed Sparse Attention(CSA)



■ Equivariant Neural Network – Hybrid Attention Mode Inspired by DeepSeek V4 Pro

Heavily Compressed Attention (HCA)



■ Equivariant Neural Network – Hybrid Attention Mode Inspired by DeepSeek V4 Pro

● CSA in QHformer

$$r_{ij} = I_{\theta}([s_{ij}, a_{ij}])$$

$$\varepsilon_i^{CSA} = \text{TopK}_{j \in N(i)}(r_{ij}; k_{CSA})$$



Only $j \in \varepsilon_i^{CSA}$

$$k_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

$$v_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

$$\alpha_{ij} = \text{softmax}(IP(q_i, k_j) / \sqrt{d})$$

$$m_i = \sum_{j \in \varepsilon_i^{CSA}} \alpha_{ij} \cdot v_{ij}$$

$$x'_i = x_i + W_{out} \cdot m_i$$



● HCA in QHformer

$$k_{ij} \in V_{L_{max}} \quad v_{ij} \in V_{L_{max}}$$



Only $l \leq L_{max}$ and $j \in \varepsilon_i^{CSA}$

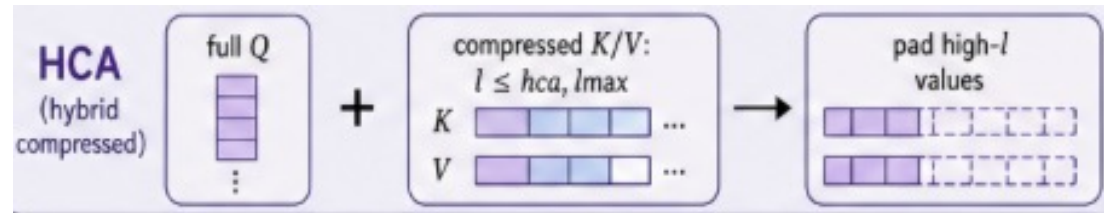
$$k_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

$$v_{ij} = \text{SO2Conv}(x_j, r_{ij}, w_{ij})$$

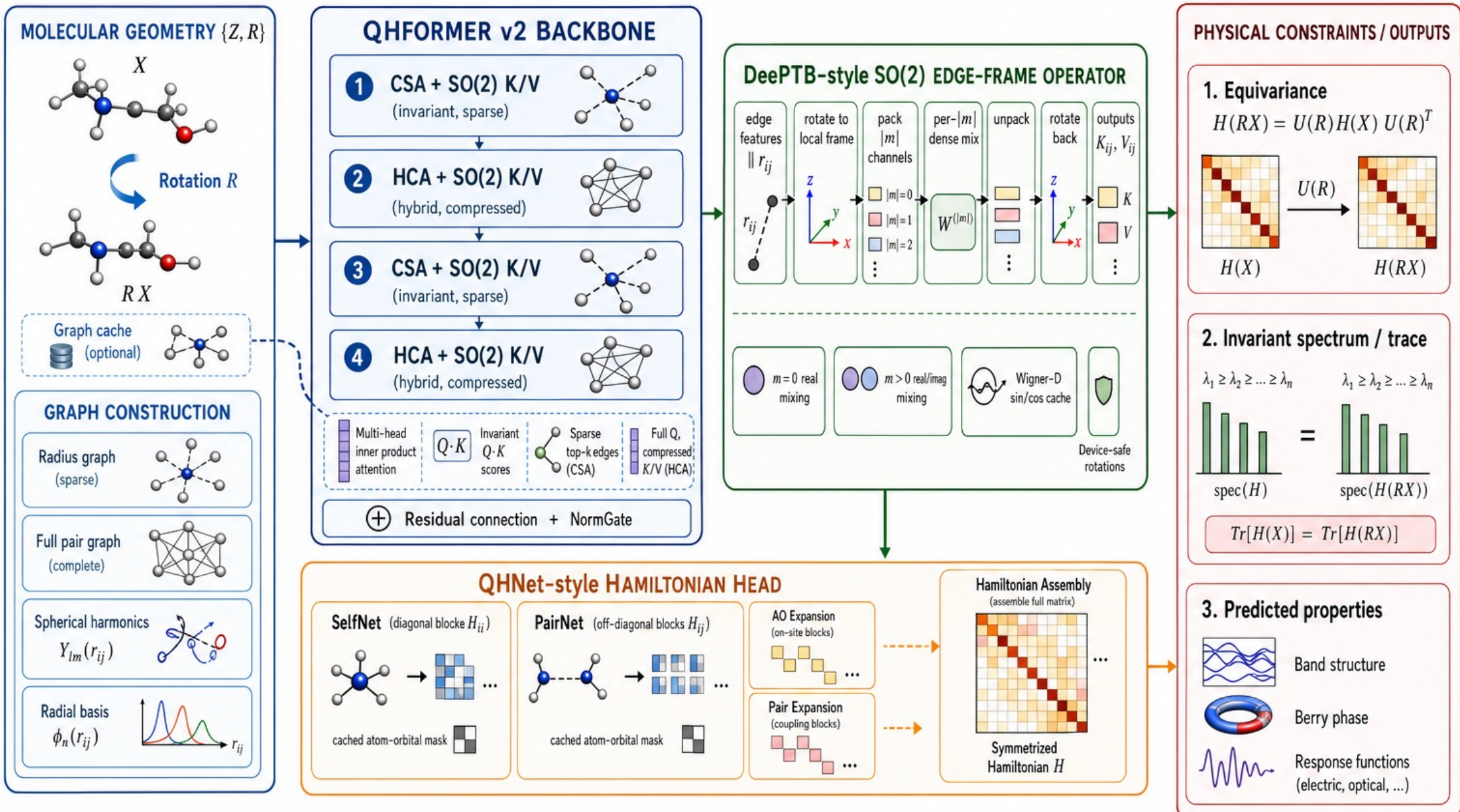
$$\alpha_{ij} = \text{softmax}(IP(q_i, k_j) / \sqrt{d})$$

$$m_i = \sum_{j \in \varepsilon_i^{CSA}} \alpha_{ij} \cdot v_{ij}$$

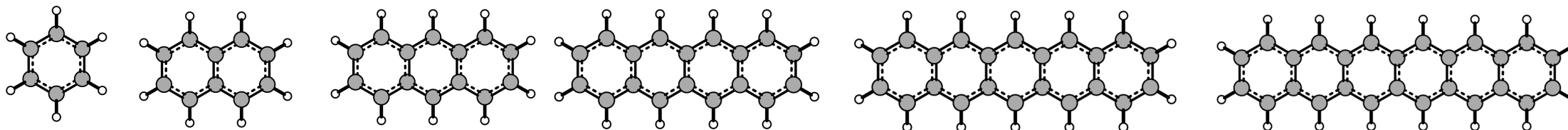
$$x'_i = x_i + W_{out} \cdot m_i$$



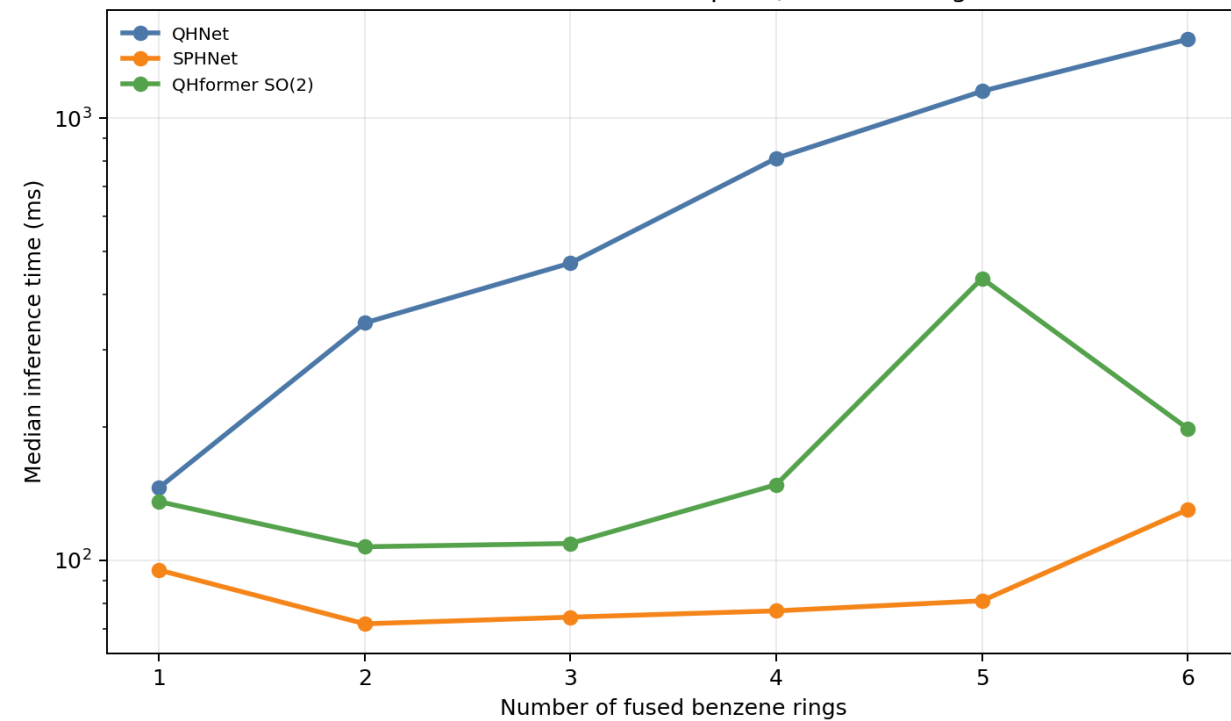
Equivariant Neural Network – Basic Architecture of QHformer_v2



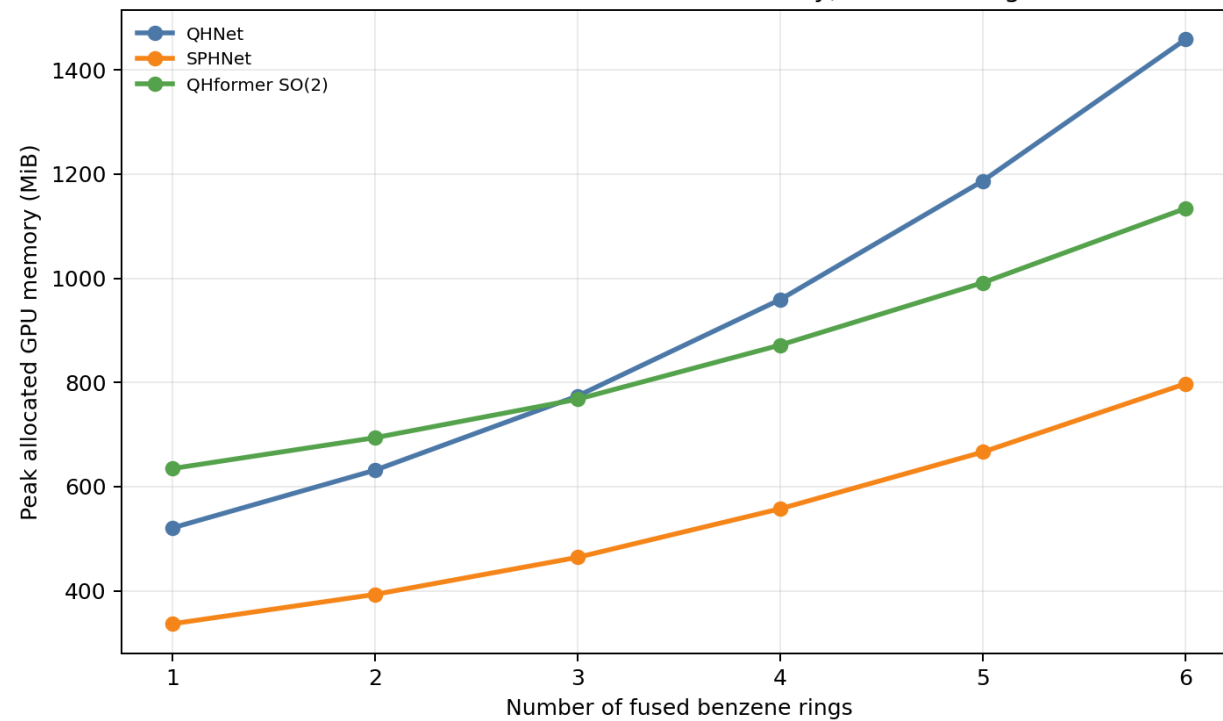
■ Equivariant Neural Network – Basic Architecture of QHfomer_v2



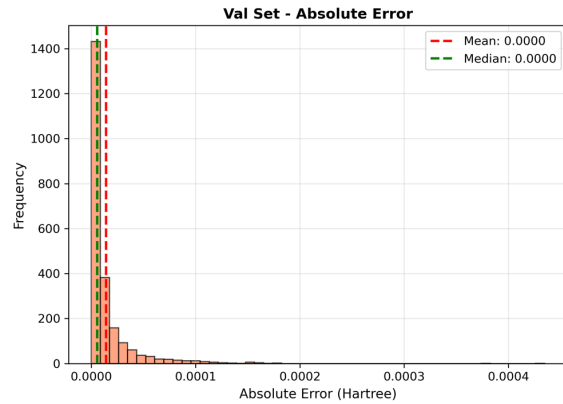
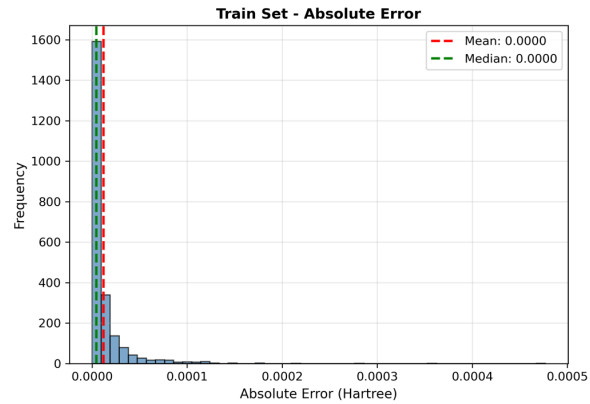
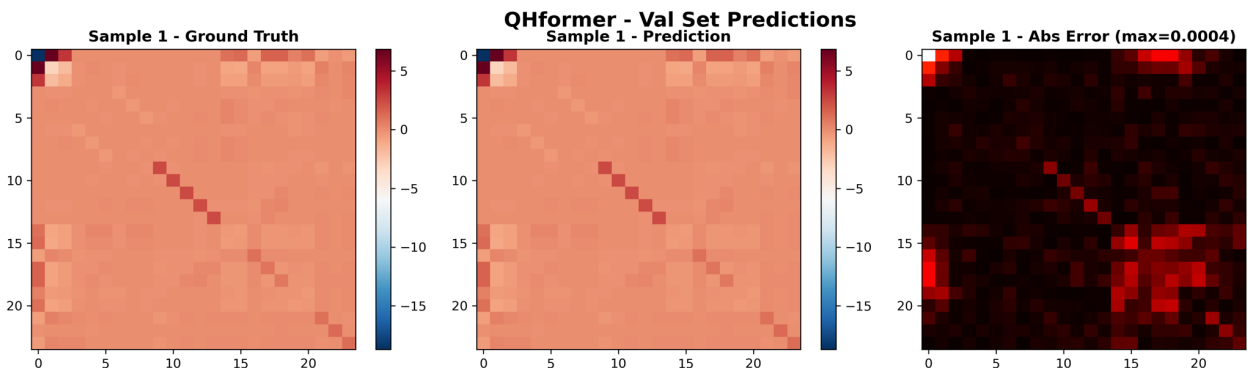
Acene Hamiltonian Inference Speed, cutoff=7 Angstrom



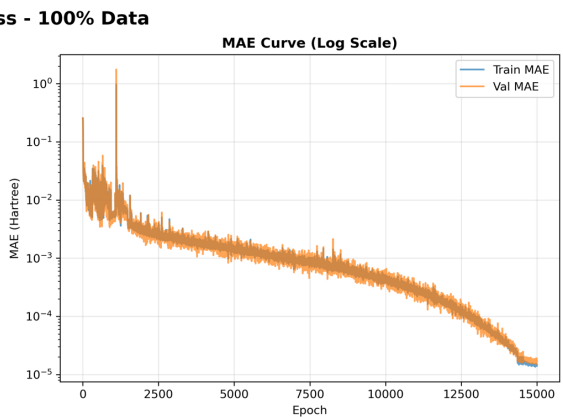
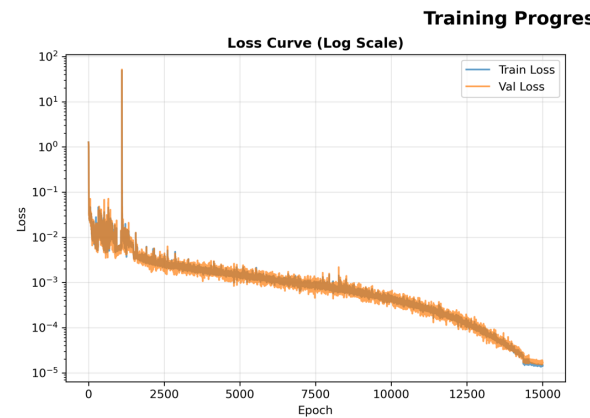
Acene Hamiltonian Inference Peak Memory, cutoff=7 Angstrom



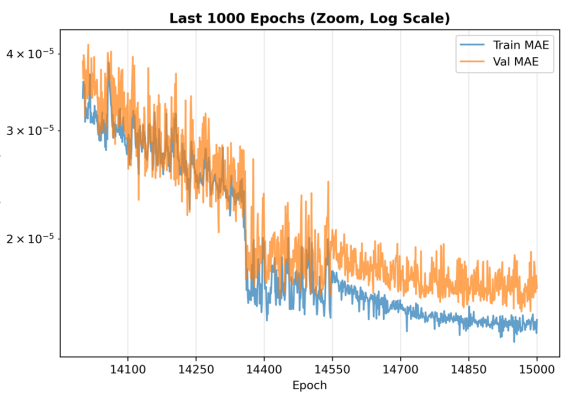
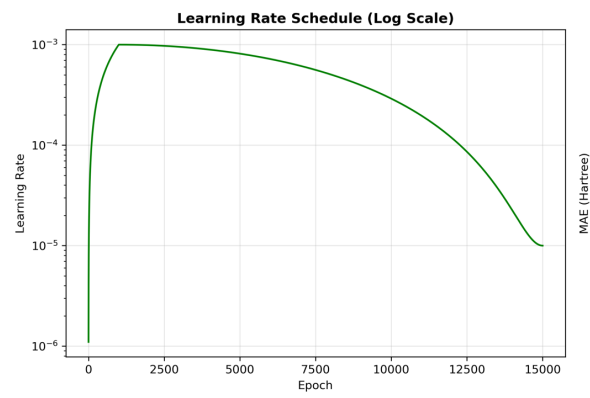
■ Equivariant Neural Network – Benchmark on MD17



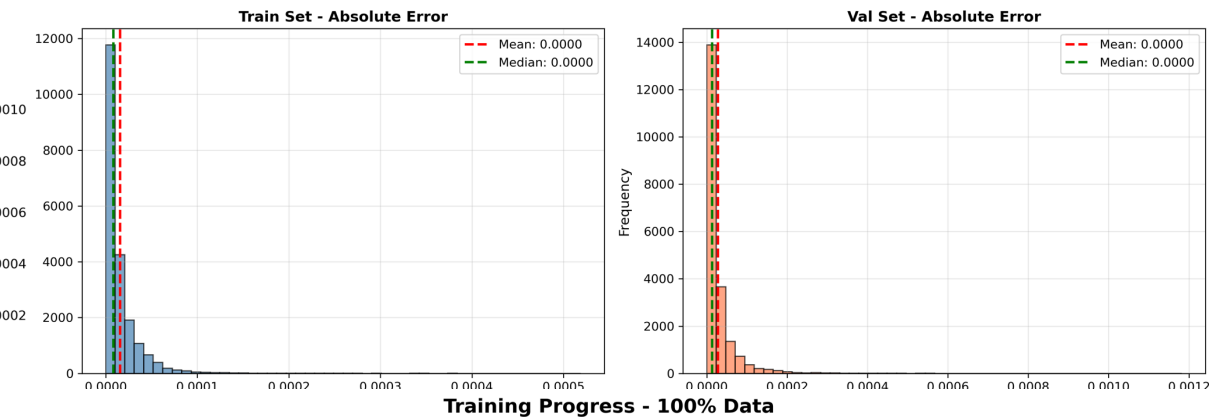
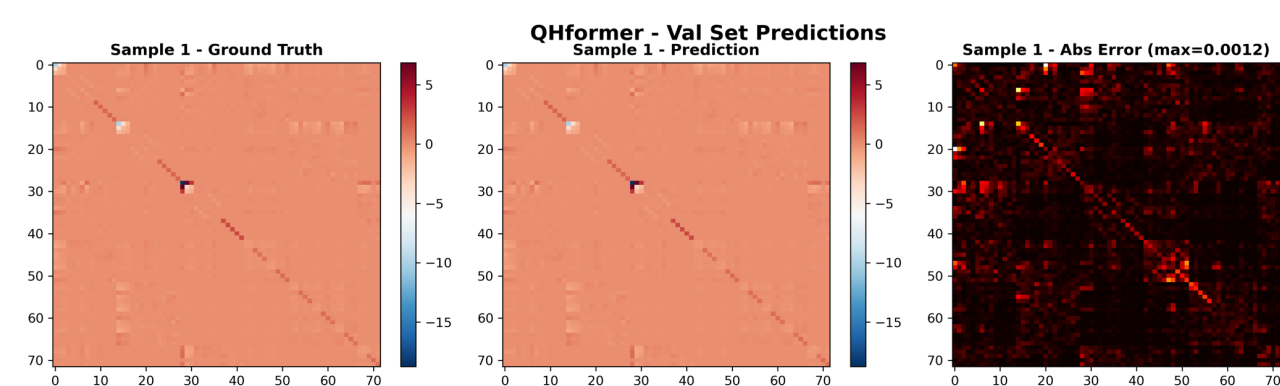
| Config | Dense TP | SO(2) | Speedup | Peak memory |
|----------------|----------|----------|---------|------------------|
| Operator only | 2.25 ms | 2.10 ms | 1.07x | 216 MB -> 151 MB |
| Full attention | 10.39 ms | 10.17 ms | 1.02x | 583 MB -> 380 MB |



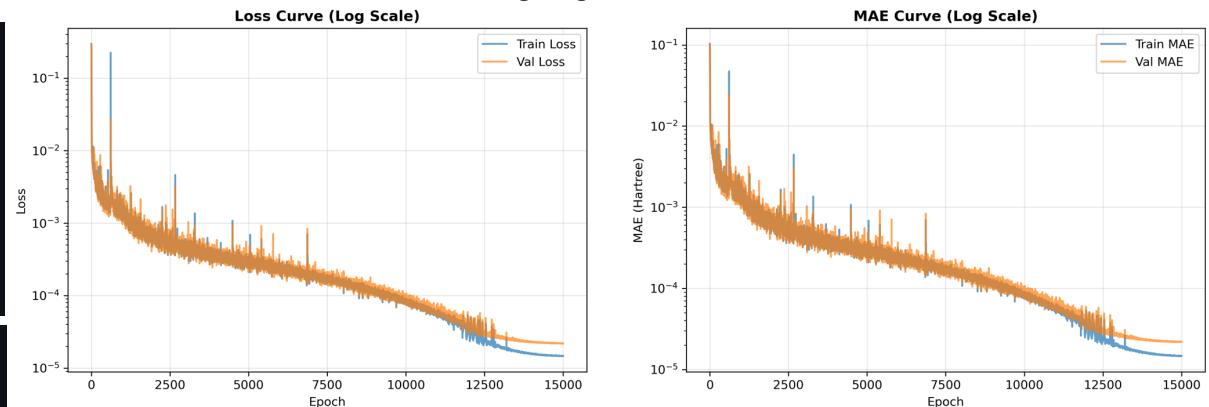
| Variant | Runtime | Speedup vs dense TP attention | Peak memory ratio |
|-------------|----------|-------------------------------|-------------------|
| Dense TP | 11.16 ms | 1.00x | 100% |
| CSA + TP | 10.53 ms | 1.06x | 33.1% |
| CSA + SO(2) | 9.65 ms | 1.16x | 24.0% |
| HCA + TP | 10.61 ms | 1.05x | 27.1% |
| HCA + SO(2) | 9.53 ms | 1.17x | 24.4% |



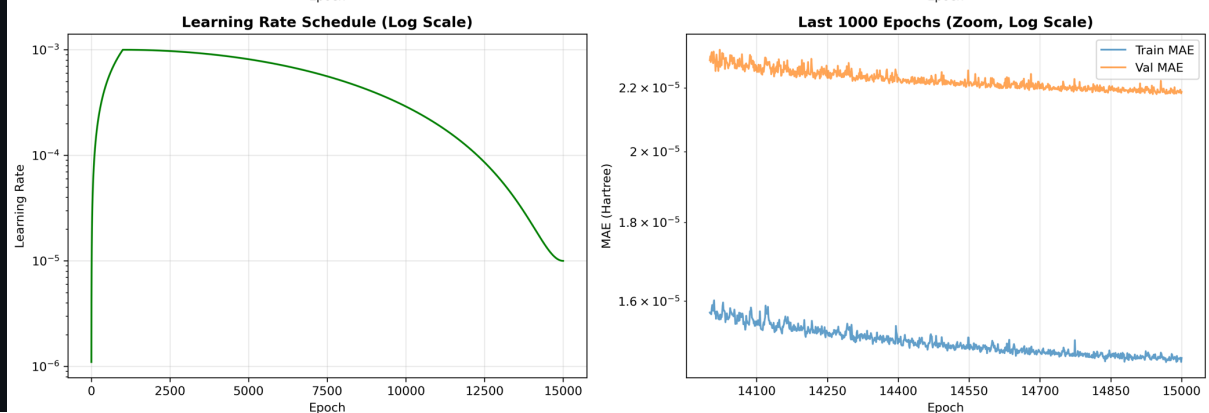
■ Equivariant Neural Network – Benchmark on MD17



| Config | Dense TP | SO(2) | Speedup | Peak memory |
|----------------|----------|----------|---------|------------------|
| Operator only | 2.25 ms | 2.10 ms | 1.07x | 216 MB -> 151 MB |
| Full attention | 10.39 ms | 10.17 ms | 1.02x | 583 MB -> 380 MB |



| Variant | Runtime | Speedup vs dense TP attention | Peak memory ratio |
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| HCA + SO(2) | 9.53 ms | 1.17x | 24.4% |



■ Equivariant Neural Network – **Functional and Outlook**

● **Functional**

- **A New $SO(2)$ Attention Mechanism for Graph Transformer Inspired by DeepSeek V4 Pro**
 - **Basic $SE(3)$ -Graph Transformer Architecture for Molecular Representation**
 - **Efficient and Accurate Hamiltonian Learning Architecture for DFT Calculation**
-

● **Outlook**

- **$SE(3)$ -Graph Transformer Architecture Training for other Equivariance-Need Tasks**
- **$SO(2)$ PairNet and SelfNet Modules or Better**
- **Combine with Full Differential DFT/TDDFT Code**
- **Combine with HamGNN, DeepH-2...(Graph Transformer based Hamiltonian Learning)**

■ DL-TDDFT – Accelerating TDDFT with CIS-like Graph Neural Network

Davidson Method Based

- **Subspace**

$$V_m = [v_1, v_2, \dots, v_m] \quad W_m = AV_m$$

- **Residuals**

$$H_m = V_m^T AV_m = V_m^T W_m$$

$$H_m y_k = \theta_k y_k, x_k = V_m y_k$$

$$r_k = Ax_k - \theta_k x_k$$

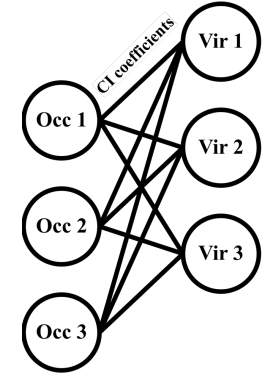
- **Expansion**

$$t_k \approx (\text{diag}(A) - \theta_k I)^{-1} r_k$$

$$V_{(m+1)} = \text{orth}([V_m, t_1, t_2, \dots])$$

Graph Neural Network Based

$$n_p = [C_p || \epsilon_p] \xrightarrow{\text{GAT-V2}}$$



- **Node**

$$o_i = f_{occ}(n_i) \quad v_a = f_{vir}(n_a)$$

- **Edge**

$$e_{ai} = f_{vir}(\eta_{ai}) \quad \eta_{ai} = [r_{ai}, \Delta\epsilon_{ai}, d_{ai}]$$

- **Interaction and Transition**

$$z_{ai} = f_{int}([o_i^l \otimes v_a^l, o_i^l - v_a^l, e_{ai}^l])$$

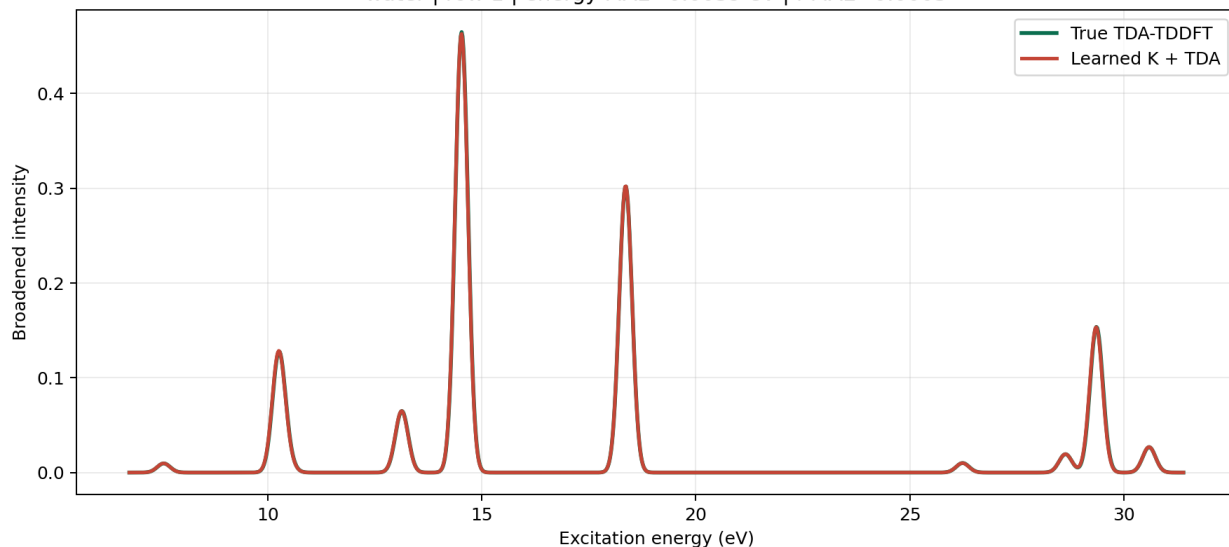
- **Pair-Pair Decoder**

$$D_{ai,bj} = f([z_{ai} \otimes z_{bj}, z_{ai} - z_{bj}, \phi_{ai,bj}])$$

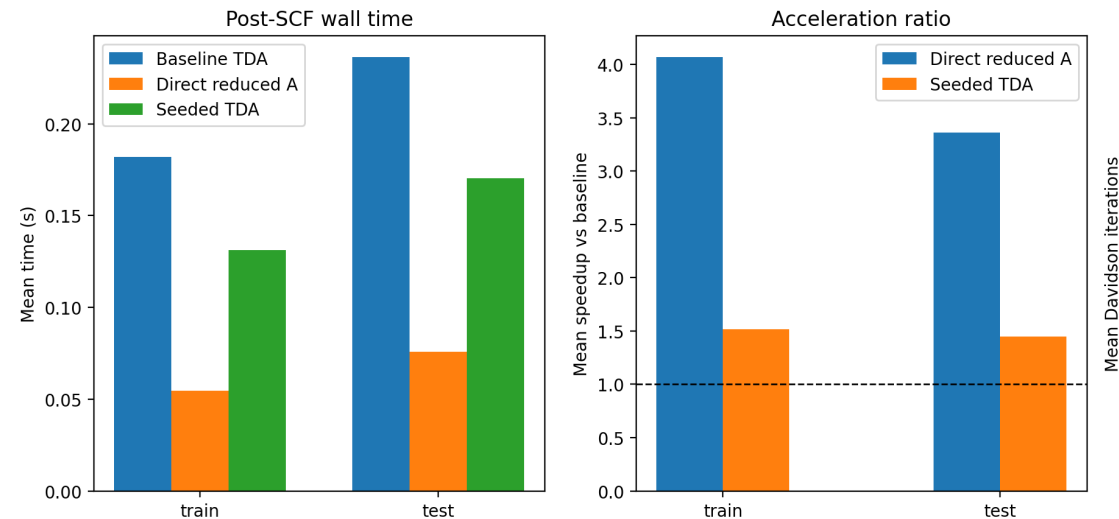
DL-TDDFT – A Test for Accelerating TDDFT

Water in Full Excitation Space - training set

water | row 1 | energy MAE=0.0039 eV | f MAE=0.0003

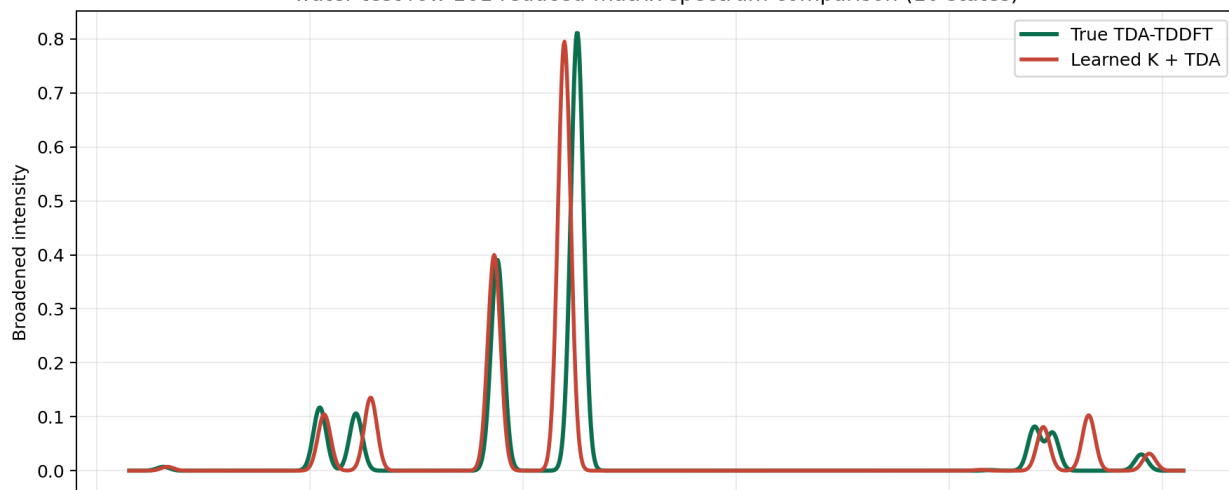


Speed up



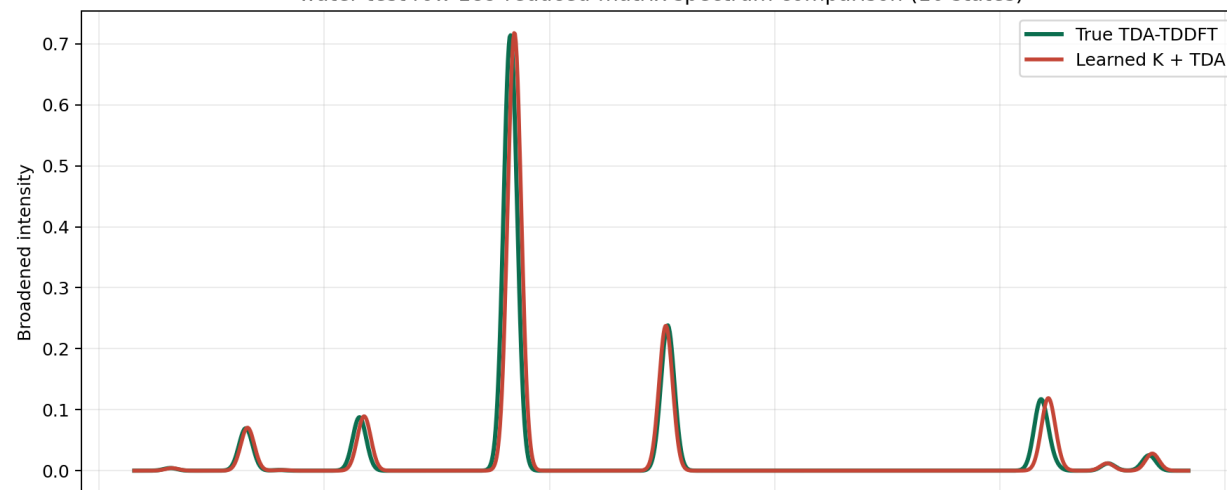
Water in Full Excitation Space - test set

water test row 161 reduced-matrix spectrum comparison (10 states)

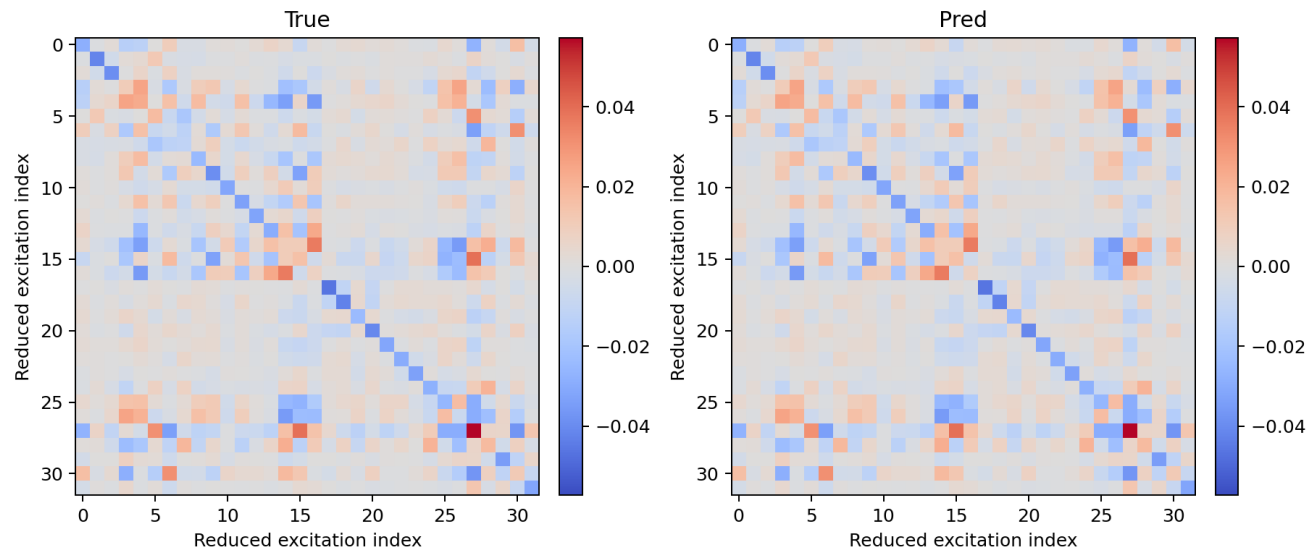


Water in Full Excitation Space - test set

water test row 189 reduced-matrix spectrum comparison (10 states)

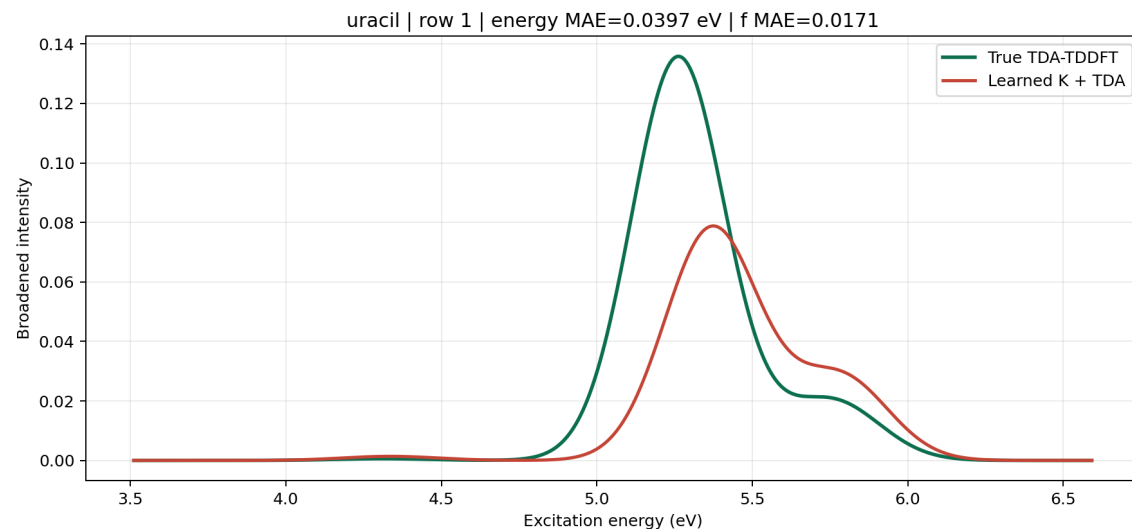


DL-TDDFT – A Test for Accelerating TDDFT

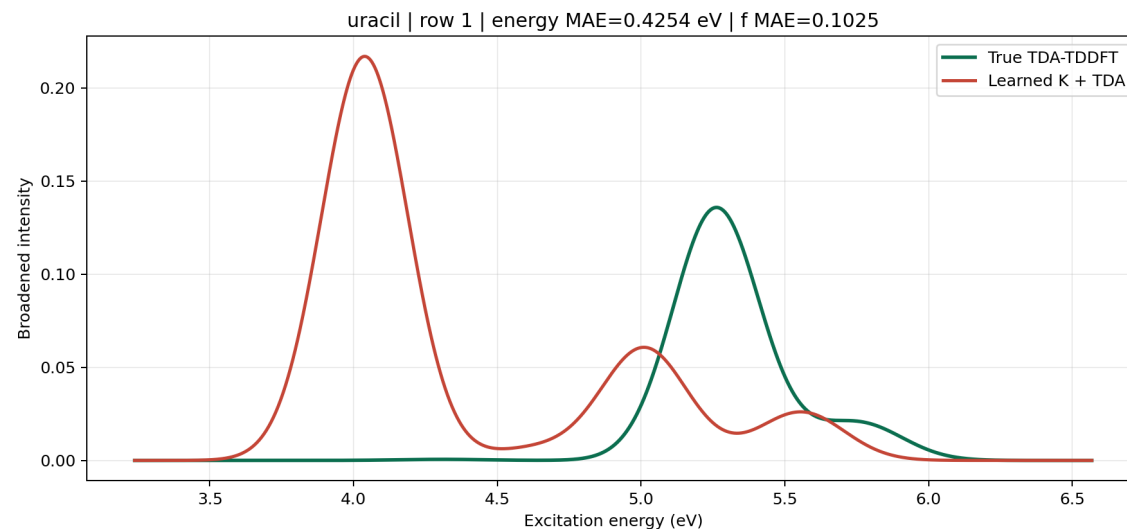


- **Good Enough? Right Enough? Differential Molecular Systems?**
 - **Compared with SpaiNN?**
 - **Phase Random?**
- ↓
- **DF/Cholesky bipartite GNN**
 - **Four-index AO/DF entry features**

Uracil in Excitation Subspace(32×32)



Uracil in Excitation Subspace(64×64)



■ Background – Inspiration From Claude Code

Water Molecule: Setup and Calculations

Computational Setup:

- **Molecule:** H₂O (water molecule)
- **Method:** TDDFT with various functionals
- **Basis Set:** 6-31G(d) and 6-31+G(d,p)
- **Functionals Tested:**
 - PBE (GGA functional)
 - B3LYP (Hybrid functional)
 - CAM-B3LYP (Long-range corrected hybrid)

Vibe Coding Approach:

- Used natural language to describe requirements
- AI assistant generated Python code for TDDFT calculations
- Automated spectrum plotting and analysis
- Interactive refinement of visualization

Comparison of Different Functionals

Key Observations:

- PBE underestimates excitation energies
- B3LYP provides better agreement with experiment
- CAM-B3LYP improves for charge-transfer states
- Basis set effects are significant

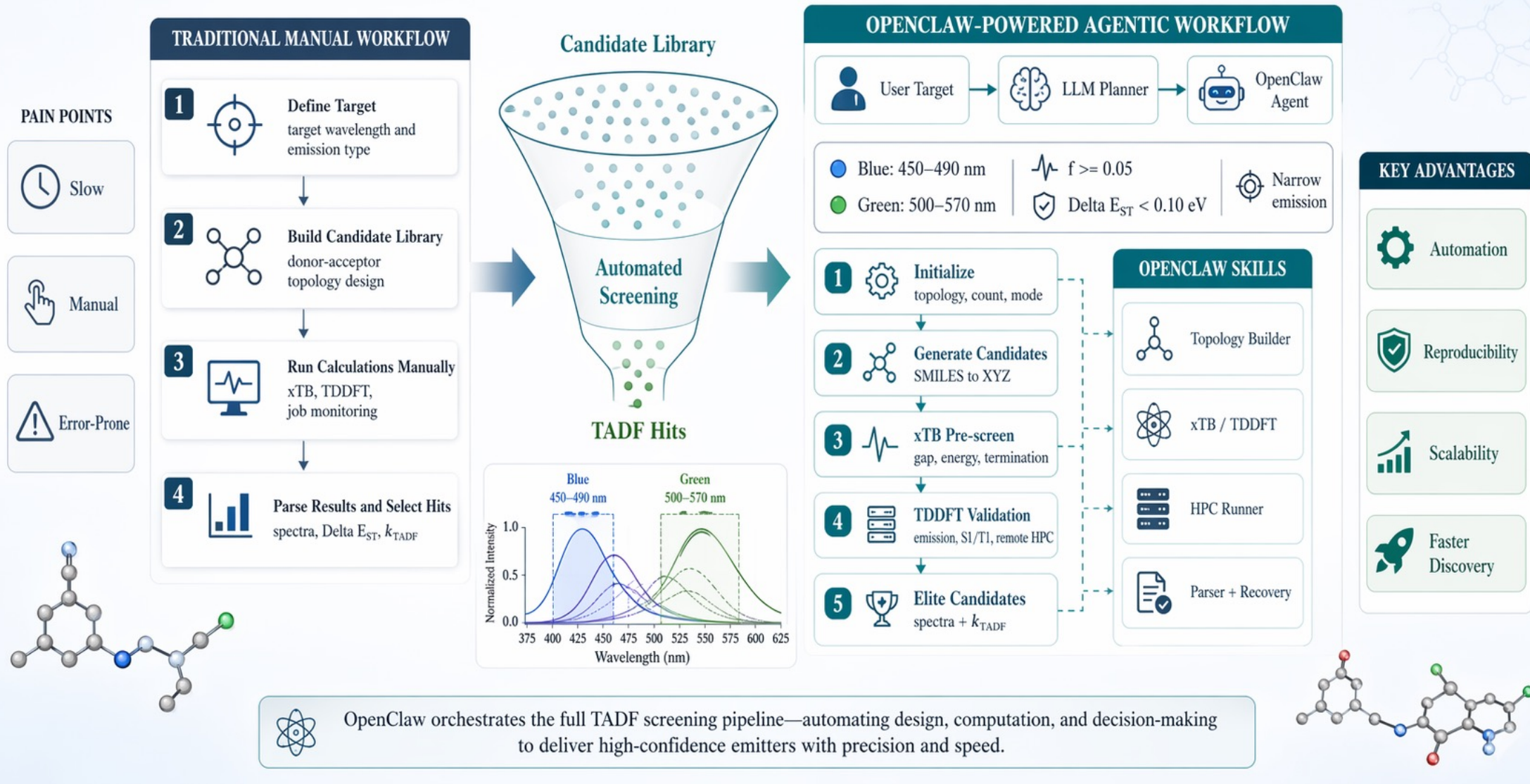
| Functional | Peak (eV) | Intensity |
|------------|-----------|-----------|
| PBE | 7.2 | 0.85 |
| B3LYP | 7.8 | 0.92 |
| CAM-B3LYP | 8.1 | 0.88 |
| Exp. | 7.9 | - |

Table 1: Comparison of excitation energies

Background – High Throughput Materials Design

github.com/silico-quantum/tadf-screening

TRADITIONAL TADF SCREENING VS. OPENCLAW-POWERED AGENTIC WORKFLOW



■ Openclaw and Hermes – Basic Architecture

```
# Silico 🦀 - AI Research Partner

## Architecture

Layer	Components
**Identity**	`SOUL.md` · `IDENTITY.md` · `USER.md`
**Memory**	`MEMORY.md` · `memory/*.md`
**Workflow**	`HEARTBEAT.md` · `AGENTS.md` · task plans
**Skills**	OpenClaw tools · chemistry workflows · automation modules

## Runtime

- **Interface**: Feishu DM
- **Execution**: Local macOS environment + optional remote HPC
- **Models**: Configurable LLM backend
- **Automation**: Scheduled research and workflow jobs

## Key Capabilities

- Quantum chemistry workflows (DFT, TDDFT, xTB screening)
- Feishu docs / drive / wiki / messaging automation
- Web research, code execution, and repo maintenance
- Long-running task orchestration and progress tracking

## Self-Evolution (OpenSpace)

Every task teaches · Every failure improves
```



```
# Hermes △ - AI Computational Chemistry Partner

## Architecture

Layer	Components
**Identity**	Hermes Agent · USER PROFILE · MEMORY
**Memory**	persistent memory · session history · reusable skills
**Tasks**	todo · cron jobs · delegated subagents
**Skills**	PySCF · xTB · Browser · Feishu · GitHub · visualization

## Runtime

- **Host**: Local Hermes environment + Feishu DM
- **Local Compute**: PySCF, Python, matplotlib, file/workspace automation
- **External Access**: web search, browser automation, messaging tools
- **Model**: OpenAI GPT-5.4 (current session)

## Key Capabilities

- Computational chemistry workflows (PySCF, xTB, spectra, PES, MD analysis)
- Scientific scripting, plotting, and reproducible project pipelines
- Web lookup, browser verification, and literature cross-checking
- Sub-agent orchestration, file management, and result delivery

## Working Style

- Direct execution first, then concise reporting
- Prefer reproducible scripts over manual operations
- Scientific correctness over cosmetic imitation
- Fast iteration with explicit documentation of approximations

## Self-Evolution

Every task teaches · Every correction sharpens the workflow
```

<https://github.com/HKUDS/OpenSpace>

■ Openclaw – A Standard Skills Group For Quantum Chemistry Calculation

Core Skills

1. Structure & Sampling

- [Molecular Sampler](#): Extract and sample molecular structures from cluster/ONIOM files. Union-Find molecule identification + distance-sorted neighbor sampling.
- [RDKit Chemistry](#): 3D conformer generation (ETKDG), molecular descriptors (LogP, TPSA), and Gasteiger charge analysis.
- [xTB Cluster MD](#): Semi-empirical MD (GFN-FF/GFN2-xTB) for organic molecular clusters with automated trajectory animation.

2. Electronic Structure Computing

- [PySCF](#): Python-based quantum chemistry. Supports Ground state (HF, KS-DFT), Excited states (LR-TDDFT, TDA), and Post-HF methods.
- [MOMAP](#): helper for molecular photophysics and charge transport. Predict radiative/non-radiative (IC/ISC) rate constants and quantum yields.

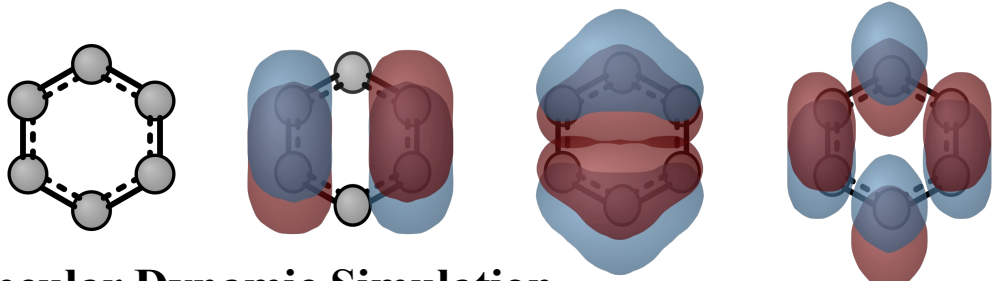
3. Analysis & Visualization

- [Multiwfn](#): Advanced wave function analysis. Population analysis (Hirshfeld, ADCH, CM5), bond orders, and spectroscopy (UV-Vis, IR, Raman).
- [xyzrender](#): Command-line driven, publication-quality molecular graphics. Supports transparent backgrounds, bond orders, and orbital rendering.
- [Orbital Analysis](#): Streamlined workflow for MO composition, energy level diagrams, and isosurface generation.

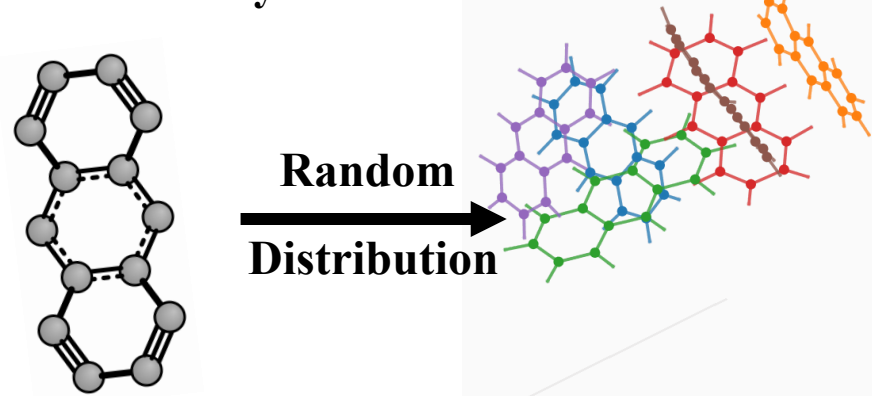
```
pyscf/  
├── SKILL.md  
├── VERSION_UPDATE.md  
├── references/  
│   ├── theory/  
│   │   ├── pyscf-advanced.md  
│   │   ├── pyscf-api-reference.md  
│   │   └── pyscf-jax-integration.md  
│   └── practice/  
│       ├── 2d-potential-energy-surface.md  
│       ├── emission-spectrum-guide.md  
│       └── emission-spectrum-workflow.md  
├── scripts/  
│   └── dft_calculation.py  
└── tools/  
    ├── analysis.py  
    ├── cascf.py  
    ├── ccsd.py  
    ├── dft.py  
    ├── geometry.py  
    ├── mp2.py  
    ├── pes.py  
    ├── scf.py  
    ├── spectrum.py  
    └── tddft.py
```

Openclaw and Hermes – A Standard Skills Group For Quantum Chemistry Calculation

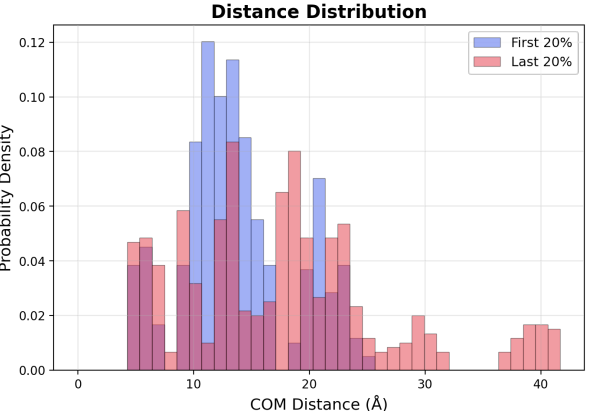
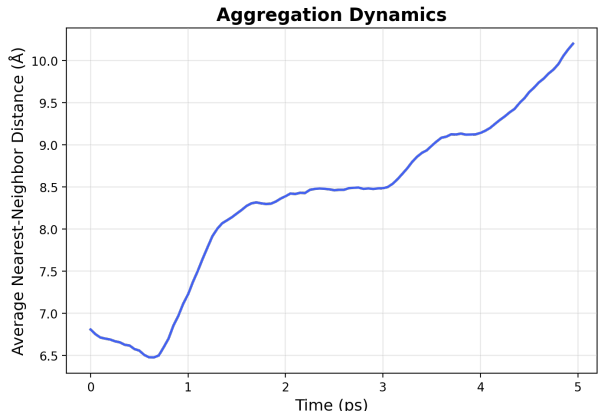
Basic Ground State Calculation



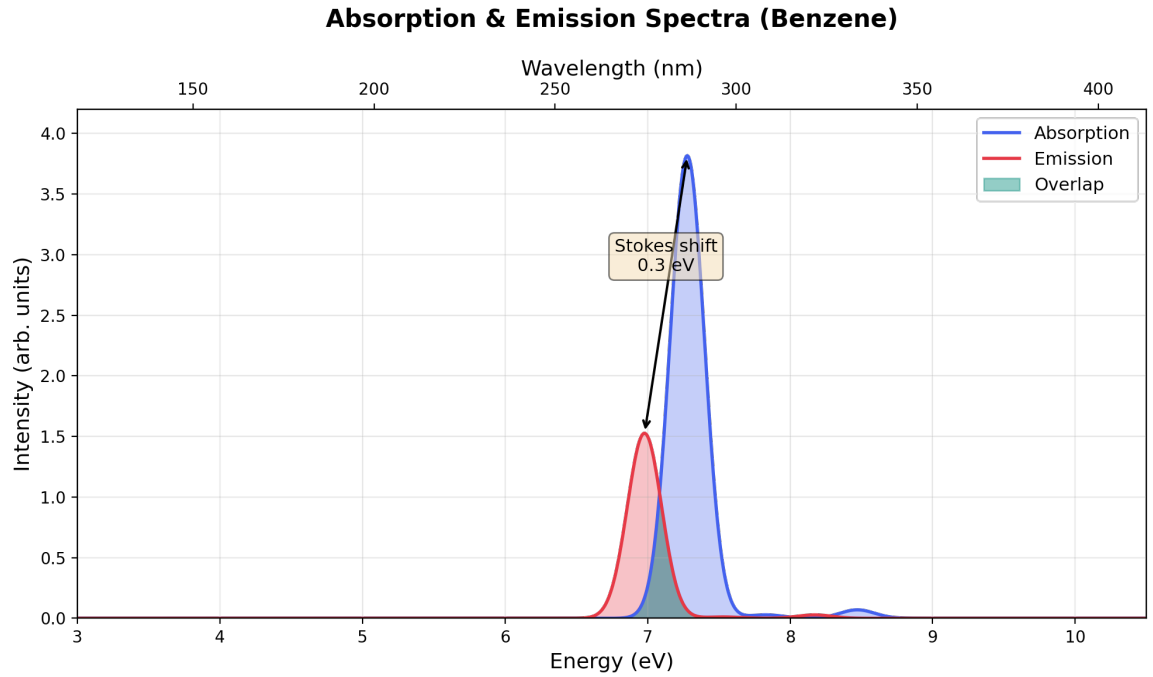
Molecular Dynamic Simulation Visualization



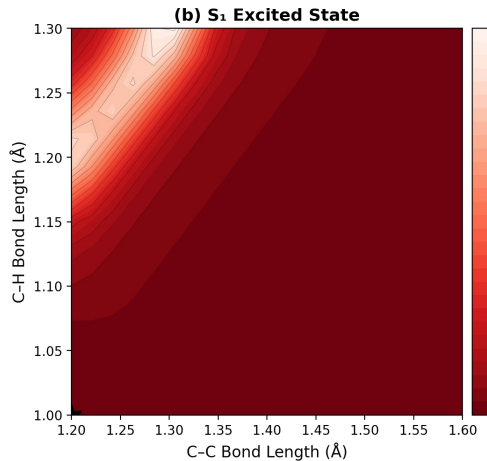
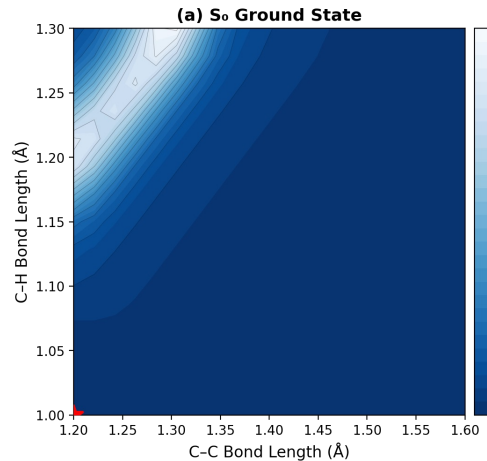
Molecular Dynamic Simulation



Absorption and Emission Spectra(Error !)

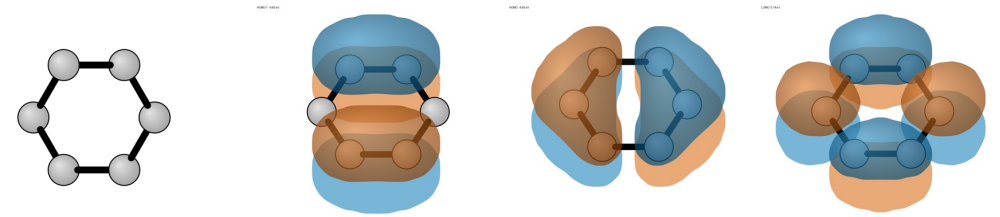


Potential Energy Surface

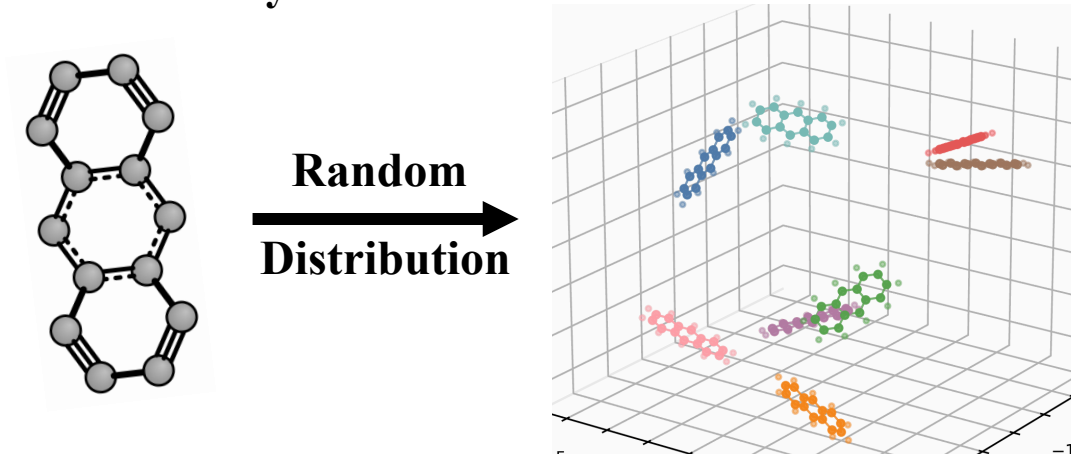


Openclaw and Hermes – A Standard Skills Group For Quantum Chemistry Calculation

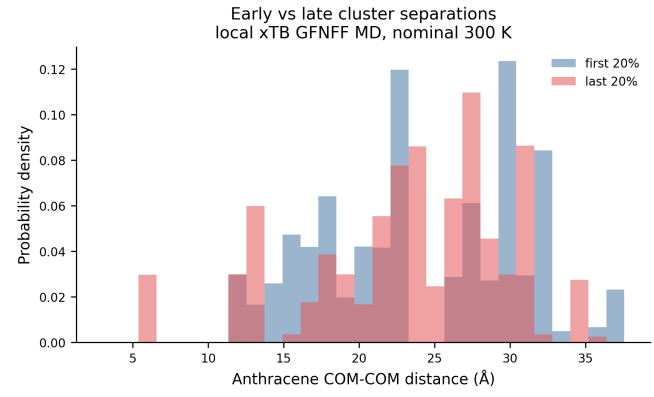
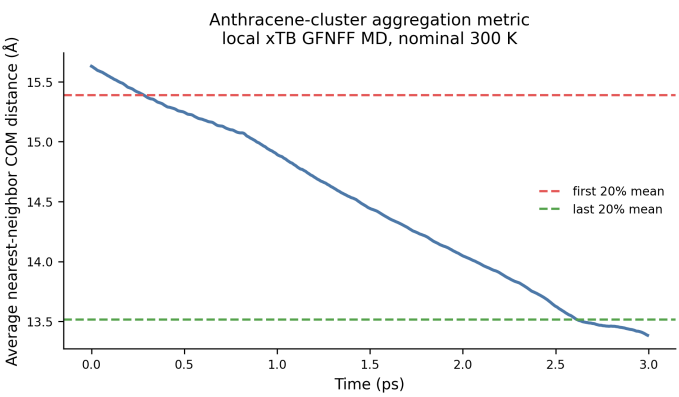
Basic Ground State Calculation



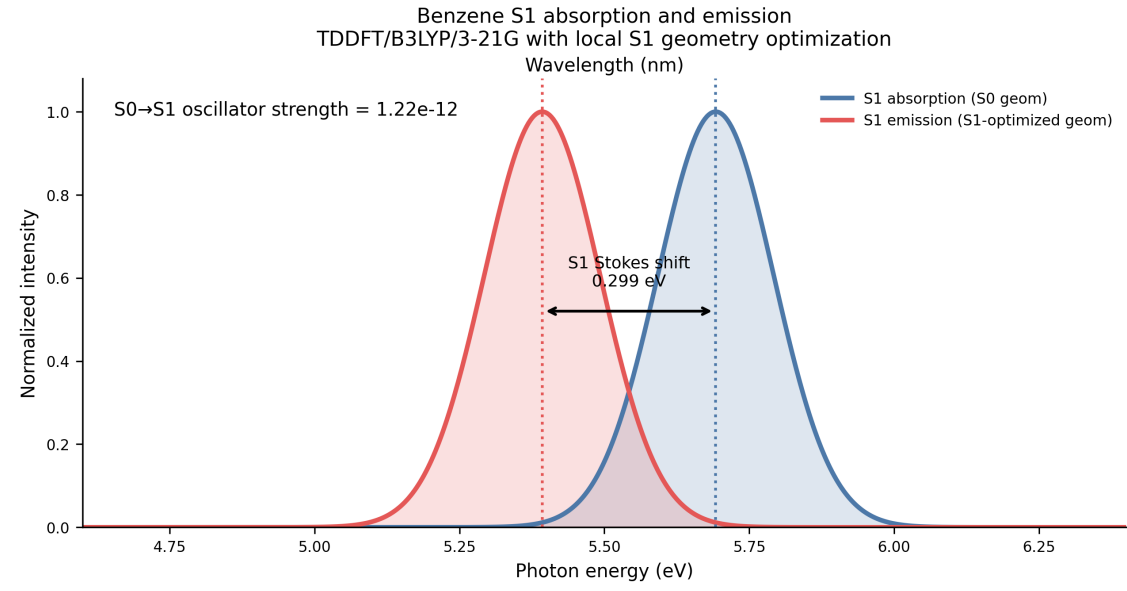
Molecular Dynamic Simulation Visualization



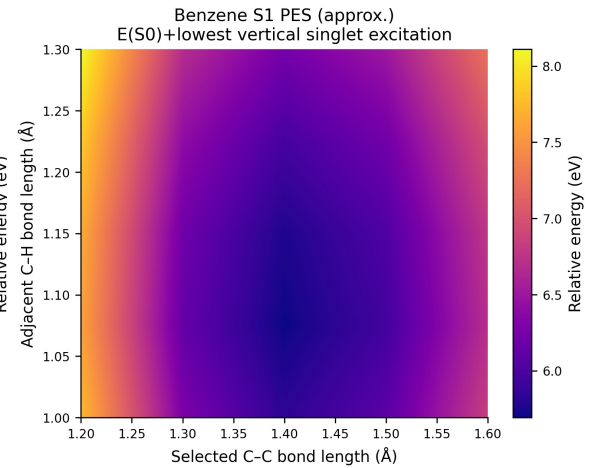
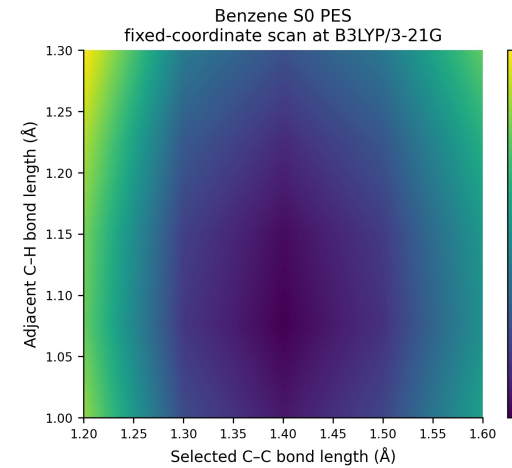
Molecular Dynamic Simulation



Absorption and Emission Spectra



Potential Energy Surface



■ Openclaw and Hermes – Skill For TADF Materials Design

Stage 0: Initialization

- └ screening_workflow_initializer.py
 - └ Confirm: topology, sample count (default 10k), interaction mode

Stage 1: Candidate Generation

- └ build_da_topology_library.py (D-A, D-A-D, A-D-A, D-pi-A...)
- └ SMILES → .xyz structure generation (export to manifest.csv)

Stage 2: xTB Pre-screening

- └ Input: manifest.csv (idx, name, xyz_path)
- └ run_xtb_batch_manifest.py → xtb_progress.csv
 - Required columns: idx, name, xyz_path, status, detail, total_energy_eh, homo_lumo_gap_ev, normal_termination
- △ If xTB ok=0 → STOP and diagnose

Stage 2B: TDDFT-xTB Wavelength Filter (optional)

- └ run_tddft_xtb_filter.py
 - Filter: emission in target range, $f \geq \text{threshold}$

Stage 3: TDDFT Validation (remote)

- └ S0 optimization
- └ Excited-state optimization (S1 for TADF/Fluorescence; T1 for Phosphorescence)
- └ Vertical emission
- └ Gate: $\Delta E_{ST} < 0.10$ eV, $f \geq 0.05$, $k_{TADF} > 10^4$ s⁻¹

Stage 4: Elite Candidates → downstream analysis

```
{
  "project": {
    "name": "green-tadf-screening-10k",
    "compute_tier": "local_basic",
    "interaction_mode": "interactive_chat",
    "question_mode": "blocking",
    "max_question_rounds": 3
  },
  "system_hardware_profile": {
    "hardware": {
      "platform": "macOS-26.1-arm64-arm-64bit",
      "os": "Darwin",
      "cpu_cores_logical": 10,
      "gpu": { "available": false, "count": 0, "names": [] }
    },
    "hpc_slurm": {
      "remote_hpc_hint": null,
      "slurm_detected": false,
      "sbatch_in_path": false,
      "squeue_in_path": false,
      "slurm_env_present": false
    }
  },
  "photophysical_targets": {
    "emission_range_nm": [500.0, 570.0],
    "emission_type": "TADF",
    "spectrum_width_requirement": "Narrow/High Color Purity",
    "default_fwhm_ev": 0.15
  },
  "fragment_database": {
    "builtin_sources": ["DeepChem", "PubChem"],
    "augment_with_custom_db": null,
    "custom_db_paths": []
  },
  "assembly_topology_rules": {
    "topology_preferences": ["D-A", "D-A-D"],

```

Openclaw and Hermes – An Example For Blue Light OLED/TADF Materials

`/skill tadf-screening`

11:20

已切到 `tadf-screening` workflow。

先把入口条件定掉，我就能直接往下跑：

1. 目标发光类型, TADF / fluorescence / phosphorescence
2. 目标发射范围, 例如 450–490 nm
3. 是否要求窄带, 以及你接受的带宽标准
4. 拓扑, D-A / D-A-D / A-D-A / D- π -A / D_n-A / 混合
5. 初始样本数, 默认 10000
6. 远程资源用哪个 profile, 比如 marcus; 如果缺 `xtb4stda/stda`, 我是否可以尝试安装
7. 监控节奏, 默认每 5 分钟检查、每 10 分钟汇报

如果你想省事, 直接回我一句:
“窄带蓝光 TADF, 450–490 nm, D-A-D, 10000, marcus, 允许安装缺失工具, 默认监控”
我就开干。

窄带蓝光 TADF, 450–490 nm, D-A-D, 10000, marcus, 允许安装缺失工具, 默认监控, 注意 marcus 的进入方式是 `ssh -> marcus2` 再 `ssh marcus`, 使用 `slurm` 进行远程的所有计算

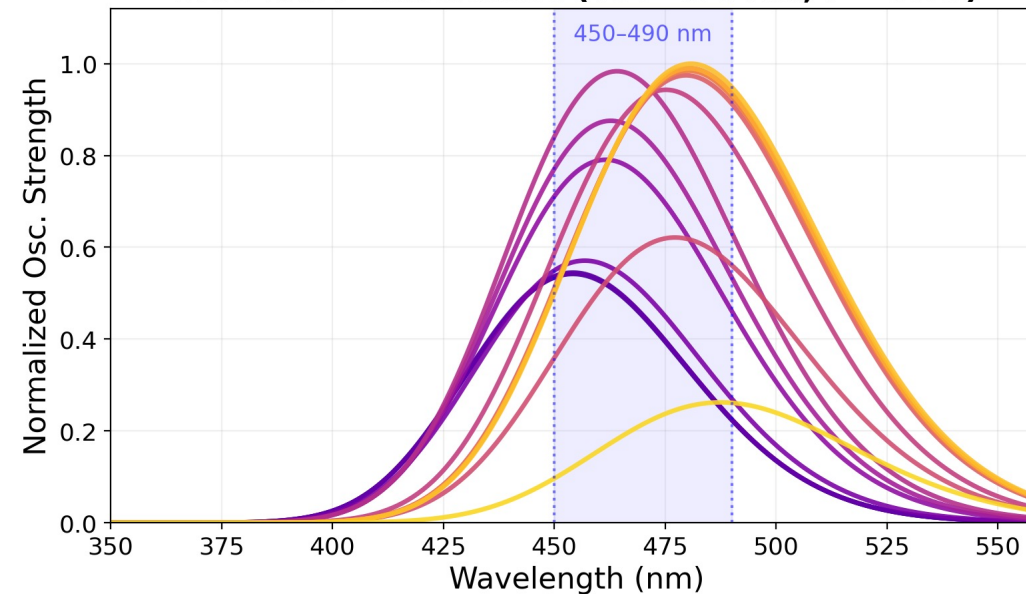
好, 我已经按这个参数把入口配好了:

- profile: `yuanjiao_marcus`
- 路径: `ssh marcus2 -> ssh marcus -> Slurm`
- 监控: 已设为每 5 分钟检查、每 10 分钟汇报
- 初始化配置已生成: `skills/tadf-screening/workflow_config_blue_10k_20260422.json`
- `BATCH_STATUS.md` 也已切到这次 batch

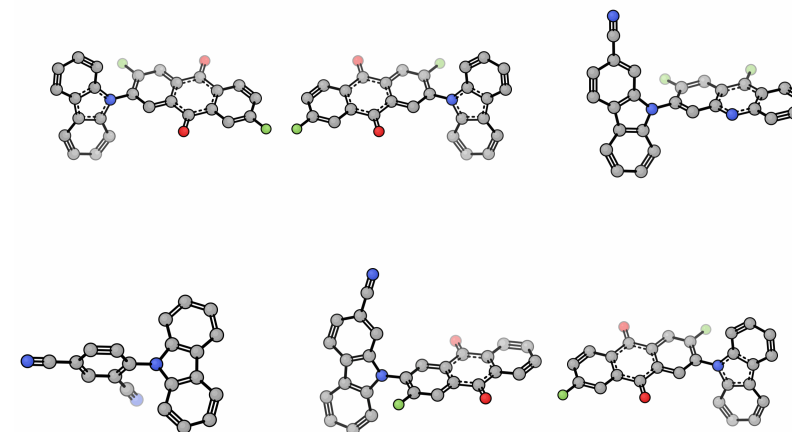
现在只差一个硬门槛才能正式往下跑:

Stage 2 的 empirical Stokes shift 取多少 eV?
我建议先用 **fixed 0.5 eV**, 这和我们前面蓝光筛选流程一致, 也最稳。
你直接回我一句“用 0.5 eV”, 我就继续进下一步。
补一句, 初始化器在本地只探测到 PySCF, 但这不影响, **Stage 3 仍会按你的要求走 marcus 上的 Gaussian + Slurm.**

Blue TADF Candidates (450–490 nm, $f > 0.05$)



| | | | |
|------------|-------------|-----------|----------------|
| CBZ-PTN | CBZ-F-AQ-F | CBZ-QX-F2 | CBZ-AQ-F2 |
| CBZ-DCBN | CBZ-CN-AQ-F | CBZ-AQ-F2 | CBZ-AQ-F2 |
| CBZ-DCBN14 | CBZ-DCBN13 | CBZ-AQ-F2 | CBZ-AQ-F2 |
| CBZ-BN-F3 | CBZ-AQ-F | CBZ-AQ-F2 | CBZ-CN-PHEN-F2 |



■ Openclaw and Hermes – Cron, Heartbeat, Memory, Dreaming and Self-evolution

- Openclaw-planer and supervisor

Cron

- Long-term tasks
- Accurate time point
- Isolated mode(work in sandbox)

Heartbeat

- Short-term tasks
- Ambiguous time point
- Only work in main process

Memory

Human

- daily Memory
- long-term memory
- semantic retrieval → answer

Dreaming

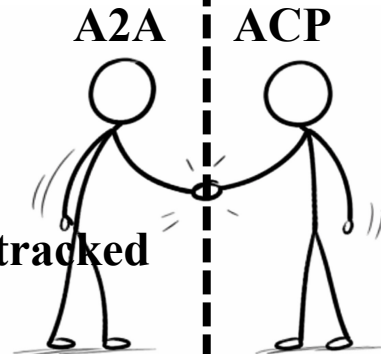
- past memory files
- semantic recall happens
- recalled chunks are logged
- frequently used / high-signal chunks get tracked
- future recall can become more targeted

- Hermes-executor and worker

Self-evolution

Real execution

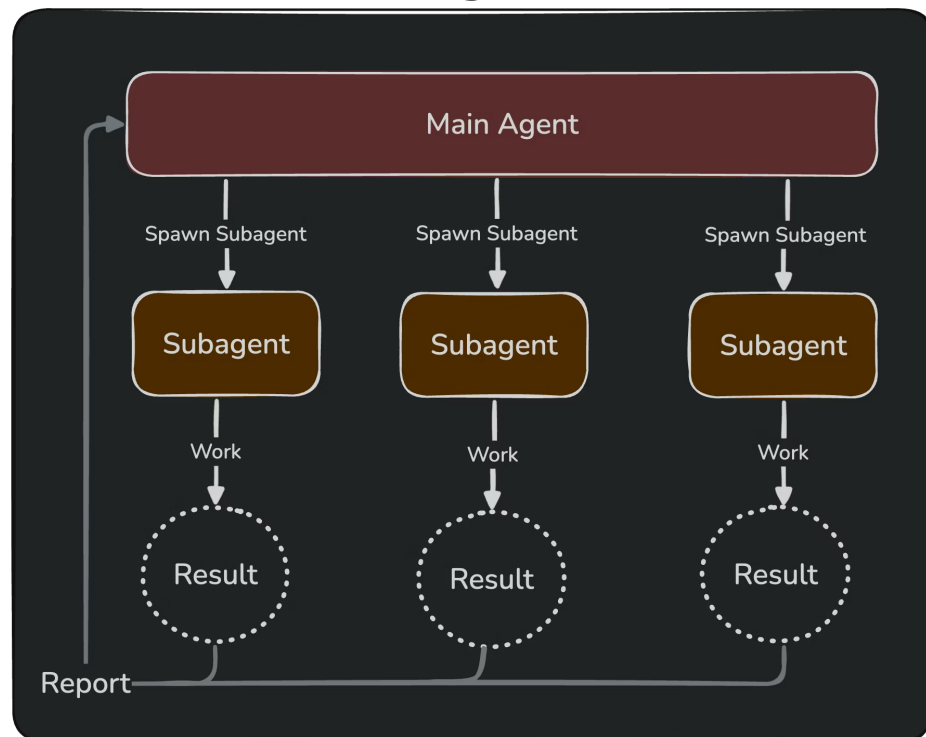
- feedback from success and failure
- distillation of reusable lessons
- memory for facts, skills for methods, workflows for reproduction
- correction and compression of weak or stale structure
- better future execution



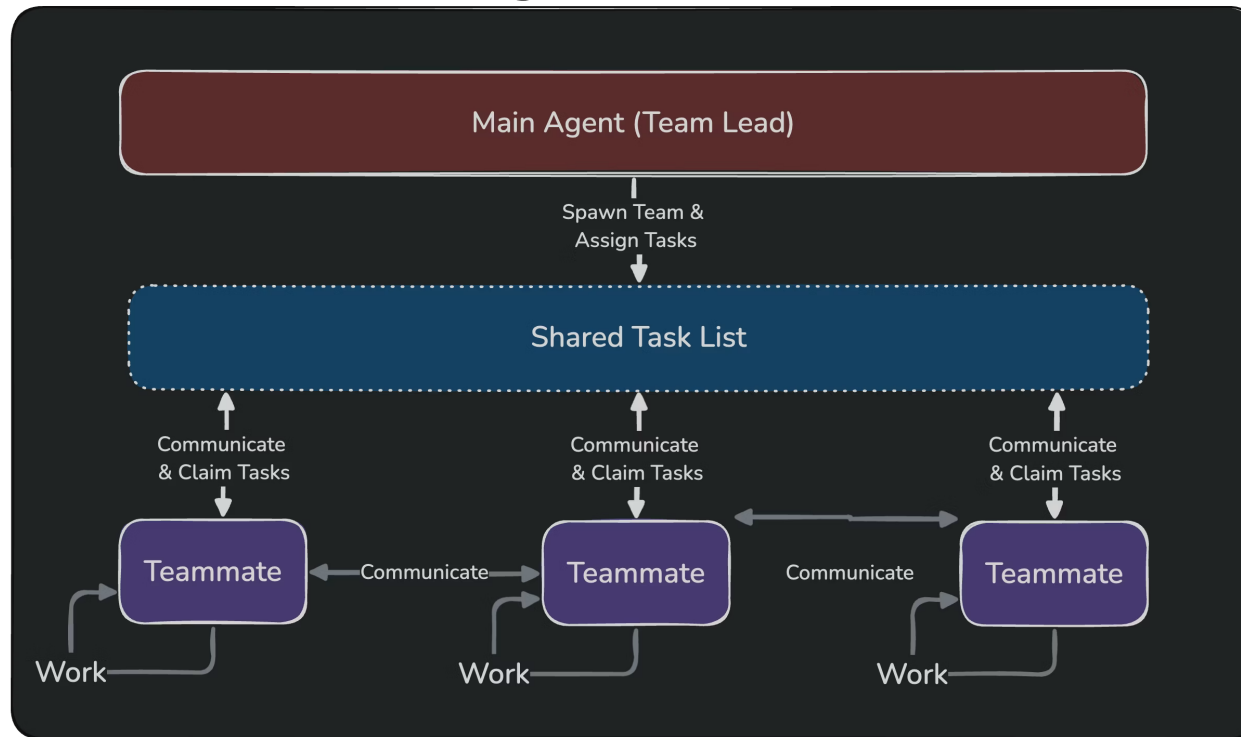
Under Exploring...

■ Openclaw and Hermes – Suitable Hardness, Expert Agents

Subagent



Agent Teams



<https://code.claude.com/docs/en/agent-teams>

- `penggroup.agent` with Agent Teams!
- Lammps AI !—More Suitable Harness, Better Agent!
- Expert agents for ab initio process !

[Github.com/karpathy/autoresearch](https://github.com/karpathy/autoresearch)

[Github.com/datawhalechina/hello-agents](https://github.com/datawhalechina/hello-agents)