

Molecular Excited States, Time-Dependent Density Functional Theory and Vibe-Coding with Agent

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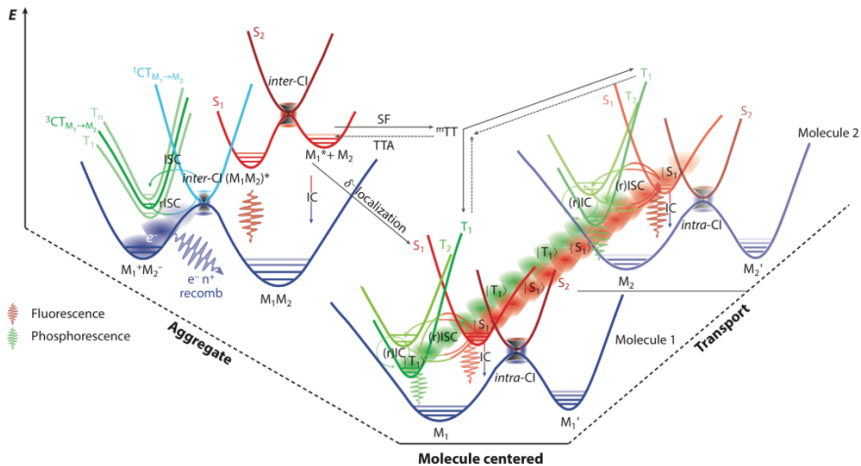
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 - Absorption Spectra Calculation from Linear Response TDDFT
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Molecular Excited States



Line spectra has two basic properties:

- **Location:** The location of the absorption peak-excitation ω_i
- **Intensity:** The height of the absorption peak-oscillator strength f_I

If we have the excited state wavefunction Ψ_I , the oscillator strength is defined as:

$$f_I = \frac{2}{3} \omega_I \sum_{n=x,y,z} |\langle \Psi_0 | \hat{r}_n | \Psi_I \rangle|^2$$

Where the Ψ_0 is the ground state wavefunction, and Ψ_I is the excited state wavefunction. We could also get the absorption spectra from the dynamic polarizability $\alpha_{ij}(\omega)$:

$$\sigma(\omega) = -\frac{4\pi\omega}{3c} \Im(\alpha_{ii}(\omega))$$

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Hohenberg-Kohn Theorem:

- HK I: The ground state or electron's density is only depended on external potential.
- HK II: For a given external potential, the energy functional is the global minimum value varying every density. And this density could be considered as the ground state electron's density.

Based on HK I ansatz, the many-electron Schrödinger equation is written in ν -representation as:

$$(\hat{T} + \hat{V}_{ee} + \hat{v})\Psi_0[\nu] = E_0[\nu]\Psi_0[\nu]$$

Based on HK II ansatz, the many-electron Schrödinger equation could be considered as a minimum problem of energy functional.

$$E_0[\nu] = \min_{\rho(\mathbf{r}) \rightarrow N} \{F[\rho(\mathbf{r})] + \int d\mathbf{r} \nu(\mathbf{r})\rho(\mathbf{r})\}$$

The Runge-Gross theorem establishes the foundation of time-dependent density functional theory (TDDFT) by proving a one-to-one correspondence between the time-dependent electron density $\rho(\mathbf{r}, t)$ and the external potential $v_{ext}(\mathbf{r}, t)$, for a given initial state.

- **Core statement:** $\rho(\mathbf{r}, t) \leftrightarrow v_{ext}(\mathbf{r}, t)$
- **Condition:** Initial state must be non-degenerate
- **Significance:** Time-dependent generalization of the Hohenberg-Kohn theorem

$$\rho(\mathbf{r}, t) \leftrightarrow \Psi(\mathbf{r}, t) \leftrightarrow v_{ext}(\mathbf{r}, t)$$

For a many-electron system, the time-dependent Schrödinger equation can be written as:

$$i\partial_t\Psi(\mathbf{r}, t) = \hat{H}\Psi(\mathbf{r}, t)$$

The details of Hamiltonian of Schrödinger equation is:

$$\hat{H} = \hat{T}(\mathbf{r}) + \hat{V}_{e-e}(\mathbf{r}) + \hat{V}_{n-e}(\mathbf{r}) + \hat{V}_{ext}(\mathbf{r}, t)$$

The action integral is defined as:

$$A = \int_{t_0}^{t_1} dt \langle \Psi | i\partial_t - \hat{H}(r, t) | \Psi \rangle$$

Just like ground state Kohn-Sham equation, the action integral of Kohn-Sham system is:

$$A_S[\rho] = B_S[\rho] - \int_{t_0}^{t_1} dt \int d^3r \rho_S(\mathbf{r}, t) v_S(\mathbf{r}, t)$$

The action integral B could be rewritten as:

$$B_S[\rho] = \int_{t_0}^{t_1} dt \sum_i \langle \phi_i[\rho] | i\partial_t - \hat{T}(\mathbf{r}) | \phi_i[\rho] \rangle + \int_{t_0}^{t_1} dt \int d^3r d^3r' \frac{\rho(\mathbf{r})\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}$$

The stationary condition of action integral gives:

$$\frac{\delta A_S[\rho]}{\delta \rho} = \frac{\delta B_S[\rho]}{\delta \rho} - v_S(\mathbf{r}, t) = 0$$

So, the action integral could be rewritten as:

$$A[\rho] = B_S[\rho] - \int_{t_0}^{t_1} dt \int d^3\mathbf{r} \rho(\mathbf{r}, t) v_{ext}(\mathbf{r}, t) \\ - \int_{t_0}^{t_1} dt \int d^3\mathbf{r} d^3\mathbf{r}' \frac{\rho(\mathbf{r})\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} - A_{xc}[\rho]$$

and the action integral of exchange-correlation is defined as:

$$A_{xc}[\rho] = B_S[\rho] - B[\rho]$$

$$B[\rho] = \int_{t_0}^{t_1} dt \langle \Psi[\rho] | i\partial_t - \hat{T}(\mathbf{r}) - \hat{V}_{e-e}(\mathbf{r}) | \Psi[\rho] \rangle$$

with adiabatic approximation of exchange-correlation functional:

$$E_{xc}[\rho] = \frac{\delta A_{xc}[\rho]}{\delta \rho} \Big|_{\rho(t)=\rho(0)}$$

the effective potential is defined as:

$$v_s(\mathbf{r}, t) = v_{ext} + \int d^3\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + E_{xc}[\rho]$$

Time-dependent Kohn-Sham equation:

$$i\partial_t\phi_i = \left[-\frac{1}{2}\nabla^2 + v_{ext} + \int d^3\mathbf{r}' \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + E_{xc}[\rho] \right] \phi_i$$

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In most of the TDDFT calculations of molecular systems, we have some basic assumptions:

- **Adiabatic approximation:** The exchange-correlation potential at any time depends only on the instantaneous electron density, neglecting memory effects.
- **Spin-restriction:** The spin-up and spin-down electron densities are assumed to be equal, simplifying the treatment of spin effects.
- **No fractional occupation:** Electrons are assumed to occupy orbitals in integer numbers, avoiding complications from partial occupancies.
- **Non-periodic systems:** The systems under study are considered to be non-periodic, which simplifies the boundary conditions and computational methods used.

The time-dependent Kohn-Sham equation is:

$$i\partial_t\phi_k(\mathbf{r}, t) = \hat{H}_{KS}(\mathbf{r}, t)\phi_k(\mathbf{r}, t)$$

with a simple external potential:

$$v_{ext}(\mathbf{r}, t) = -e\mathbf{r} \cdot \mathbf{E}_0\delta(t) = -e\mathbf{r} \cdot \mathbf{E}_0 \frac{1}{2\pi} \int_{-\infty}^{+\infty} e^{-i\omega t} d\omega$$

So, the ground state orbitals can be simply replaced by a time-evolution operator:

$$\phi_k(\mathbf{r}, t = 0^+) = \exp(i\mathbf{e}\mathbf{r} \cdot \mathbf{E}_0 t)\phi_k(\mathbf{r}, t = 0^-)$$

and the time-dependent dipole moment is defined as:

$$\mu(t) = -e \int \rho(\mathbf{r}, t)\mathbf{r}d^3\mathbf{r}$$

The we could calculate the dynamic polarizability with Fourier transform of time-dependent dipole moment:

$$\alpha_{ij}(\omega) = \frac{1}{E_{0j}} \int_0^{\infty} \exp(-i\omega t) [\mu_i(t) - \mu_i(0)] dt$$

Finally, the absorption spectrum comes from the diagonal elements of dynamic polarizability:

$$\text{Absorption Spectrum} \rightarrow \alpha_{ii}(\omega)$$

Expand time-dependent Kohn-Sham orbitals with perturbation parameter λ :

$$\phi_i(\mathbf{r}, t) = \phi_i^{(0)}(\mathbf{r}, t) + \lambda\phi_i^{(1)}(\mathbf{r}, t) + \lambda^2\phi_i^{(2)}(\mathbf{r}, t) + \mathcal{O}(\lambda^3)$$

External perturbation potential:

$$\hat{H}_{KS}(\mathbf{r}, t) = \hat{H}_{KS}^{(0)}(\mathbf{r}) + \lambda v_{ext}^{(1)}(\mathbf{r}, t) + \lambda \hat{H}_{KS}^{(1)}(\mathbf{r}, t)$$

Density expansion:

$$\rho(\mathbf{r}, t) = \sum_i f_i |\phi_i|^2 = \rho^{(0)}(\mathbf{r}, t) + \lambda\rho^{(1)}(\mathbf{r}, t) + \lambda^2\rho^{(2)}(\mathbf{r}, t) + \mathcal{O}(\lambda^3)$$

in detail:

$$\rho^{(0)}(\mathbf{r}, t) = \sum_i n_i |\phi_i^{(1)}|^2$$

$$\rho^{(1)}(\mathbf{r}, t) = \sum_i n_i |[\phi_i^{(0)}]^* [\phi_i^{(1)}] + [\phi_i^{(1)}]^* [\phi_i^{(0)}]|$$

The first-order response Hamiltonian is defined as:

$$\hat{H}_{KS}^{(1)}(\mathbf{r}, t) = \int d^3\mathbf{r}' \frac{\rho^{(1)}(\mathbf{r}', t)}{|\mathbf{r} - \mathbf{r}'|} + \int d^3\mathbf{r}' f_{xc}^{(0)}(\mathbf{r}, t; \mathbf{r}', t') \rho^{(1)}(\mathbf{r}', t')$$

and the TDKS equation is:

$$i\partial_t \phi_i^{(1)}(\mathbf{r}, t) = \hat{H}_{KS}^{(0)}(\mathbf{r}) \phi_i^{(1)}(\mathbf{r}, t) + [\nu_{ext}^{(1)}(\mathbf{r}, t) + \hat{H}_{KS}^{(1)}(\mathbf{r}, t)] \phi_i^{(0)}(\mathbf{r}, t)$$

Consider a periodic perturbation with single frequency ω for most of the cases:

$$v_{ext}^{(1)}(\mathbf{r}, t) = v_{ext}^{+\omega}(\mathbf{r})e^{i\omega t} + h.c.$$

So, the general solution of first-order TDKS equation is:

$$\phi_i(\mathbf{r}, t) = e^{-i\varepsilon_i^{(0)}t - \lambda i\Delta\varepsilon_i^{(1)}t}$$

$$\times \{ \phi_i^{(0)}(\mathbf{r}) + \lambda [\phi_i^{(1),+\omega}(\mathbf{r})e^{i\omega t} + \phi_i^{(1),-\omega}(\mathbf{r})e^{-i\omega t}] \} + O(\lambda^2)$$

Where the $\phi_i^{(1),+\omega}(\mathbf{r})$ and $\phi_i^{(1),-\omega}(\mathbf{r})$ are the first-order response orbitals with frequency of $+\omega$ and $-\omega$. And the $\Delta\varepsilon_i^{(1)}$ is the level shift of first-order response Hamiltonian.

$$\Delta\varepsilon_i^{(1)} = \int dt \langle \phi_i^{(0)} | [v_{ext}^{(1)} + \hat{H}_{KS}^{(1)}] | \phi_i^{(0)} \rangle$$

So, the first-order density is:

$$\rho^{(1)}(\mathbf{r}, t) = \sum_i n_i \{ [\phi_i^{(0)}]^* \phi_i^{+\omega, (1)} + [\phi_i^{-\omega, (1)}]^* \phi_i^{(0)} \} e^{-i\omega t} + c.c.$$

After some algebra, we could get the Sternheimer equation:

$$\begin{aligned} & i\partial_t e^{-i\varepsilon_i^{(0)}t - \lambda i\Delta\varepsilon_i^{(1)}t} \{ \phi_i^{(0)}(\mathbf{r}) + \lambda [\phi_i^{(1), +\omega}(\mathbf{r}) e^{i\omega t} + \phi_i^{(1), -\omega}(\mathbf{r}) e^{-i\omega t}] \} \\ &= \hat{H}_{KS}^{(0)}(\mathbf{r}) e^{-i\varepsilon_i^{(0)}t - \lambda i\Delta\varepsilon_i^{(1)}t} \{ \phi_i^{(0)}(\mathbf{r}) + \lambda [\phi_i^{(1), +\omega}(\mathbf{r}) e^{i\omega t} + \phi_i^{(1), -\omega}(\mathbf{r}) e^{-i\omega t}] \} \\ &+ \lambda \{ [\int d^3f_{Hxc} \rho^{(1)}(\mathbf{r}', t) + v_{ext}^{(1)}(\mathbf{r}, t)] \phi_i^{(0)}(\mathbf{r}) \} e^{-i\varepsilon_i^{(0)}t - \lambda i\Delta\varepsilon_i^{(1)}t} \end{aligned}$$

Now we divide the equation into two parts with frequency of $+\omega$ and $-\omega$ for resonant and anti-resonant solution. So we could rewrite the Sternheimer equation in a compact form:

For resonant solution ($+\omega$):

$$[\hat{H}_{KS}^{(0)} - \varepsilon_i^{(0)} + \omega + i\eta] \phi_i^{(1),+\omega}(\mathbf{r}) = -Q_i^{+\omega}(\mathbf{r}) \phi_i^{(0)}(\mathbf{r})$$

where $Q_i^{+\omega}(\mathbf{r}) = \int d^3\mathbf{r}' f_{Hxc} \rho^{+\omega,(1)}(\mathbf{r}', t) + v_{ext}^{+\omega}(\mathbf{r})$

For anti-resonant solution ($-\omega$):

$$[\hat{H}_{KS}^{(0)} - \varepsilon_i^{(0)} - \omega + i\eta] \phi_i^{(1),-\omega}(\mathbf{r}) = -Q_i^{-\omega}(\mathbf{r}) \phi_i^{(0)}(\mathbf{r})$$

where $Q_i^{-\omega}(\mathbf{r}) = \int d^3\mathbf{r}' f_{Hxc} \rho^{-\omega,(1)}(\mathbf{r}', t) + v_{ext}^{-\omega}(\mathbf{r})$

with a decay factor η of external perturbation in $e^{-\eta t}$.

The electron-hole basis is defined as:

$$\phi_i^{(1)} = \sum_a c_{ai} \phi_a^{(0)}(\mathbf{r})$$

Then, rewrite the first-order Sternheimer equation in electron-hole basis:

$$\begin{aligned} & \sum_{aj} (-\omega + \varepsilon_j^{(0)}) \delta_{ab} \delta_{ij} c_{aj}^{+\omega} + \sum_{aj} (\omega + \varepsilon_i^{(0)}) \delta_{ab} \delta_{ij} c_{aj}^{-\omega} \\ &= \sum_{aj} \varepsilon_a^{(0)} \delta_{ab} \delta_{ij} c_{aj}^{+\omega} + \sum_{aj} \varepsilon_a^{(0)} \delta_{ab} \delta_{ij} c_{aj}^{-\omega} \\ &+ \langle \phi_b^{(0)} | f_{Hxc}[\rho^{(0)}] \rho^{(1)} + v_{ext}^{(1)} | \phi_i^{(0)} \rangle \end{aligned}$$

The Hartree-exchange-correlation kernel:

$$f_{Hxc}(\mathbf{r}, \mathbf{r}') = \frac{1}{|\mathbf{r} - \mathbf{r}'|} + f_{xc}(\mathbf{r}, \mathbf{r}')$$

Coupling matrices in electron-hole basis:

$$K_{bi,aj} = \int d^3\mathbf{r} \int d^3\mathbf{r}' \phi_a^{*(0)}(\mathbf{r}') \phi_j^{(0)}(\mathbf{r}') \\ \times f_{Hxc}(\mathbf{r}, \mathbf{r}') \phi_b^{*(0)}(\mathbf{r}) \phi_i^{(0)}(\mathbf{r})$$

Compact form:

$$\langle \phi_b^{(0)} | f_{Hxc}[\rho^{(0)}] \rho^{(1)} | \phi_i^{(0)} \rangle = \sum_{aj} n_j \{ K_{bi,aj} (c_{aj}^{+\omega} e^{-i\omega t} + c_{aj}^{-\omega} e^{i\omega t}) \\ + K_{bi,ja} (c_{aj}^{+\omega} e^{i\omega t} + c_{aj}^{-\omega} e^{-i\omega t}) \}$$

with the coupling matrix $K_{bi,aj}$ as defined previously.
The Casida equation in matrix form:

$$\begin{bmatrix} -\Delta E - \mathbf{K} & -\mathbf{K}' \\ \mathbf{K}' & \Delta E + \mathbf{K} \end{bmatrix} \begin{bmatrix} \text{Re}[B^{+\omega}] \\ \text{Re}[B^{-\omega}] \end{bmatrix} = \omega \begin{bmatrix} \text{Re}[B^{+\omega}] \\ \text{Re}[B^{-\omega}] \end{bmatrix}$$

where $\Delta E_{bi,aj} = (\varepsilon_a - \varepsilon_i)\delta_{ab}\delta_{ij}$

We rewrite the Casida equation in a more familiar form:

$$\begin{bmatrix} A & B \\ B^* & A^* \end{bmatrix} \begin{bmatrix} X \\ Y \end{bmatrix} = \omega \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} X \\ Y \end{bmatrix}$$

with the matrix elements:

A-matrix:

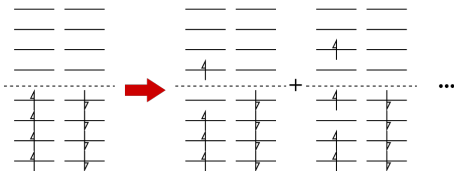
$$A_{bi,aj} = \delta_{ij}\delta_{ab}(\epsilon_j - \epsilon_b) + \int d\mathbf{r} \int d\mathbf{r}' \phi_i^*(\mathbf{r})\phi_b(\mathbf{r}) \\ \times \left[\frac{1}{|\mathbf{r} - \mathbf{r}'|} + \frac{\delta^2 E_{xc}}{\delta\rho(\mathbf{r})\delta\rho(\mathbf{r}')} \right] \phi_a^*(\mathbf{r}')\phi_j(\mathbf{r}')$$

B-matrix:

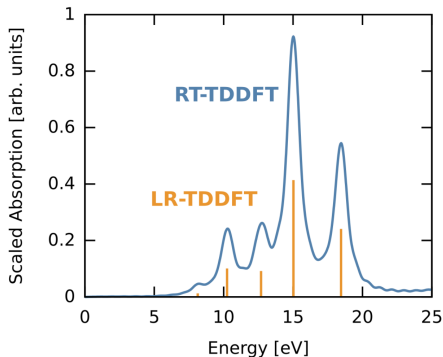
$$B_{bi,aj} = \int d\mathbf{r} \int d\mathbf{r}' \phi_i^*(\mathbf{r})\phi_b(\mathbf{r}) \\ \times \left[\frac{1}{|\mathbf{r} - \mathbf{r}'|} + \frac{\delta^2 E_{xc}}{\delta\rho(\mathbf{r})\delta\rho(\mathbf{r}')} \right] \phi_j^*(\mathbf{r}')\phi_a(\mathbf{r}')$$

Overview of three Approaches

- Time-Propagation Approach
- Sternheimer Approach
- Casida Approach



Water Gas-Phase 6-31G/TD-PBE0 Absorption



Appendix-Matrix Size of Hamiltonian in DFT and TDDFT

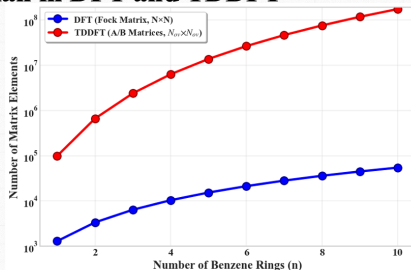
Casida Equation

$$\begin{pmatrix} A & B \\ B^* & A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} \quad \psi_{ex} = \sum_{ai} x_{ai} \phi_{ai}$$

$$A_{ia,jb} = \delta_{ij} \delta_{ab} (\epsilon_a - \epsilon_i) + \int dr \int r' \phi_i(\mathbf{r}) \phi_a^*(r) \left\{ \frac{1}{|\mathbf{r}-\mathbf{r}'|} + f_{xc} \right\} \phi_b^*(r') \phi_j(r')$$

$$B_{ia,jb} = \int dr \int r' \phi_i(\mathbf{r}) \phi_a^*(r) \left\{ \frac{1}{|\mathbf{r}-\mathbf{r}'|} + f_{xc} \right\} \phi_b^*(r') \phi_j(r')$$

$$\psi_{ai} = \sum_{ai} y_{ai} \phi_{ai}$$



Ground State Hamiltonian Matrix: $\sim O(N_e^3)$ for calculation

- $(N_{occ} + N_{virt}) \times (N_{occ} + N_{virt})$

Excited State AB Matrix: $\sim O(N_e^5)$ for calculation $\sim O(N_e^4)$ for memory

- $(2N_{occ} \times N_{virt}) \times (2N_{occ} \times N_{virt})$

- $(N_{occ} \times N_{virt}) \times (N_{occ} \times N_{virt})$ in Tamm-Dancoff Approximation

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Given the Casida matrix:

$$\mathcal{L} = \begin{pmatrix} A & B \\ -B^* & -A^* \end{pmatrix}$$

and we want to solve

$$\mathcal{L}\Psi_k = \omega_k\Psi_k$$

where Ψ_k stacks (X_k, Y_k) .

Assume we have a set of orthonormal subspace trial vectors:

$$\{\Psi_j\}_{j=1}^m, \quad \Psi_j = \begin{pmatrix} X_j \\ Y_j \end{pmatrix}$$

Construct matrix $W \in \mathbb{C}^{2N \times m}$, with columns Ψ_j .

Project \mathcal{L} into this subspace:

$$H_{\text{eff}} = W^\dagger \mathcal{L} W \in \mathbb{C}^{m \times m}$$

Solve the projected problem:

$$H_{\text{eff}} \mathbf{y}_i = \omega_i \mathbf{y}_i$$

Ritz vectors:

$$\Psi_i^{(\text{Ritz})} = W \mathbf{y}_i$$

Residuals:

$$\mathbf{r}_i = \mathcal{L} \Psi_i^{(\text{Ritz})} - \omega_i \Psi_i^{(\text{Ritz})}$$

If all $\|\mathbf{r}_i\|$ are below tolerance, the solution is found. Otherwise, use preconditioned residuals to further expand subspace W and repeat.

If the residual is too large, expand the subspace as follows:

- 1 Compute the residual:

$$\mathbf{r}_i = \mathcal{L}\Psi_i^{(\text{Ritz})} - \omega_i\Psi_i^{(\text{Ritz})}$$

- 2 Apply a preconditioner:

$$t_i \approx \frac{\mathbf{r}_i}{\text{diag}(H_{\text{eff}}) - \omega_i}$$

- 3 Orthonormalize t_i against existing subspace vectors.
- 4 If t_i is not linearly dependent ($\|t_i\|$ big enough), add it to the subspace.
- 5 Repeat the Rayleigh-Ritz projection with the enlarged subspace.

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Vibe Coding represents a new paradigm where developers interact with AI coding assistants through natural language conversations to build software solutions.

Key characteristics:

- Natural language interface for coding
- Iterative refinement through conversation
- AI handles implementation details
- Human focuses on high-level design
- Rapid prototyping and exploration

Vibe Coding in Practice: AI-Assisted Development Environment

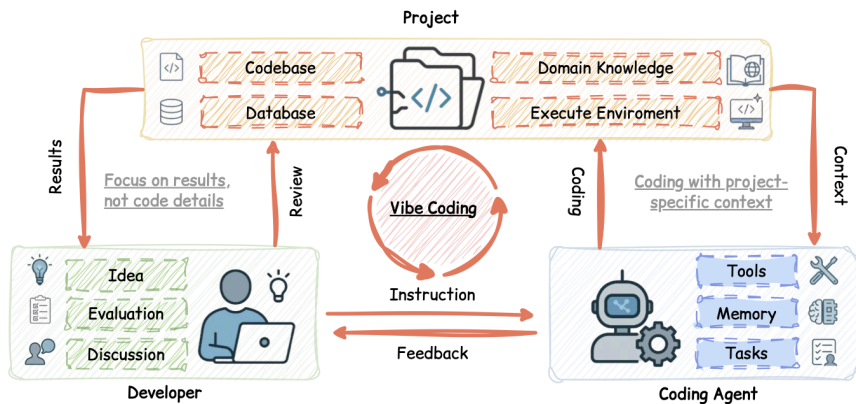


Figure 1: AI-Assisted Development Environment

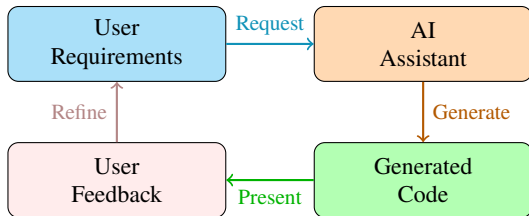


Figure 3: Vibe Coding Iterative Workflow

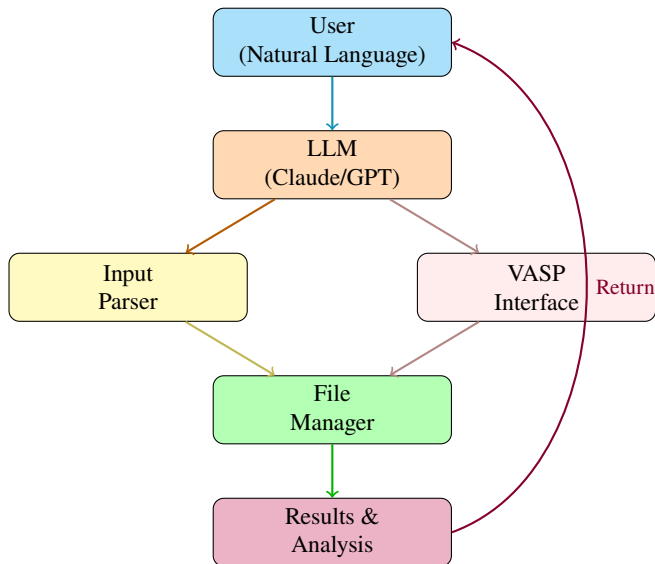


Figure 4: VASPilot Architecture ¹

Core Capabilities:

- Natural language input for VASP calculations
- Automatic INCAR, KPOINTS, POSCAR generation
- Job submission and monitoring
- Result extraction and analysis
- Integration with popular quantum chemistry packages

User Request:

”Calculate the band structure of silicon with PBE functional”



VASpilot Response:

- Generates INCAR with PBE functional
- Creates KPOINTS file
- Sets up POSCAR structure
- Submits calculation to queue
- Returns band structure results

Figure 5: Example VASpilot Interaction

Computational Setup:

- **Molecule:** H₂O (water molecule)
- **Method:** TDDFT with various functionals
- **Basis Set:** 6-31G(d) and 6-31+G(d,p)
- **Functionals Tested:**
 - PBE (GGA functional)
 - B3LYP (Hybrid functional)
 - CAM-B3LYP (Long-range corrected hybrid)

Vibe Coding Approach:

- Used natural language to describe requirements
- AI assistant generated Python code for TDDFT calculations
- Automated spectrum plotting and analysis
- Interactive refinement of visualization

Water Molecule Absorption Spectrum

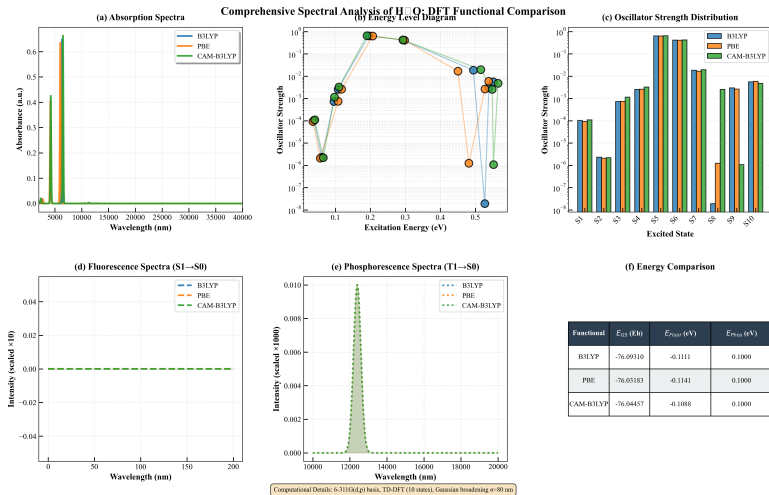


Figure 6: Absorption spectrum of water molecule calculated with TDDFT using different functionals

Key Observations:

- PBE underestimates excitation energies
- B3LYP provides better agreement with experiment
- CAM-B3LYP improves for charge-transfer states
- Basis set effects are significant

Functional	Peak (eV)	Intensity
PBE	7.2	0.85
B3LYP	7.8	0.92
CAM-B3LYP	8.1	0.88
Exp.	7.9	-

Table 1: Comparison of excitation energies

Workflow:

1 Natural Language Request:

- "Calculate absorption spectrum of water molecule using TDDFT with B3LYP functional and 6-31G(d) basis set"

2 AI Code Generation:

- Python script using PySCF
- Automatic geometry optimization
- TDDFT calculation
- Spectrum extraction and plotting

3 Interactive Refinement:

- Adjust plotting style
- Add Gaussian broadening
- Compare multiple functionals
- Annotate peaks

Advantages:

- **Accessibility:** Lower barrier to entry
- **Efficiency:** Rapid prototyping
- **Flexibility:** Easy modification and exploration
- **Learning:** Natural learning curve
- **Documentation:** Self-documenting conversations

Applications:

- Method development
- Rapid screening
- Educational tools
- Automated workflows

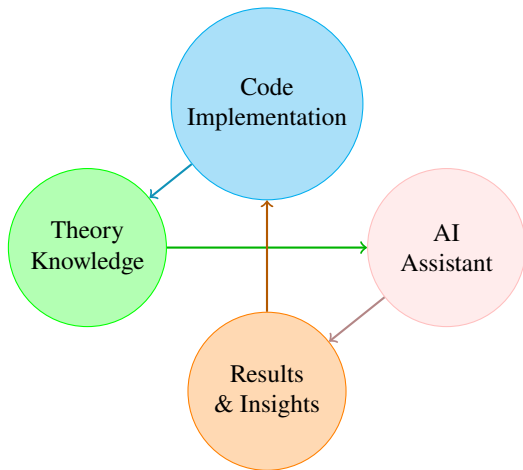


Figure 7: Vibe Coding Iterative Development Cycle

Problem Statement:

- Rapid growth of scientific literature in electronic structure theory and AI
- Time-consuming to manually track relevant papers
- Need for automated, personalized paper collection
- Integration of theoretical chemistry with AI tools

Objectives:

- Automated daily paper fetching from arXiv
- Keyword-based filtering (electronic structure + AI)
- LaTeX PDF report generation
- Cross-platform compatibility
- Scheduled execution with notifications

Interactive Development with AI:

- 1 **Initial Request:** "Create a Python program to collect arXiv papers on electronic structure and AI, generate PDF reports"
- 2 **AI Iterations:**
 - Architecture design
 - Code implementation (6 core modules)
 - Bug fixing (datetime, Jinja2, LaTeX)
 - Portability improvements
- 3 **User Feedback Loop:**
 - Testing and validation
 - Feature requests (notifications, scheduling)
 - Documentation improvements
- 4 **Final Deployment:** GitHub repository with automatic scheduling

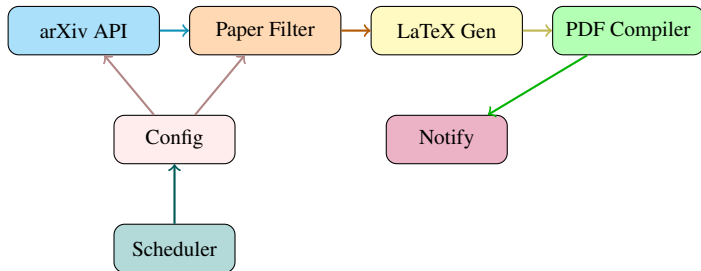


Figure 8: ArXiv Paper Collector Architecture

Six Core Modules:

- 1 **arxiv_fetcher.py**
arXiv API integration
- 2 **paper_filter.py**
Keyword-based filtering
- 3 **latex_generator.py**
LaTeX document generation
- 4 **pdf_compiler.py**
PDF compilation
(pdflatex/xelatex)
- 5 **scheduler.py**
Task scheduling
- 6 **notifications.py**
System & email notifications

Key Features

- ✓ 1000+ lines of Python code
- ✓ Cross-platform support
- ✓ YAML configuration
- ✓ Automatic installation
- ✓ Scheduled execution
- ✓ Notification system

Sample Output:

- **Date:** 2026-01-12
- **Papers Collected:** 394 papers (7 days)
- **Groups:**
 - Electronic Structure: 327 papers
 - Artificial Intelligence: 317 papers
 - Uncategorized: 14 papers
- **PDF Size:** 170 KB

Report Contents:

- Paper title and authors
- arXiv ID and PDF download link
- Publication date and categories
- Formatted abstract (truncated)
- Hyperlinked references

Cron Job Configuration:

- Automatic daily execution at 10:00 AM
- Log file: `output/cron.log`
- Error handling and retries

Notification System:

- Desktop notifications (macOS/Linux/Windows)
- Email notifications via SMTP
- Success/failure status updates

Sample Notification

*”Successfully collected 394 papers
PDF: `output/papers/arxiv_papers_2026-01-12.pdf`”*

Repository:

- <https://github.com/STOKES-DOT/arxiv-paper-collector>
- Open source (MIT License)
- Complete documentation
- Installation scripts for all platforms

Portability Features:

- Cross-platform (Windows/macOS/Linux)
- Virtual environment support
- User configuration directory (`~/ .config/arxiv-collector`)
- Path auto-expansion
- One-command setup: `./install.sh`

Development Time: ~2 hours (from concept to deployment)

Key Advantages Shown:

- **Rapid Prototyping:** Working code after initial prompt
- **Iterative Refinement:** Bug fixes and features through conversation
- **Cross-Disciplinary:** Combined TDDFT knowledge with software engineering
- **Best Practices:** Clean code, documentation, version control
- **Deployment:** GitHub integration, CI/CD ready

Impact:

- Automated daily literature review
- Saved hours of manual work
- Customizable for any research field
- Shareable with research community

TDDFT:

- Powerful method for excited states
- Three main approaches (Time-Propagation, Sternheimer, Casida)
- Balance between accuracy and computational cost

Vibe Coding:

- Natural language interface
- AI-assisted development
- Democratizing computational chemistry

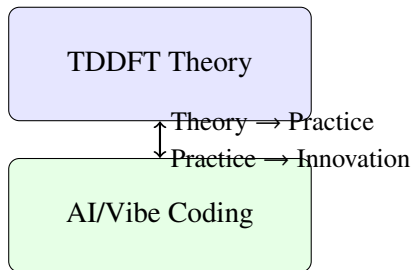


Figure 9: Synergy of Theory and AI