

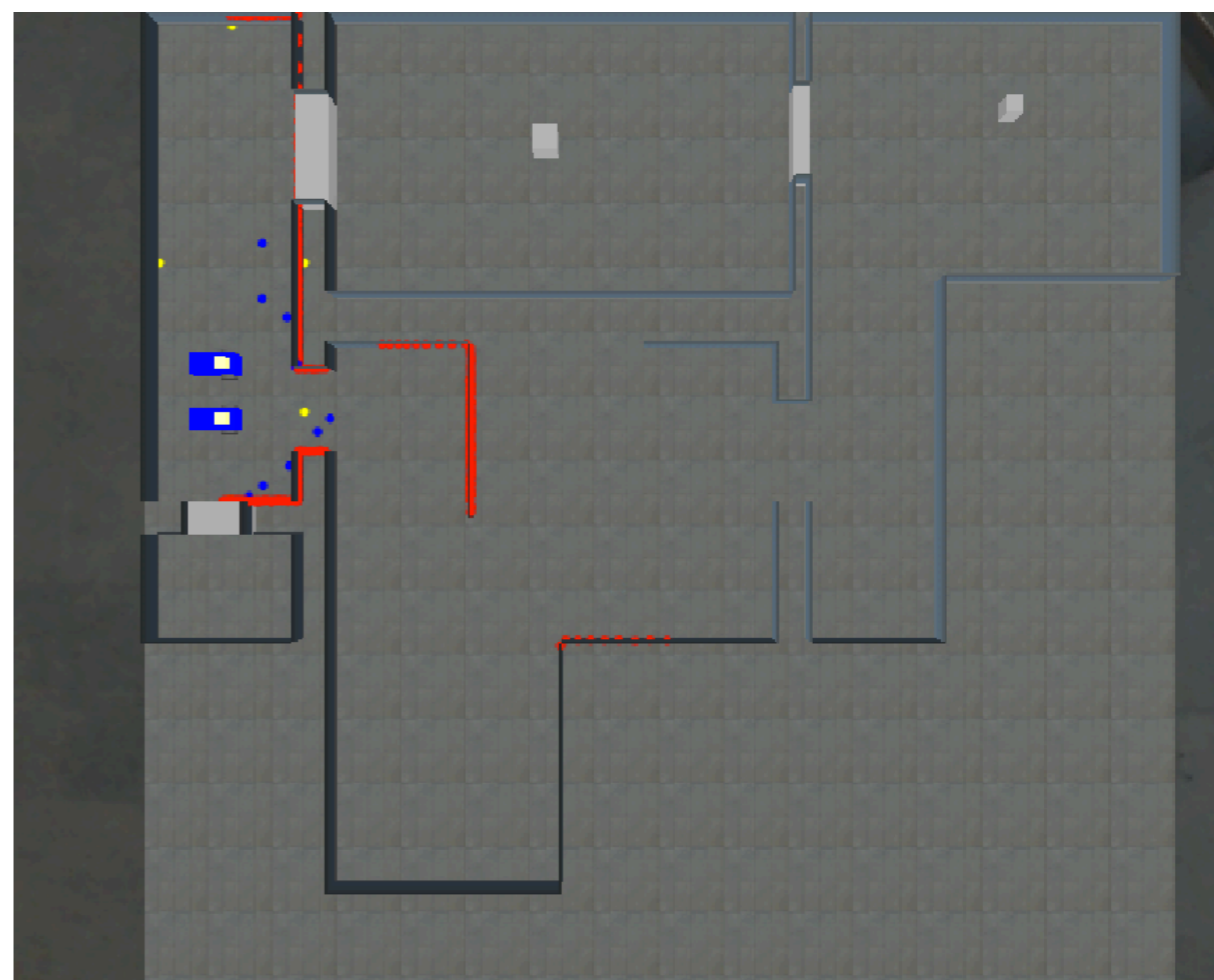
Soar Robot Unleashed

Keegan R. Kinkade

21 February 2012

Soar Robot Environment

- ❖ Soar Robot Project
 - ❖ Differentially driven robot utilizing LIDAR (Light Detection And Ranging)
 - ❖ Encoders estimate robot's trajectory
- ❖ What additional machinery is required to place agent in world?



Input Link

^{^io.input-link}

Area Description

- ^{^id}
- ^{^type}
- ^{^gateway}
 - ^{^id}
 - ^{^x}, ^{^y}, ^{^distance}
 - ^{^direction}
 - ^{^to} (2x)
 - ^{^door}
 - ^{^id}
 - ^{^state}
- ^{^wall}
 - ^{^direction}
 - ^{^open}
 - ^{^to}
 - ^{^x}, ^{^y}, ^{^distance}
- ^{^light}

About the Robot

- ^{^self}
 - ^{^name}
 - ^{^area}
 - ^{^headlight}
 - ^{^battery}
 - ^{^pose}
 - ^{^x}
 - ^{^x-velocity}
 - ^{^y}
 - ^{^y-velocity}
 - ^{^yaw}
 - ^{^yaw-velocity}

LIDAR

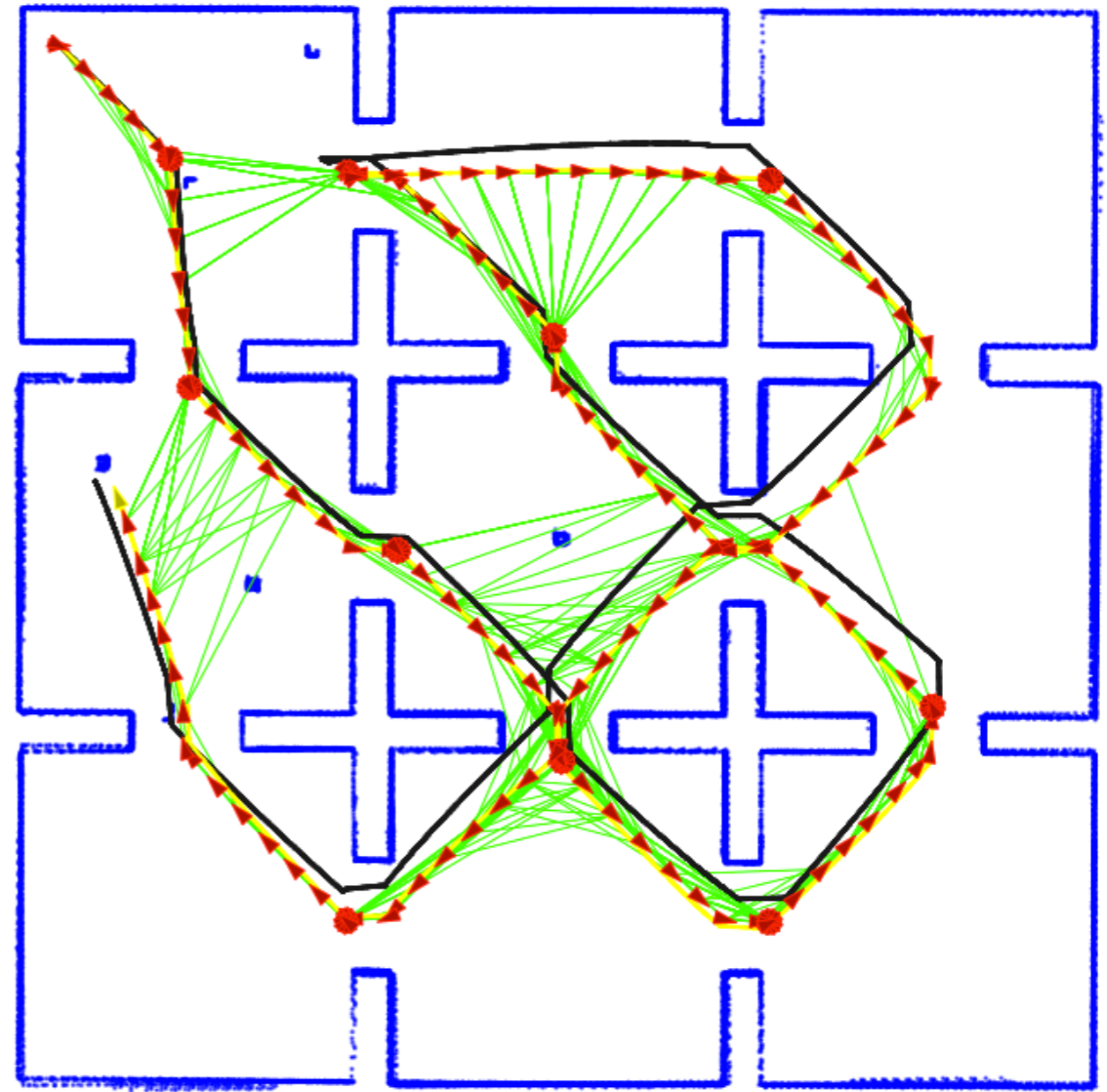
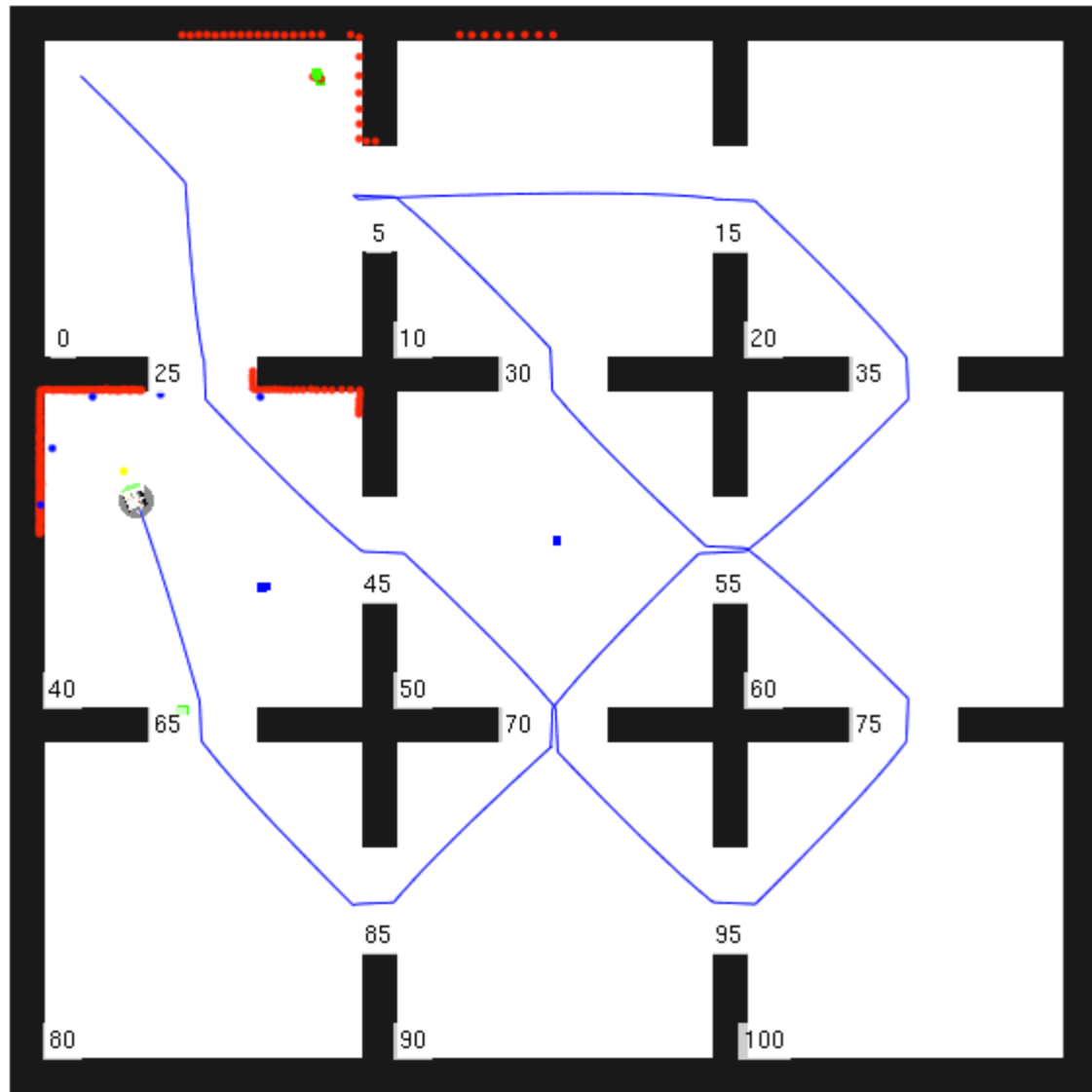
- ^{^lidar}
- ^{^range}
- ^{^id}
- ^{^distance}
- ^{^rel-bearing}

Objects

- ^{^object}
 - ^{^id}
 - ^{^visible}
 - ^{^x}
 - ^{^y}
 - ^{^distance}
 - ^{^...}

SLAM

**Topological
Mapping**



Simultaneous Localization & Mapping

Simultaneous Localization and Mapping

- ❖ While robot is exploring unknown environment:

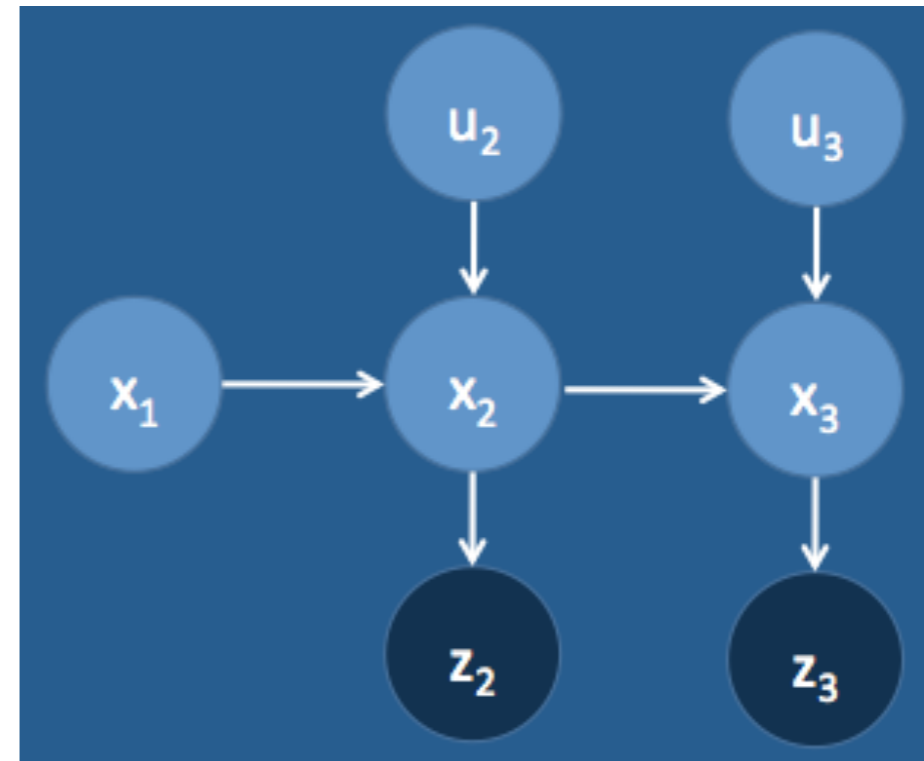
- ❖ **GIVEN**: Robot's movement commands and observations of unknown environment

- ❖ **ESTIMATE**: Map of features and robot's path through environment

- ❖ Probabilistically motivated problem:

- ❖ Errors within robot's movement and observations

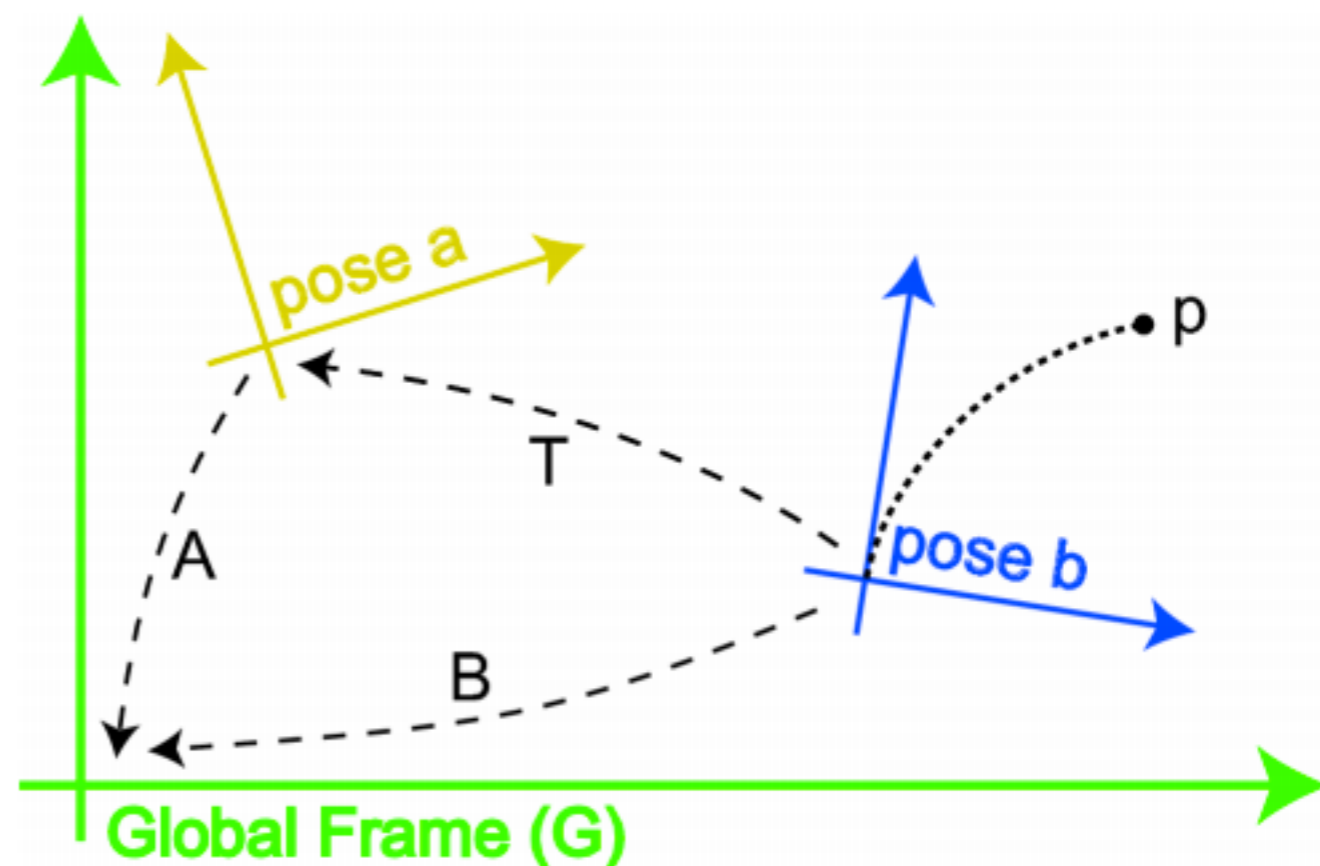
$$p(s, f \mid u, z, d)$$



Pose / Feature Graphs

- ❖ Poses and Features represented as 'Nodes'
- ❖ Connected by 'Edges' composed of Rigid Body Transformations
- ❖ Additional observations create an overdetermined system
- ❖ Feature p in Global Frame:

$$\begin{aligned} p' &= Ap \\ &= ABp \end{aligned}$$



$$T = \begin{bmatrix} \cos(\Delta\theta) & -\sin(\Delta\theta) & \Delta x \\ \sin(\Delta\theta) & \cos(\Delta\theta) & \Delta y \\ 0 & 0 & 1 \end{bmatrix}$$

Non-Linear SLAM

* Edge \rightarrow Observation: $z_i = f_i(x)$

* Observation Residual: $r_i = z_i - f_i(x)$

* Scale Residual by Observation Confidence:

$$\chi_i^2 = (z_i - f_i(x))^T \Sigma_i^{-1} (z_i - f_i(x))$$

* Typical Observations \neq Linear

* Stack linearized observations using Jacobian:

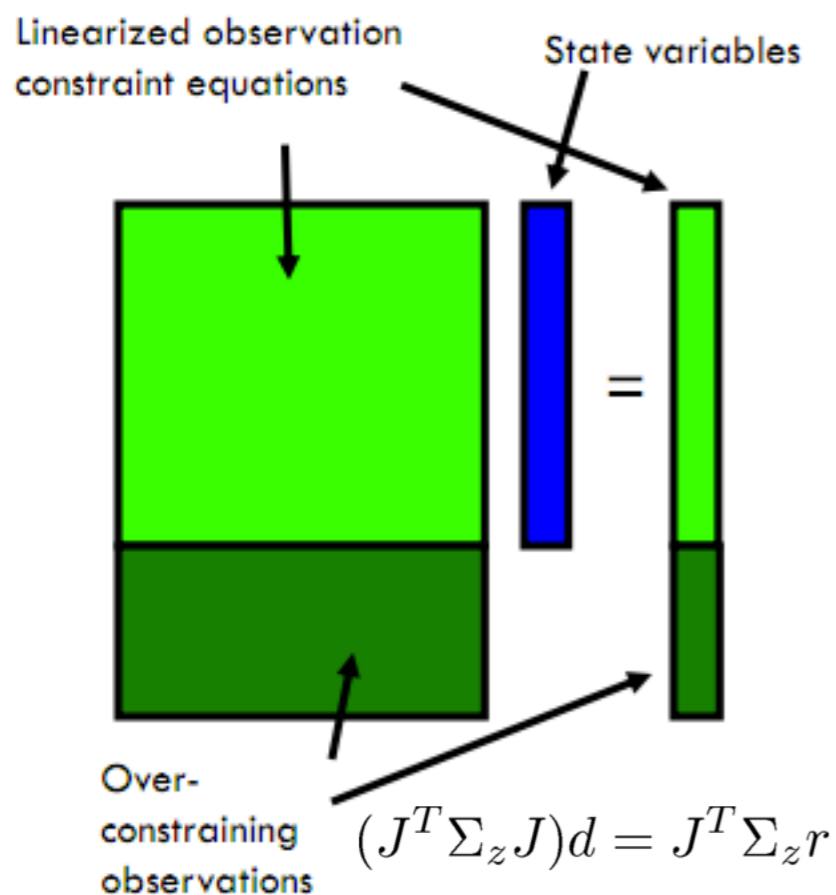
$$\chi^2 \approx (Jd - r)^T \Sigma^{-1} (Jd - r), \text{ where}$$

* r is the observation residual

* d is the linearization residual $(x - x_0)$

* Differentiate χ^2 with respect to d , solve for d which minimizes the χ^2 error

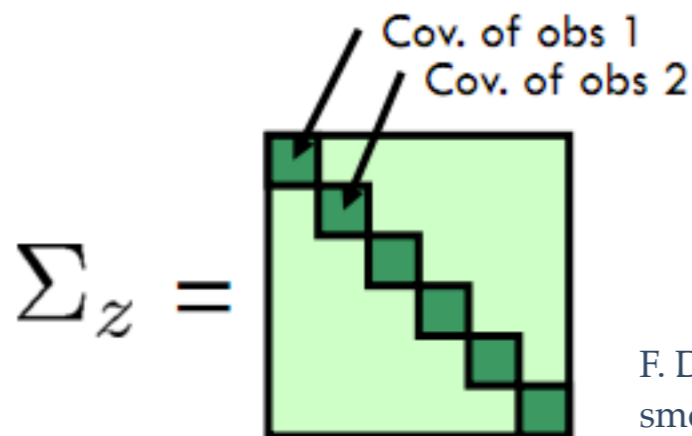
Square root SAM



- ❖ Naive Solution:

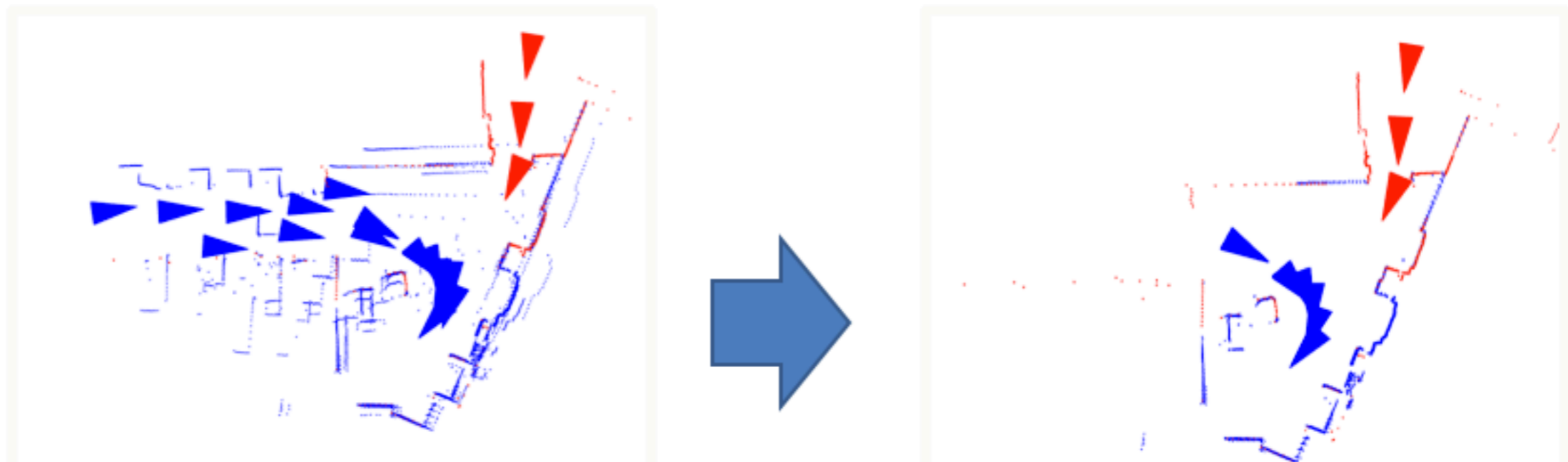
$$d = \underbrace{(J^T \Sigma_z^{-1} J)^{-1}}_{\text{Information Matrix}} J^T \Sigma_z^{-1} r$$

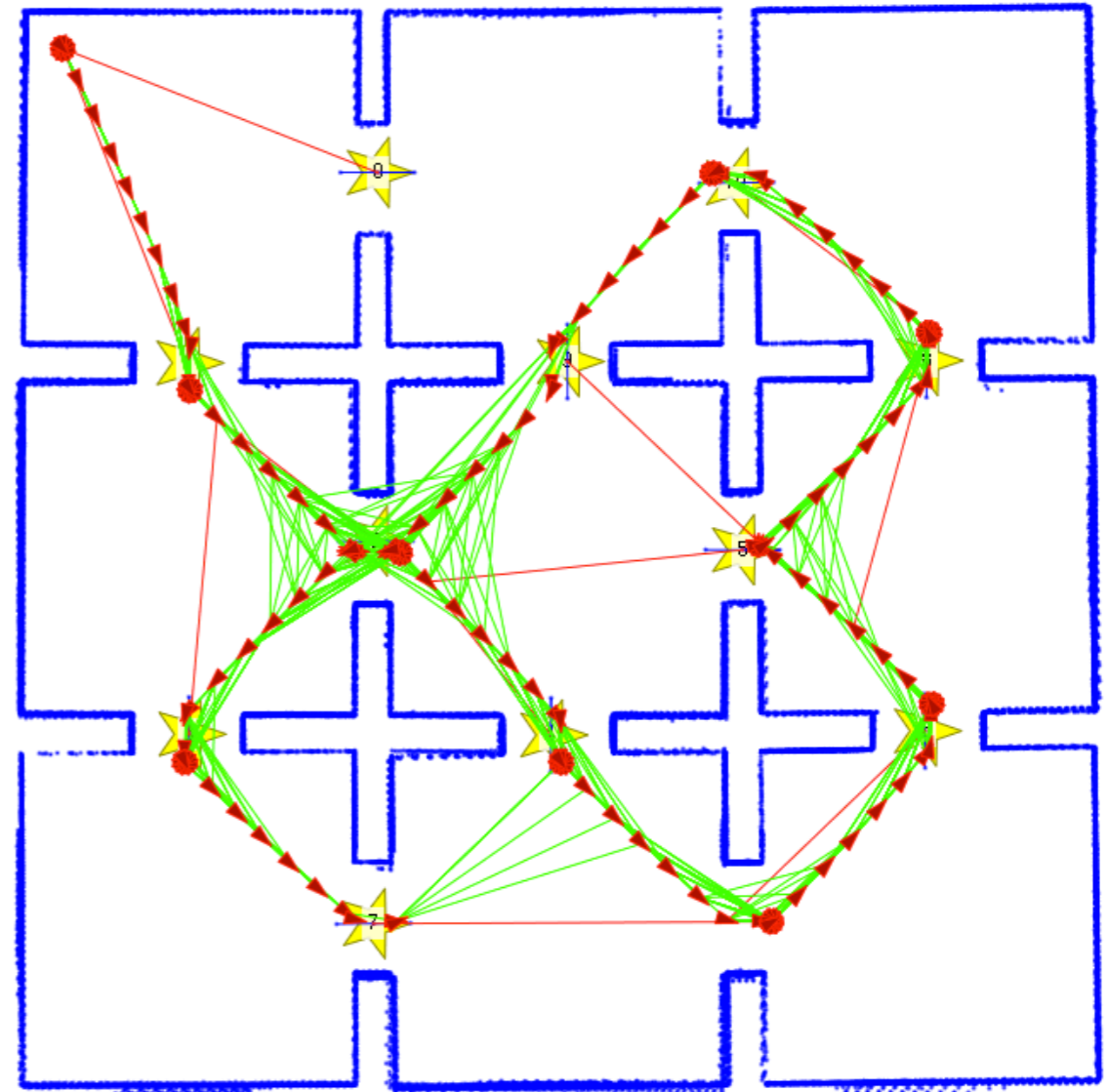
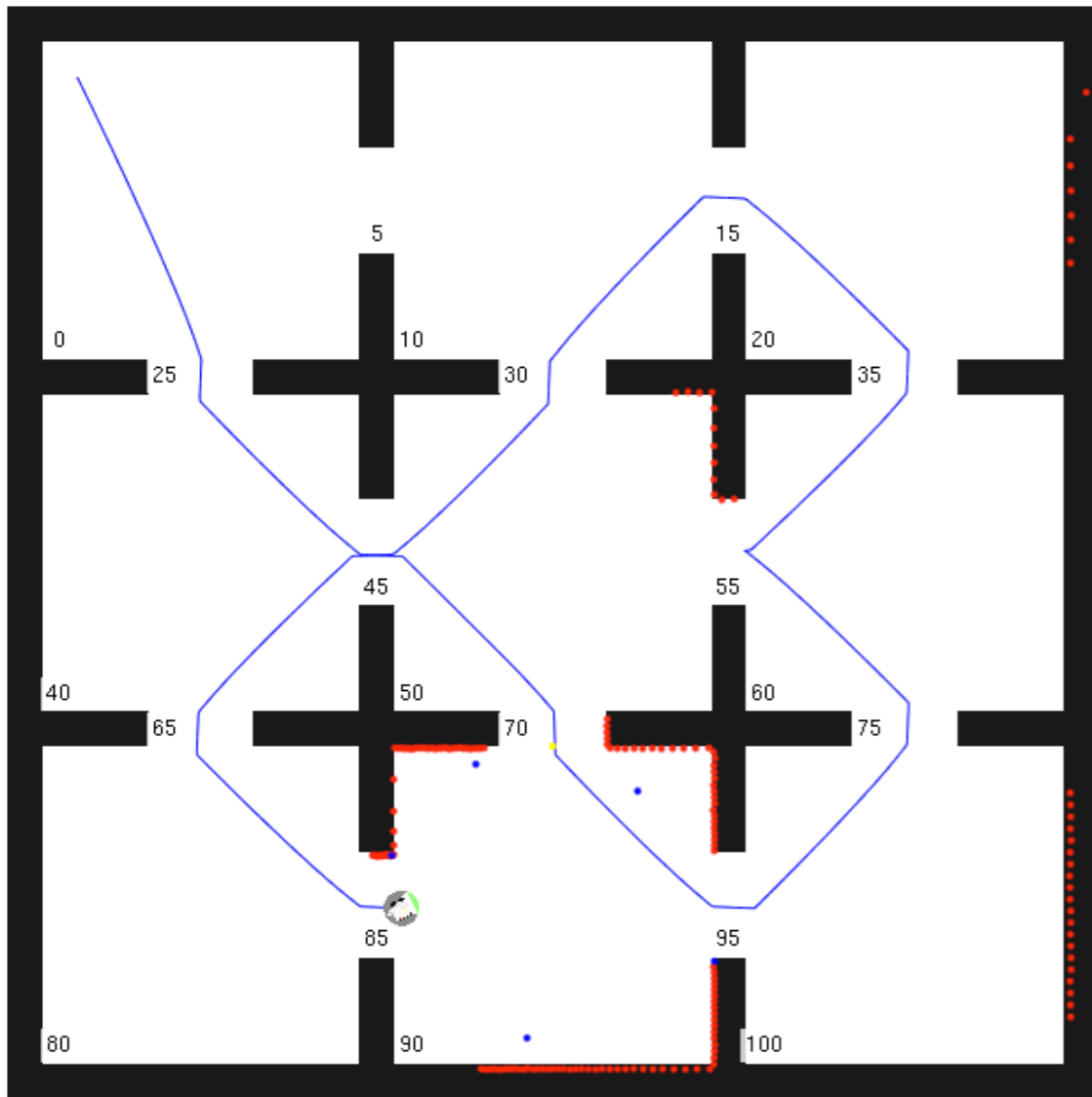
- ❖ Typically impractical due to matrix inversion complexity $\sim O(N^3)$
 - ❖ Other SLAM methods attempt to approximate this
- ❖ Solution: Exploit sparsity within the information matrix
 - ❖ Reorder nodes to induce additional sparsity
 - ❖ Back solve using Cholesky decomposition



Loop Closure

- ❖ Using LIDAR to close the loop:
 - ❖ Determine if robot is in the location of a previous pose
 - ❖ Attempt to create RBT between two poses using their corresponding LIDAR scans
 - ❖ Resolution Scan Matching algorithm to align points of individual scans

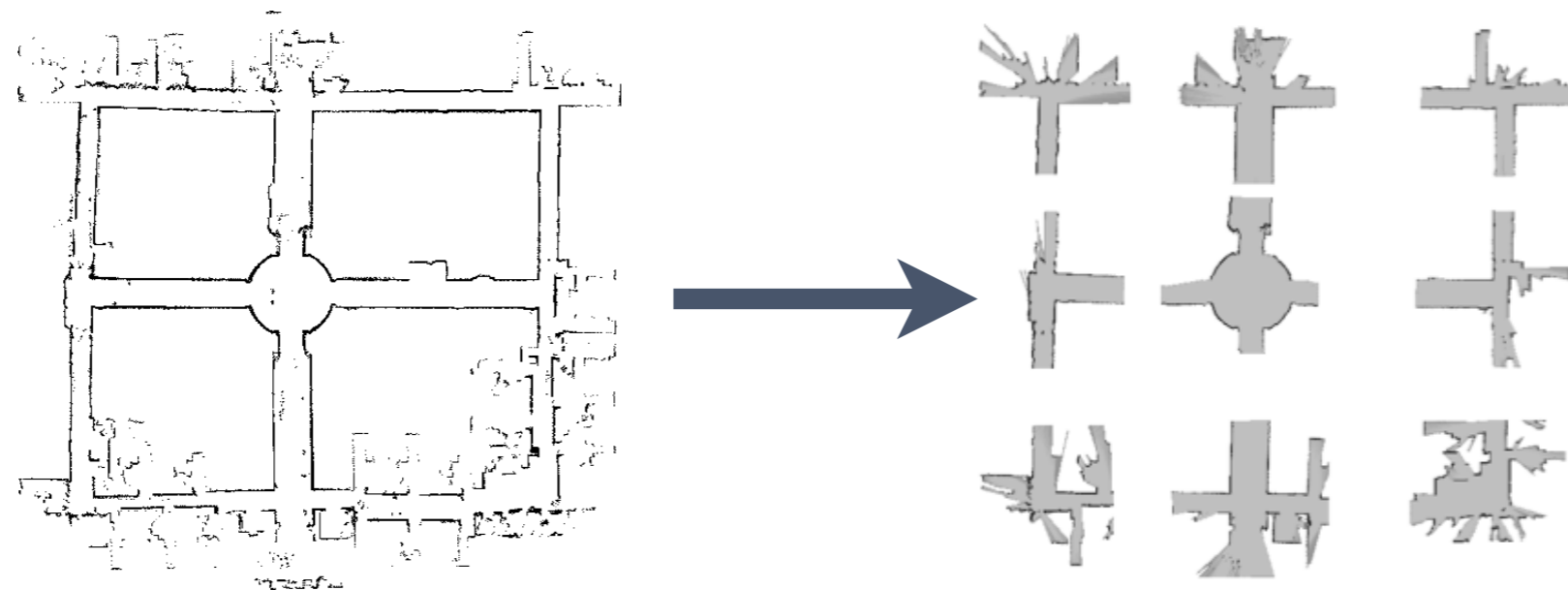




Topological Mapping

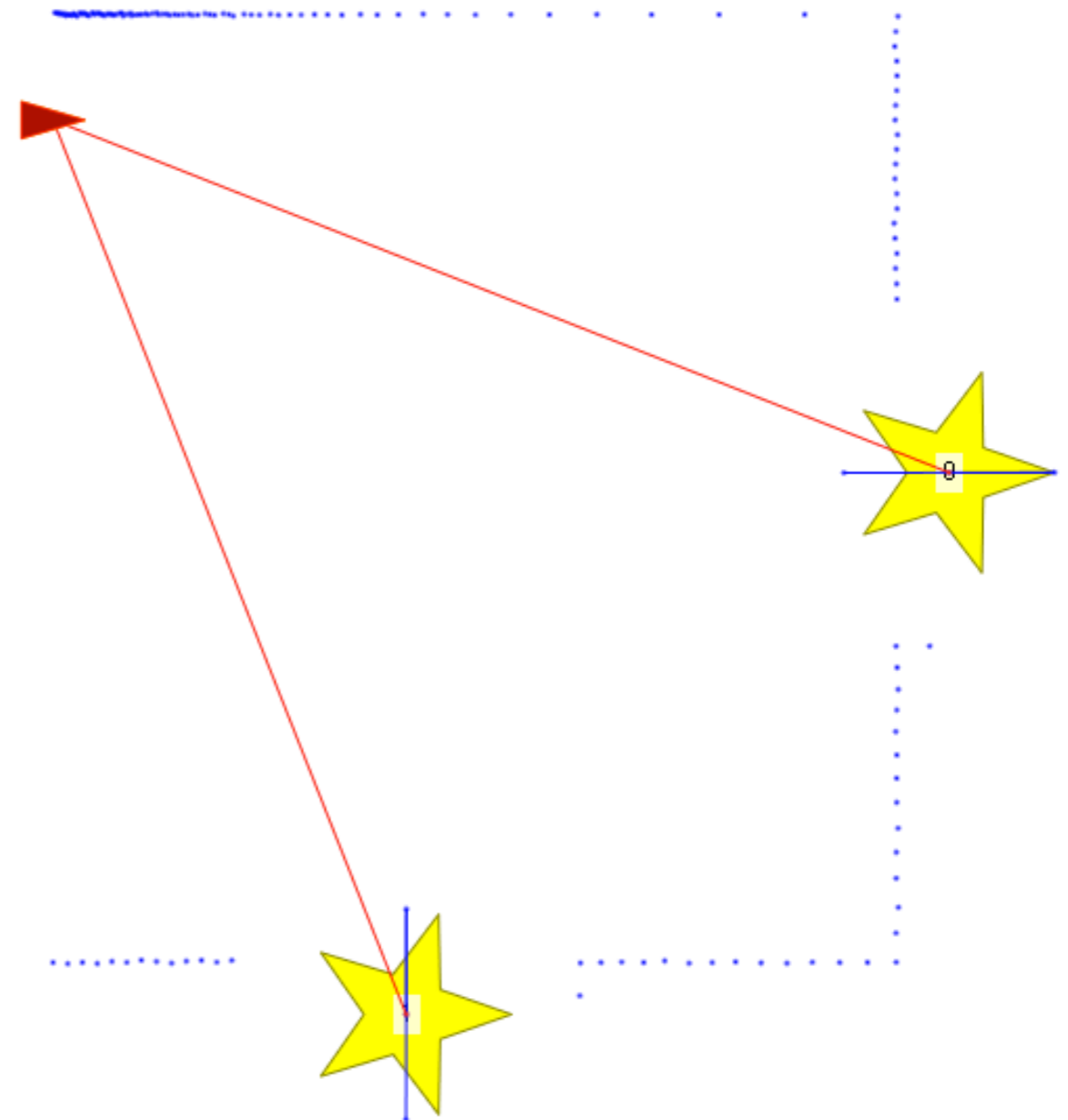
Topological Mapping

- ❖ While robot is exploring unknown environment:
 - ❖ **GIVEN**: SLAM output: Current estimate of robot poses and corresponding LIDAR scans.
 - ❖ **ESTIMATE**: Map of rooms and how those rooms are connected.

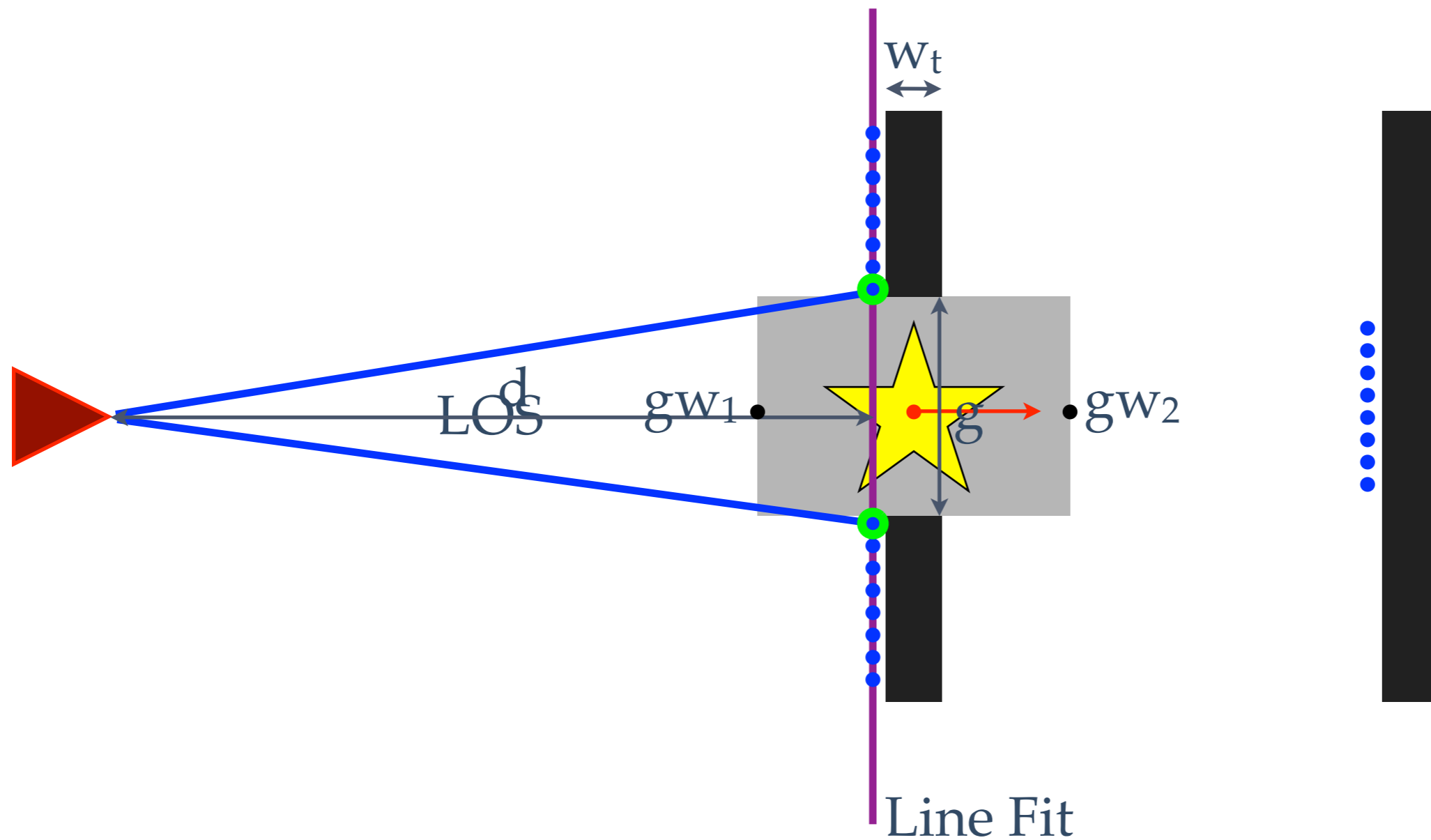


Topological Features: Doors

- ❖ For each new pose added:
 - ❖ Find 'Drop-Off' Points
 - ❖ Test 'Drop-Off' Points
 - ❖ Gap
 - ❖ Distance
 - ❖ Line Fit
 - ❖ Line of Sight
 - ❖ Set Door Direction \perp Line Fit
 - ❖ Set Location WRT Wall Thickness



Door Finder Example

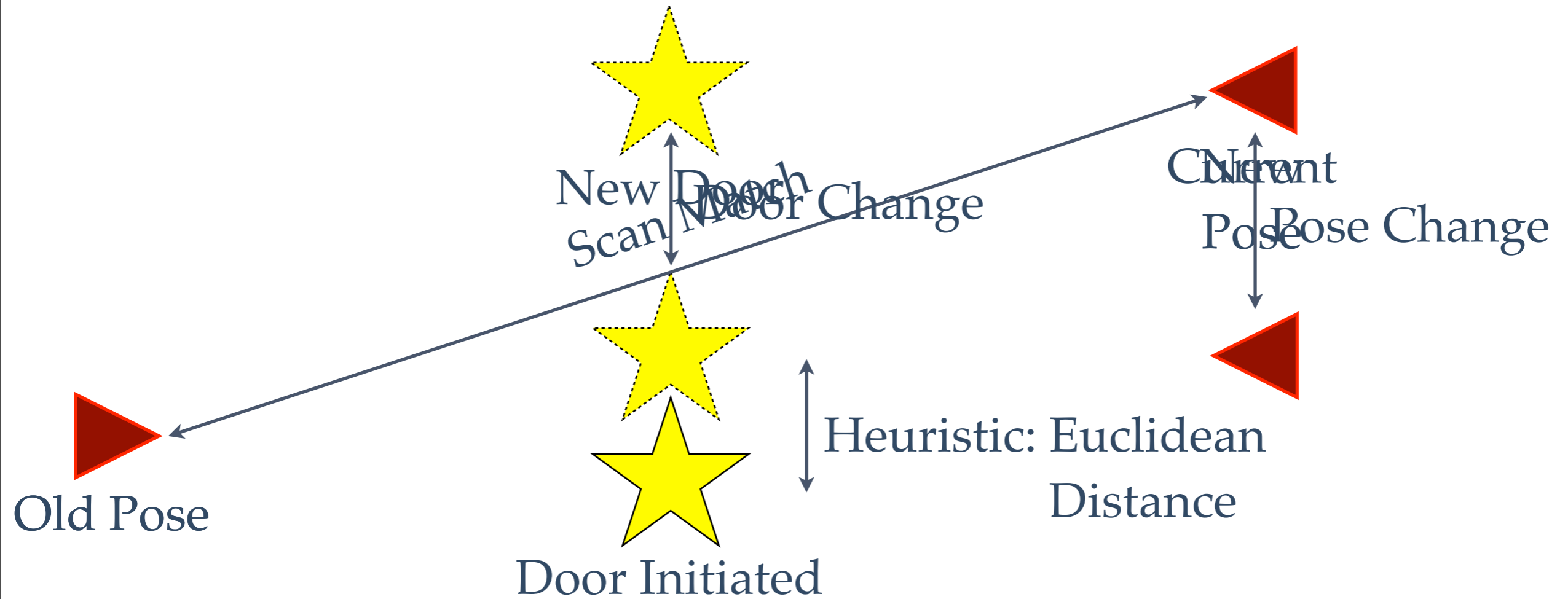


Data Association

- ❖ How do we determine if robot finds old / new door?
- ❖ Double Gated Nearest-Neighbor Search
- ❖ Greedy: $O(mn)$
- ❖ Issues?



Data Association Heuristic

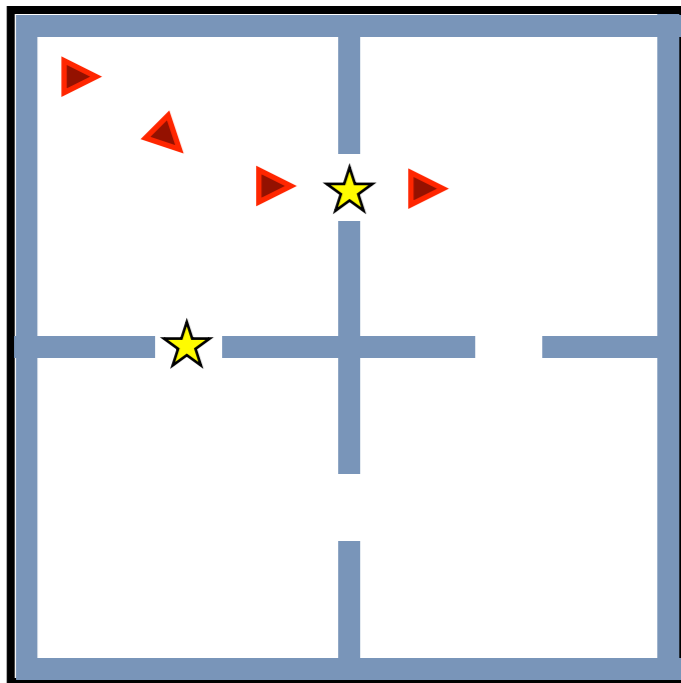


Room Connections

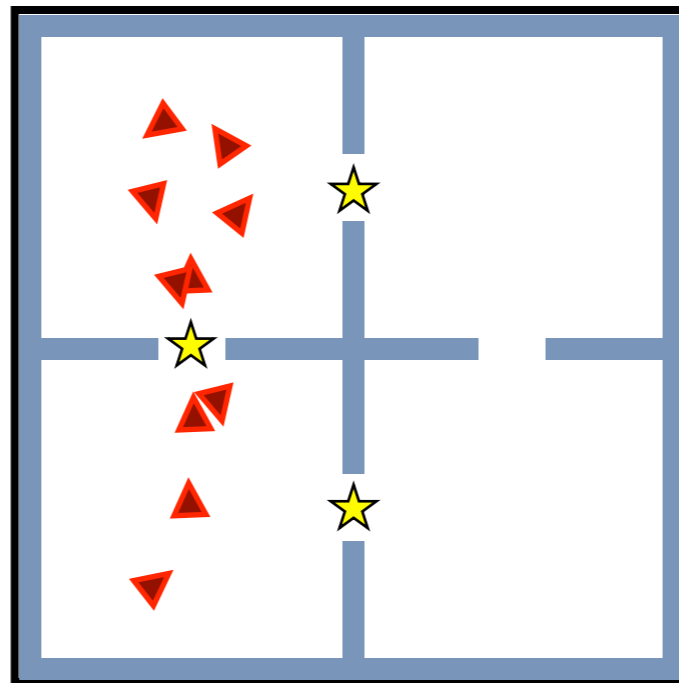
❖ Which doors connect what rooms?

❖ 3-Unique Possibilities

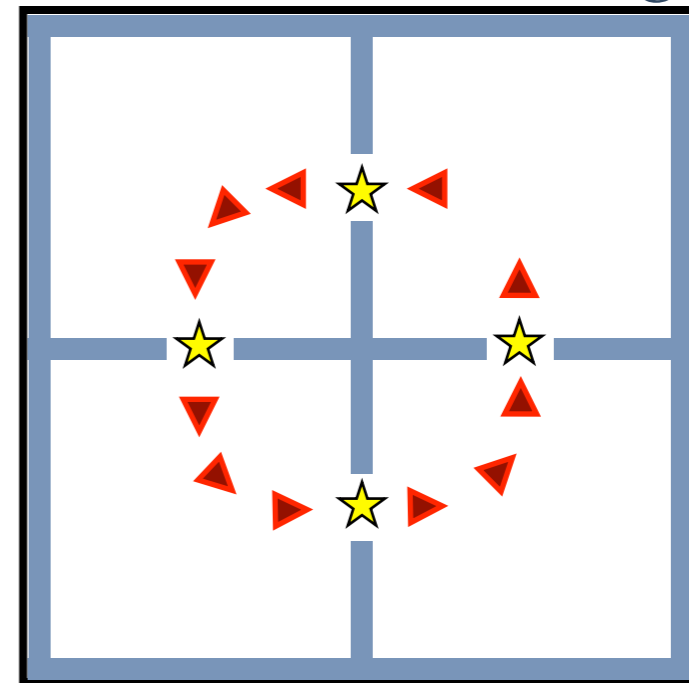
1.) Enter New Room

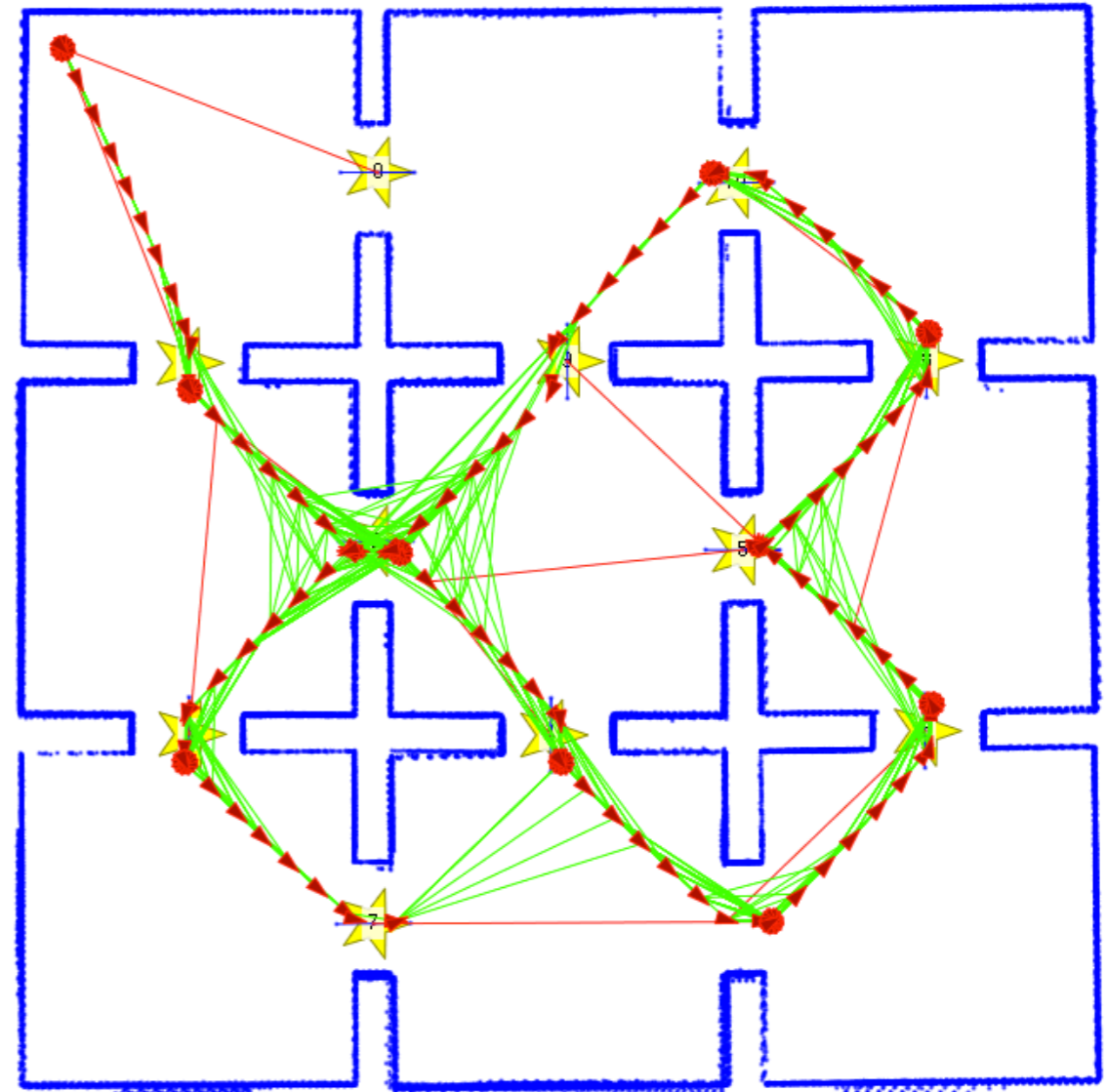
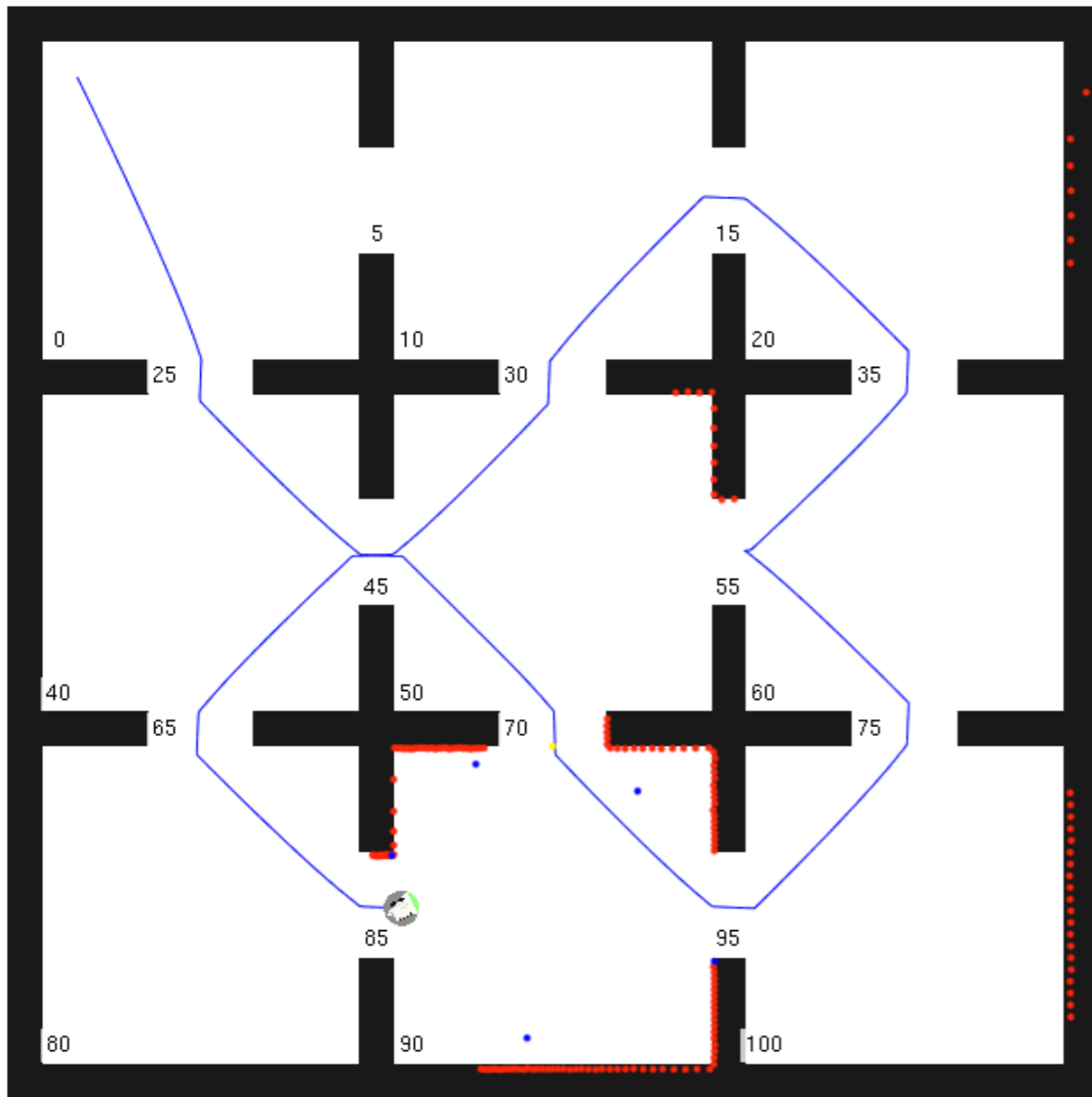


2.) Enter Old Room



3.) Enter Old Room Without Knowledge





Full System Demo

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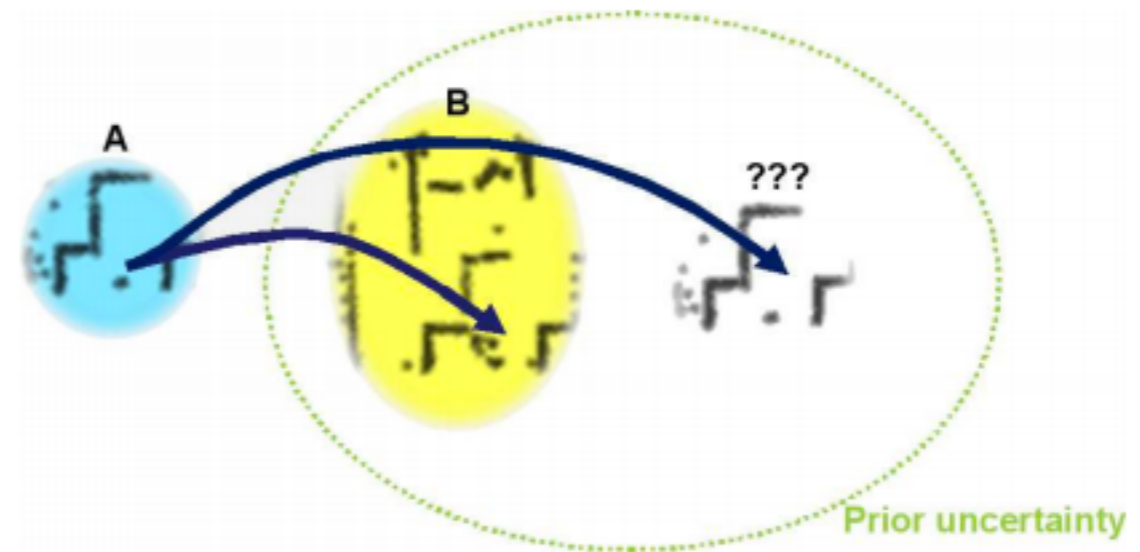
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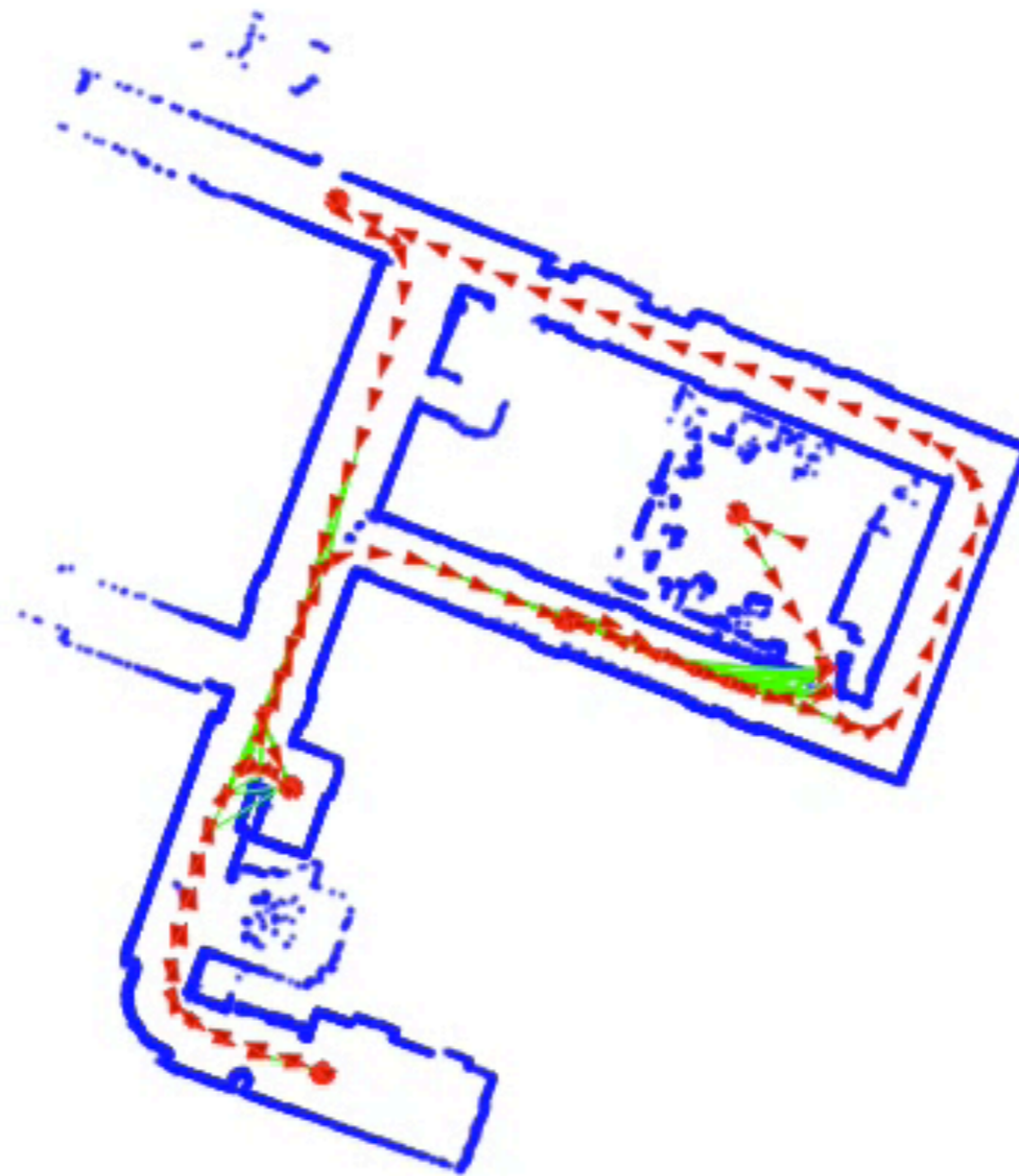
^{^object}
 ^{^id}
 ^{^visible}
 ^{^x}
 ^{^y}
 ^{^distance}
 ^{^...}

Simulated

Future Work

- ❖ Additional Feature Extraction
- ❖ Cooperation:
 - ❖ Loop Closing
 - ❖ Topological Mapping





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