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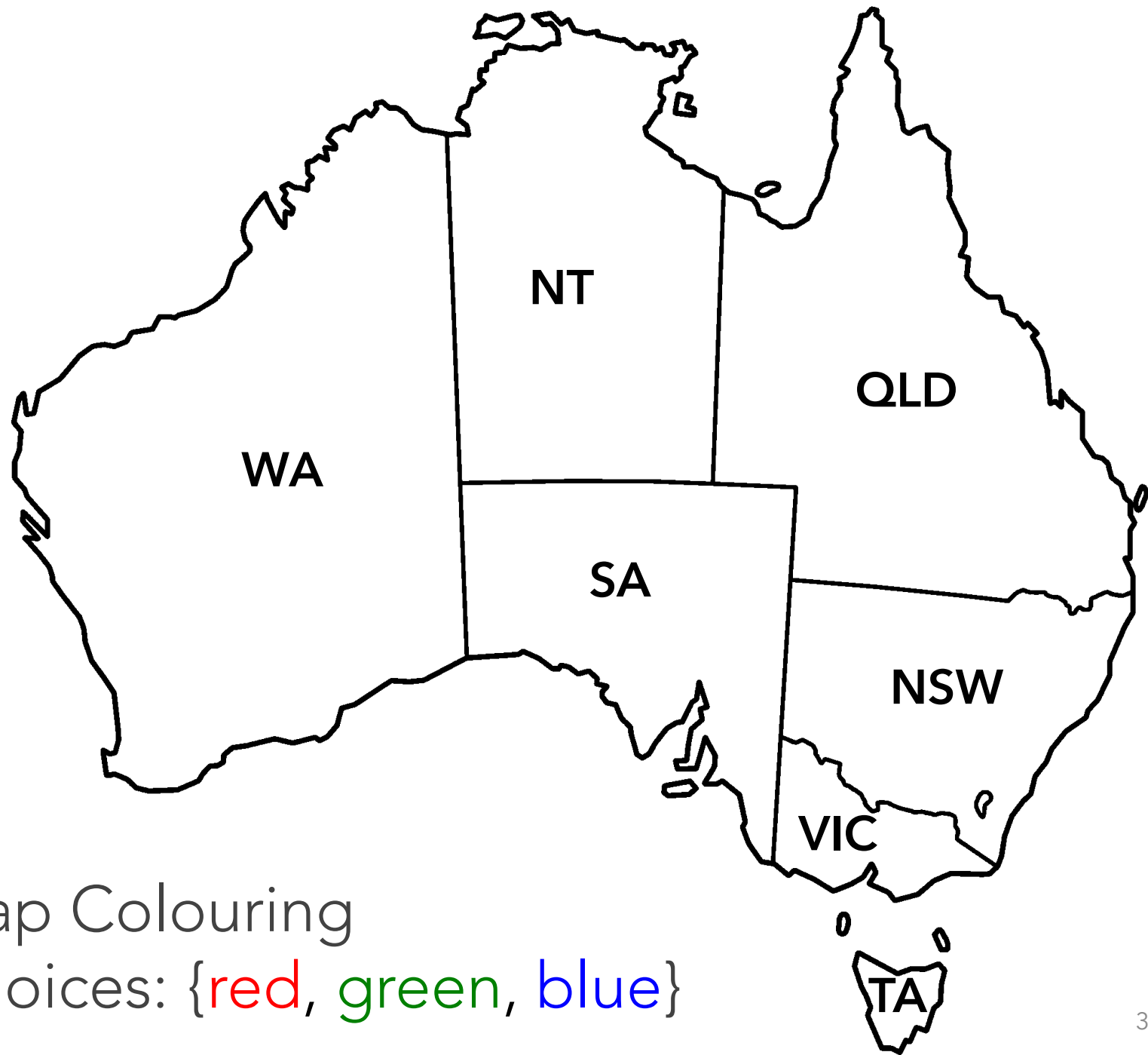
# Episodic memory (retrievals) as a CSP

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# Motivation

- > Retrievals have poor time complexity
- > Where do we start?
- > Constraint Satisfaction Problems
  - Tap into vast research base
- > What works? What doesn't?
  - We can be *very* domain-specific
- > Provides easy way to model *any* changes



Map Colouring

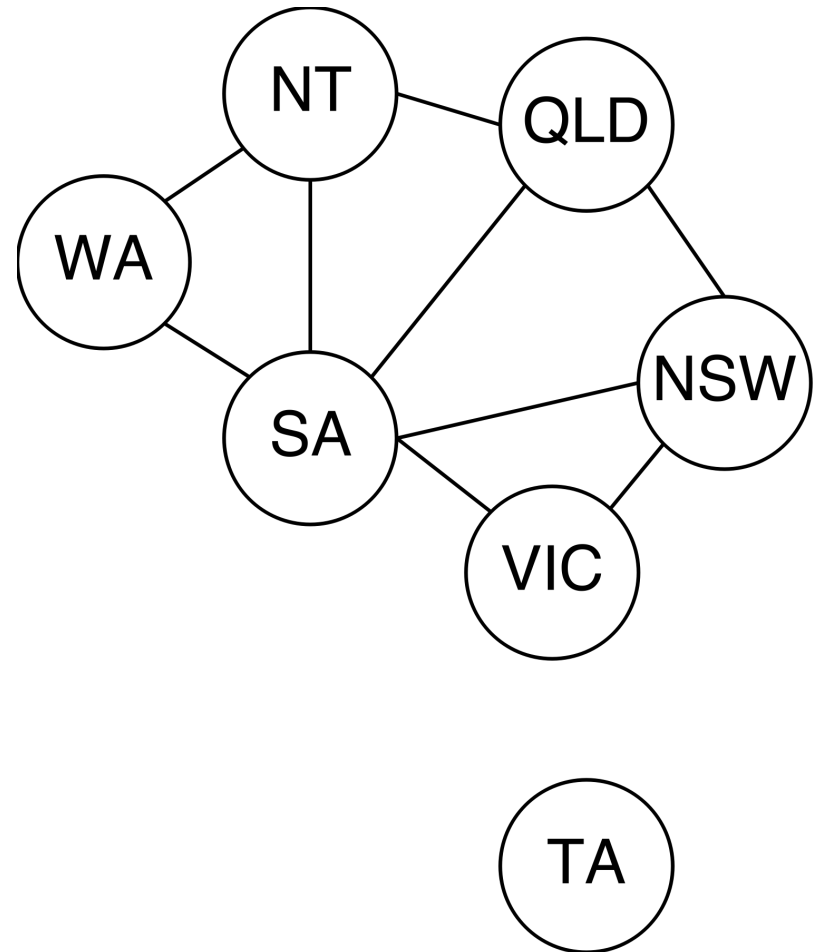
Choices: {red, green, blue}



A Solution

# Primal Constraint Graph

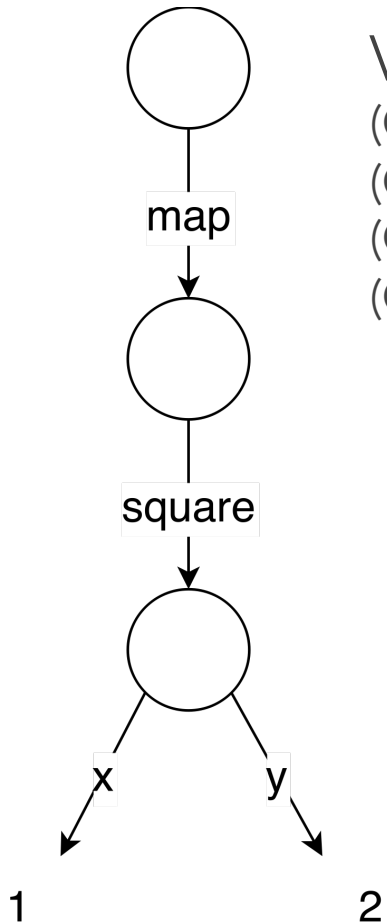
- > Nodes are variables
- > Domain is {red, green, blue}
- > Arcs are binary constraints
- >  $C_{x,y} = (r,g),(r,b),(g,b), (g,r),(b,g),(b,r)$
- > or  $C_{x,y} = (x \neq y)$
- > We can exploit this structure



# Stuff you probably know

- > We have:
  - A cue as a set of WMEs
  - A set of every unique element that has ever appeared in working memory (the WMG)
  - A list of intervals for each element representing the times they were active

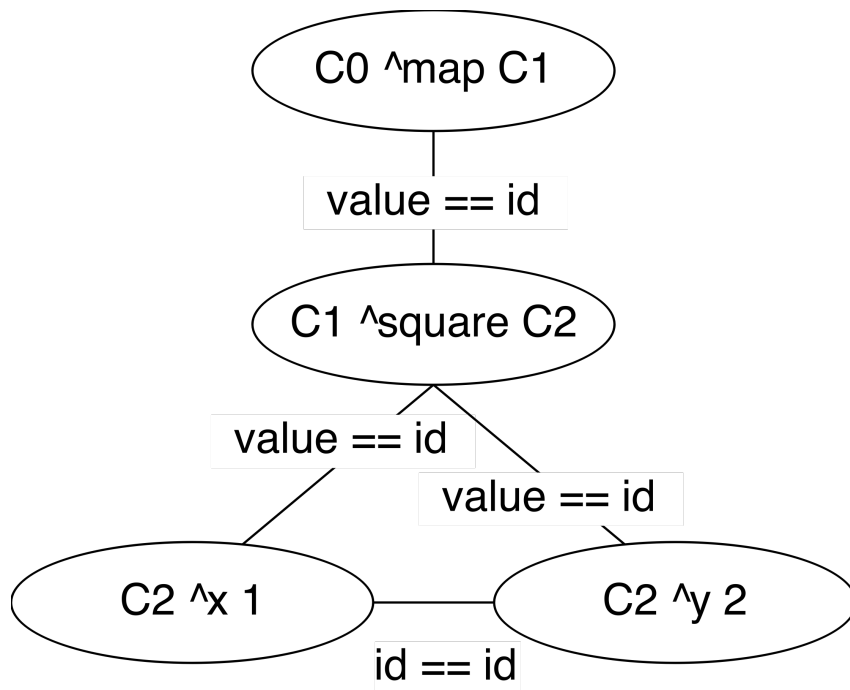
# Epmem as a CSP



Variables:  
( $C0 \wedge_{\text{map}} C1$ )  
( $C1 \wedge_{\text{square}} C2$ )  
( $C2 \wedge_x 1$ )  
( $C2 \wedge_y 2$ )

- > Domain of each variable is every element in the WMG where the constant values match
- > Can further restrict for cues starting at root
- > For example:
  - Domain of ( $C2 \wedge_x 1$ ) is every value with attribute  $x$  and value  $1$

# Epmem Primal Constraint Graph



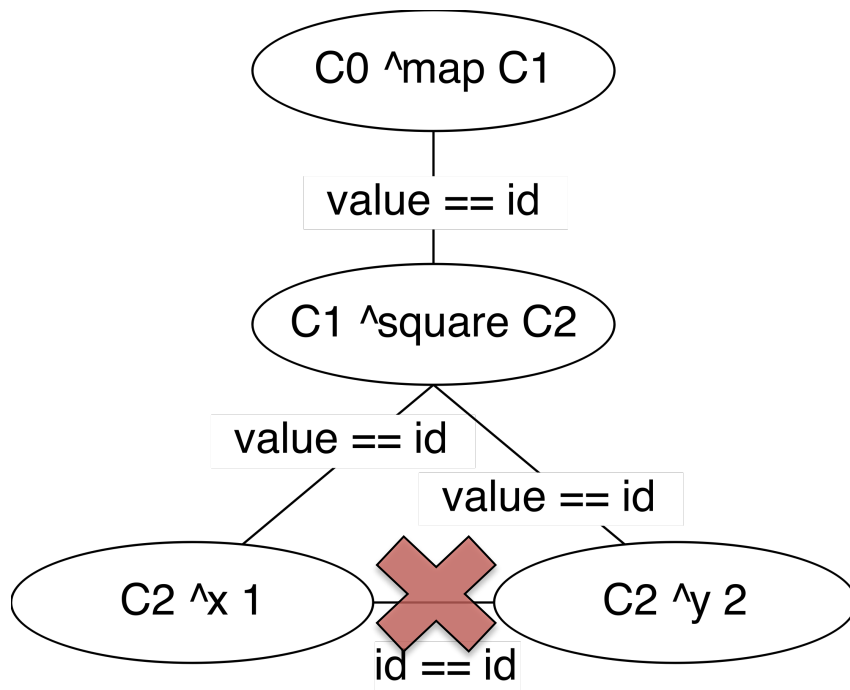
- > Any variables that share ids are constrained
- > Also n-ary temporal constraint (not shown)
- > How do we solve this?



# CSP solving techniques/heuristics

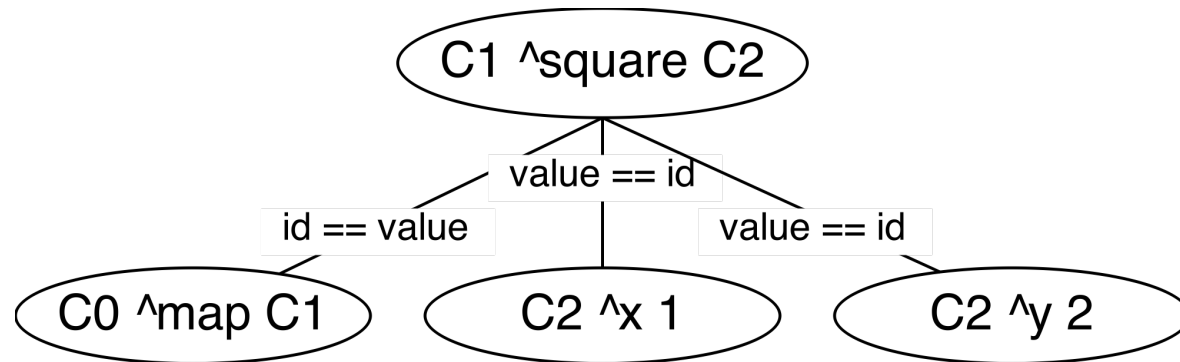
- > Search (generating solutions)
  - Backtracking (naïve, intelligent, look-ahead)
- > Inference (preprocessing/filtering)
  - Prune the search space
  - Create a tightened, but equivalent, problem
- > Variable ordering
- > Exploitation of constraint graph structure

# Exploiting structure



- > We want width-1 tree structures
- > Want to maximise graph degree centrality (we think)
- > Must identify redundant constraints

# Directional arc consistency (DAC)



- > When we backtrack, pick an ordering:
  - Instantiate parent ( $C1 \wedge \text{square } C2$ ) first
  - Instantiate children after (heuristics define child order)
- > Before we backtrack:
  - Delete values in the domain of the parent which don't satisfy a constraint with all of its children

# “Revise” example (id == value)

## Parent

Domain[**C1**  $\wedge$ square C2]

- (**O3**  $\wedge$ square O57)
- (**O0** square O247)
- (**O3**  $\wedge$ square O75)
- (**O0**  $\wedge$ square O68)
- (**O3**  $\wedge$ square O34)

## Child

Domain[C0  $\wedge$ map **C1**]

- (O0  $\wedge$ map **O3**)

Implemented using sets (of value ids in this case)

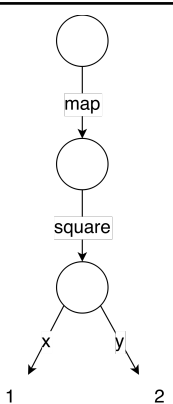
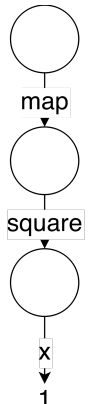
$O(k)$ ,  $k = \max(|\text{Dom}|)$

- > Delete unsupported values (where id  $\neq$  O3)
- > Repeat for all children
- > If domain becomes empty at any point  $\rightarrow$  no solutions
- > All values in the parent participate in a solution

# Arc consistency

- > Backtrack-free for one solution
- > For all solutions, do DAC again (down the tree)
- > This establishes arc consistency (AC)
- > All values participate in a solution
- > Better complexity than standard AC algorithms (controlled propagation)

# Empirically (tanksoar: ~30000eps)

Cue	Metric	Naive	DAC	AC
 <p>1 result</p>	<b>Node visits <math>O(ek)</math></b>	<b>547</b>	<b>7</b>	<b>7</b>
	Consistency checks $O(1)$	17512	103	3
	Set adds for revise $O(1)$		128	131
	Set membership checks for revise $O(1)$		408	536
	<b>Sum of constant checks</b>	<b>17512</b>	<b>639</b>	<b>670</b>
	<b>CPU time (ms)</b>	<b>32.7</b>	<b>.774</b>	<b>.706</b>
 <p>16 results</p>	<b>Node visits <math>O(ek)</math></b>	<b>515</b>	<b>35</b>	<b>35</b>
	Consistency checks $O(1)$	16034	545	152
	Set adds for revise $O(1)$		64	96
	Set membership checks for revise $O(1)$		410	474
	<b>Sum of constant checks</b>	<b>16034</b>	<b>1019</b>	<b>722</b>
	<b>CPU time (ms)</b>	<b>32.0</b>	<b>4.01</b>	<b>3.37</b>

# Generating solutions

## 1. Process cue

- Remove redundant constraints
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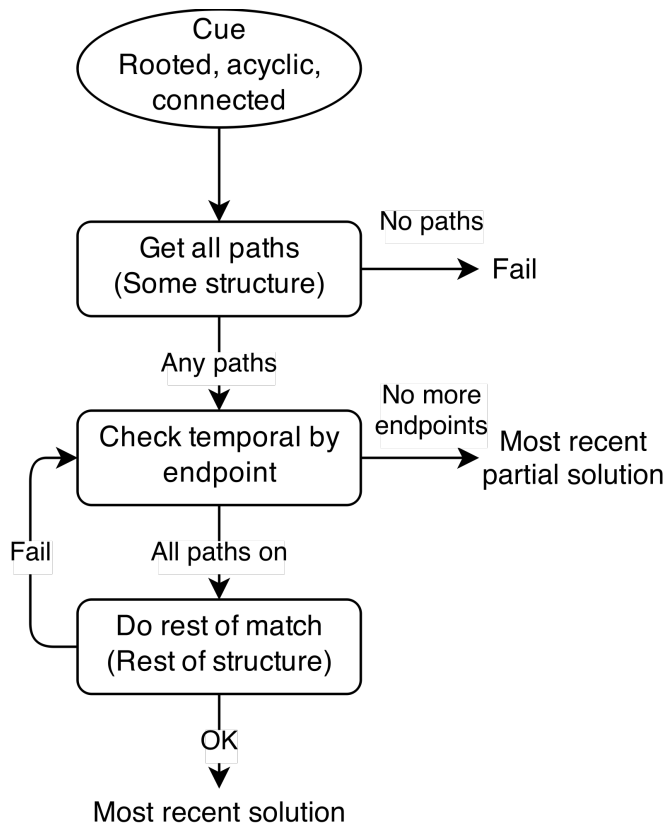
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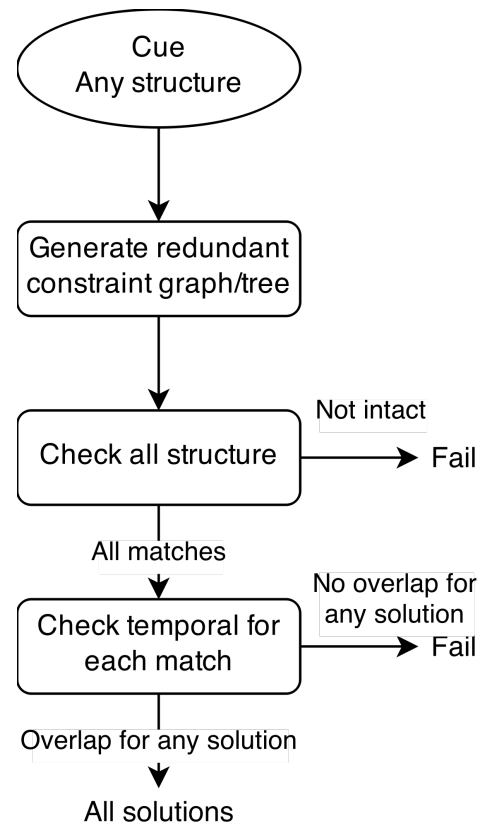
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4. **Check temporal overlap by merging pairs of interval lists for each solution [ $O(nm)$ ]**

# Comparison

## Soar Implementation



## This Implementation



# Pluses

- > Few (if any) restrictions on cue structure (can be disjoint, cyclic, non-rooted)
- > Easy to model extensions ( $C_2 \wedge x > \emptyset$ )
- > Structure is most constrained
- > No possibility of multiple complex graph matches
- > Retrieve all solutions
- > Parallelisation is fine-grained
- > Same principles for production matcher

# Needs work

- > Retrieval is still unbounded
- > Poor when many solutions
- > Partial solutions not considered (yet)
- > More investigation needed
  - Variable ordering
  - Dealing with cycles
  - Look-ahead

## **BUT**

- > The problem is defined.
- > All extensions can use the CSP formulation
- > We just tweak the techniques

Thank you

**QUESTIONS?**