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Parallel programming in Julia

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WestGrid webinar - slides and functions at https://git.io/Jtdge

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- Please mute your microphone and camera unless you have a question
- To ask questions at any time, type in Chat, or Unmute to ask via audio
 - please address chat questions to "Everyone" (not direct chat!)
- Raise your hand in Participants



Email training@westgrid.ca

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2021 IEEE Vis Contest

https://scivis2021.netlify.app

- Co-hosting 2021 SciVis Contest with IEEE Vis
- Dataset: 3D simulation of Earth's mantle convection covering 500 Myrs of geological time
- Contest is open to anyone (no research affiliation necessary), dataset available now
- Wanted: pretty pictures + problem-specific analysis of descending / rising flows
- Prizes + opportunity to present
- July 31, 2021 deadline for Contest entry submissions



| Intro • | | | Distributed 00000000000 | DistributedArrays 0000 | | |
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- We teach serial Julia in our courses, also see https://git.io/Jtdge
- Today's topic: what unique features does Julia bring to parallel programming?
- Targeting both multi-core PCs and distributed-memory clusters

✔ Base.Threads

✔ Distributed.jl

🖌 ClusterManagers.jl

✔ DistributedArrays.jl

✔ SharedArrays.jl

- Dagger.jl
- Concurrent function calls ("lightweight threads" for suspending/resuming computations)
- MPI.jl
- MPIArrays.jl
- LoopVectorization.jl
- FLoops.jl
- ThreadsX.jl
- Transducers.jl
- GPU-related packages

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Let's start Julia by typing "julia" in bash:

using Base.Threads # otherwise will have to preface all functions/macros with `Threads.`
nthreads() # by default, Julia starts with a single thread of execution

If instead we start with "julia -t 4" (or "JULIA_NUM_THREADS=4 julia" prior to 1.5):

```
using Base.Threads
nthreads()  # now 4 threads
@threads for i=1:10  # parallel for loop using all threads
    println("iteration $i on thread $(threadid())")
end
a = zeros(10)
@threads for i=1:10
    a[i] = threadid()  # should be no collision: each thread writes to its own part
end
a
```

Threads1 0000

Distributed

Filling an array: perfect parallel scaling¹

@threads are well-suited for shared-memory data parallelism without any reduction

```
n = Int64(1e9)
a = zeros(n);
Otime for i in 1:n
    a[i] = log10(i)
end
using Base.Threads
Otime Othreads for i in 1:n
    a[i] = log10(i)
end
```

¹Whether I am doing this inside or outside a function is not the point here ... besides, you don't know (more on this in slide 8)

This code is not thread-safe:

```
total = 0
@threads for i = 1:Int(1e6)
global total += i
end
println("total = ", total)
```

- race condition: multiple threads updating the same variable at the same time
- a new result every time
- unfortunately, @threads does not have built-in reduction support

Intro Threads1 Slow series Threads2 Distributed Distributed Arrays Julia set Shared Arrays N-bod 00000

This code is not thread-safe:

```
total = 0
@threads for i = 1:Int(1e6)
    global total += i
end
println("total = ", total)
```

- race condition: multiple threads updating the same variable at the same time
- a new result every time
- unfortunately, @threads does not have built-in reduction support

Let's make it thread-safe (one of many solutions):

```
total = Atomic{Int64}(0)
@threads for i in 1:Int(1e6)
        atomic_add!(total, i)
end
println("total = ", total[])
```

- this code is supposed to be much slower: threads waiting for others to finish updating the variable
- atomic variables not really designed for this type of usage
- \Rightarrow let's do some benchmarking

Threads1 0000

Benchmarking in Julia

Running the loop in the global scope (without a function):

- direct summation
- @time includes JIT compilation time (marginal here)
- total is a global variable to the loop

```
Otime for i in 1:n
```

Packaging the loop in the local scope of a function:

- Julia replaces the loop with the formula
 - Kwe don't want this! n(n+1)/2
- first function call results in compilation,

@time here includes only runtime

```
function quick (n)
    Qtime for i in 1:n
```

- 1. force computation \Rightarrow compute something more complex than simple integer summation
- exclude compilation time \Rightarrow package into a function + precompile it 2.
- make use of optimizations for type stability and other factors \Rightarrow package into a function 3.
- time only the CPU-intensive loops 4.
- 5. for shorter runs (ms) may want to use <code>@btime</code> from BenchmarkTools

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Slowly convergent series

• The traditional harmonic series \sum

ties
$$\sum_{k=1}^{\infty} \frac{1}{k}$$
 diverges

 However, if we omit the terms whose denominators in decimal notation contain any digit or string of digits, it converges, albeit very slowly (Schmelzer & Baillie 2008), e.g.



 For no denominators with "9", assuming linear convergence in the log-log space, we would need 10⁷³ terms to reach 22.92, and almost 10²⁰⁵ terms to reach 22.92067661

Checking for substrings in Julia

Checking for a substring is one possibility

```
if !occursin("9", string(i))
        <add the term>
end
```

• Integer exclusion is ${\sim}4{ m X}$ faster (thanks to Par

(thanks to Paul Schrimpf from the Vancouver School of Economics @UBC)

```
function digitsin(digits::Int, num)
   base = 10
        base \star = 10
        if (num % base) == digits  # last N digits in 'num' == digits
        num \div = 10
    <add the term>
```

Intro Threads1 Slow series **Threads2** Distributed Distributed Arrays Julia set SharedArrays o oooo oo ooo ooo ooo ooo

Timing the summation: serial code

Let's switch to 10⁹ terms, start with the serial code:

```
function slow(n::Int64, digits::Int)
    total = Int64(0)
    @time for i in 1:n
        if !digitsin(digits, i)
            total += 1.0 / i
        end
    end
    println("total = ", total)
end
slow(10, 9)
slow(Int64(1e9), 9)  # total = 14.2419130103833
```

\$ julia serial.jl # serial runtime: 22.00s 21.85s 22.03s

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Timing the summation: using an atomic variable

• Threads are waiting for the atomic variable to be released \Rightarrow should be slow:

```
using Base.Threads
function slow(n::Int64, digits::Int)
    total = Atomic{Float64}(0)
    @time @threads for i in 1:n
        if !digitsin(digits, i)
            atomic_add!(total, 1.0 / i)
        end
    end
    println("total = ", total[])
end
slow(10, 9)
slow(Int64(1e9), 9)  # total = 14.241913010383
```

Timing the summation: an alternative thread-safe implementation

Each thread is updating its own sum, no waiting \Rightarrow should be faster:

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Timing the summation: using heavy loops

• Might be the fastest of the three parallel implementations:

```
using Base.Threads
function slow(n::Int64, digits::Int)
    Otime Othreads for threadid in 1:numthreads
        local start = (threadid-1) *threadSize + 1
        local finish = threadid < numthreads ? (threadid-1)*threadSize+threadSize : n</pre>
    end
```

\$ julia heavyThreads.jl # runtime on 1 thread: 24.05s 24.67s 24.75s
\$ julia -t 4 heavyThreads.jl # runtime on 4 threads: 9.93s 10.21s 10.24s

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Timing the summation: using heavy loops (cont.)

#!/bin/bash
#SBATCH --ntasks=1
#SBATCH --cpus-per-task=...
#SBATCH --mem-per-cpu=3600M
#SBATCH --time=00:10:00
module load StdEnv/2020 julia/1.5.2
julia -t \$SLURM_CPUS_PER_TASK heavyThreads.jl

Cedar (avg. over 3 runs):

| code | computing |
|----------|-----------|
| serial | 47.8s |
| 2 cores | 27.5s |
| 4 cores | 15.9s |
| 8 cores | 18.5s |
| 16 cores | 8.9s |

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Parallelizing with multiple Unix processes (MPI tasks)

- Distributed provides multiprocessing environment to allow programs to run on multiple processors in shared or distributed memory
- Julia's implementation of message passing is one-sided, typically with higher-level operations like calls to user functions on a remote process
 - a remote call is a request by one processor to call a function on another processor; returns a remote/future reference
 - the processor that made the call proceeds to its next operation while the remote call is computing
 - you can obtain the remote result with fetch()
- Single control process + multiple worker processes
- Processes pass information via messages underneath, not via shared memory

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Launching worker processes

1. From the terminal

\$ julia -p 8 # open REPL, start Julia control process + 8 worker processes
\$ julia -p 8 code.jl # run the code with Julia control process + 8 worker processes

2. From a job submission script

```
#!/bin/bash
#SBATCH --ntasks=8
#SBATCH --cpus-per-task=1
#SBATCH --mem-per-cpu=3600M
#SBATCH --time=00:10:00
srun hostname -s > hostfile  # parallel I/C
sleep 5
julia --machine-file ./hostfile ./code.jl
```

- All three methods launch workers ⇒ combining them will result in 16 (or 24!) workers
- Select one method and use it

3. From Julia

```
using Distributed addprocs(8)
```

Important: use either (1) or (3) with Slurm on CC clusters as well: usually no need for a machine file

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Process control

Let's start Julia with "julia" (single control process):

```
using Distributed
addprocs(4)  # add 4 worker processes
for i in workers()  # remove all workers
   t = rmprocs(i, waitfor=0)
workers()
addprocs(4)
```

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| @ev | erywh | ere | | | | |

Let's restart Julia with "julia" (single control process):

```
using Distributed
addprocs(4) # add 4 worker processes
@everywhere function showid() # define the function everywhere
   println("my id = ", myid())
@everywhere showid()
@everywhere println(x)  # get errors: x is not defined elsewhere
@everywhere println($x)
```

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|-----|-------|--|-----------------------------|---------------------------|--|--|
| @sp | awnat | | | | | |

a=12
@spawnat 2 println(a) # will print 12 from worker 2

What @spawnat does here:

- 1. pass the namespace of local variables to worker 2
- 2. spawn function execution on worker 2
- 3. return a Future handle (referencing this running instance) to the control process
- 4. return REPL to the control process (while the function is running on worker 2)

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| @sp | awnat | | | | | |

a=12
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- 4. return REPL to the control process (while the function is running on worker 2)

| Threads1 | | Distributed | DistributedArrays | | |
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Back to the slow series

Let's restart Julia with "julia -p 2" (control process + 2 workers):

using Distributed

```
@everywhere function digits:n(digits::Int, num)
base = 10
while (digits ÷ base > 0)
base *= 10
end
while num > 0
if (num % base) == digits
return true
end
num ÷= 10
end
slow(10, 9)
slow(10, 9)
slow(Int64(le9), 9)
# serial run: total = 14.2419130103833, 25.0s 24.7s 26.2s
@everywhere slow(Int64(le9), 9)
# runs on 3 (control + 2 workers) cores simultaneously, 32.9s+3
```

(with ~33s wallclock time) but each core performs the same calculation ...

| Threads1 | | Distributed | DistributedArrays | | |
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Back to the slow series

Let's restart Julia with "julia -p 2" (control process + 2 workers):

using Distributed

```
@everywhere function digits:n(digits::Int, num)
base = 10
while (digits ÷ base > 0)
base *= 10
end
while num > 0
if (num % base) == digits
return true
end
num ÷= 10
end
slow(10, 9)
slow(10, 9)
slow(Int64(1e9), 9)
# runs on 3 (control + 2 workers) cores simultaneously, 32.9
@everywhere function slow(n::Int64, digits::Int)
total = Int64(0)
@time for i in 1:n
if !digitsin(digits, i)
total += 1.0 / i
end
end
end
end
end
slow(10, 9)
# serial run: total = 14.2419130103833, 25.0s 24.7s 26.2s
# serial runs on 3 (control + 2 workers) cores simultaneously, 32.9
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# serial runs on 3 (control + 2 workers) cores simultaneously, 32.9
# serial runs on 3 (control + 2 workers) cores simultaneously, 32.9
# serial runs on 3 (control + 2 workers) cores si
```

runs on 3 (control + 2 workers) cores simultaneously, 32.9s+32.6s+32.7s, # (with ~33s wallclock time) but each core performs the same calculation ...

Question: how long will the following code (last line) take?

addprocs(2) # for the total of 4 workers
>>> redefine digitsin() and slow() everywhere
@everywhere slow(Int64(1e9), 9)

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Parallelizing our slow series

Let's restart Julia with "julia" (single control process):

```
using Distributed
>>> redefine digitsin() everywhere
   @time for i in taskid:ntasks:n # partial sum with a stride 'ntasks'
a = @spawnat :any slow(Int64(1e9), 9, 1, 2)
b = @spawnat : any slow(Int64(1e9), 9, 2, 2)
```

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Parallelizing our slow series

Let's restart Julia with "julia" (single control process):

```
using Distributed
>>> redefine digitsin() everywhere
   @time for i in taskid:ntasks:n # partial sum with a stride 'ntasks'
a = @spawnat :any slow(Int64(1e9), 9, 1, 2)
b = @spawnat : any slow(Int64(1e9), 9, 2, 2)
```

- 2X speedup!
- Different order of summation \Rightarrow slightly different numerical result
- Not scalable: only limited to a small number of sums each spawned with its own Future reference

Solution 1: use an array of Future references

We could create an array (using *array comprehension*) of Future references and then up add their respective results:

```
r = [@spawnat p slow(Int64(1e9), 9, i, nworkers()) for (i,p) in enumerate(workers())]
print("total = ", sum([fetch(r[i]) for i in 1:nworkers()]))
# runtime with 2 simultaneous processes: 10.26+12.11s
```

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Solution 2: parallel for loop with summation reduction

There is actually a simpler solution:

```
using Distributed
@everywhere function digitsin(digits::Int, num)
                                                       function slow(n::Int64, digits::Int)
    base = 10
                                                            @time total = @distributed (+) for i in 1:n
        base \star = 10
        if (num % base) == digits
        num ÷= 10
end
```

\$ julia parallelFor.jl # with 2 processes: 10.82s 11.34s 11.40s
\$ julia parallelFor.jl # with 4 processes: 9.48s 10.37s 9.62s (changing to addprocs(4))

| | | Distributed | DistributedArrays | | Summary |
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Parallel for on Cedar

```
#SBATCH --ntasks=... # number of MPI tasks
```

```
#SBATCH --cpus-per-task=1
```

#SBATCH --nodes=1-1 # change process distribution across nodes

#SBATCH --mem-per-cpu=3600M

```
#SBATCH --time=0:5:0
```

```
#SBATCH --account=...
```

```
module load StdEnv/2020 julia/1.5.2
```

```
echo $SLURM_NODELIST
```

```
# comment out addprocs() in the code
julia -p $SLURM_NTASKS parallelFor.jl
```

Cedar (avg. over 3 runs):

| code | computing |
|-------------------------|-----------|
| serial | 48.2s |
| 2 cores, same node | 42.8s |
| 4 cores, same node | 12.2s |
| 8 cores, same node | 7.6s |
| 16 cores, same node | 6.8s |
| 32 cores, same node | 2.0s |
| 32 cores across 6 nodes | 11.3s |

| Threads1 | | Distributed | DistributedArrays | | |
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Solution 3: use pmap to map arguments to processes

```
using Distributed
@everywhere function digitsin(digits::Int, num)
        base *= 10
        if (num % base) == digits
        num \div = 10
end
```

```
@everywhere function slow((n, digits, taskid, ntasks))
    for i in taskid:ntasks:n # partial sum
nw = nworkers()
println("total = ", sum(pmap(slow, args)))
```

sum(pmap(x->slow(x), args)) # alternative syntax

Optional integration with Slurm

https://github.com/JuliaParallel/ClusterManagers.jl

To integrate Slurm launcher/flags into your Julia code

Convenience, but not a necessity

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- 🔍] add DistributedArrays
- A DArray is split across several processes (set of workers), either on the same or multiple nodes
 - this allows use of arrays that are too large to fit in memory on one node
 - each process operates on the part of the array it owns ⇒ very natural way to achieve parallelism for large problems
- Each worker can read any elements using their global indices
- Each worker can write only to the part that it owns ⇒ automatic parallelism and safe execution

```
DistributedArrays
                                                       0000
DistributedArrays (cont.)
Code for presenter in learning/distributedArrays.jl
using Distributed
@everywhere using DistributedArrays
data[1,1], data[n,5]
data.dims
@spawnat 2 data.localpart[1,1] = 1.5
for i in workers()
    @spawnat i println(localindices(data))
@everywhere function fillLocalBlock(data)
                                                         for i in workers()
                                                         @fetchfrom 2 data.localpart
                                                         minimum(data), maximum(data) # parallel reduction
```

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One-liners to generate distributed arrays

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Building a distributed array from local pieces

Example adapted from Baolai Ge's presentation

Let's restart Julia with "julia" (single control process):

```
using Distributed
using DistributedArrays
@everywhere using LinearAlgebra
@everywhere function tridiagonal(n)
                                                                       0
                                                                             0
                                                                                                    0
                                                                                        0
                                                                                              0
@everywhere function upperRight(n)
                                                           _1
                                                                            0
                                                                                  0
                                                                                        0
                                                                                              0
                                                                                                    0
   la = zeros(n, n)
                                                            0
                                                                       2
                                                                                   0
                                                                                        0
                                                                                              0
                                                                                                    0
                                                            0
                                                                 0
                                                                             2
                                                                                  -1
                                                                                        0
                                                                                              0
                                                                                                    0
                                                                      -1
@everywhere function lowerLeft(n)
                                                                                              0
                                                                                                    0
                                                            0
                                                                 0
                                                                       0
                                                                                        -1
   la = zeros(n, n)
                                                            0
                                                                 0
                                                                       0
                                                                             0
                                                                                                   0
                                                                                             _1
                                                            0
                                                                 0
                                                                       0
                                                                             0
                                                                                  0
                                                                                       -1 2
                                                                                                   -1
                                                            0
                                                                 0
                                                                       0
                                                                             0
                                                                                   0
                                                                                        0
                                                                                             ^{-1}
d11 = @spawnat 2 tridiagonal(4)
d21 = @spawnat 4 upperRight(4)
d = DArray(reshape([d11 d12 d21 d22], (2,2)))
```

Julia set

Julia set (no relation to Julia language!)

A set of points on the complex plane that remain bound under infinite recursive transformation f(z). We will use the traditional form $f(z) = z^2 + c$, where c is a complex constant.

- 1. pick a point $z_0 \in \mathbb{C}$
- 2. compute iterations $z_{i+1} = z_i^2 + c$ until $|z_i| > 4$
- 3. $\xi(z_0)$ is the iteration number at which $|z_i| > 4$
- 4. limit max iterations at 255
 - $\xi(z_0) = 255 \Rightarrow z_0$ is a stable point
 - the quicker a point diverges, the lower its $\xi(z_0)$ is
- 5. plot $\xi(z_0)$ for all z_0 in a rectangular region $-1 \le \mathfrak{Re}(z_0) \le 1, -1 \le \mathfrak{Im}(z_0) \le 1$

For different *c* we will get very different fractals.



 $c = 0.355 \pm 0.355i$

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Demo: computing and plotting the Julia set for c = 0.355 + 0.355i

```
Code for presenter in juliaSet/juliaSetSerial.jl
```

```
using ProgressMeter, NetCDF
```

```
function pixel(i, j, width, height, c, zoomOut)
z = (2*(j-0.5)/width-1)+(2*(i-0.5)/height-1)im
# rescale to -1:1 in the complex plane
z *= zoomOut
for i = 1:255
z = z^2 + c
if abs(z) >= 4
return i
end
end
return 255
end
n = Int(8e3)
height, width = n, n
println("Computing Julia set ...")
data = zeros(Float32, height, width);
eshowprogress for i in 1:height, j in 1:width
data[i,j] = pixel(i, j, width, height, c, zoomOut)
end
println("Writing NetCDF ...")
filename = "test.nc"
isfile(filename) && rm(filename)
nccreate(filename, "xi", "x", collect(1:height), "y",
collect(1:width), t=NC_FLOAT,
mode=NC_NETCDF4, compress=9);
ncwrite(data, filename, "xi");
```

- We experimented with plotting with Plots and ImageView, but these were very slow ...
- Instead, saving to NetCDF and plotting in ParaView

| | | Distributed | DistributedArrays | Julia set | | |
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| | | | | | | |

Parallelizing the Julia set

We have a large array \Rightarrow let's use DistributedArrays and compute it in parallel

```
< using ProgressMeter, NetCDF
---
> using NetCDF
> @everywhere using Distributed, DistributedArrays
< function pixel(i, j, width, height, c, zoomOut)
---
> @everywhere function pixel(i, j, width, height, c, zoomOut)
```

| | | Distributed | DistributedArrays | Julia set | | |
|--|--|-------------|-------------------|-----------|--|--|
| | | | | 00000 | | |
| | | | | | | |

Parallelizing the Julia set

We have a large array \Rightarrow let's use DistributedArrays and compute it in parallel

```
< using ProgressMeter, NetCDF
> using NetCDF
> @everywhere using Distributed, DistributedArrays
< function pixel(i, j, width, height, c, zoomOut)
> @everywhere function pixel(i, j, width, height, c, zoomOut)
> @everywhere function fillLocalBlock(data, width, height, c, zoomOut)
      h, w = localindices(data)
              data.localpart[iLocal, jLocal] = pixel(i, j, width, height, c, zoomOut)
> end
```

| Threads1 | | Distributed | DistributedArrays | Julia set | | Summary |
|----------|--|-------------|-------------------|-----------|--|---------|
| | | | | 00000 | | |
| | | | | | | |

Parallelizing the Julia set (cont.)

```
< data = zeros(Float32, height, width);
< @showprogress for i in 1:height, j in 1:width
< data[i,j] = pixel(i, j, width, height, c, zoomOut)
---
> data = dzeros(Float32, height, width);  # distributed 2D array of 0's
> @time @sync for i in workers()
> @spawnat i fillLocalBlock(data, width, height, c, zoomOut)
> nonDistributed = zeros(Float32, height, width);
> nonDistributed = zeros(Float32, height, width);
> nonDistributed[:,:] = data[:,:];  # ncwrite does not accept DArray type
>
< ncwrite(data, filename, "xi");
---
> powrite(nonDistributed_filename_"xi");
```

using NetCDF

Julia set 00000

Parallel Julia set code

```
@everywhere using Distributed, DistributedArrays
@everywhere function pixel(i, j, width, height, c, zoomOut)
        if abs(z) >= 4
height, width, c, zoomOut = n, n, 0.355 + 0.355im, 1.2
@everywhere function fillLocalBlock(data,width, height,
        iLocal = i - h.start + 1
                pixel(i, j, width, height, c, zoomOut)
```

data = dzeros(Float32, height, width); Otime Osync for i in workers() @spawnat i fillLocalBlock(data, width, height,

```
nonDistributed = zeros(Float32, height, width);
```

```
isfile(filename) && rm(filename)
         mode=NC NETCDF4, compress=9);
```

Parallel Julia set code

using NetCDF

```
@everywhere using Distributed, DistributedArrays
@everywhere function pixel(i, j, width, height, c, zoomOut)
       if abs(z) >= 4
height, width, c, zoomOut = n, n, 0.355 + 0.355im, 1.2
        iLocal = i - h.start + 1
               pixel(i, j, width, height, c, zoomOut)
                             $ julia -p 2 juliaSetDistributedArrays.jl
```

```
nonDistributed = zeros(Float32, height, width);
nonDistributed[:,:] = data[:,:];
# ncwrite does not accept DArray type
```

```
# serial runtime: 37s 37s
1 # serial runtime: 28.2s 31.6s 32.3s
1 # with 2 processes: 14.9s 14.9s 15.8s
```

| | | | Distributed 00000000000 | DistributedArrays 0000 | SharedArrays ●00 | |
|------|--------|-----|----------------------------|---------------------------|---------------------|--|
| Shai | redArr | ays | | | | |

- Part of the Julia Standard Library (comes with the language)
- A SharedArray is shared across processes (set of workers) on the same node
 - full array is stored on the control process
 - significant cache on each worker
- Similar to DistributedArrays, you can read elements using their global indices from any worker
- Unlike with DistributedArrays, with SharedArrays you
 - can write into any part of the array on any worker ⇒ potential for a race condition and indeterministic outcome with a poorly written code!
 - are limited to a set of workers on the same node

```
SharedArrays
                                                                   000
SharedArrays (cont.)
using Distributed, SharedArrays
addprocs(4)
a = SharedArray{Float64}(30);
@fetchfrom 2 sum(a) # correct (30.0)
@fetchfrom 3 sum(a) # correct (30.0)
@sync @spawnat 2 a[:] .= 2.0 # can assign from any worker!
@fetchfrom 3 sum(a)
b = SharedArray{Float64}((1000), init = x \rightarrow x = 1.0) # use a function to initialize 'b'
@everywhere using SharedArrays
@fetchfrom 2 localindices(b)
```

Let's fill each element with its corresponding myd() value:

b = SharedArray{Float64}((1000), init = x -> x .= myid()) # indeterminate outcome!

b = SharedArray{Float64}((1000), init = x -> x[localindices(x)] .= myid()) # parallel init

| | | | Distributed 00000000000 | DistributedArrays 0000 | SharedArrays ००● | |
|------|--------|-------|----------------------------|---------------------------|---------------------|--|
| 2D 3 | Shared | Array | | | | |

```
using Distributed, SharedArrays
addprocs(4)
a = SharedArray{Float64}(10000,10000);
@distributed for i in 1:10000  # parallel for loop split across all workers
    for j in 1:10000
        a[i,j] = myid()  # ID of the worker that initialized this element
    end
end
a  # available on all workers
a[1:10,1:10]  # on the control process
@fetchfrom 2 a[1:10,1:10]  # on worker 2
```

Slow series

Threads2 00000 Distributed 000000000000 DistributedArray 0000 Julia set 00000 SharedArrays 000 Summa o

N-body

Brute-force $\mathcal{O}(N^2)$ accurate solver

• Problem: place *N* identical particles randomly in a unit cube, zero initial velocities

Method:

- force evaluation via direct summation
- single variable (adaptive) time step (smaller Δt when any two particles are close)
- time integration: more accurate than simple forward Euler + one force evaluation per time step
- two parameters: softening length and Courant number
- In a real simulation, you would replace:
 - direct summation with a tree- or mesh-based $\mathcal{O}(N \log N)$ code
 - current integrator with a higher-order scheme, e.g. Runge-Kutta
 - current timestepping with hierarchical particle updates
 - for long-term stable evolution with a small number of particles, use a symplectic orbit integrator

Expected solutions:

- 2 particles: should pass through each other, infinite oscillations
- 3 particles: likely form a close binary + distant 3rd particle (hierarchical triple system)
- many particles: likely form a gravitationally bound system, with occasional ejection

```
N-body
                                         Distributed
                                                                                                000000
Serial N-body code
                                             @showprogress for iter = 1:niter
using Plots, ProgressMeter
                                                             force[i,:] -= (x[i, :] .- x[j,:]) / distSquared^1.5;
                                                     x[i,:] .+= v[i,:] .* dt .+ 0.5 .* oldforce[i,:] .* dt^2;
                                                 if iter%freg == 0
soft = softeningLength^2;
                                                 end
oldforce = zeros(Float32, npart, 3);
                                             @showprogress for i = 1:nframes
                                                 plt = plot(npart, xlim=(-0.5, 1.5), ylim=(-0.5, 1.5),
                                                            zlim=(-0.5,1.5), seriestype=:scatter3d,
                                                            legend=false, dpi=:300);
                                                 scatter3d!(history[1:npart,1,i], history[1:npart,2,i],
                                                            history[1:npart,3,i], markersize = 2);
                                                 png("frame" * lpad(i, 4, '0'))
                                             end
```

| | | | Distributed 00000000000 | DistributedArrays 0000 | | N-body oo●ooo | |
|------|-------|--|----------------------------|---------------------------|--|------------------|--|
| Solu | ation | | | | | | |

2 bodies





A frame is saved every 300 steps + variable timesteps

 \Rightarrow in these movies the time arrow represents the time step number (not time!)

1 Slow s

Threads2 00000 Distributed

Distributed Array

Julia set ooooo SharedArrays 000 N-body 000●00 Summar

Parallelizing the N-body code

Many small arrays \Rightarrow let's use SharedArrays and fill them in parallel

> using Distributed, SharedArrays

> addprocs(2)

Slow series

Threads2 00000 Distributed 00000000000 Distributed Array

Julia set

SharedArra 000 N-body 000●00 Summar o

Parallelizing the N-body code

Many small arrays \Rightarrow let's use SharedArrays and fill them in parallel

```
> using Distributed, SharedArrays
> history = SharedArray{Float32}((npart, 3, nframes), init = x \rightarrow x = 0.0);
< oldforce = zeros(Float32, npart, 3);
```

Slow series

Threads2 00000 Distributed 0000000000 Distributed Arra 0000 Julia set 00000 SharedArrays 000 Summa o

N-body

000000

Parallelizing the N-body code

Many small arrays \Rightarrow let's use SharedArrays and fill them in parallel

```
> using Distributed, SharedArrays
> addprocs(2)
> v = SharedArray{Float32}((npart, 3), init = x \rightarrow x = 0.0);
> history = SharedArray{Float32}((npart, 3, nframes), init = x \rightarrow x = 0.0);
< oldforce = zeros(Float32, npart, 3);
      tmin = @distributed (min) for i = 1:npart
```

WestGrid webinar - slides and functions at https://git.io/Jtdge 2021-Mar-17 43/46

Intro
oThreads1
cococSlow series
cococThreads2
cococDistributed
cococDistributed Arrays
cococJulia set
cococSharedArrays
cococN-body
cococSummary
cococParallel N-body code@showprogress for iter = 1:niter
tmin = 0 distributed (min) for i = 1:npart
tmin = 1.e10
force[i,:] .= 0.@showprogress for iter = 1:niter
tmin = 1.e10
force[i,:] .= 0.using Plots, ProgressMeter
using Distributed, SharedArrays
addprocs (4)@showprogress for iter = 1:niter
tmin = 1.e10
force[i,:] .= 0.using Plots, ProgressMeter
using Distributed, SharedArrays
addprocs (4)@showprogress for iter = 1:niter
tmin = 1.e10
force[i,:] .= 0.using Plots, ProgressMeter
using Distributed, SharedArrays
addprocs (4)@sum((x[i,:] .- x[j,:]).^2) + soft;
force[i,:] -= (x[i, :] .- x[j,:]) / distSquared^1.5;
tmin = min(tmin, sqrt(distSquared /
sum((v[i,:] .- v[j,:]).^2)));npart = 20
niter = Int(1e5)
freq = 300end

ourant = 1e-3 ofteningLength = 0.01

end

```
dt = min(tmin*courant, 0.001);  # limit the initial step
for i = 1:npart
    x[i,:] .+= v[i,:] .* dt .+ 0.5 .* oldforce[i,:] .* dt^2;
    v[i,:] .+= 0.5 .* (oldforce[i,:] .+ force[i,:]) .* dt;
    oldforce[i,:] .= force[i,:];
end
```

en

```
if iter%freq == 0
    history[:, :, trunc(Int, iter/freq)+1] = x;
end
```

end

N-body 00000

Parallel performance: 2-core laptop and Cedar

Laptop, 20 particles, 10⁵ steps:

| code | computing | animation |
|--------------------|-----------|-----------|
| serial | 3m47s | 1m32s |
| 2 parallel workers | 3m50s | 1m30s |
| 4 parallel workers | 4m17s | 1m29s |

Laptop, 100 particles, 10³ steps:

| code | computing |
|--------------------|-----------|
| serial | 59s |
| 2 parallel workers | 36s |
| 4 parallel workers | 37s |

Laptop, 300 particles, 10³ steps:

| code | computing |
|--------------------|-----------|
| serial | 7m48s |
| 2 parallel workers | 4m52s |
| 4 parallel workers | 4m23s |

Cedar, 100 particles, 10³ steps:

| code | computing |
|----------|-----------|
| serial | 1m23s |
| 2 cores | 46s |
| 4 cores | 29s |
| 8 cores | 22s |
| 16 cores | 18s |
| 32 cores | 19s |

module load StdEnv/2020 julia/1.5.2

sbatch/salloc --nodes=1-1 --ntasks=... julia -p \$SLURM_NPROCS nbodyDistributedShared.jl

```
sbatch/salloc --ntasks=1 --cpus-per-task=...
julia -p $SLURM CPUS PER TASK nbodyDistributedShared.jl
```

| | | | Distributed 00000000000 | DistributedArrays 0000 | | Summary • |
|-----|-------|--|----------------------------|---------------------------|--|--------------|
| Sum | nmary | | | | | |

- We covered Julia's multi-threading and multi-processing
 - showed timings both on a 2-core laptop (with hyperthreading) and on up to 32 cores on Cedar
- DistributedArrays vs. SharedArrays
- Parallelized 3 computationally intensive problems: slow series, Julia set, N-body
- Useful resources:
 - "Julia at Scale" forum https://discourse.julialang.org/c/domain/parallel
 - Baolai Ge's (SHARCNET) webinar on parallel Julia https://youtu.be/xTLFz-5a5Ec
 - brief introduction to parallel computing in Julia (some additional concepts not covered in this webinar) https://codingclubuc3m.github.io/2018-06-06-Parallel-computing-Julia.html
 - performance tips https://docs.julialang.org/en/v1/manual/performance-tips

