

Correlating hydrodynamic and acoustic fields in a turbulent combustor through community-based dimensionality reduction of vortical networks

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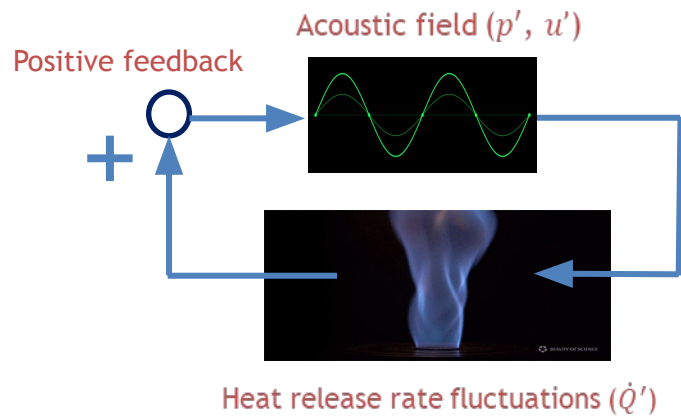
²Department of Aerospace Engineering, IIT Madras, India

³Oak Ridge National Laboratory, USA

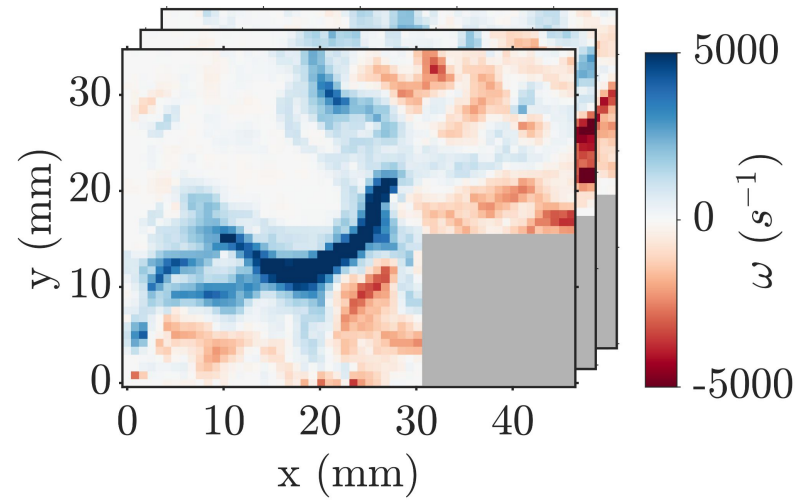
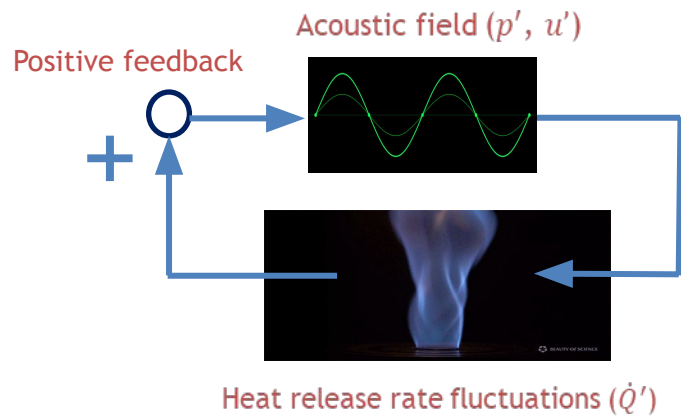
Acknowledgement:

Office of Naval Research Global
Institute of Eminence Initiative, Govt. of India
Office of Science of the US Department of Energy

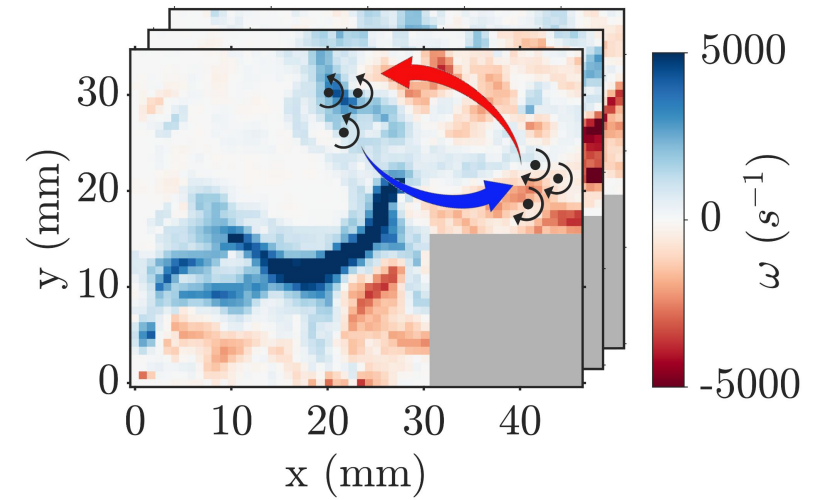
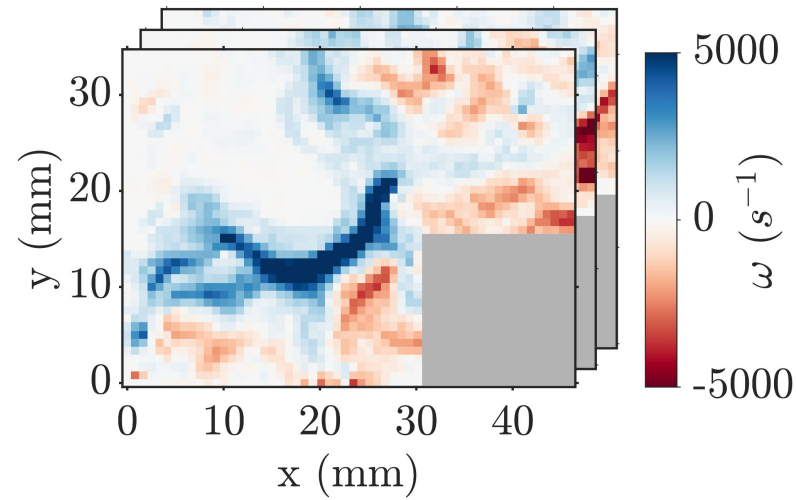
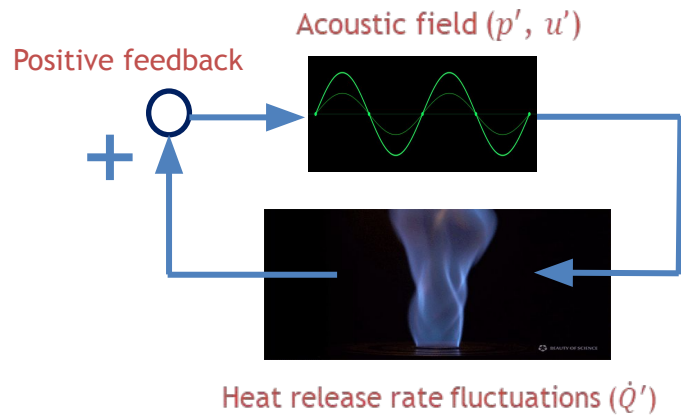
Positive feedback between acoustic pressure and heat release rate oscillations



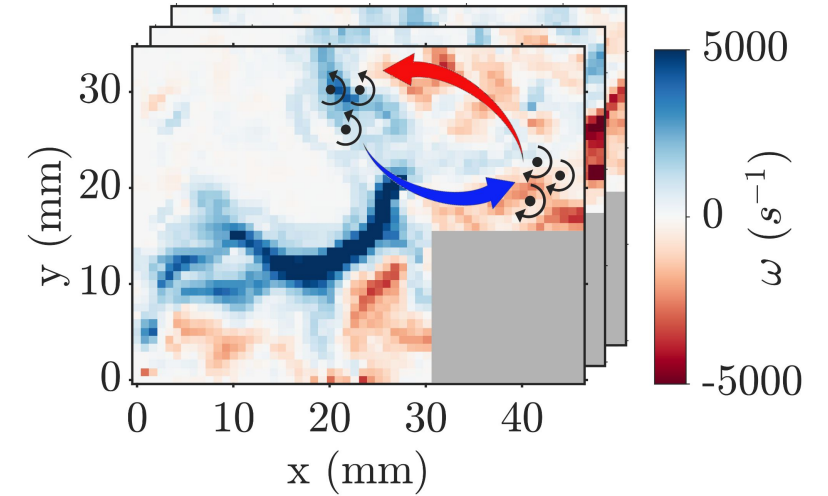
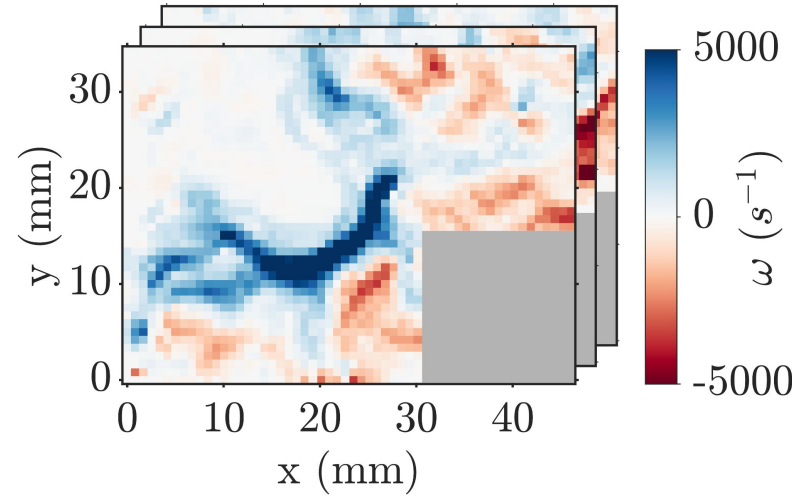
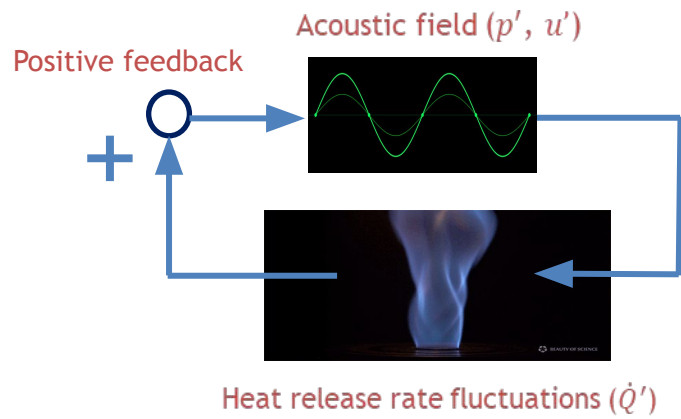
Vortical structures drive thermoacoustic instability in many combustors



Understand the relation between vortical interactions and acoustic pressure oscillations

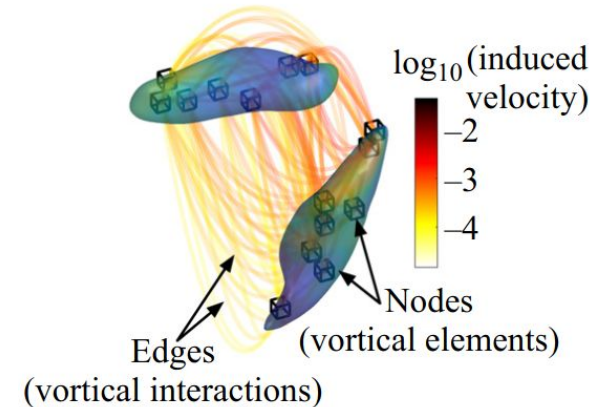


Complex networks provide a convenient framework to work with a large number of interactions

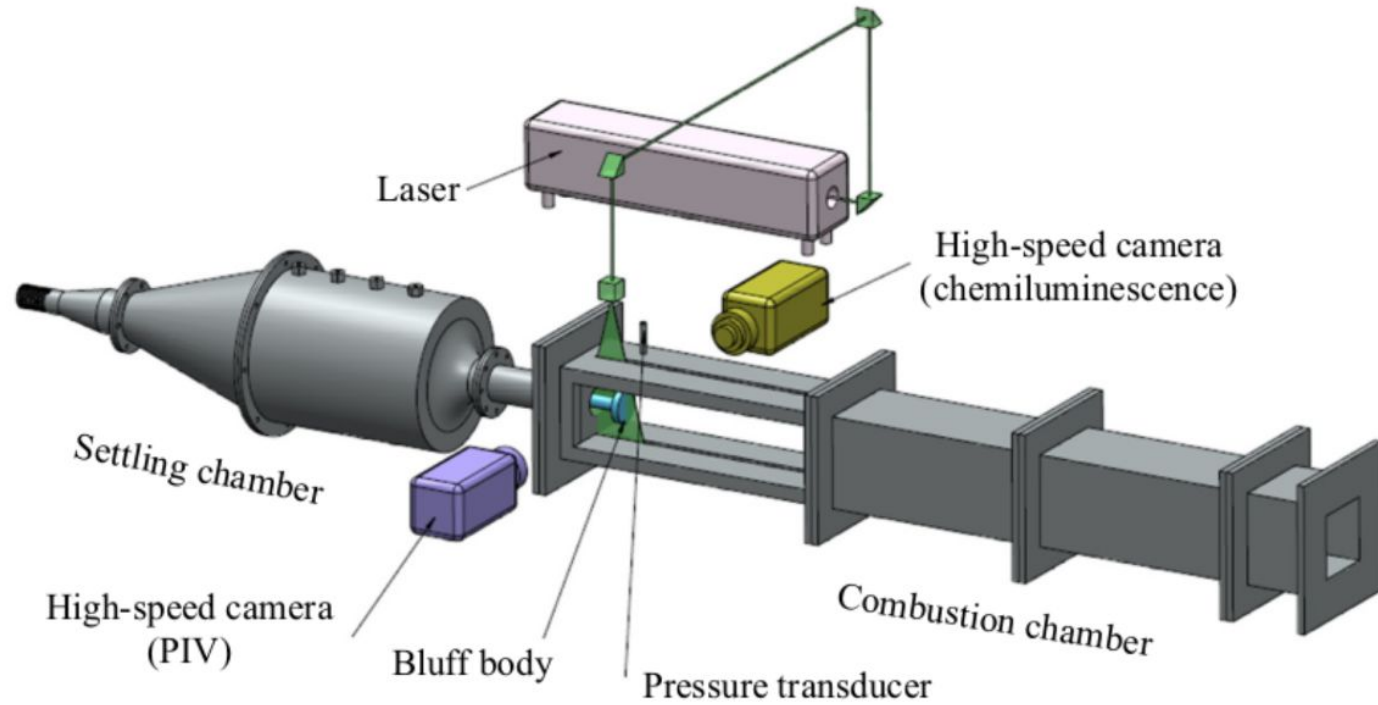


45×60 cells
 ≈ 1.5 million interactions

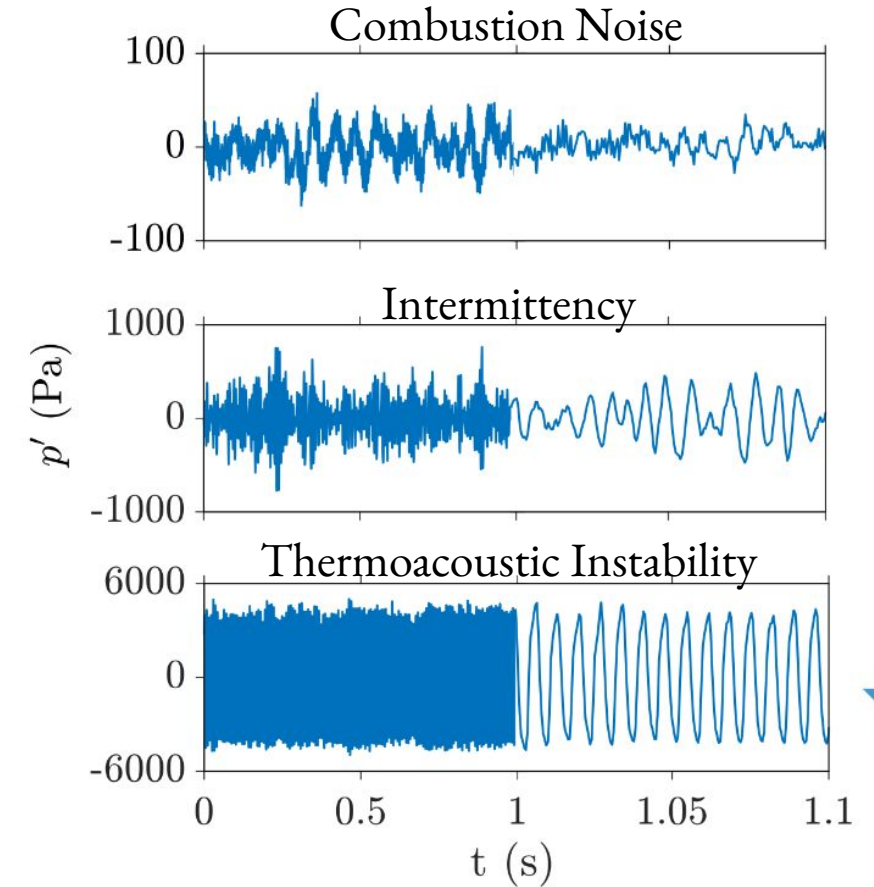
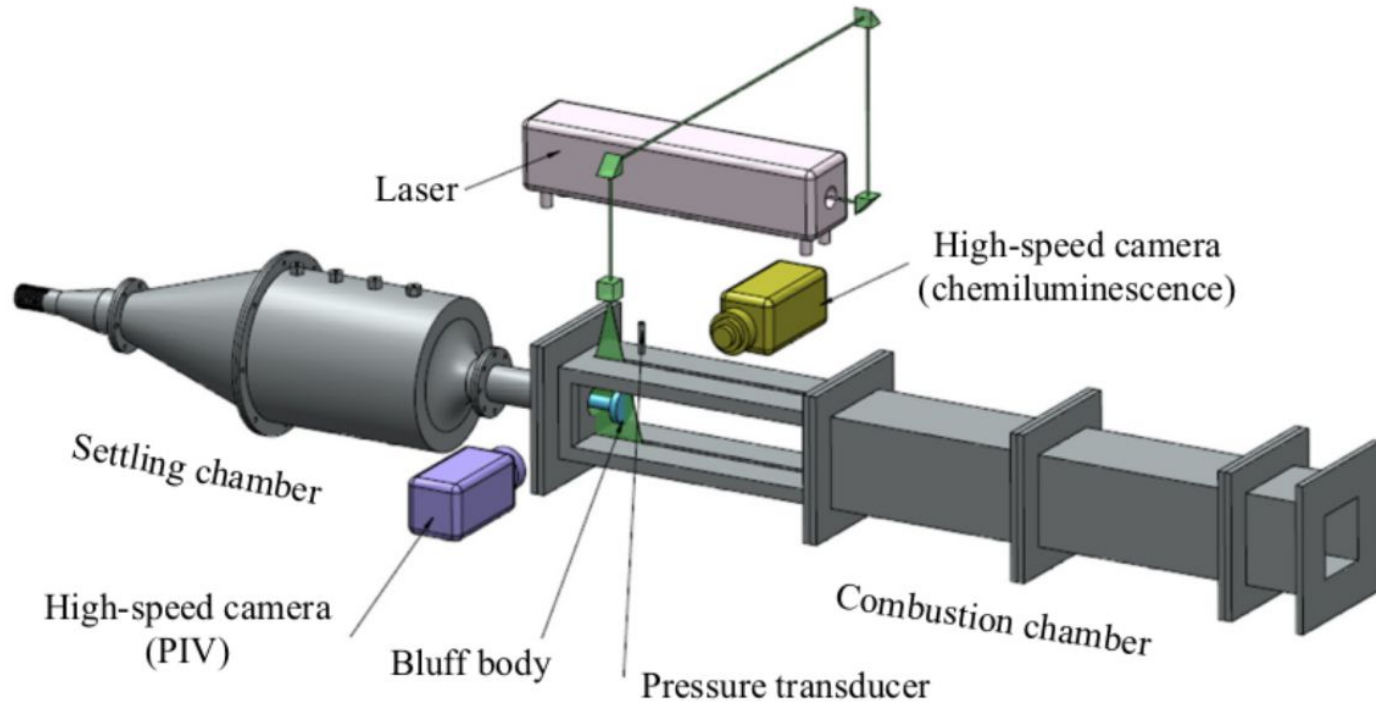
Network representation of vortical interactions



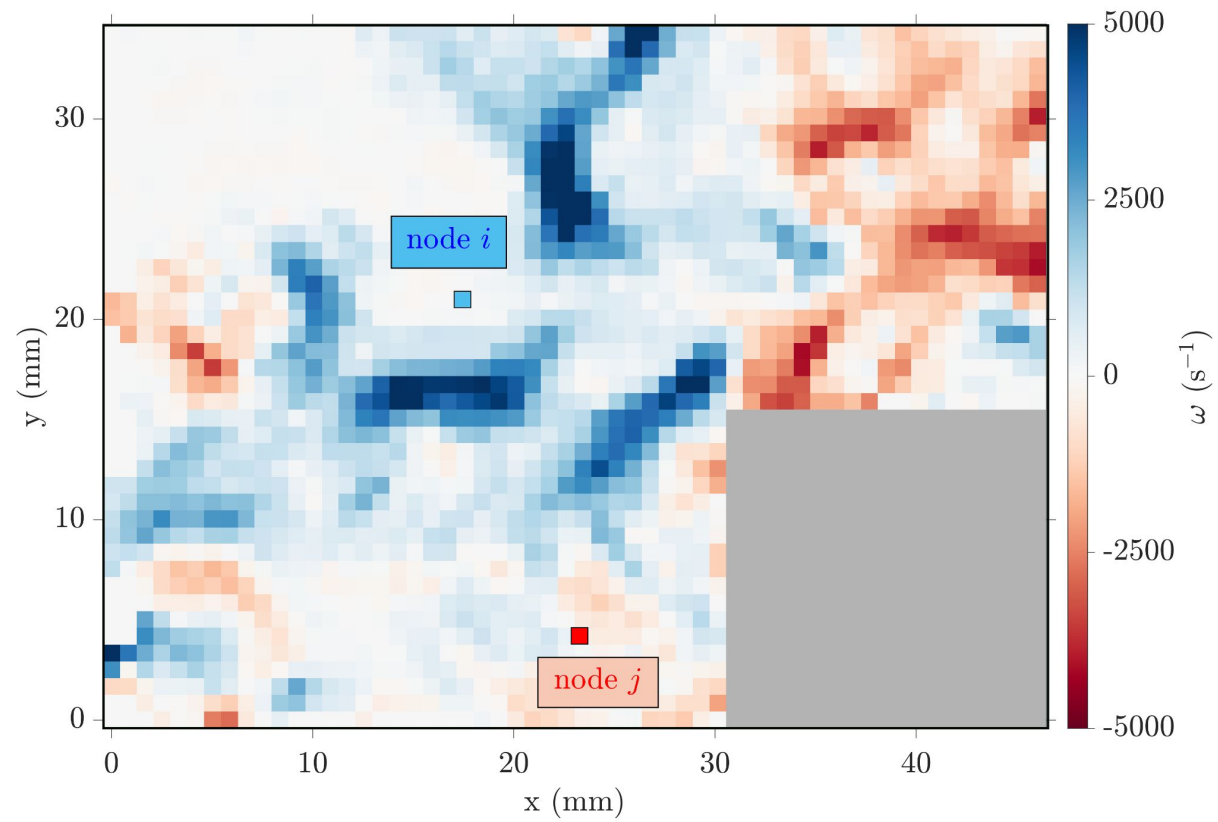
Bluff-body stabilized turbulent combustor



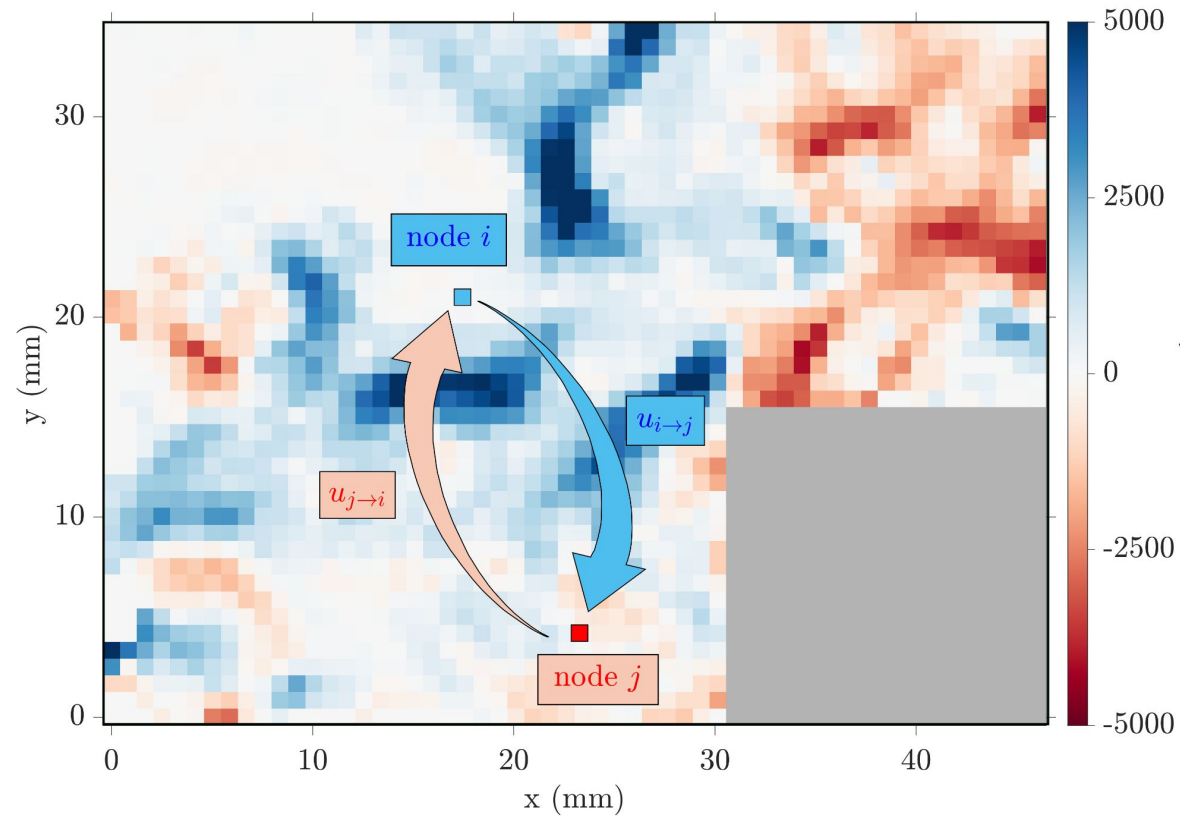
Bluff-body stabilized turbulent combustor - states of combustion noise, intermittency, and thermoacoustic instability



Cells of PIV computation domain - nodes of a complex network

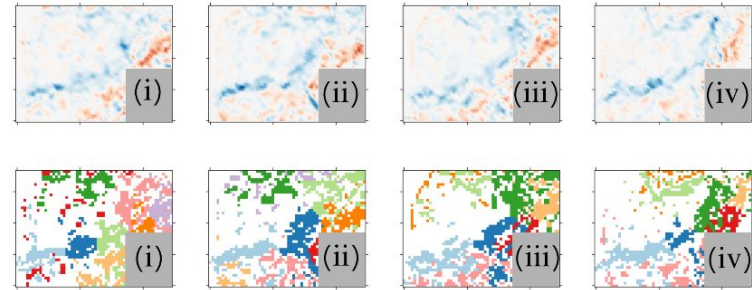
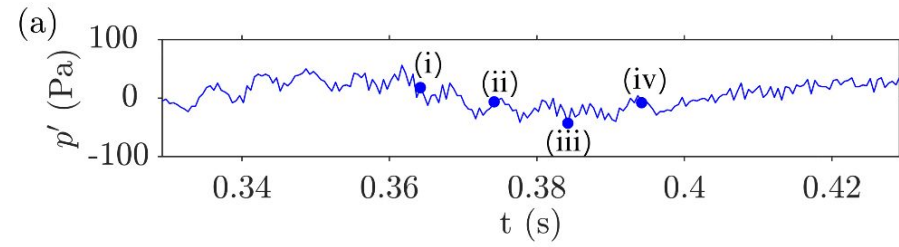


Induced velocity calculated from Biot-Savart law - directed links of a weighted complex network

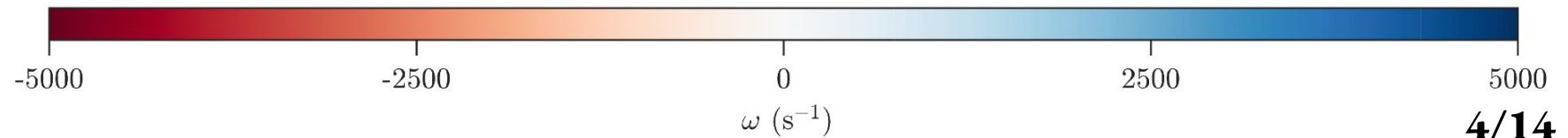


$$\mathbf{u}_{i \rightarrow j} = \frac{1}{2\pi} \int_{S_i} \frac{\omega_i(\mathbf{r}', t) \times (\mathbf{r}_j - \mathbf{r}'_i)}{\|\mathbf{r}_j - \mathbf{r}'_i\|_2^2} dS_i$$

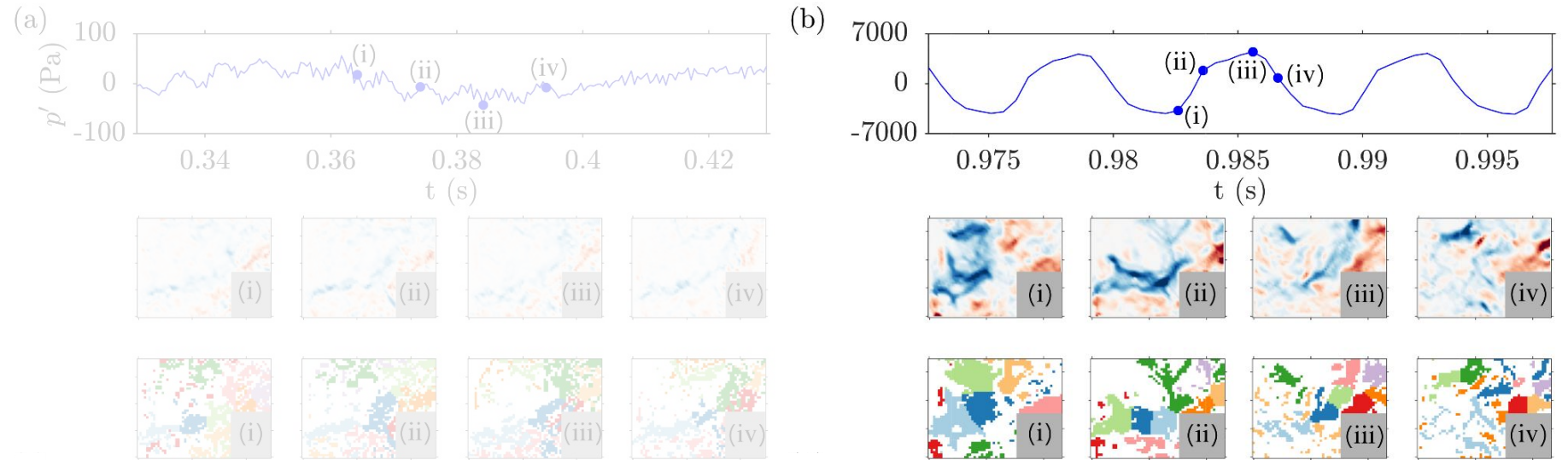
Vortical communities during different dynamical states



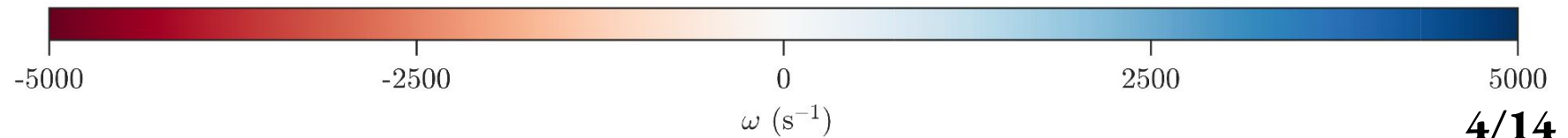
Combustion noise



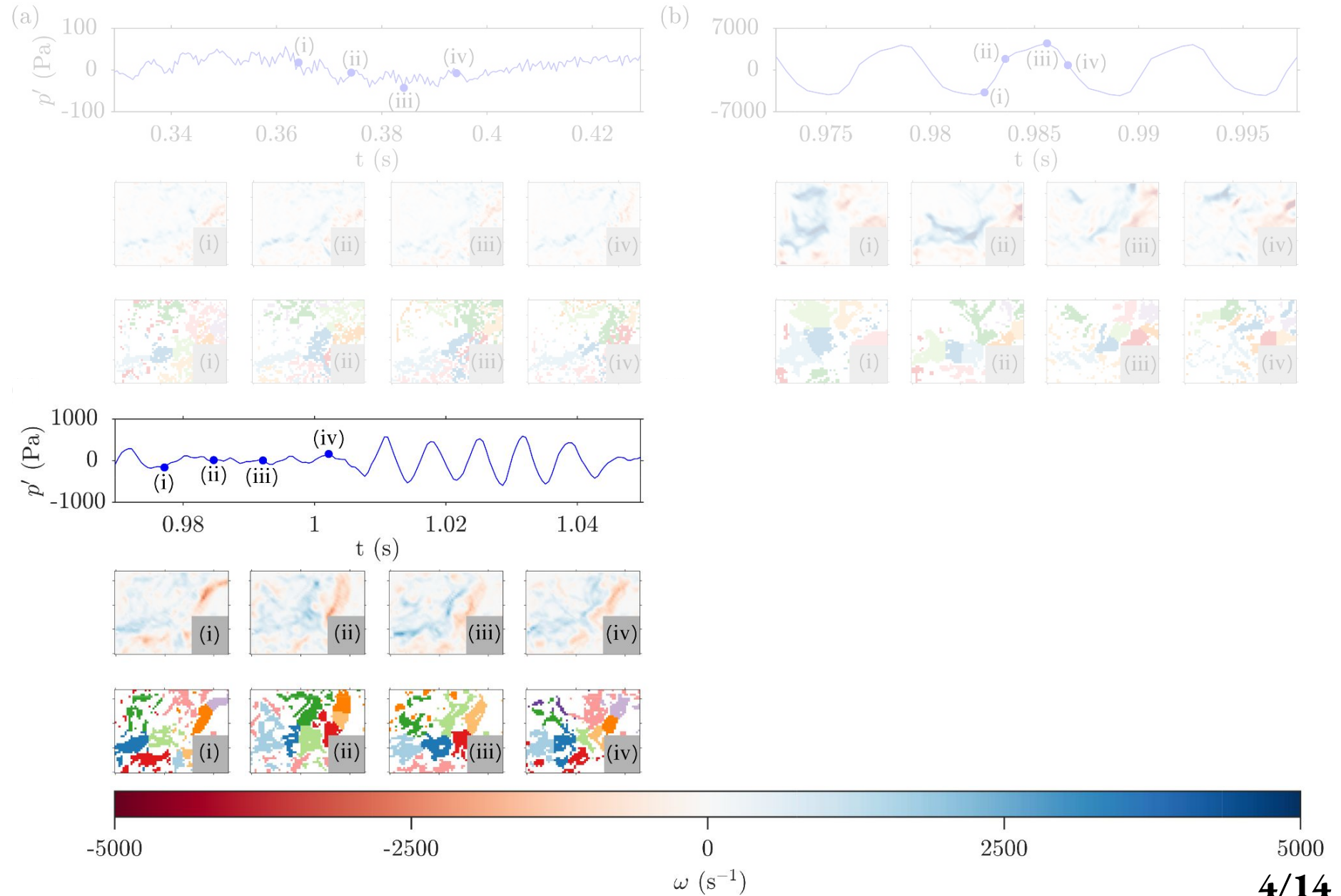
Vortical communities during different dynamical states



Thermoacoustic instability

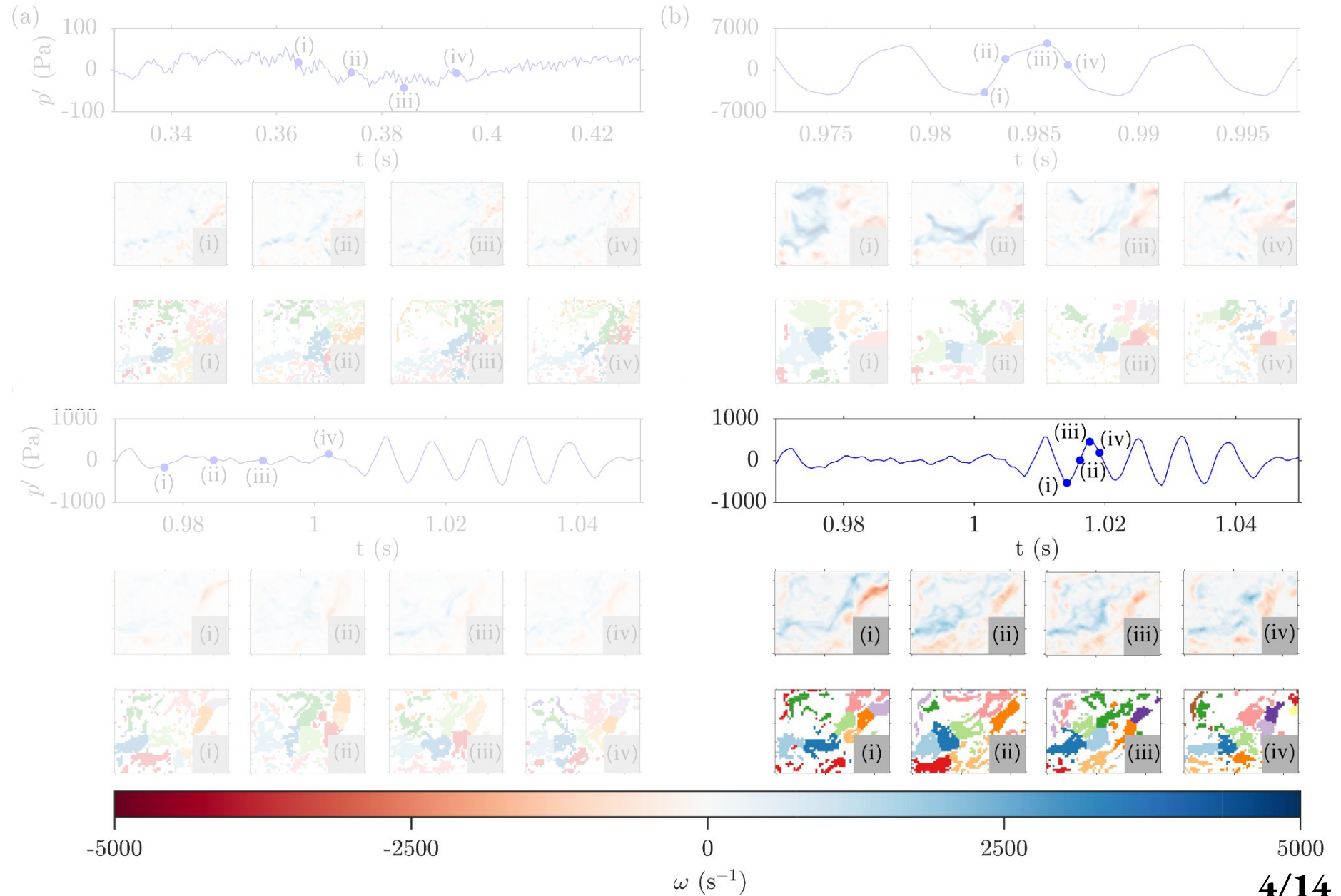


Vortical communities during different dynamical states



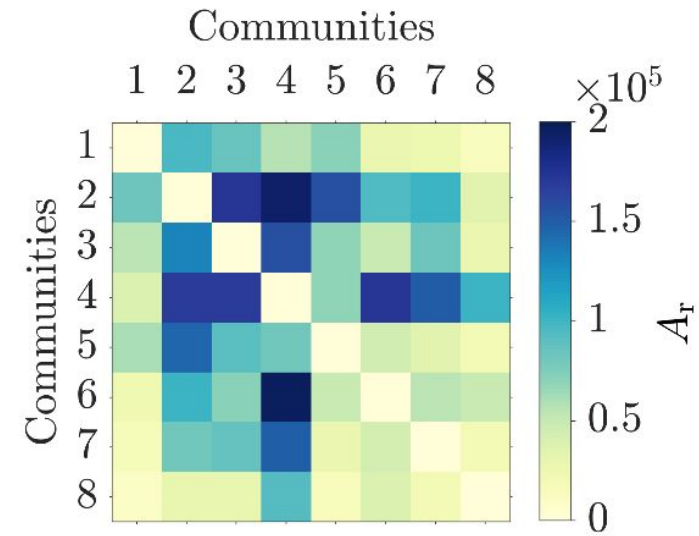
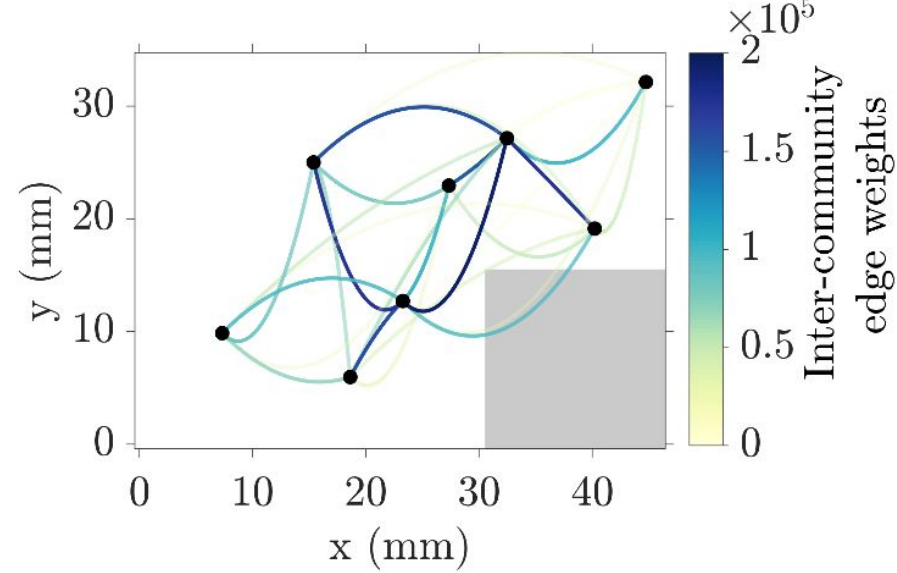
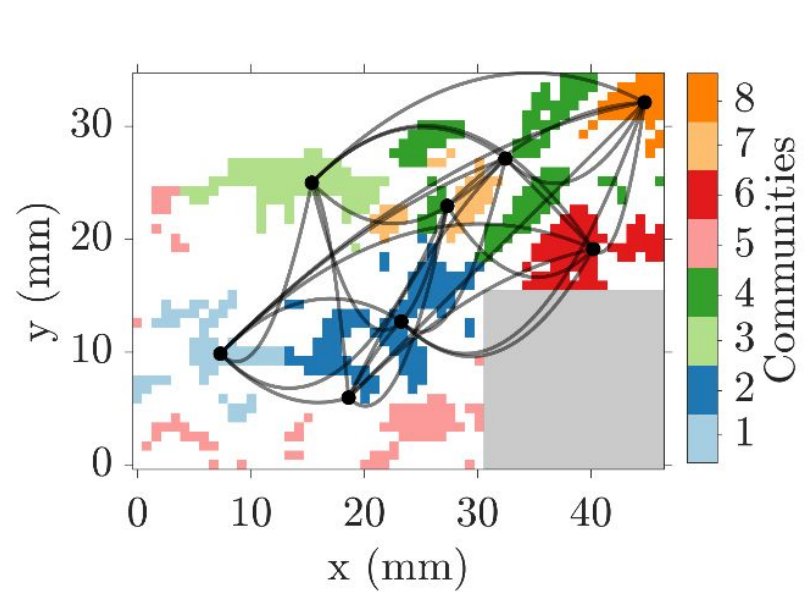
Aperiodic epoch of intermittency

Vortical communities during different dynamical states

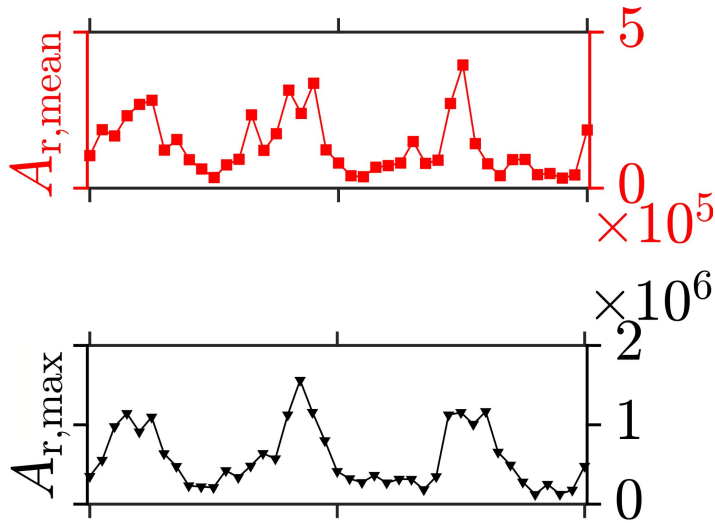
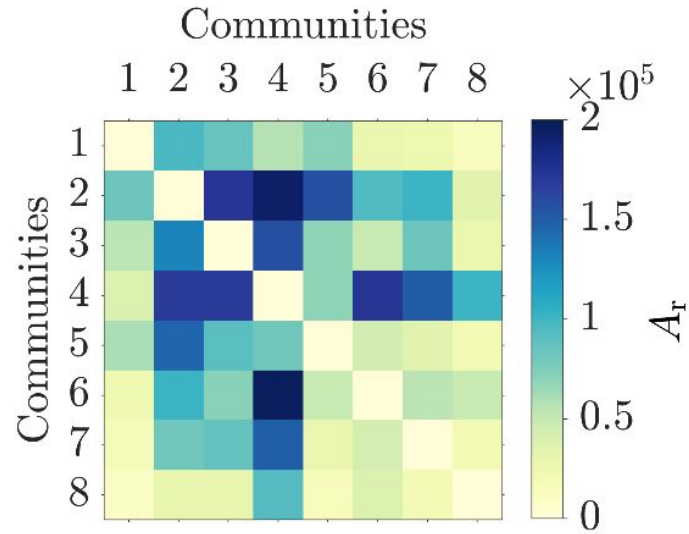


Periodic epoch of intermittency

At each time instant, communities are condensed through their weighted centroids to form **inter-community reduced networks**



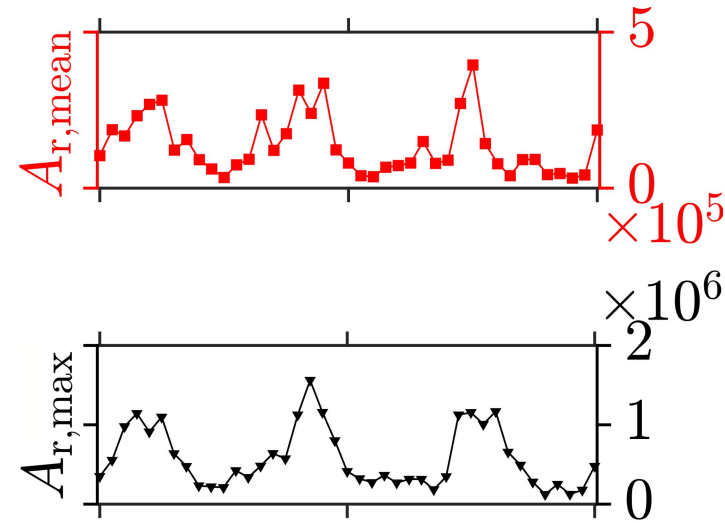
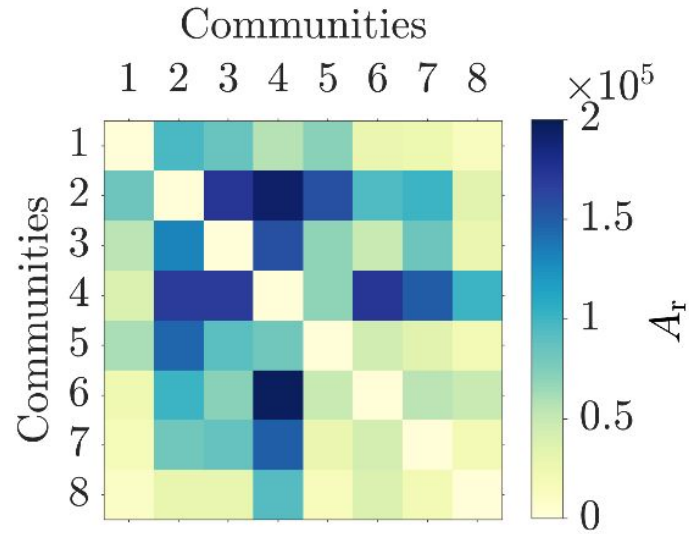
Network measures considered - mean and maximum of the reduced adjacency matrix



Average of all inter-community interactions

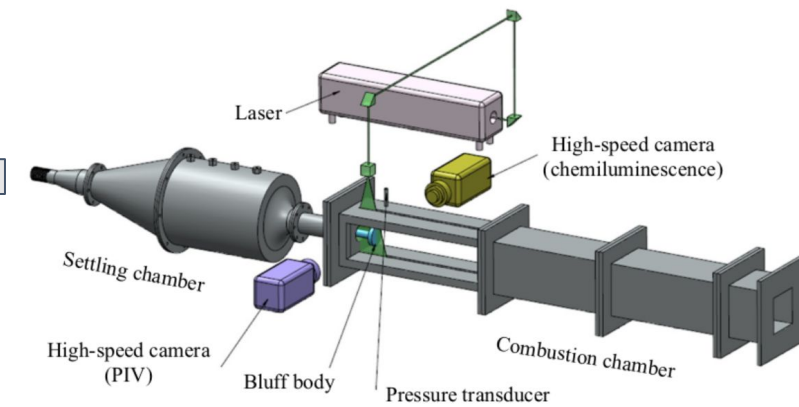
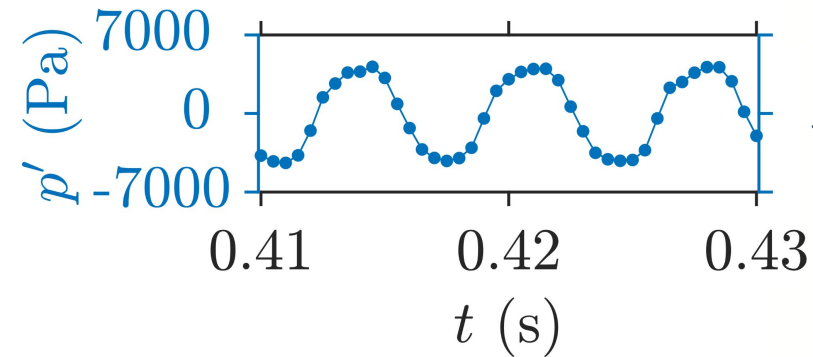
Maximum of all inter-community interactions

Evaluate correlation between temporal evolution of network measures and acoustic pressure fluctuations

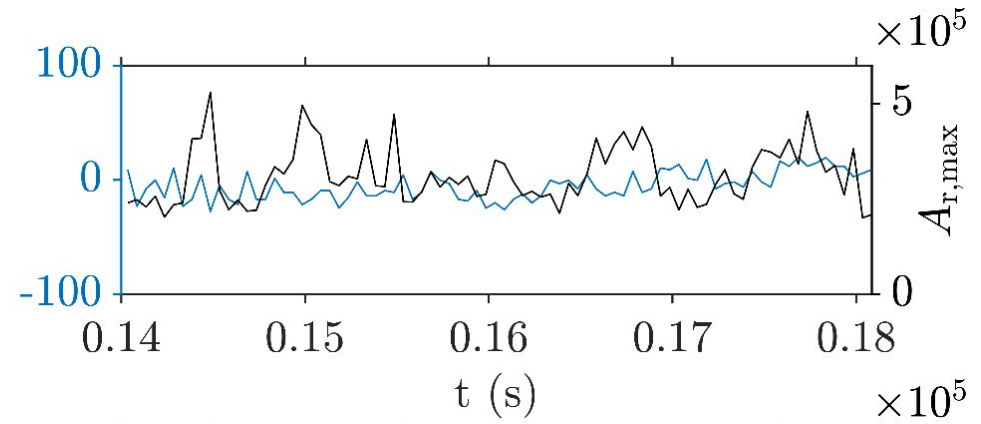
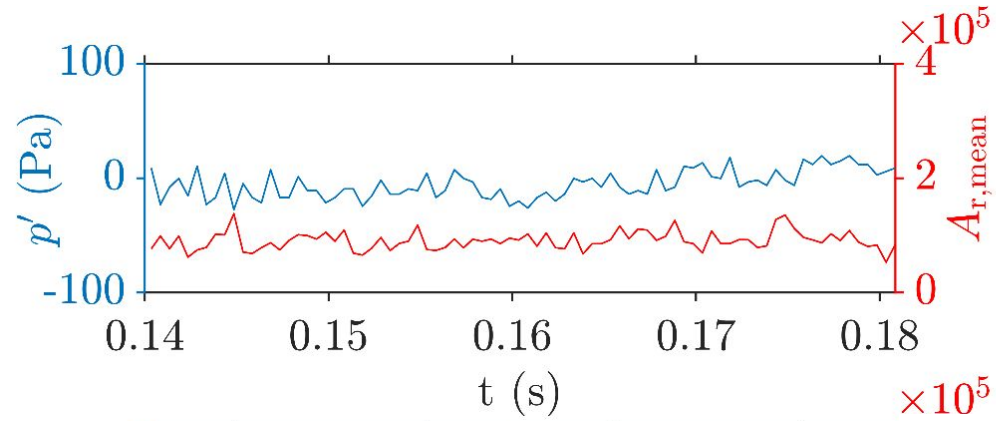


Average of all inter-community interactions

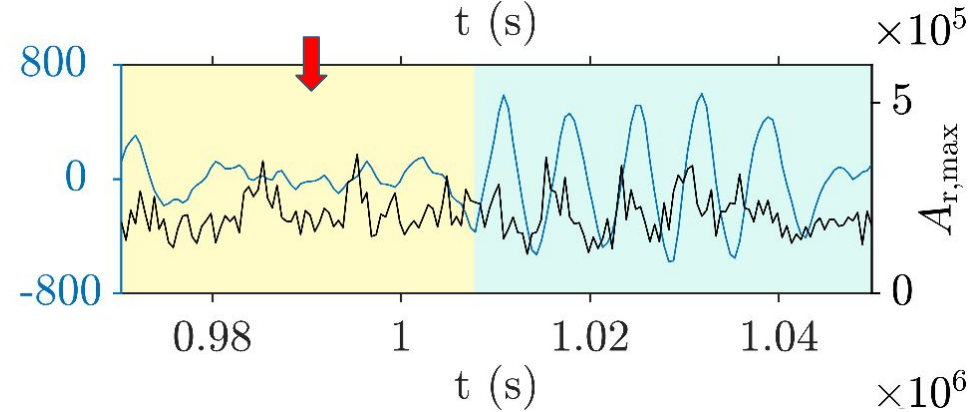
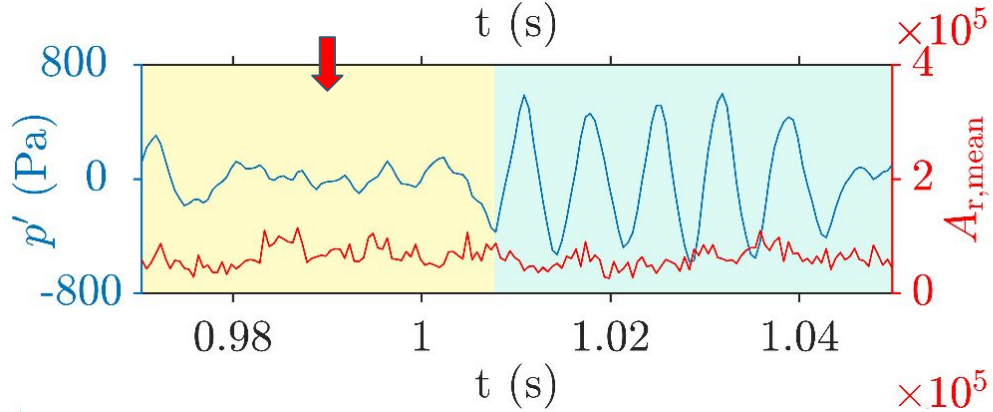
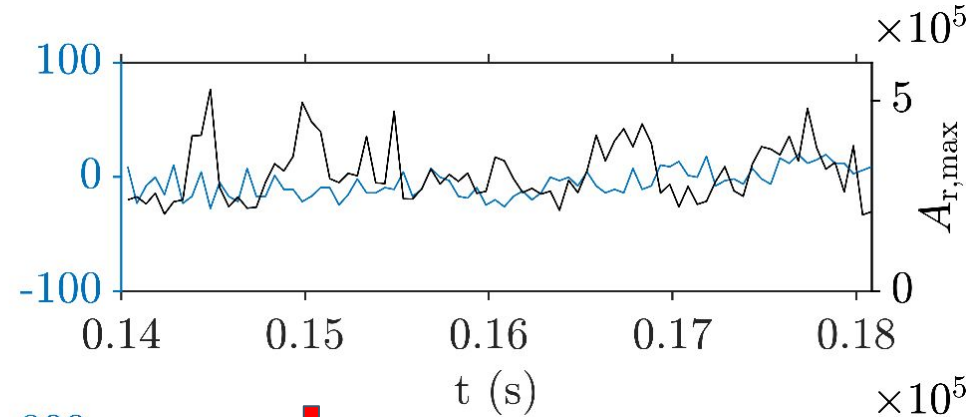
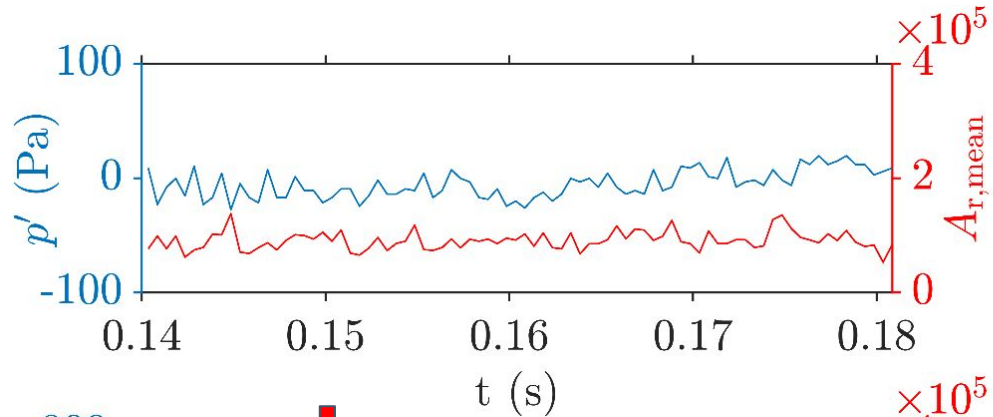
Maximum of all inter-community interactions



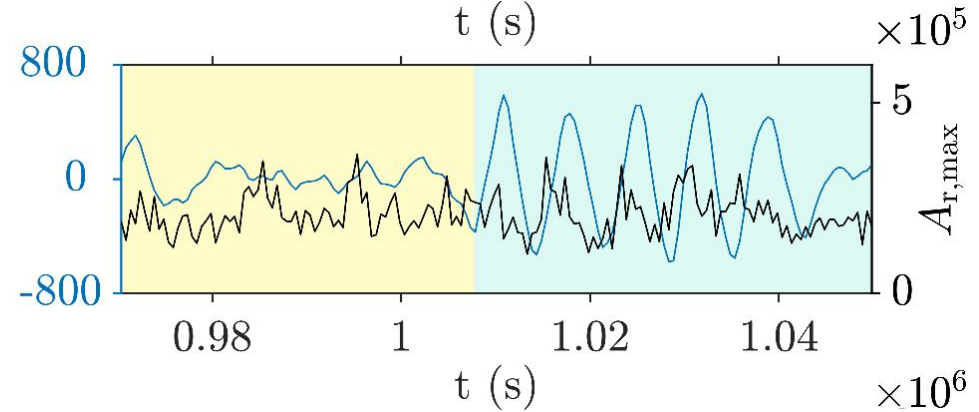
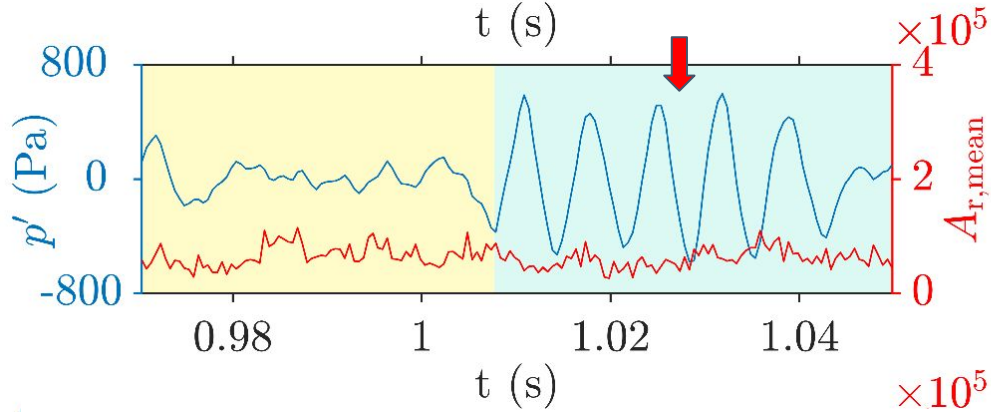
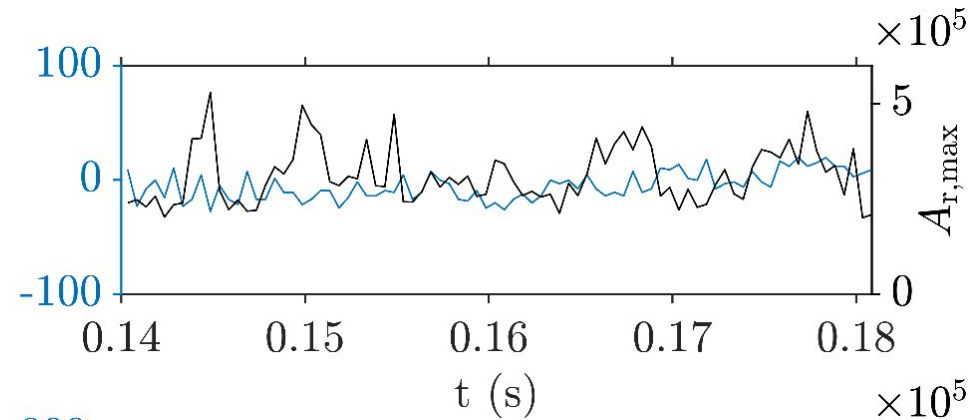
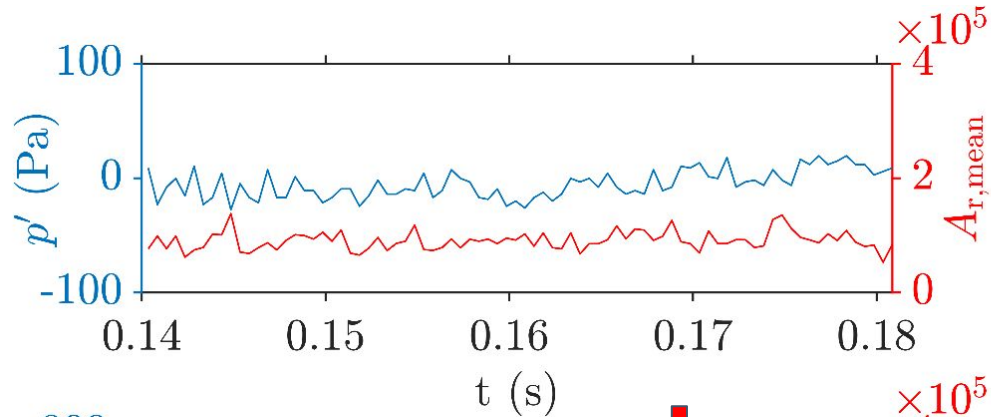
Combustion noise - aperiodic dynamics of networks measures



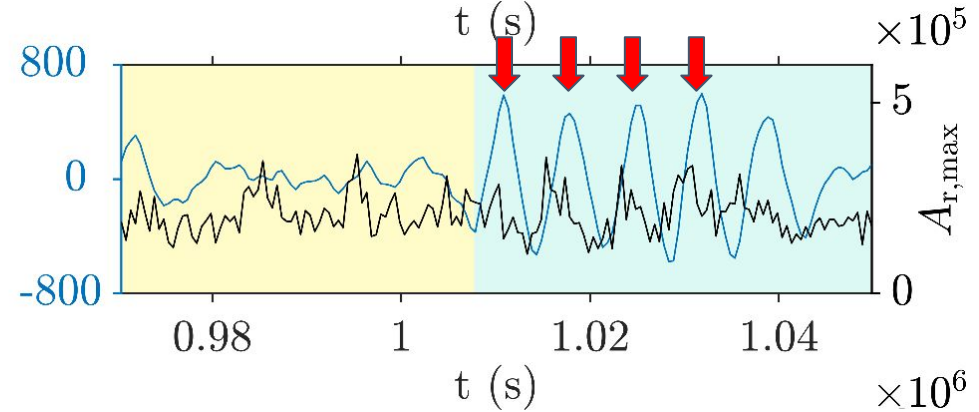
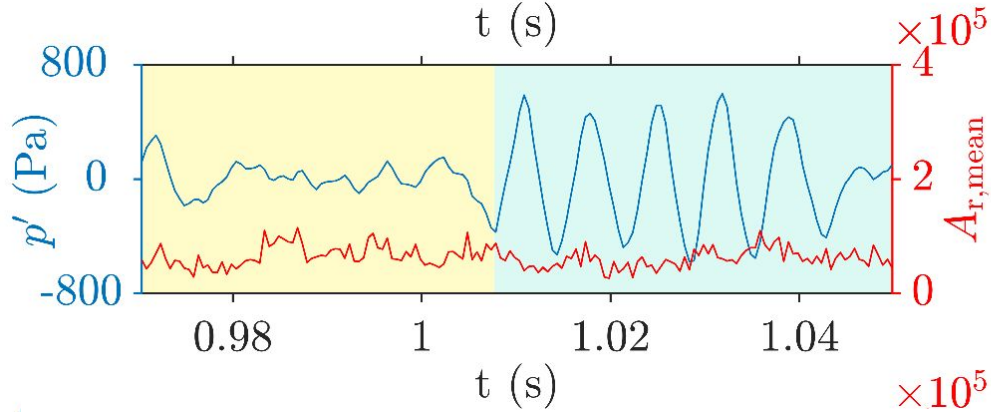
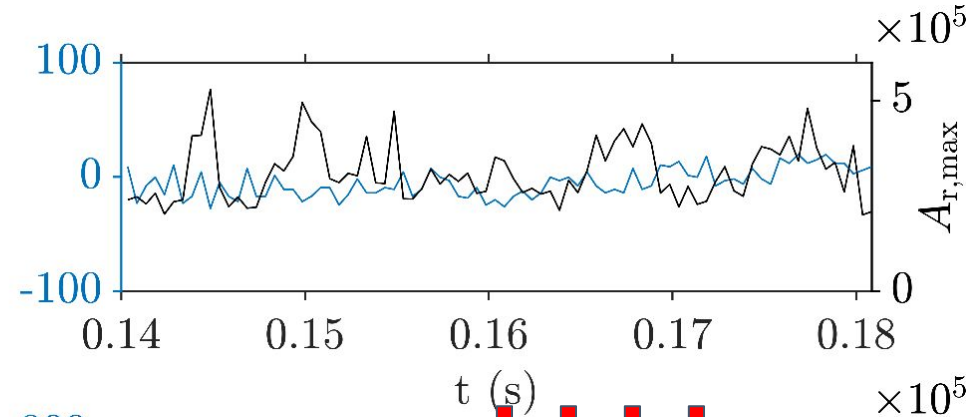
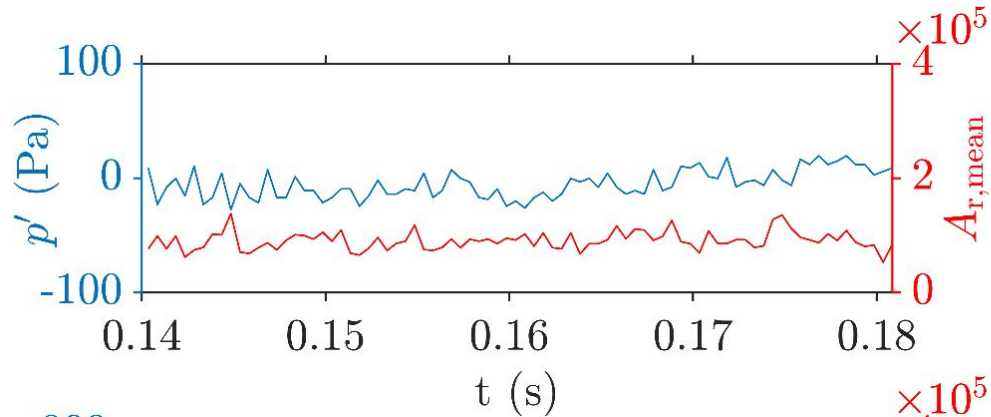
Intermittency - network measures are aperiodic during the aperiodic epoch of intermittency



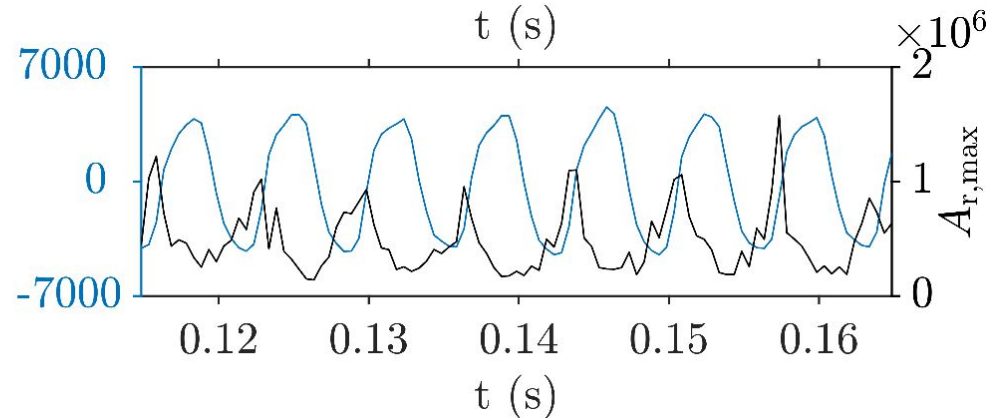
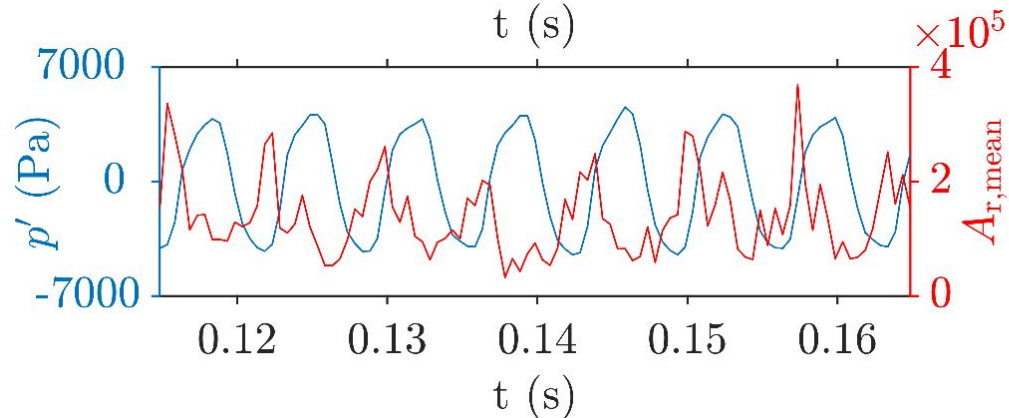
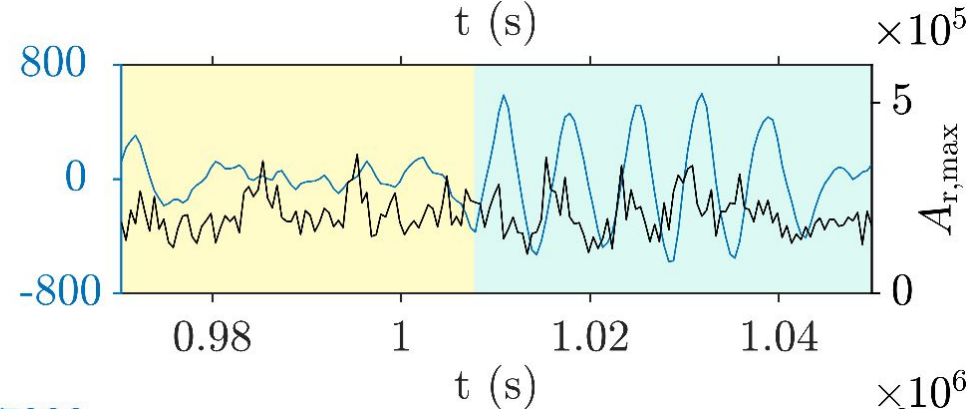
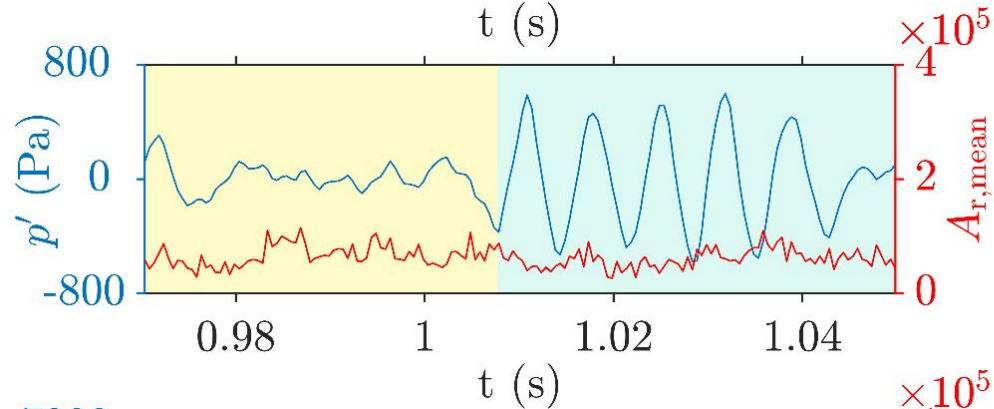
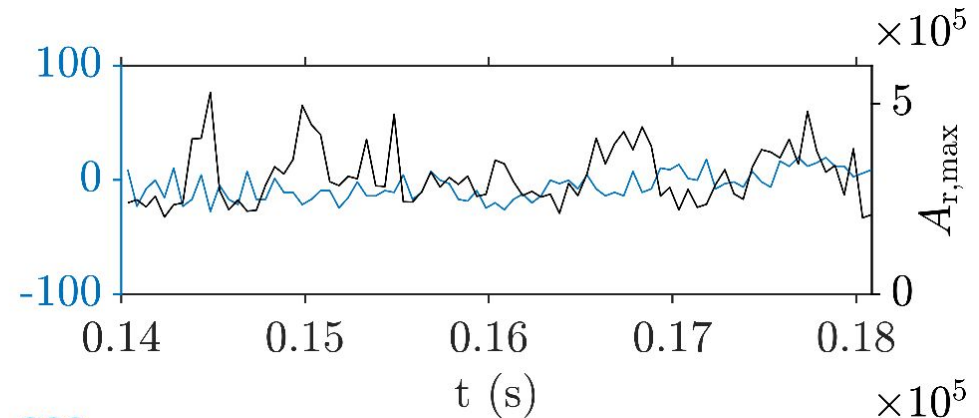
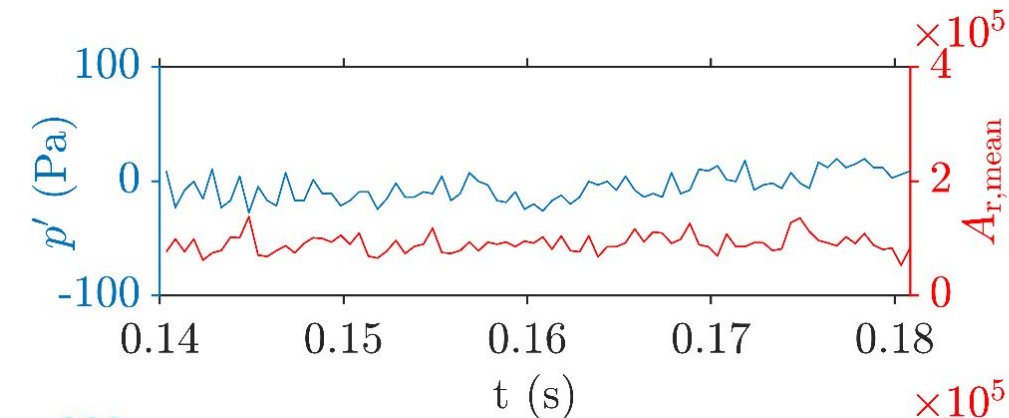
Intermittency - taking average of inter-community interactions smears out the periodic information of the flow field



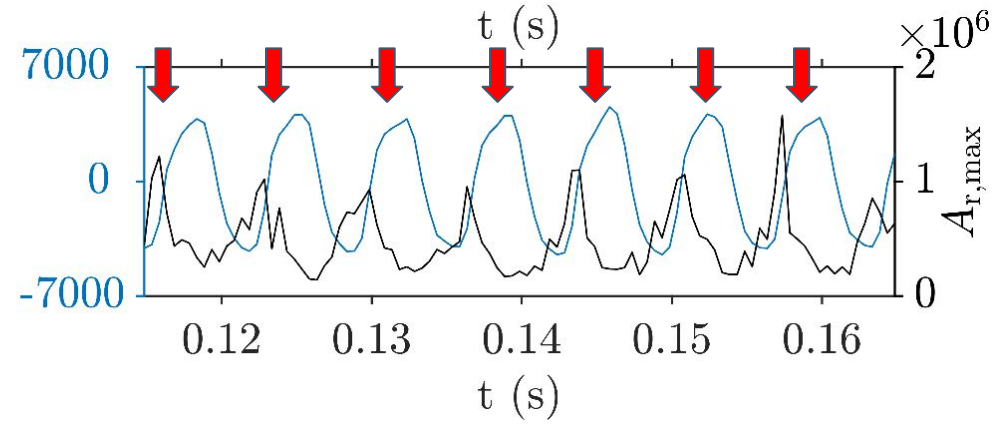
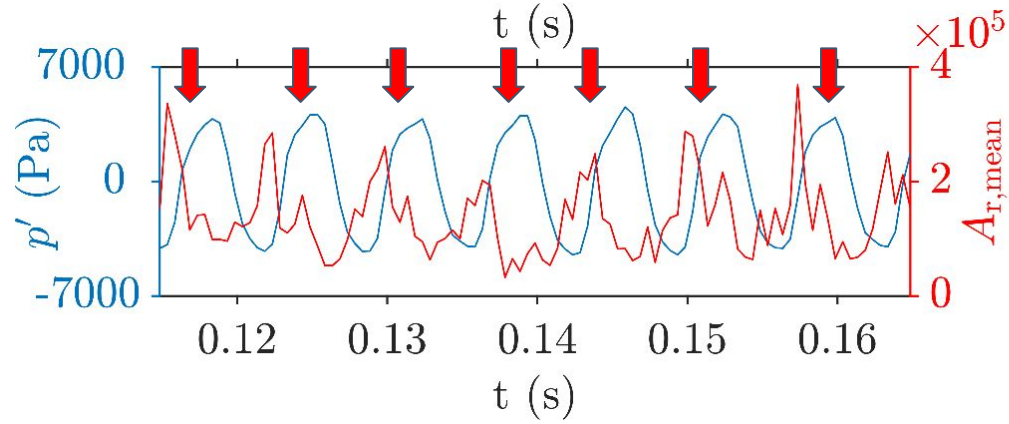
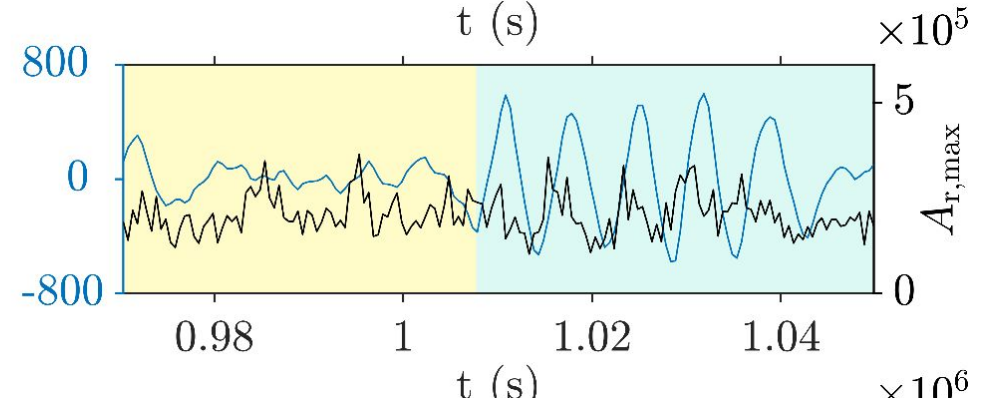
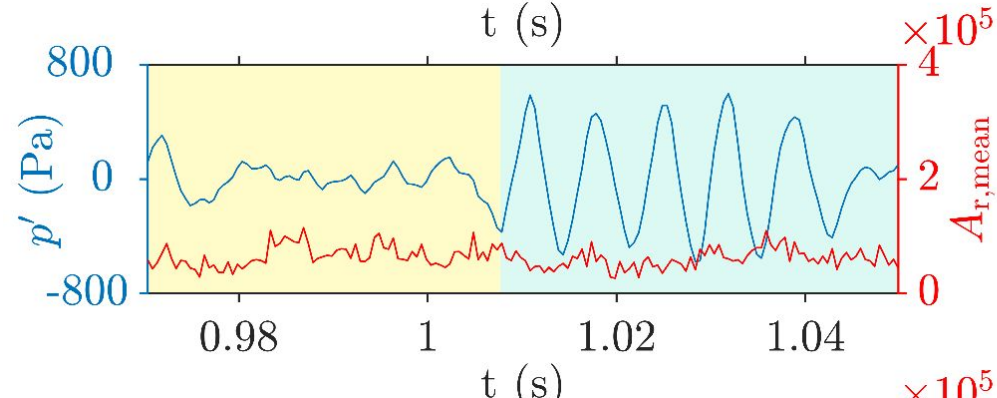
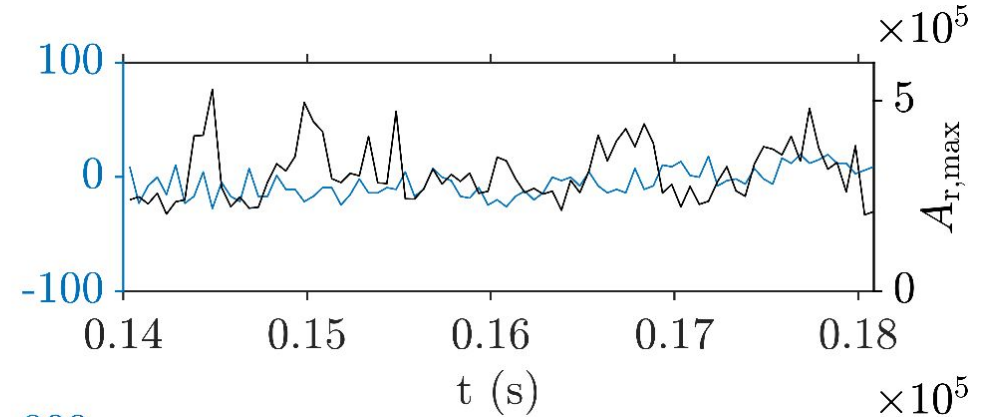
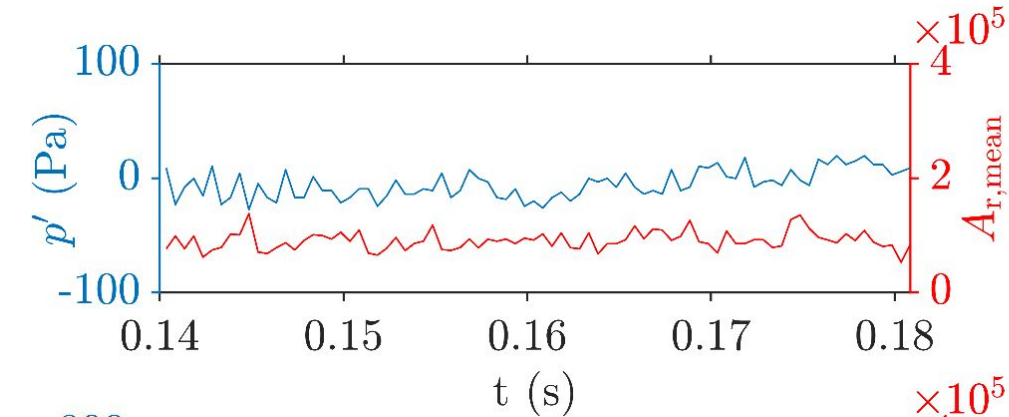
Intermittency - maximum inter-community interactions captures the periodicity of acoustics during the periodic epoch



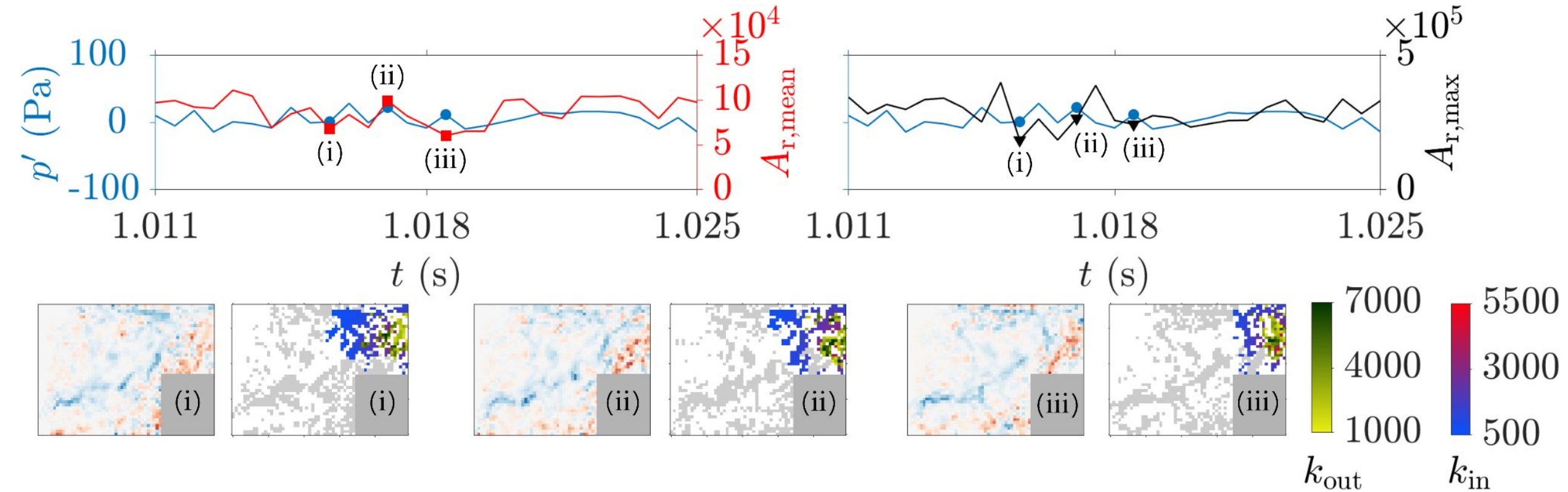
Thermoacoustic instability - network measures are periodic



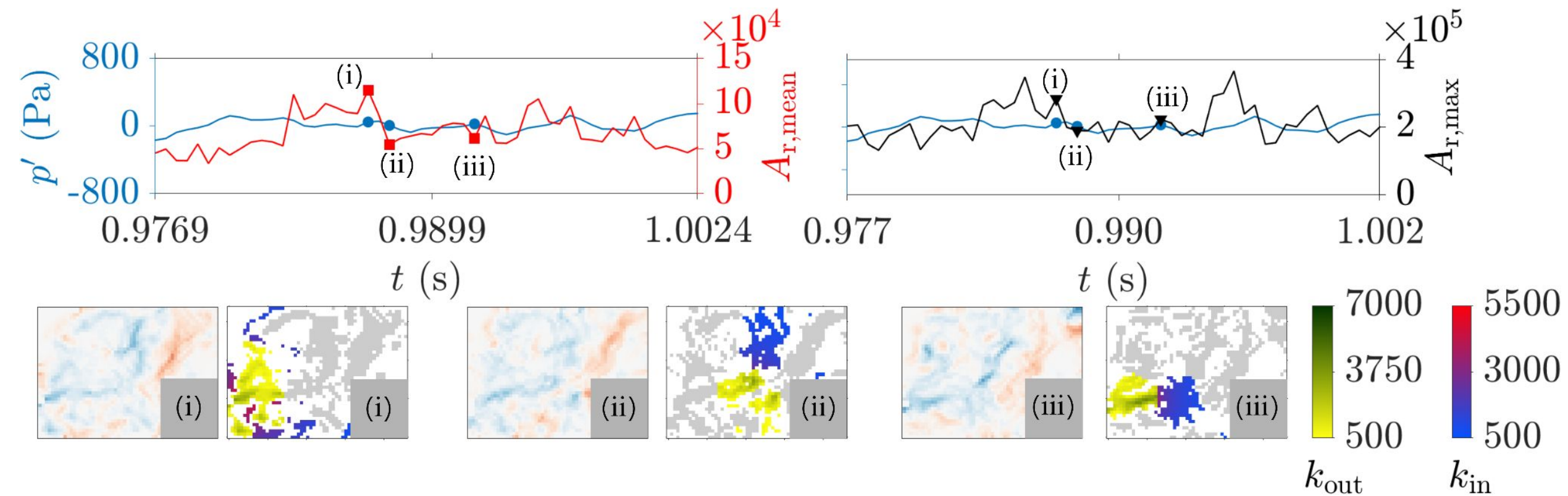
Thermoacoustic instability - significant delayed correlation between acoustics and network measures



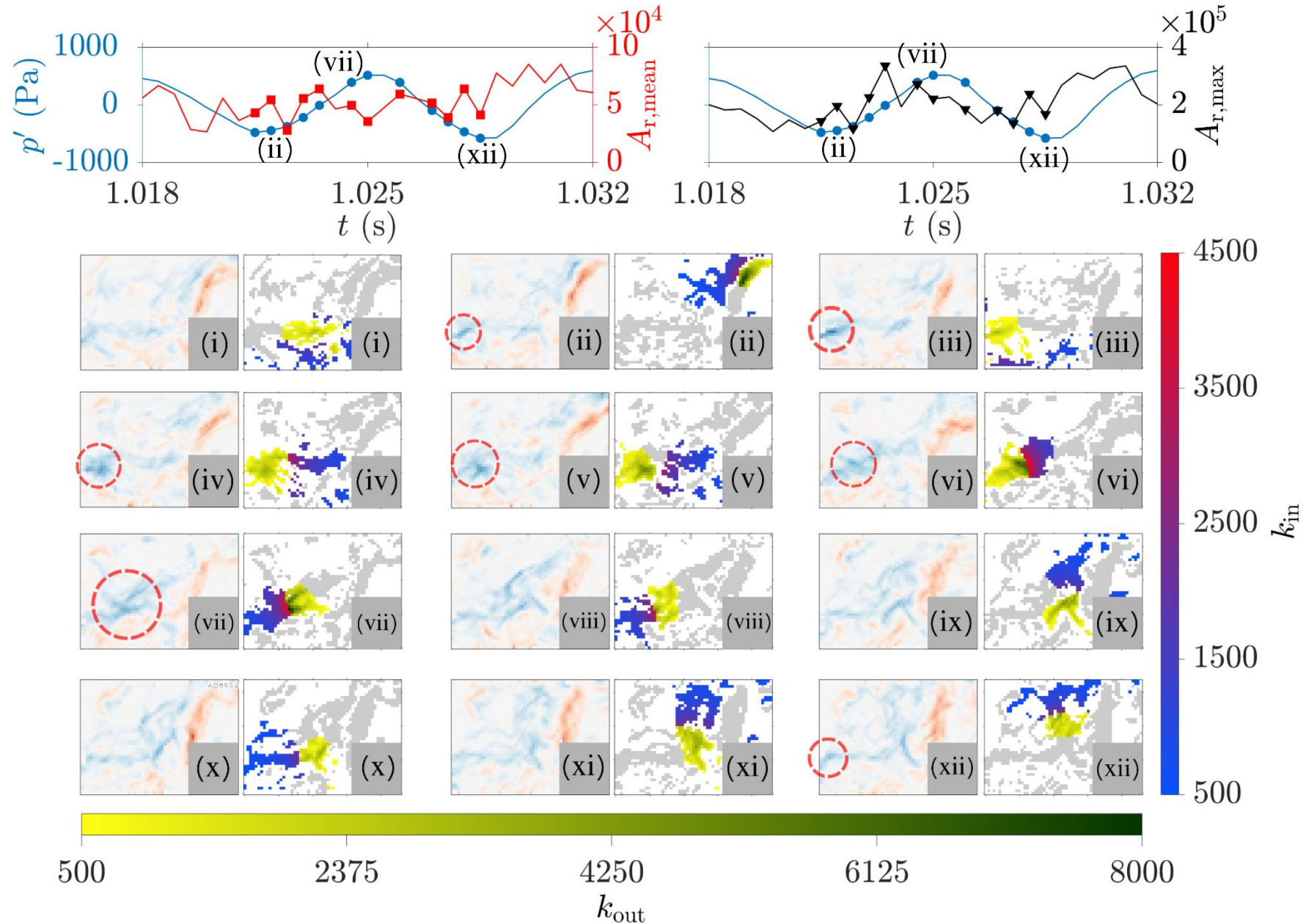
Combustion noise - significant vortex shedding from the upstream tip of bluff body



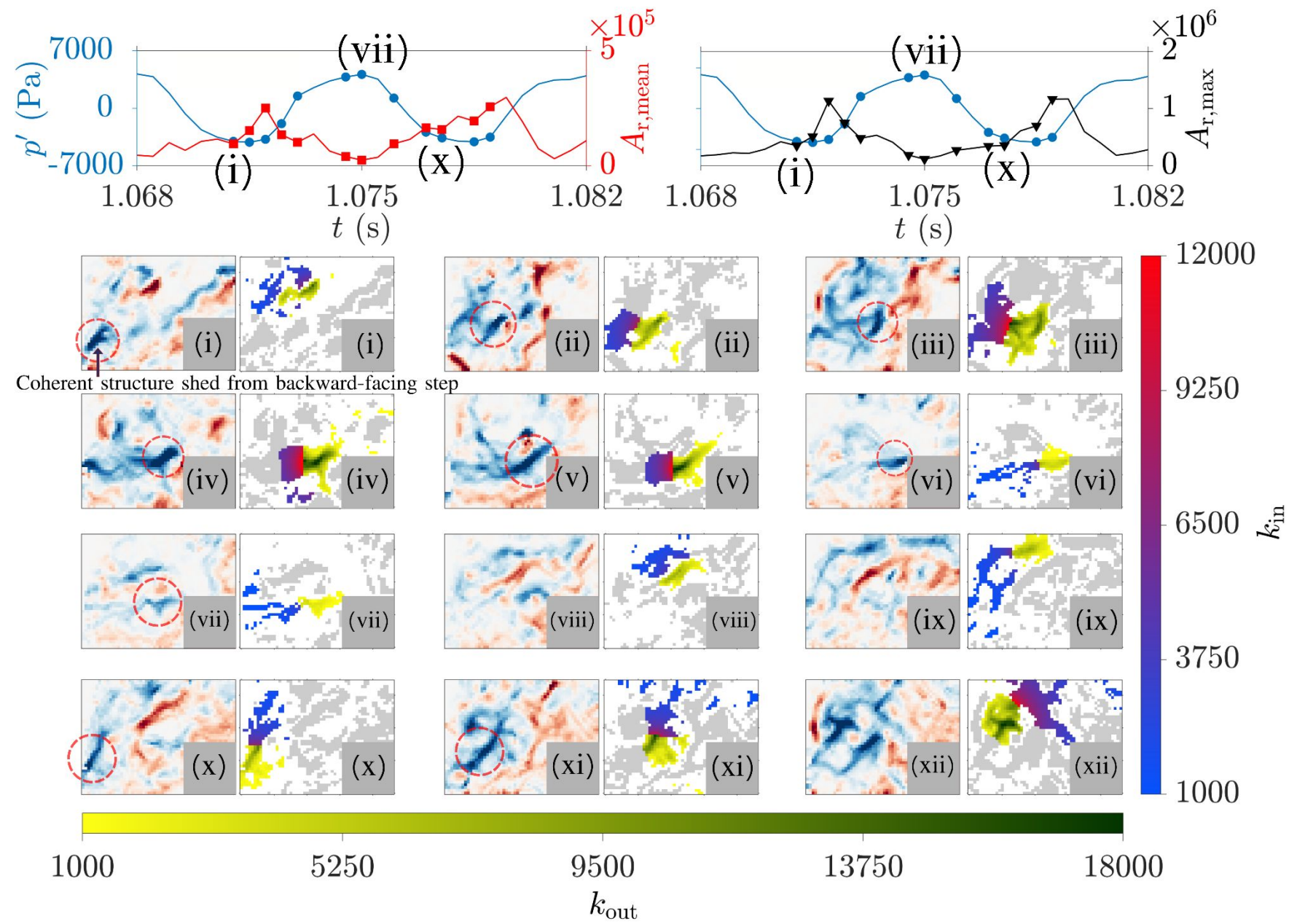
Aperiodic epoch of intermittency - aperiodic temporal variation of network measures



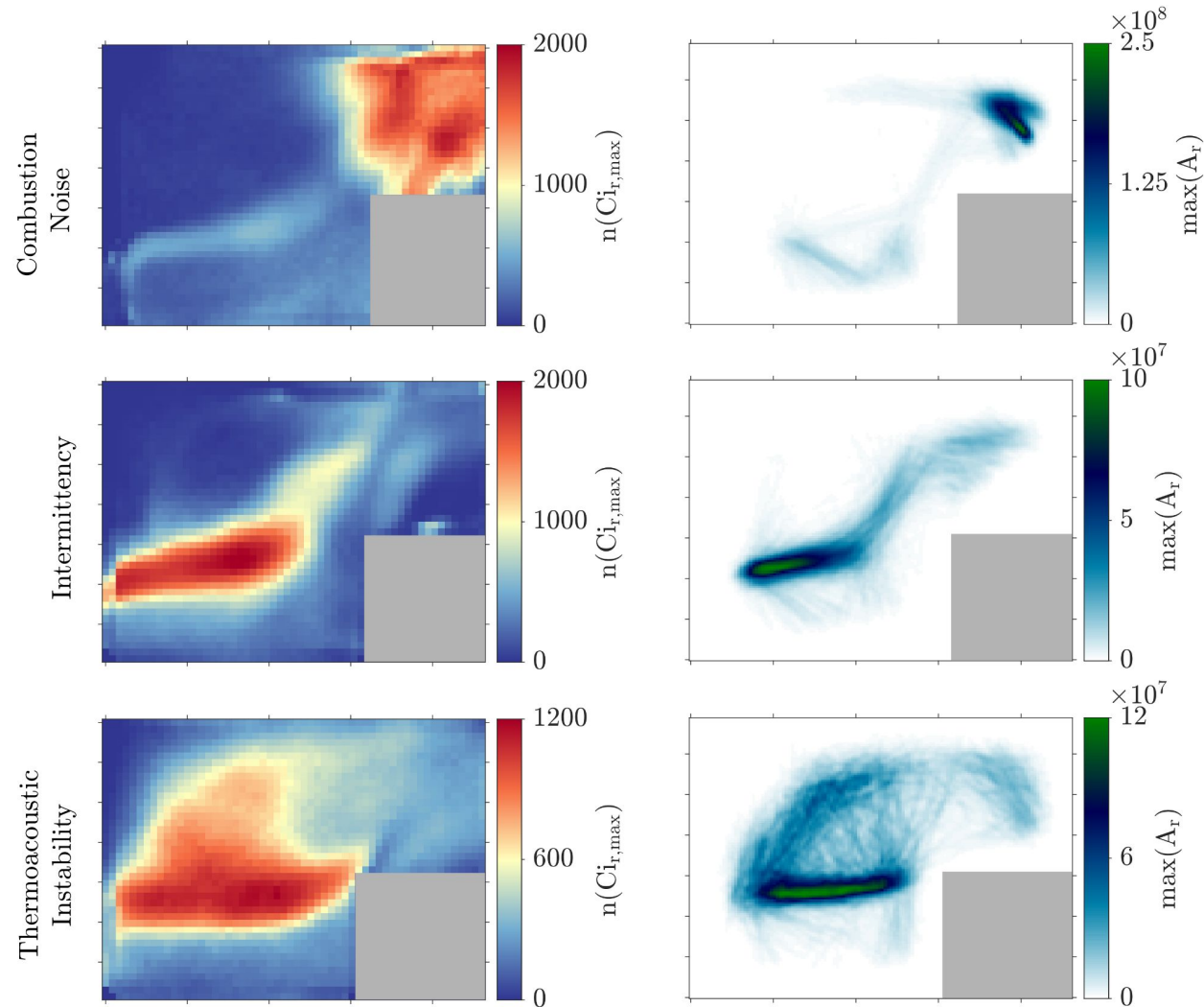
Periodic epoch of intermittency - periodic emergence of vortices



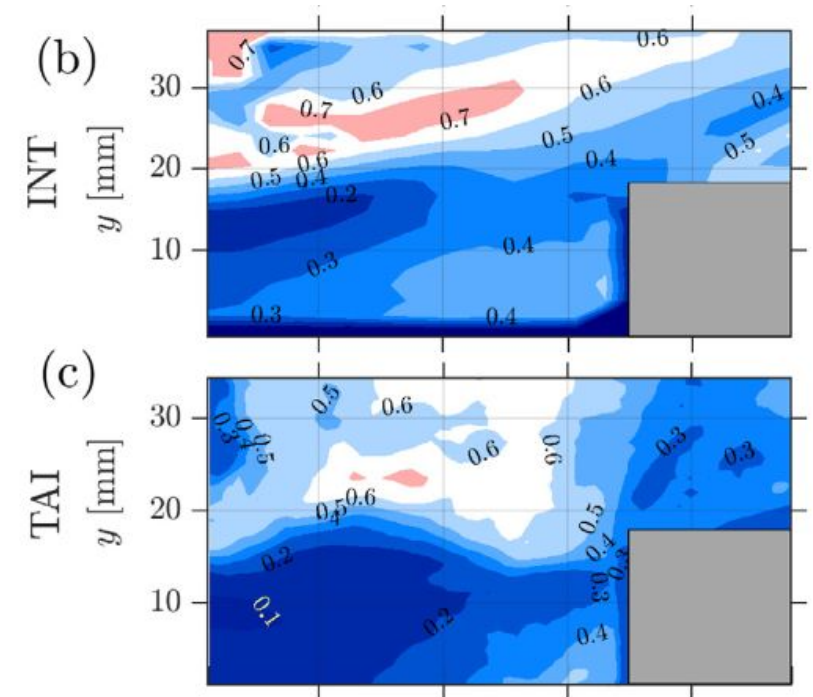
Thermoacoustic instability - periodic dynamics of network measures



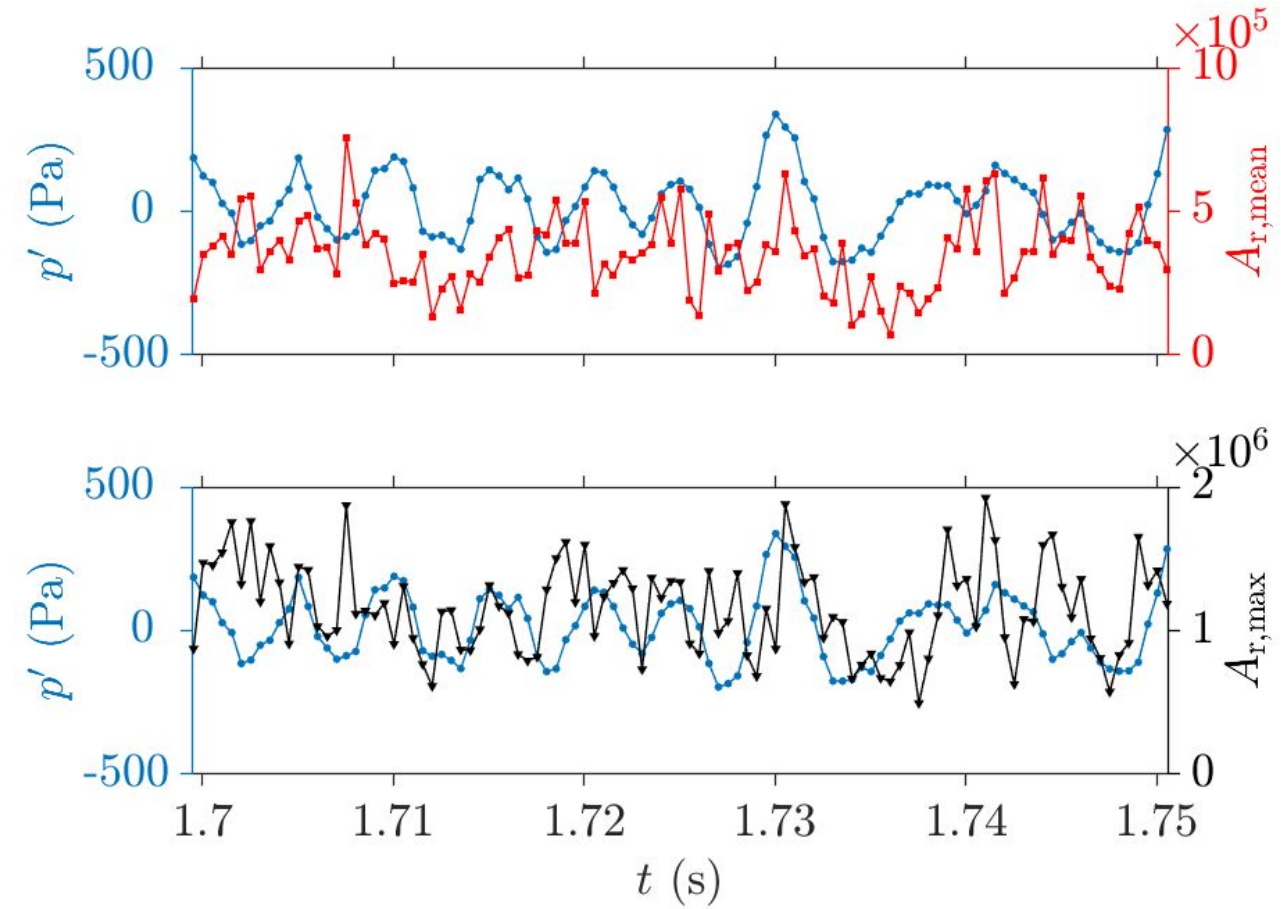
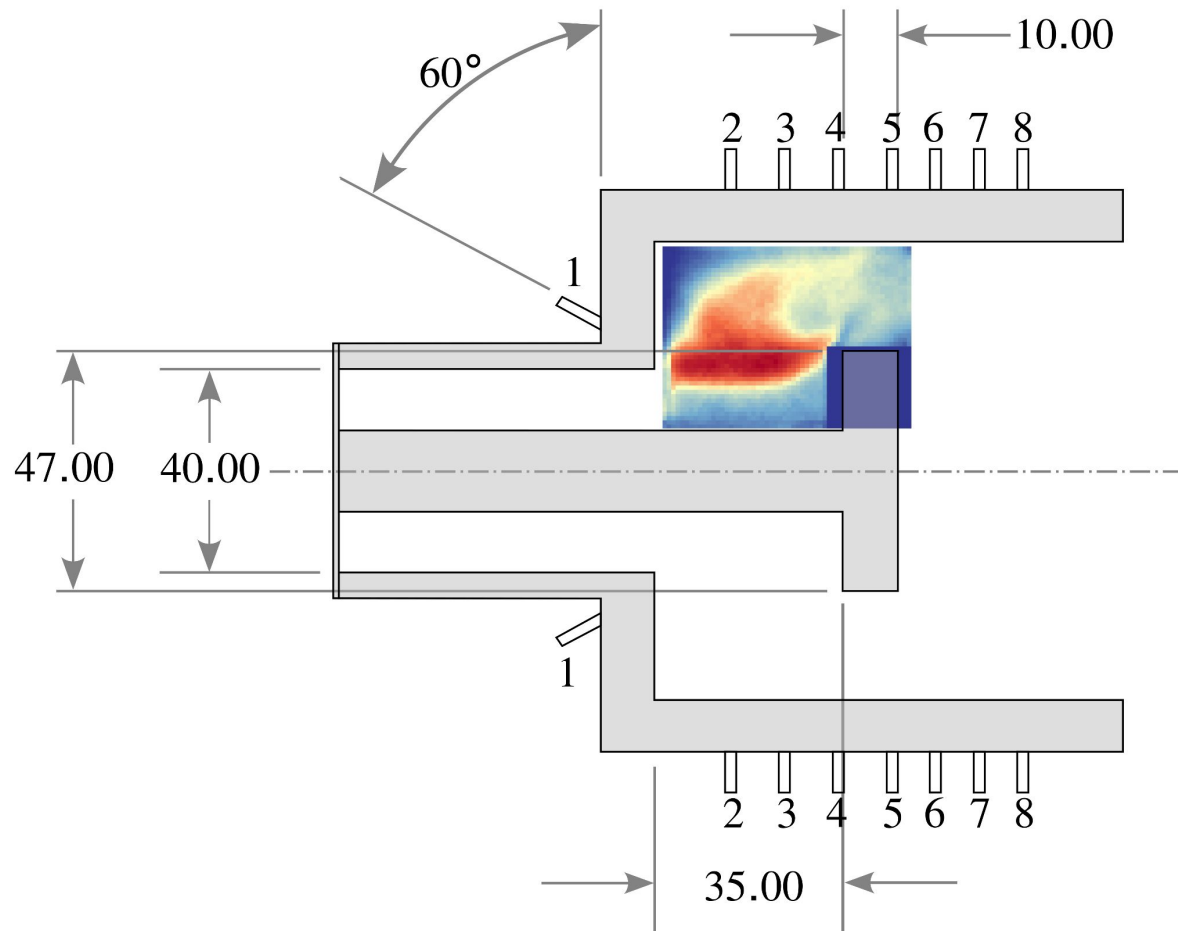
Critical regions - probability distribution of communities with largest inter-community interactions



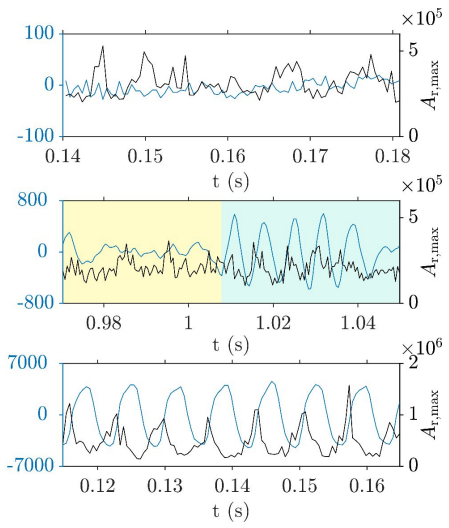
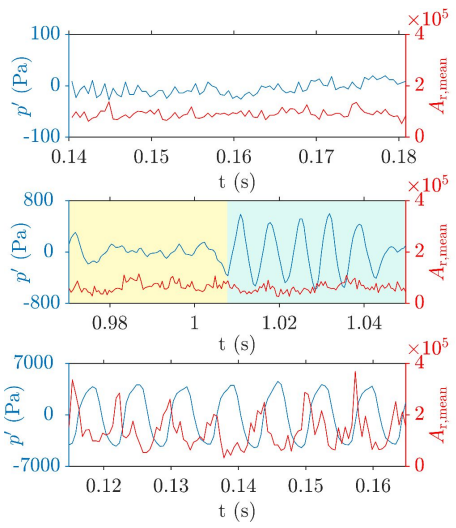
Hurst exponent (Roy et al., Combust. Flame, 2021)



Smart passive control - mitigation of thermoacoustic instability via air microjets

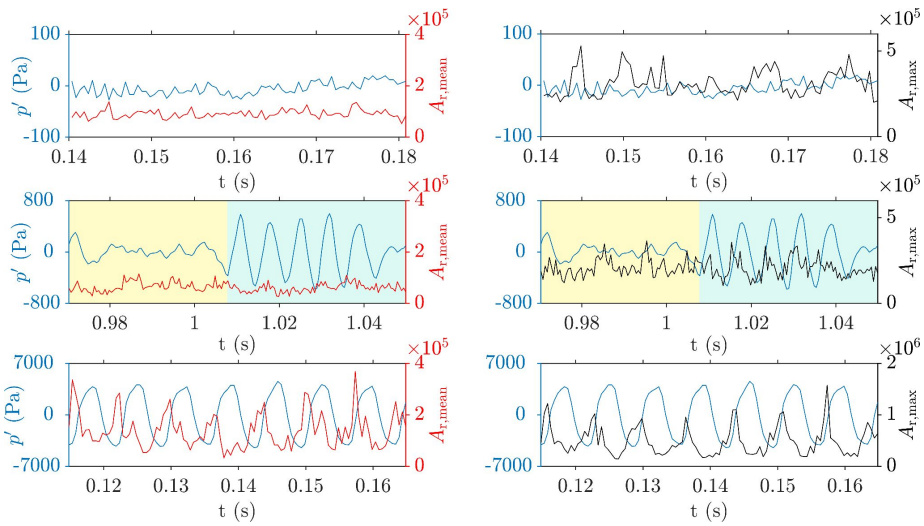


Summary

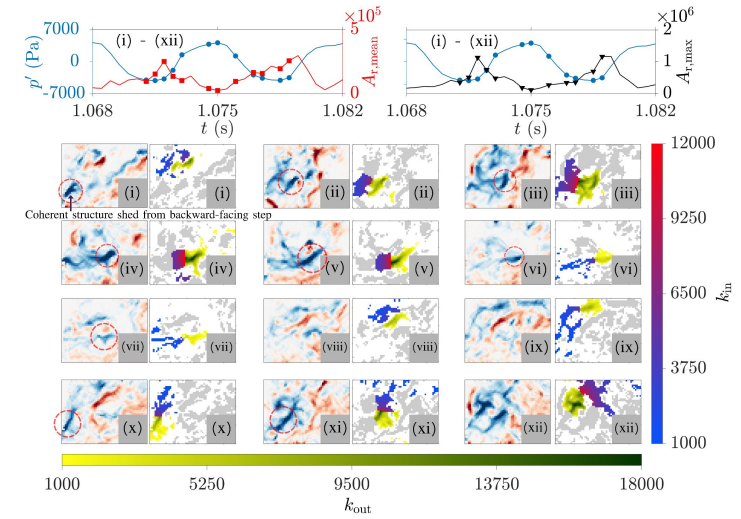


Interplay between
vortical
interactions and
acoustics
quantified via
vortical network
measures

Summary

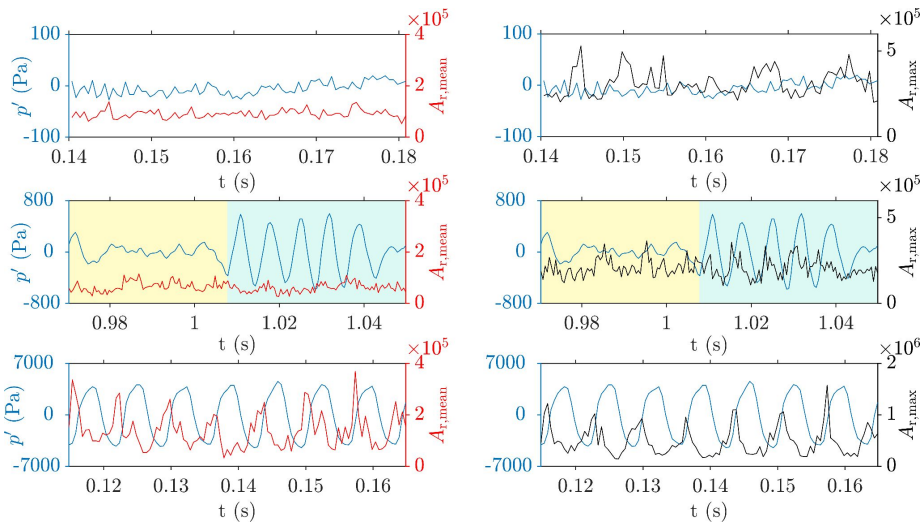


Interplay between
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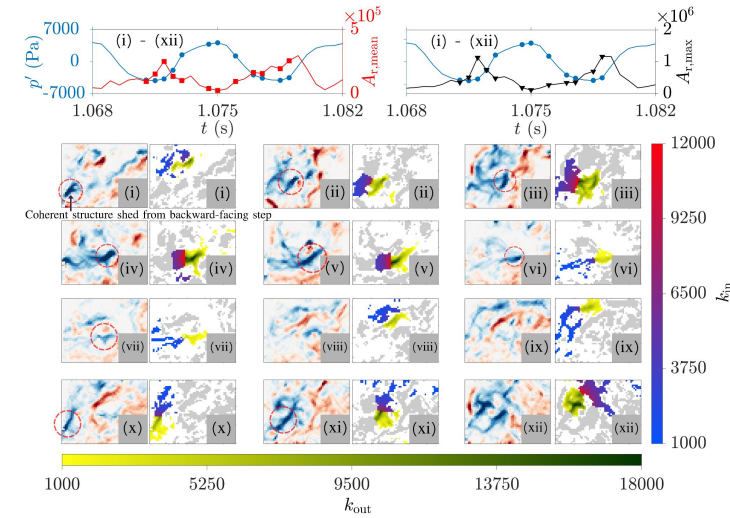


Temporal evolution
of influential
vortical
communities in the
reaction field of
the combustor

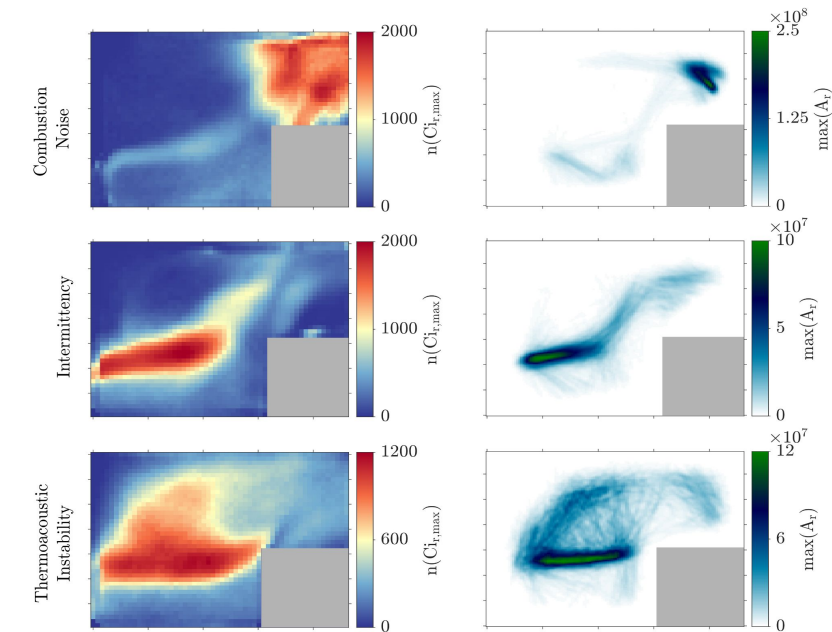
Summary



Interplay between vortical interactions and acoustics quantified via vortical network measures

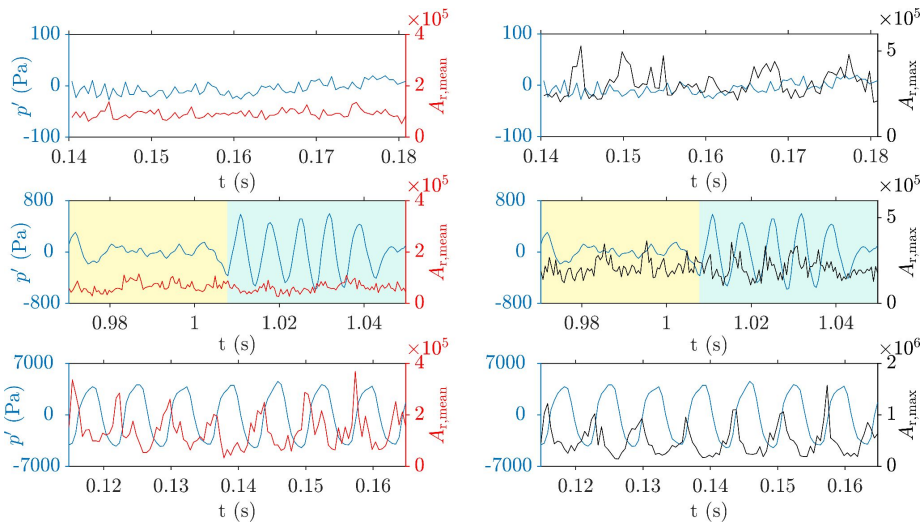


Temporal evolution of influential vortical communities in the reaction field of the combustor

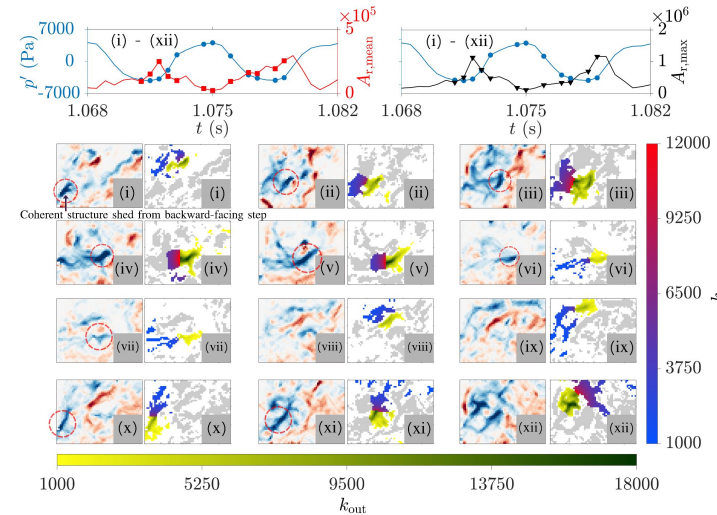


Spatial probability of locating most influential communities during the state of thermoacoustic instability

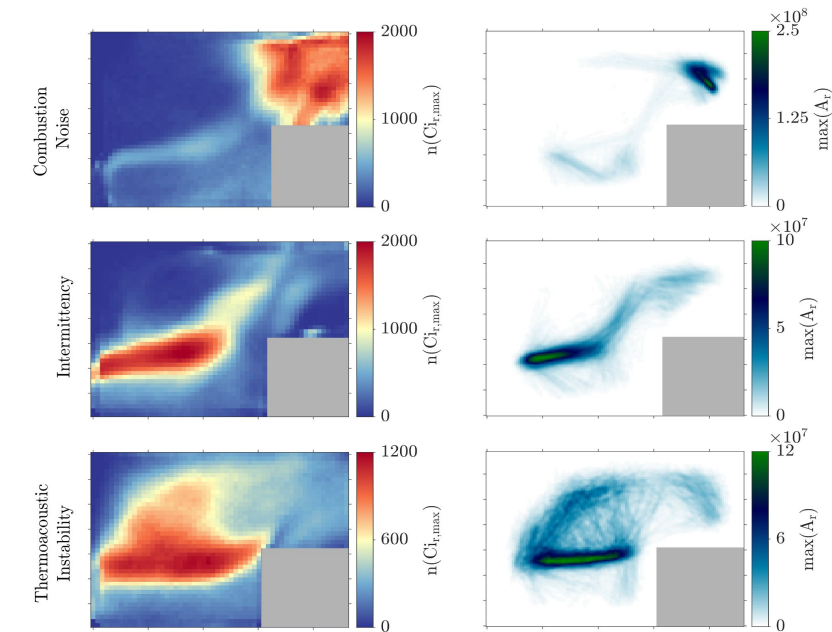
Summary



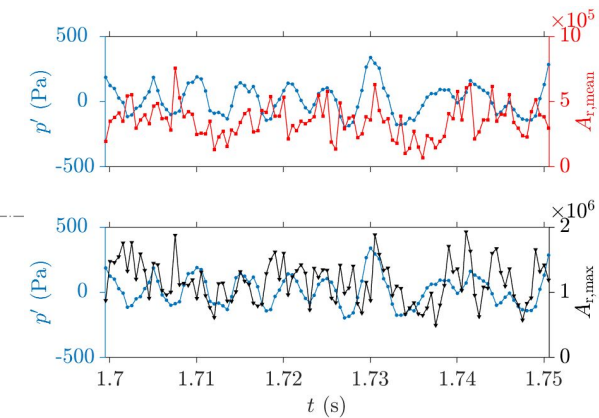
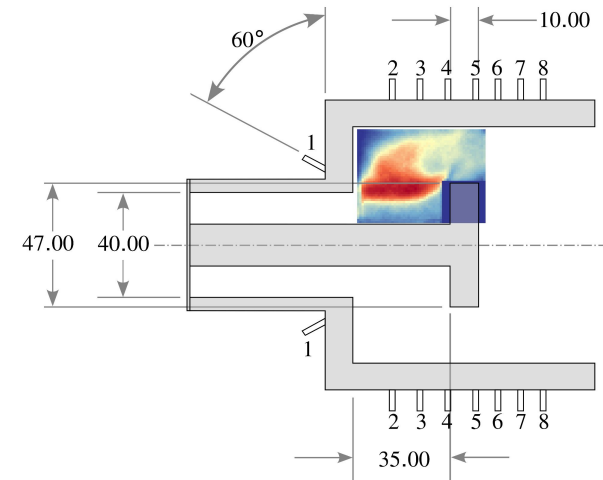
Interplay between vortical interactions and acoustics quantified via vortical network measures



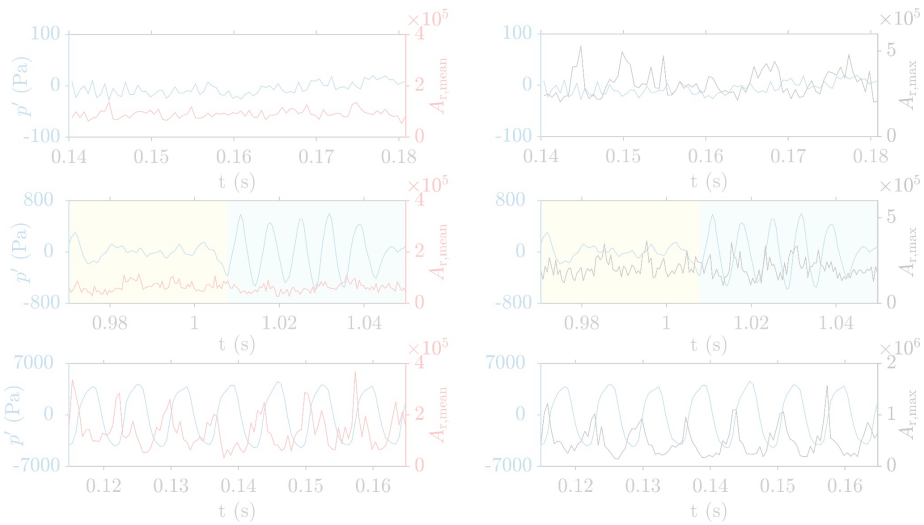
Temporal evolution of influential vortical communities in the reaction field of the combustor



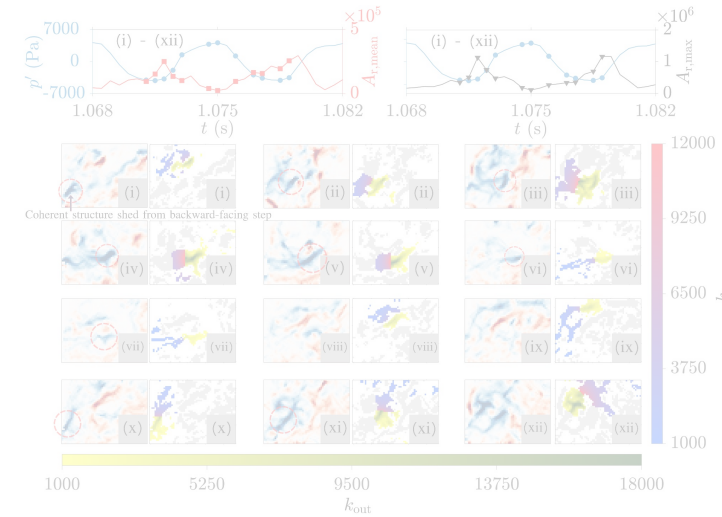
Spatial probability of locating most influential communities during the state of thermoacoustic instability



Summary

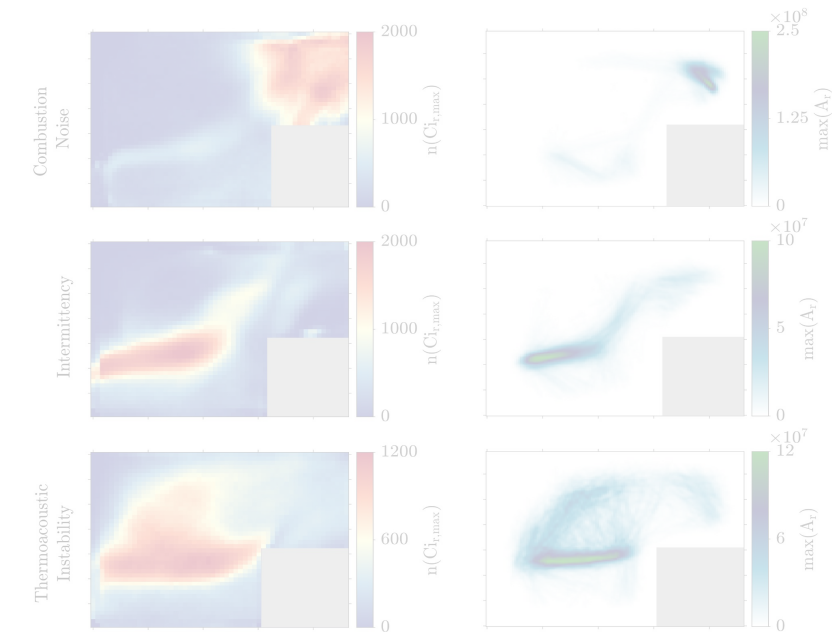


Interplay between vortical interactions and acoustics quantified via vortical network measures



Temporal evolution of influential vortical communities in the reaction field of the combustor

Thank you



Spatial probability of locating most influential communities during the state of thermoacoustic instability

