



**IEEE PES ISGT  
Europe 2024  
Conference**  
Dubrovnik, Croatia  
October 14th - 17th

# How to design economic mechanisms for efficient operation of low-inertia power grids

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# 3 topics covered



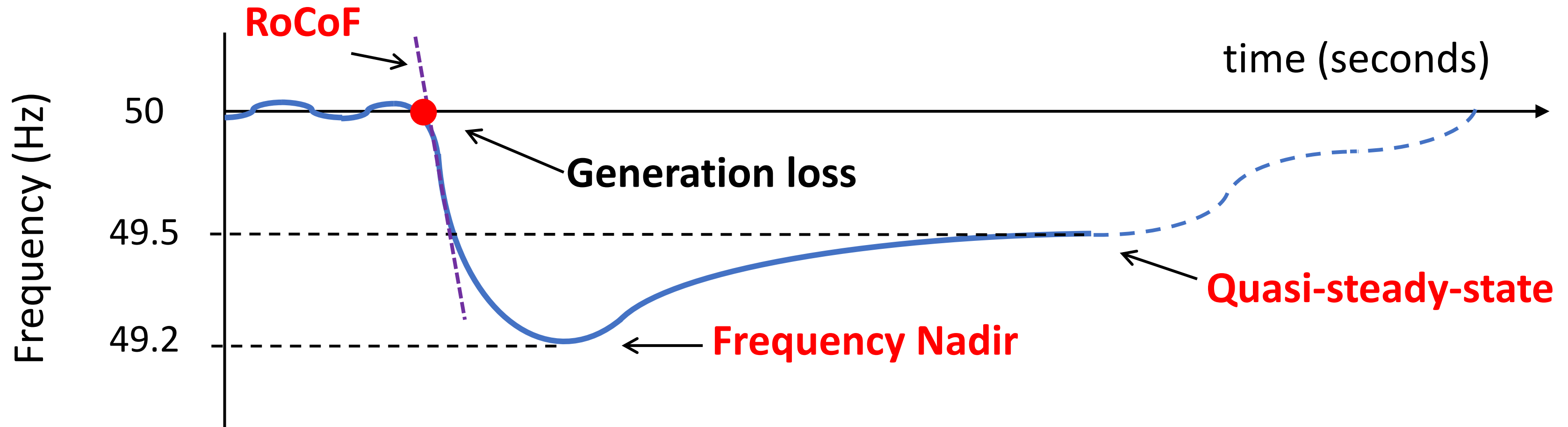
1. **Unlocking the support from DER** via risk-constrained optimization
2. From **low-level control** instructions to **system-level optimization** via data-driven methods
3. **Who should pay** for frequency-containment services?

## Paper:

C. O'Malley, L. Badesa et al., "Frequency Response from Aggregated V2G Chargers With Uncertain EV Connections," *IEEE Trans. on Power Systems*, 2023



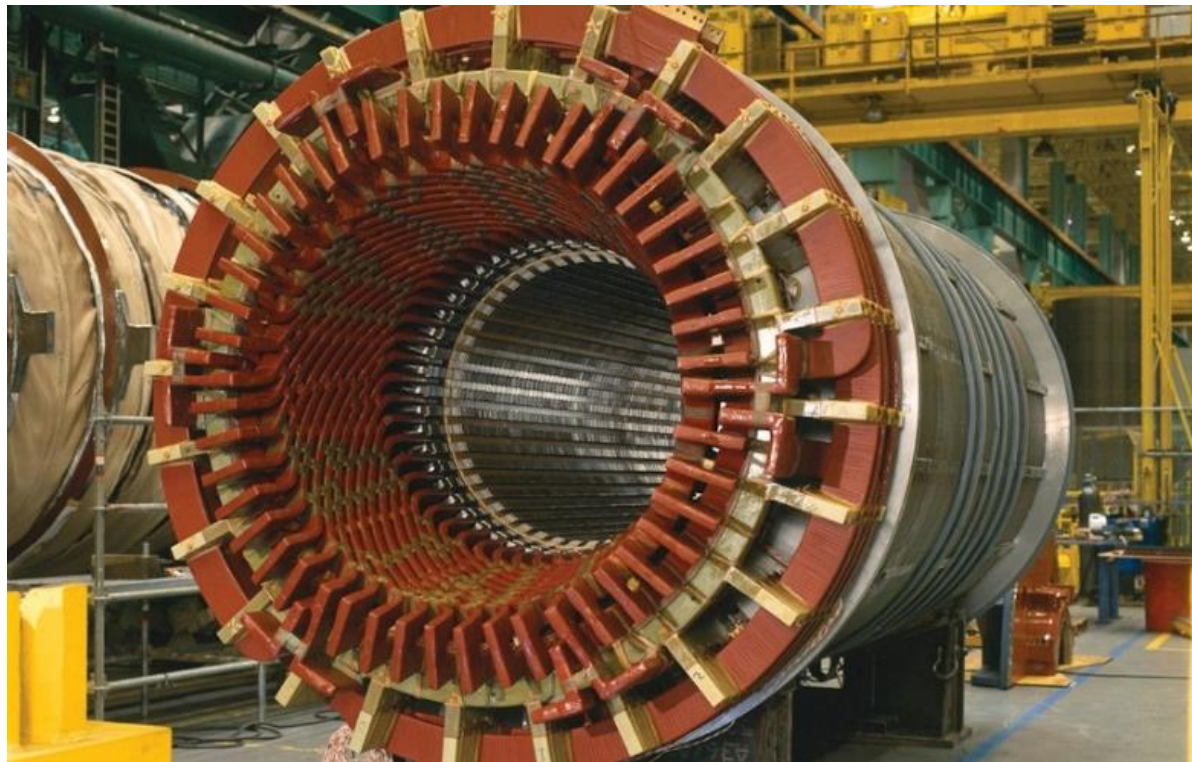
# Frequency stability



Key to keep frequency within safe limits to avoid demand disconnection!

# Lower inertia on the road to lower emissions

*Thermal generators  
(nuclear, gas, coal...):*



*Most renewables:  
**no inertia***



Decarbonization



The **risk of instability**  
has increased!

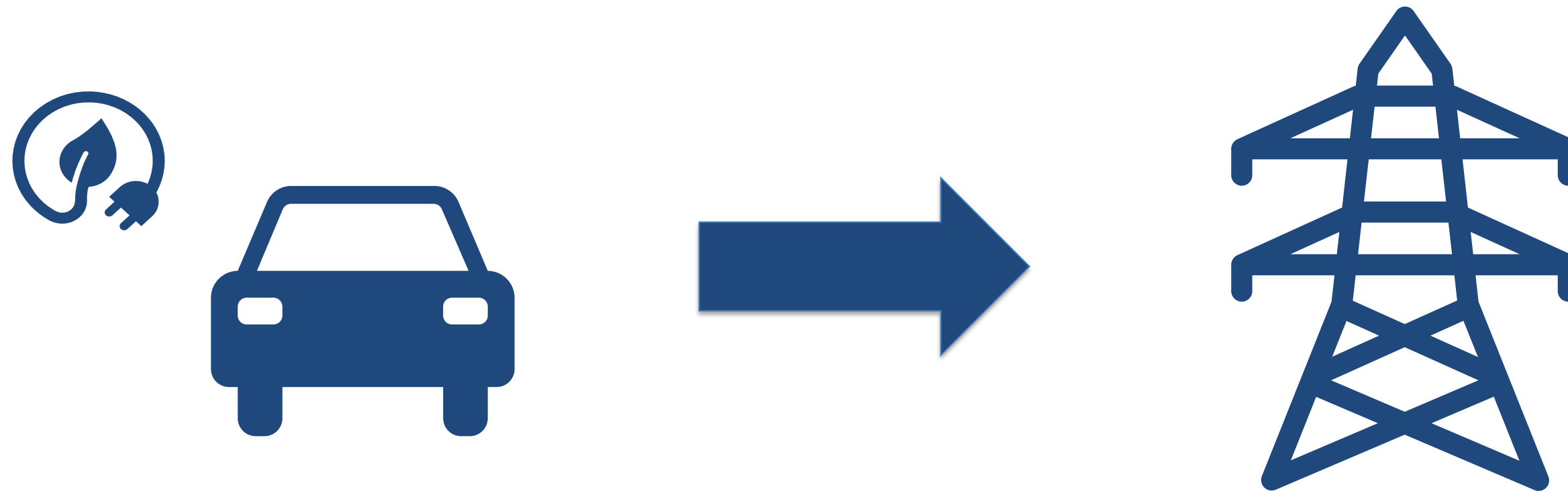


**Inertia stores kinetic energy:**

this energy gave us time to contain a sudden generation-demand imbalance

# Unlocking support from Distributed Energy Resources

- **DER could be very valuable** to support system stability, but they are **inherently uncertain**
- We focus on **Vehicle-to-Grid (V2G)**: the system operator cannot control when the EV owners plug in their vehicles



# Why is this important?

Now



Future

Stability through **gas plants**

- **Pros:** certain + reliable
- **Cons:** expensive + polluting

Stability services from **DER**

- **Pros:** abundant + **cheap**
- **Cons:** uncertain

# Stability conditions for optimization



What is the **value of V2G** as a countermeasure to low inertia?

Mapping the stability boundary



*Described by  
**differential equations**  
(timescale of sub-seconds)*

*Based on  
**algebraic equations**  
(timescale of min/hours)*



# Uncertainty within the stability conditions



We propose the use of **chance constraints**:

$$\text{Probability of complying with stability limit} \geq 1 - \epsilon$$

↑  
Uncertainty in  
**EV plug-in** times



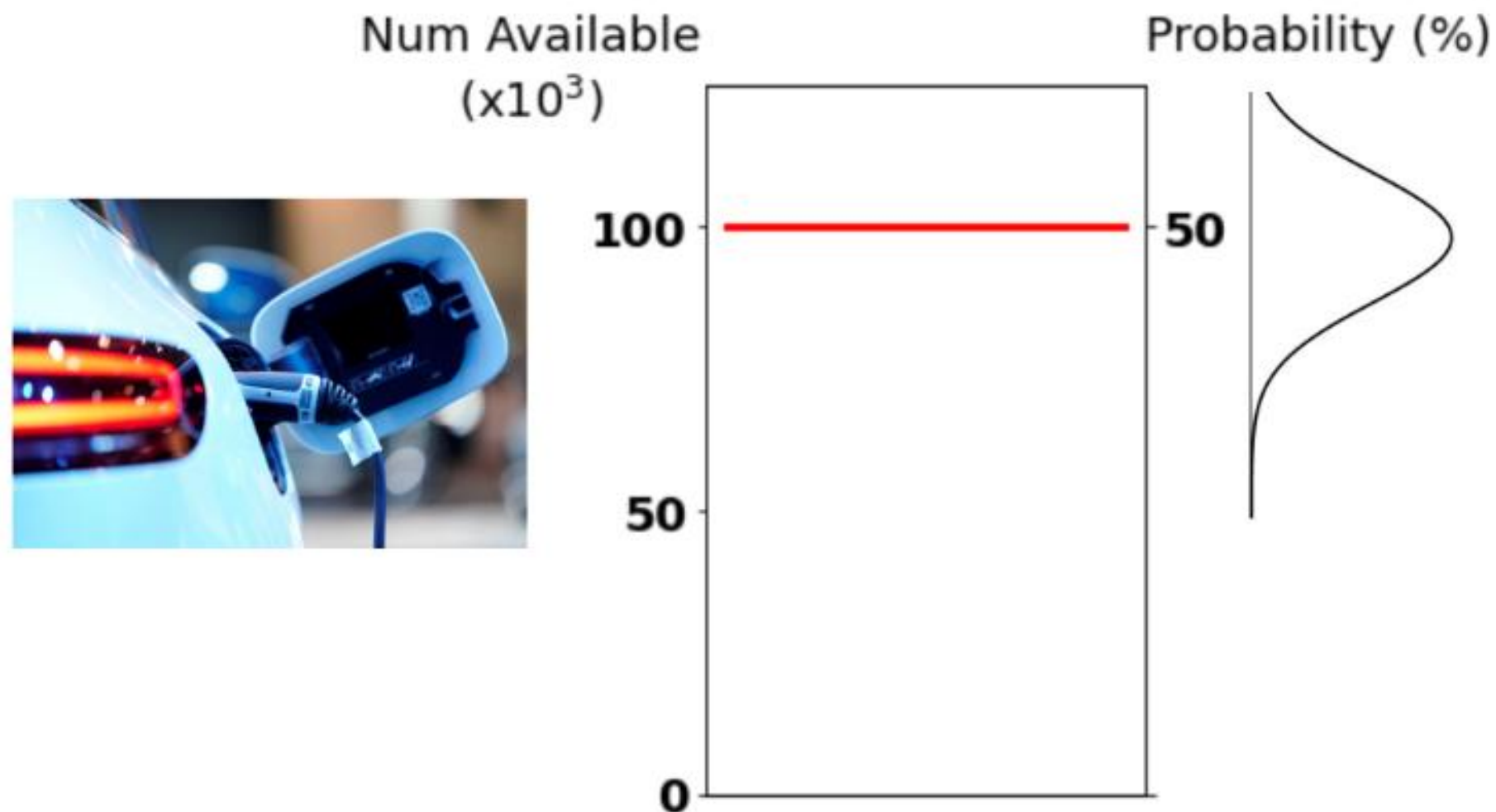
↑  
**Risk** appetite  
(e.g., 1% chance of  
under-delivery)





# What do we mean by risk?

## Probabilistic forecast for EV connections



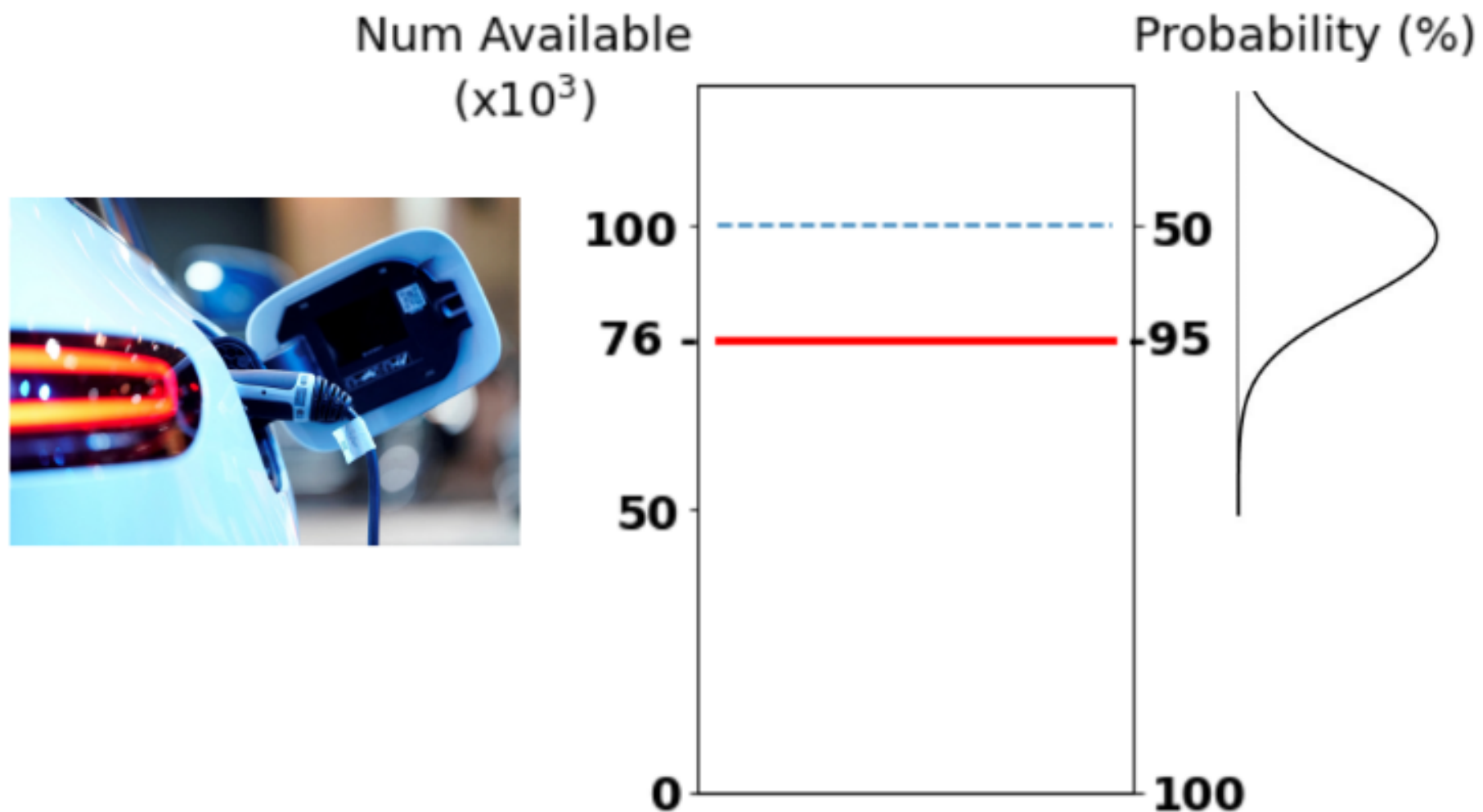
## Naïve scheduling:

- Use **deterministic forecast** (mean)
- Count on 100k EVs
- **50% chance** of having less than expected

**Risky!**

# What do we mean by risk?

## Probabilistic forecast for EV connections

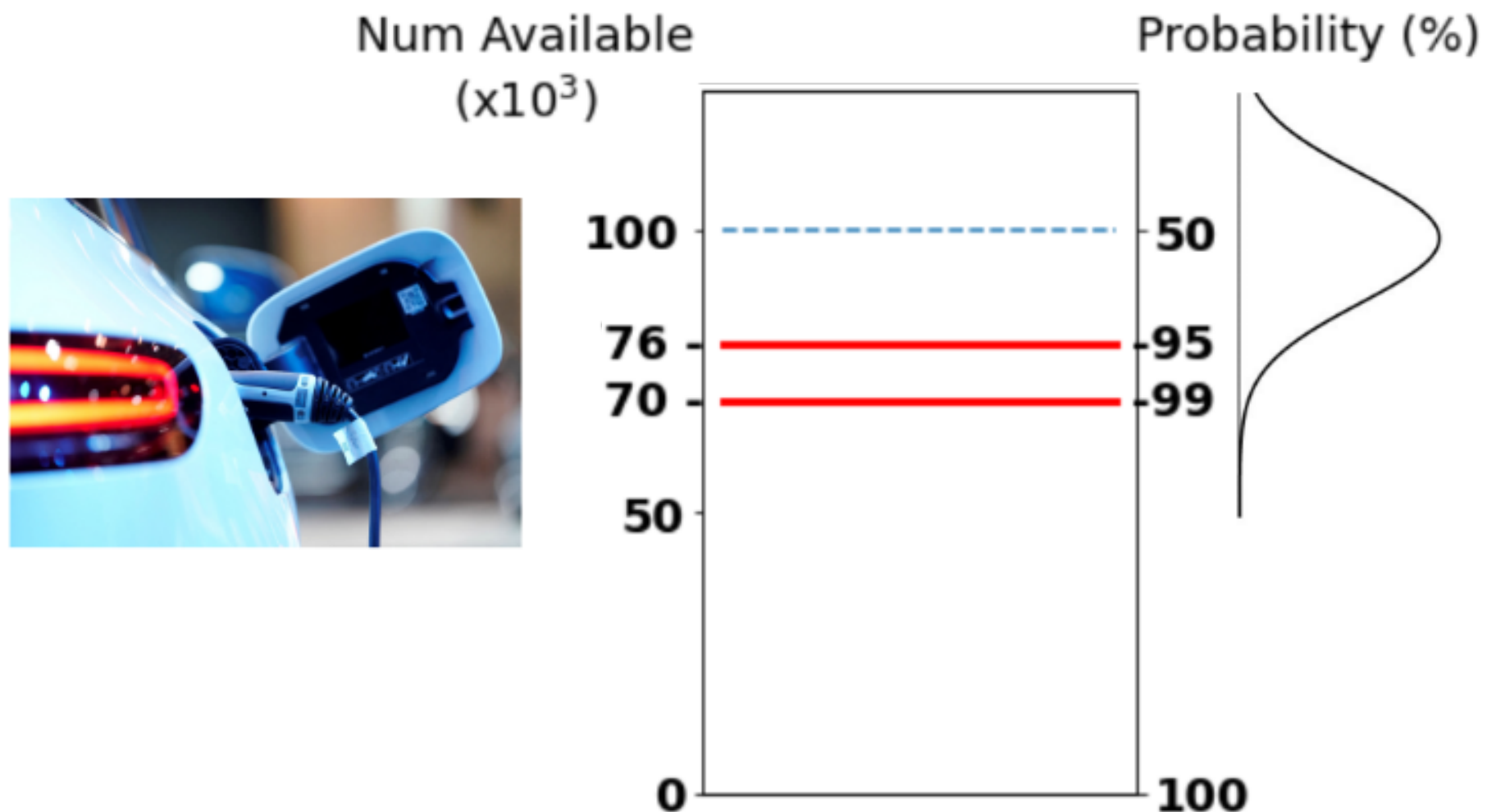


## Risk-limited scheduling:

- Specify **risk tolerance** (e.g., 5%)
- Count on **76k EVs**

# What do we mean by risk?

## Probabilistic forecast for EV connections



## Risk-limited scheduling:

- Specify **risk tolerance** (e.g., **1%**)
- Count on **70k EVs**

**Lower risk** implies less support from EVs considered

# Steps for deducing chance constraints

1. Model system frequency via **single-machine swing equation**:

$$\frac{2H}{f_0} \frac{d\Delta f}{dt} = R^{EV}(t) + R^{ND}(t) + R^G(t) - PL_{max}$$

2. **Solve swing equation** to obtain RoCoF and nadir **constraints**:

$$\mathbb{P} \left[ \left( \frac{H}{f_0} - \frac{(R^{ND} + R^{EV}) \cdot T_1}{4\Delta f_{max}} \right) \frac{R^G}{T_2} \geq \left( \frac{PL_{max} - (R^{ND} + R^{EV})}{2\sqrt{\Delta f_{max}}} \right)^2 \right] \geq 1 - \epsilon$$

3. Use a **convex reformulation** for the non-convex chance constraints

# Convexification of chance constraint



Several options for the **convex reformulation**:

The **more information** available in the forecast,  
the **less conservative** the reformulation:

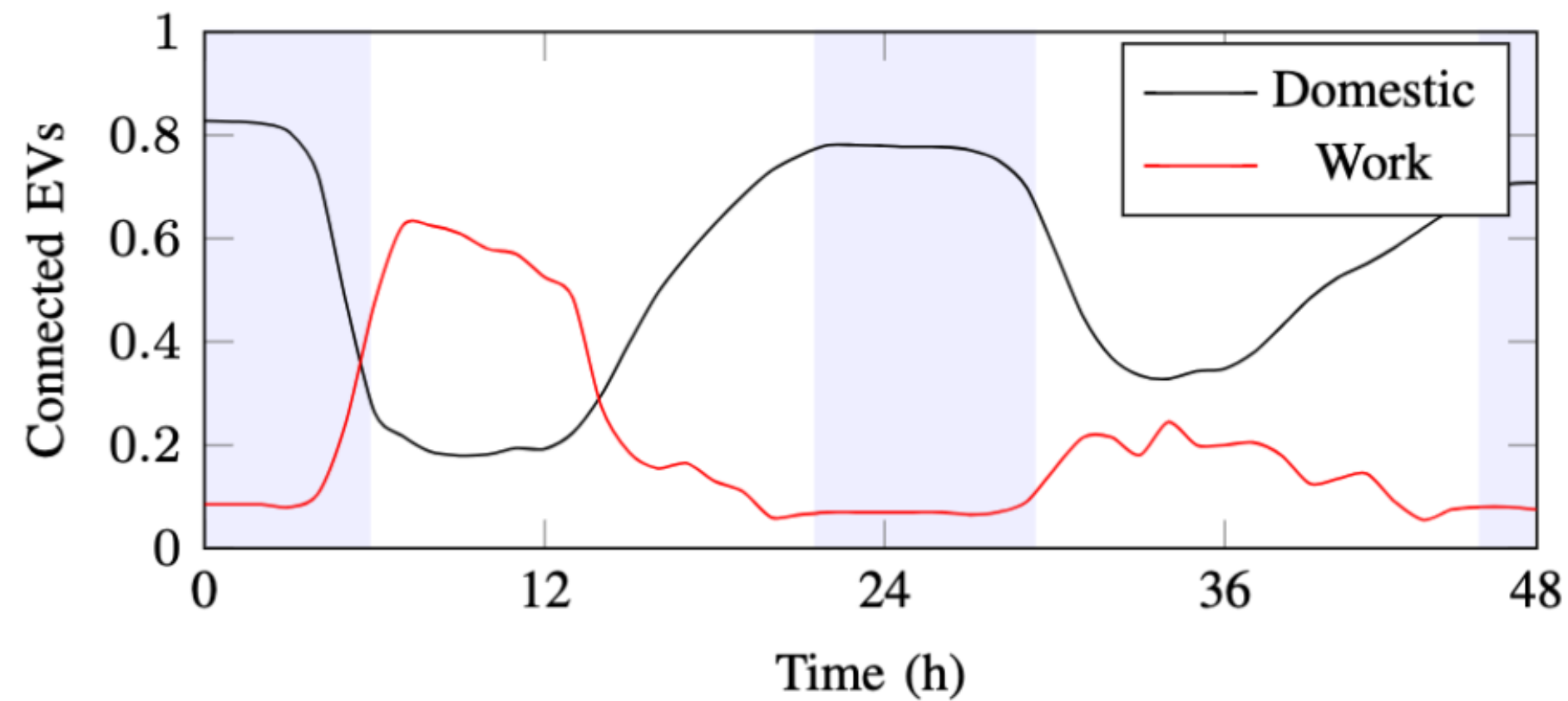
- **Gaussian** uncertainty?
- **Unimodal** distribution? (single peak)
- Only mean and variance known?
- **Distributionally-robust** formulation (most conservative)

# Results for Great Britain

- **Frequency-secured UC** run for a full year in 2030
- Two **EV fleets** considered:
  - **'Domestic V2G'**: 85,000 units, 10 kW chargers
  - **'Work V2G'**: 15,000 units, 20 kW chargers
- **Risk** of under-delivery set at **1%**
  - Does **not mean** 1% risk of **violating security**: that risk is extremely small (largest *N-1* contingency needs to happen too)

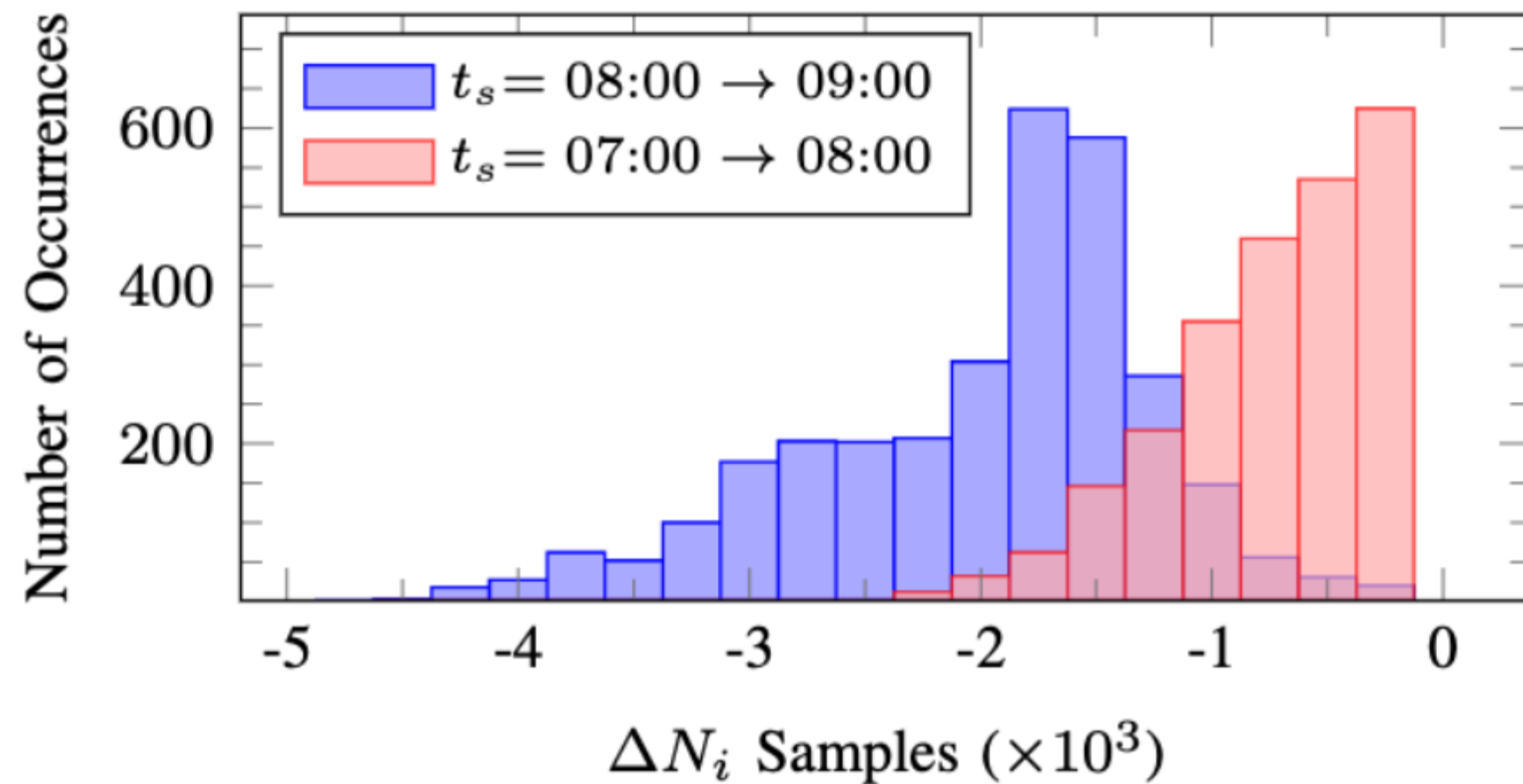
# EV connectivity forecasting and data analysis

Data from UK Department of Transport, 2017



# Test for ambiguity set

Domestic fleet disconnections  
on weekday



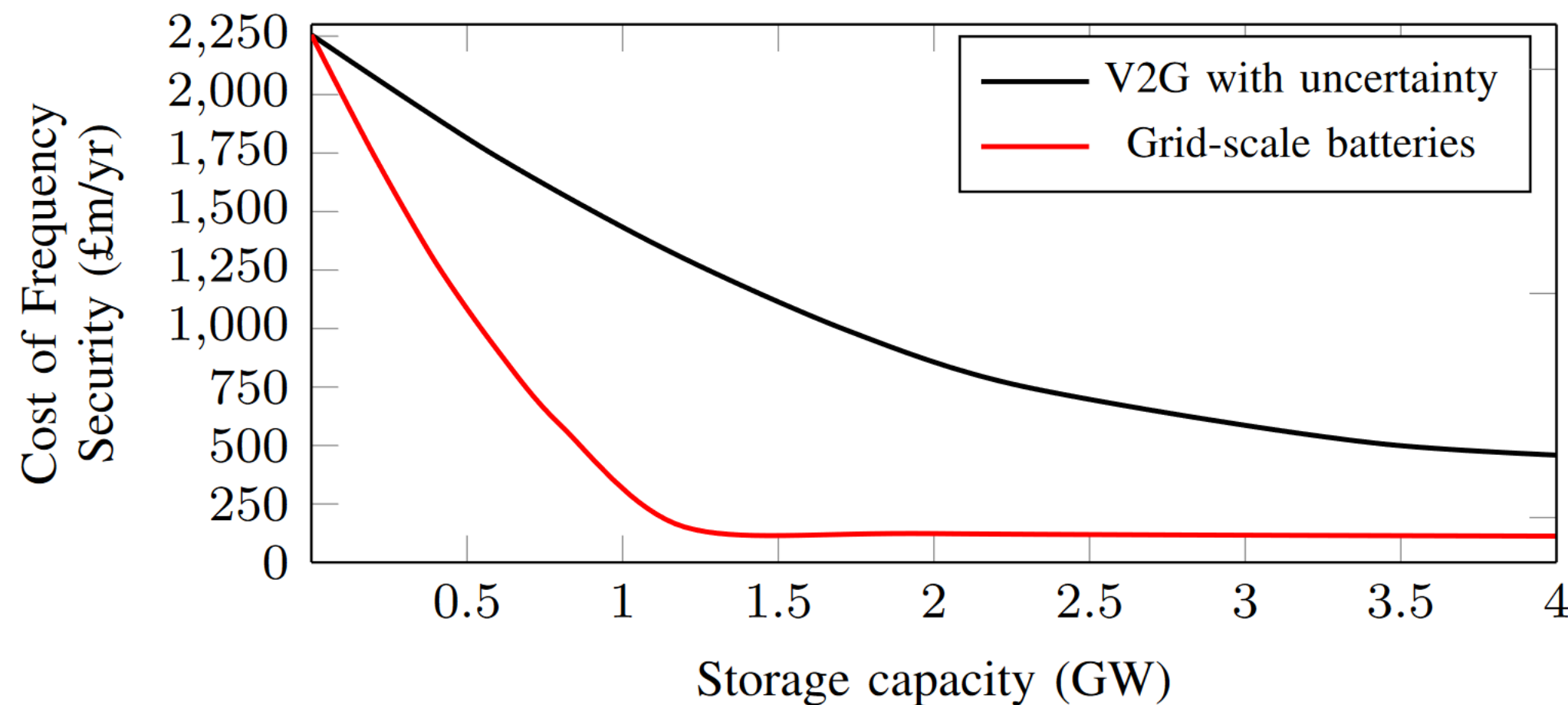
- **Not Gaussian**
- **Unimodal** with high confidence (from Shapiro-Wilk test)



# Results: comparison of V2G to BESS

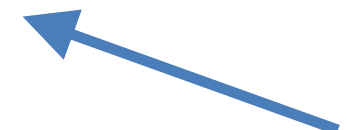
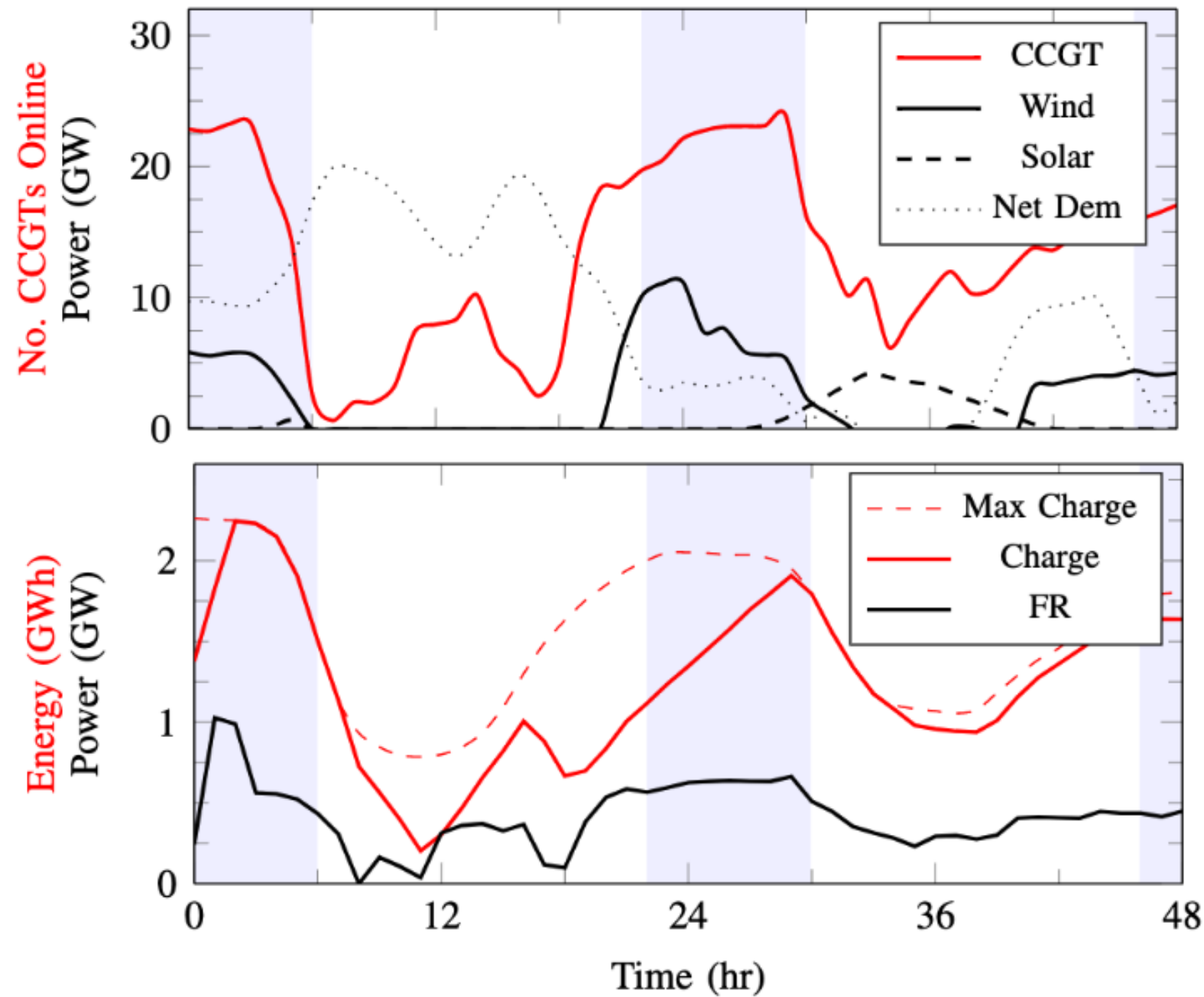
V2G capacity shown to be **one third as valuable** as stationary BESS

- EV chargers only have an **EV connected ~40% of the time**
- EV chargers are subject to **uncertainty**

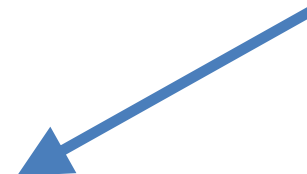


But EVs have **no additional investment cost!**

# Where does this value come from?



**Fewer CCGTs**  
are needed,



thanks to  
**frequency support**  
from **EVs**

# Thank you for your attention!

All papers and some related code on my website:

<https://badber.github.io/>