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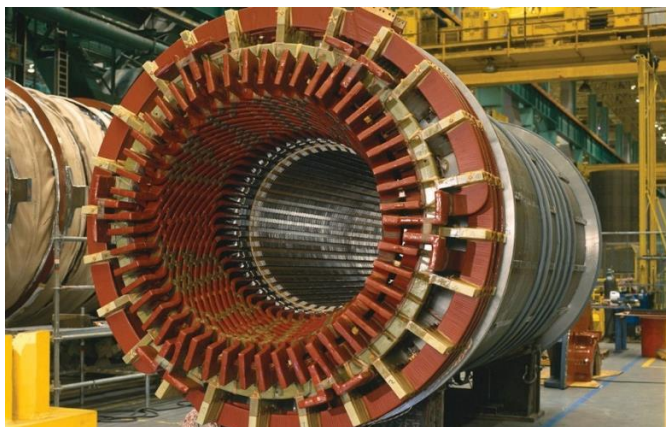
# Probabilistic Scheduling of Under-Frequency Load Shedding to Secure Credible Contingencies in Low Inertia Systems

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# Motivation: Lower inertia on the road to lower emissions

Thermal generators  
(nuclear, gas, coal...):



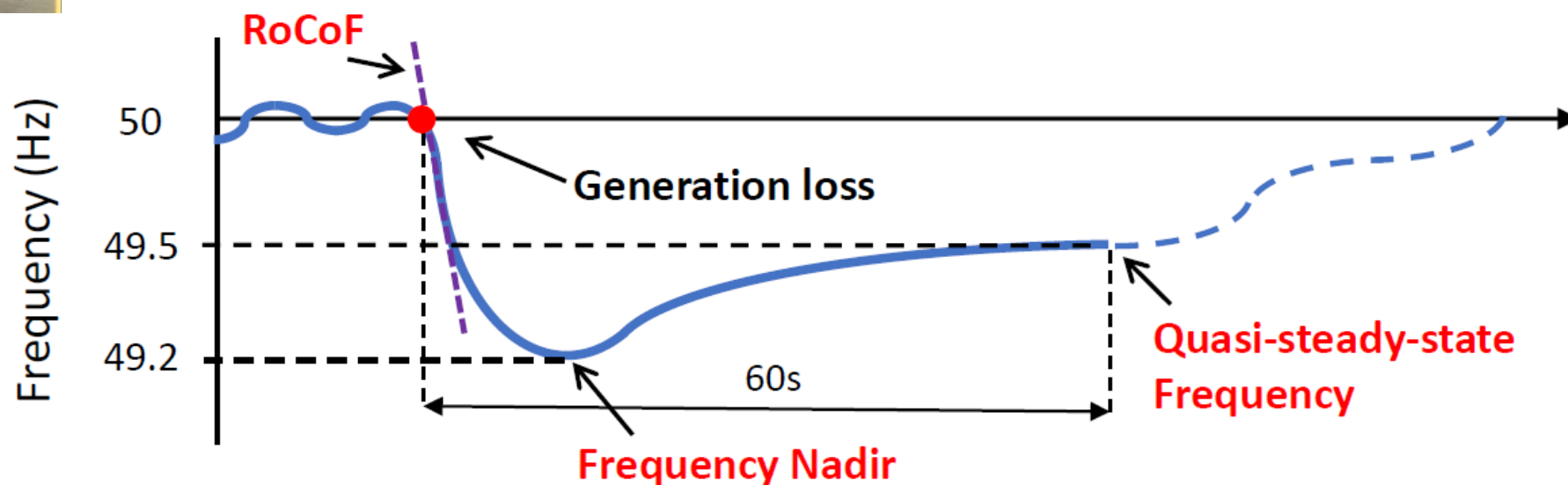
Most renewables:  
**no inertia**



Decarbonisation



Inertia is no longer a by-product of energy:  
It is now **more expensive**  
**to keep the system stable**





# Question we tried to answer:

How valuable is it to accept some UFLS after big outages?

## How to answer this question?

### Frequency-secured Unit Commitment

$$\min \sum_{g \in \mathcal{G}} c_g^{\text{nl}} \cdot y_g + c_g^{\text{m}} \cdot P_g \longrightarrow \text{Minimise fuel and commitment costs}$$

$$\text{s.t.} \quad \sum_{g \in \mathcal{G}} P_g + \sum_{\forall i} (P_i - P_i^{\text{curt}}) = P_D \longrightarrow \text{Load-balance constraint}$$

RoCoF constraint

Nadir constraint

q-s-s constraint

Frequency-security constraints

(plus other typical UC constraints)

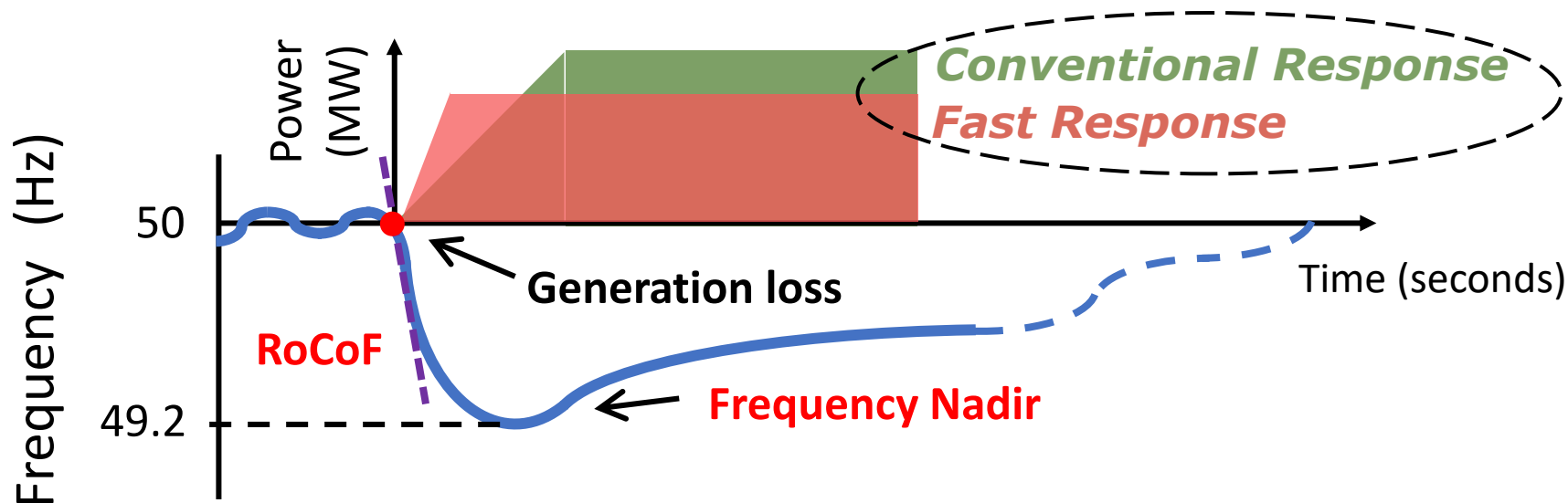
**Main contribution:**  
We incorporate **UFLS** as a decision variable within the frequency-security constraints

# Frequency-security constraints

## Solving the swing equation

$$\frac{2H}{f_0} \cdot \frac{d\Delta f(t)}{dt} = \text{FR}(t) - P_L + \text{UFLS}(t)$$

Loss of largest power infeed  
(N-1 reliability)



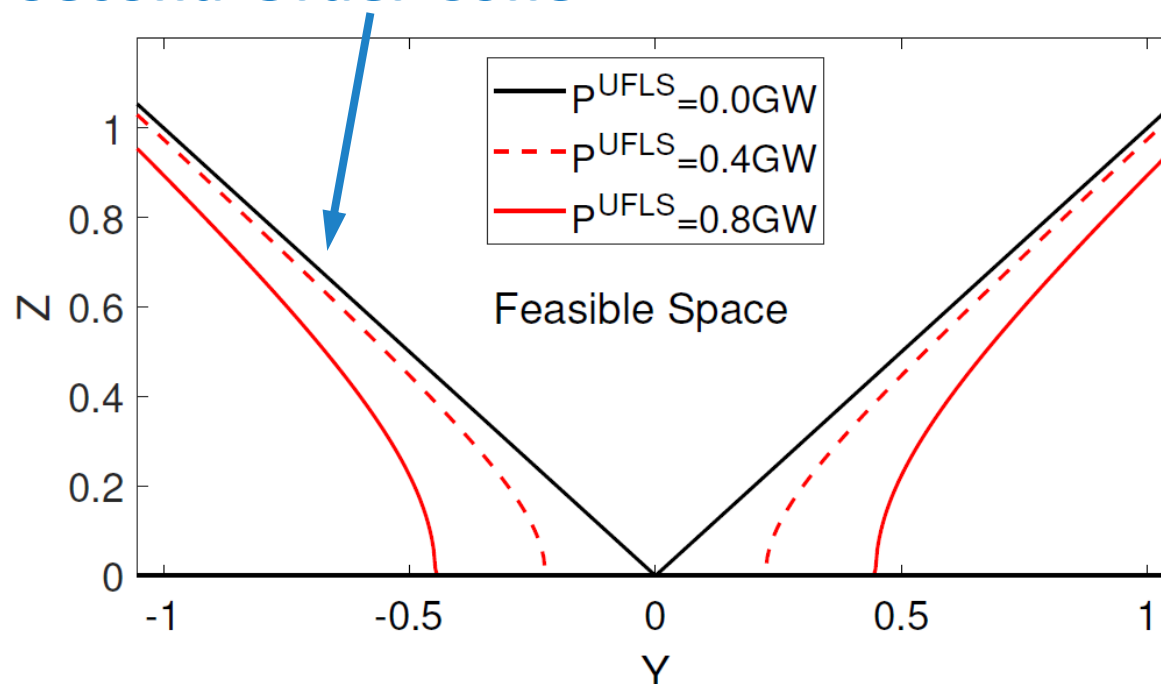
**Triggered** once frequency reaches the **UFLS activation threshold**

(this time depends on the system inertia and frequency response)

# Nadir constraint: non-convex due to UFLS

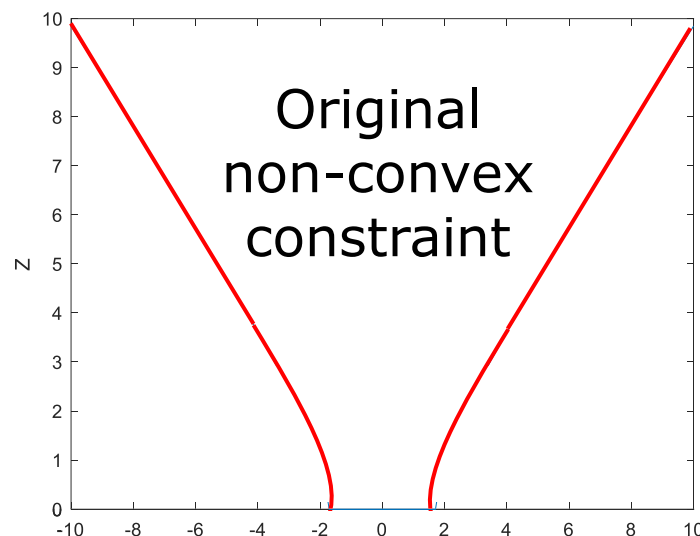
$$\underbrace{\left( \frac{H}{f_0} - \frac{R_1 \cdot T_1}{4\Delta f_{trig}} \right)}_{= z} \underbrace{\frac{R_2}{T_2}}_{= x} \geq \underbrace{\left( \frac{PL_{max} - R_1}{2\sqrt{\Delta f_{trig}}} \right)^2}_{= y} - \underbrace{\left( \frac{P^{UFLS}}{2\sqrt{\Delta f_{trig}}} \right)^2}_{= u}$$

## Second-Order Cone



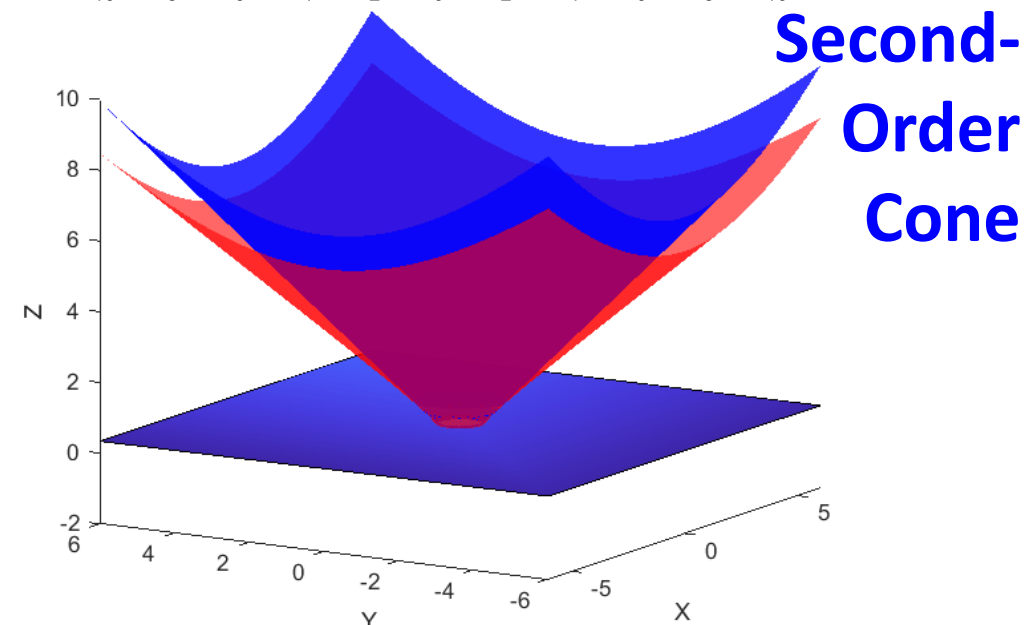
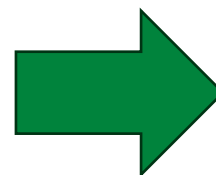
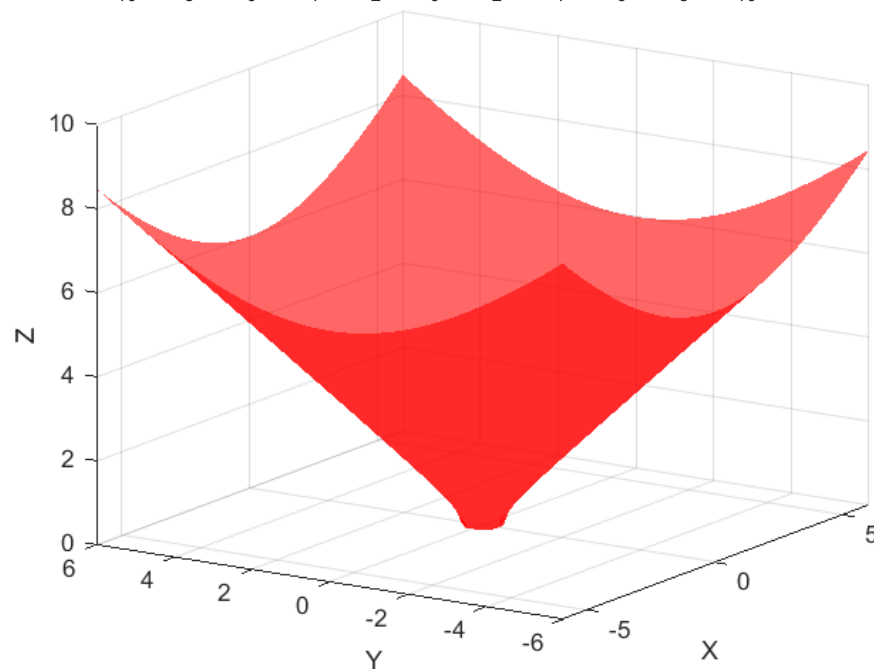
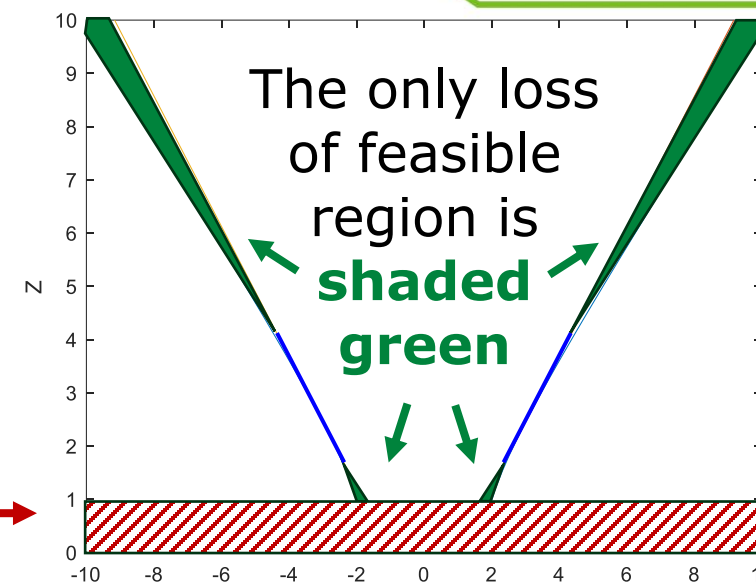
A higher volume of **UFLS**  
moves the constraint  
further away from convexity

# Nadir constraint: convex approximation



We compute the **least conservative approximation** possible

Not feasible due to other power system constraints →



# Results: value of UFLS for largest loss

UFLS is penalised at the Value of Lost Load in the objective function of the UC

**Savings of hundreds of million £ per year in Great Britain**

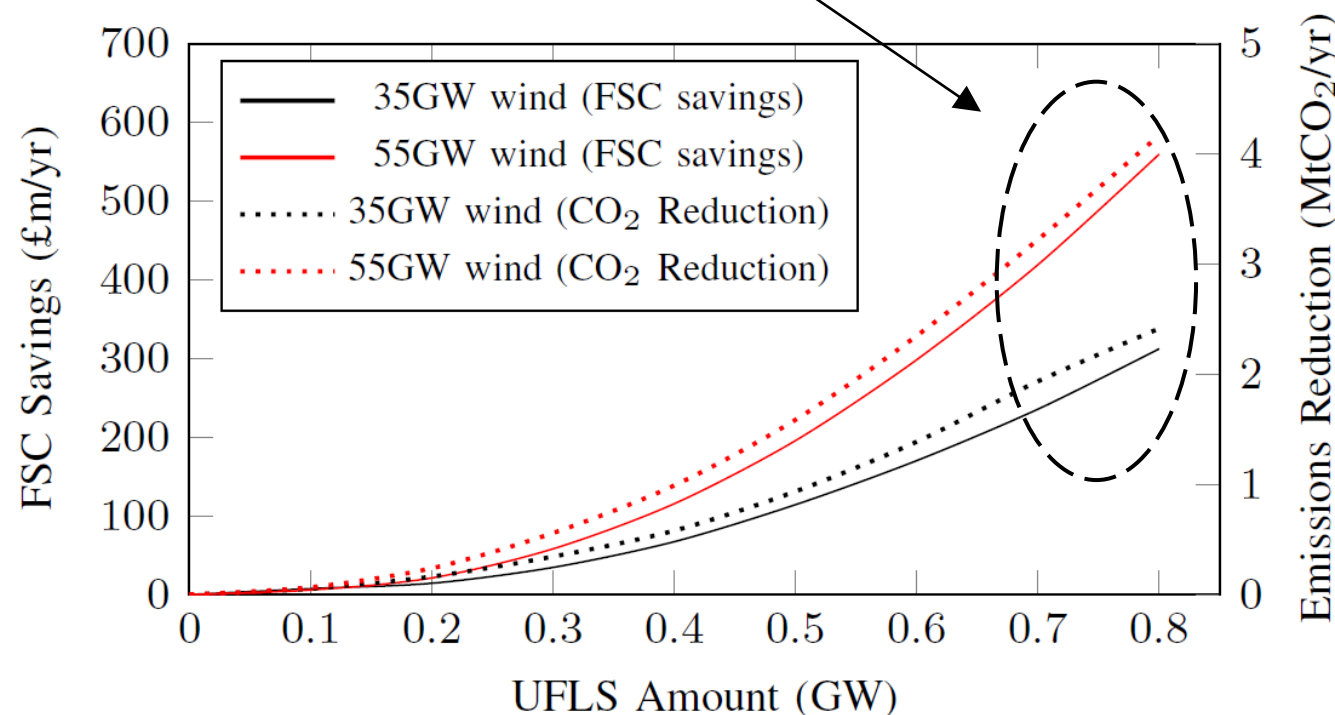
**Cost of activating UFLS for largest loss**

$$\min \sum_{g \in \mathcal{G}} c_g^{\text{nl}} \cdot y_g + c_g^{\text{m}} \cdot P_g + \underbrace{\pi_{\text{UFLS}}}_{\text{Probability of largest loss occurring}} \cdot \underbrace{P_{\text{UFLS}} \cdot \text{VoLL}}_{\text{Volume of UFLS needed (decision variable)}}$$

Probability of largest loss occurring      Volume of UFLS needed (decision variable)

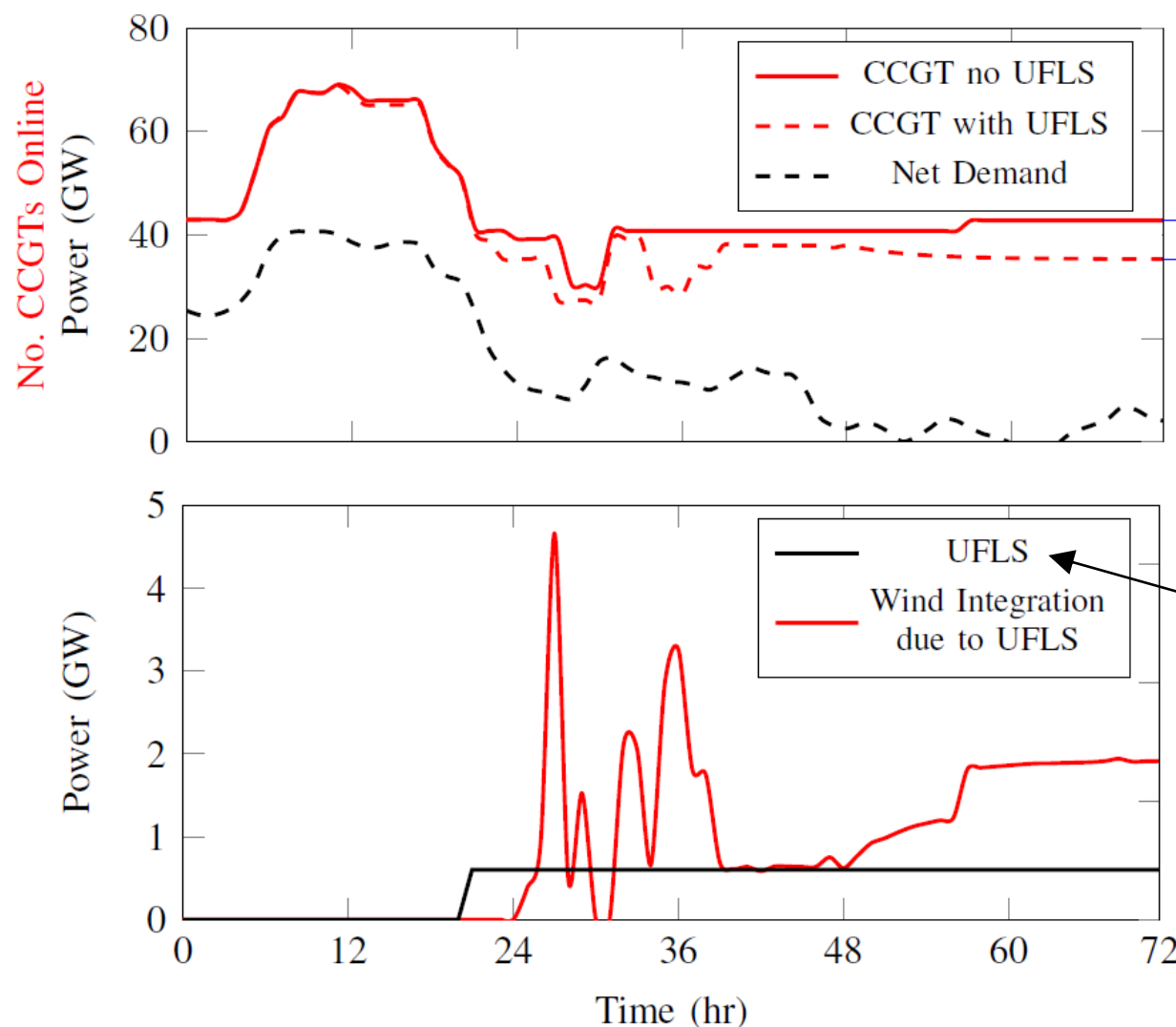
Where do these **savings** come from?

→ next slide



# Results: value of UFLS for largest loss

Example of 72 hours of operation:



If some **UFLS** is considered as a 'service', **fewer gas plants are needed** to increase inertia and frequency response (economic and emissions savings)

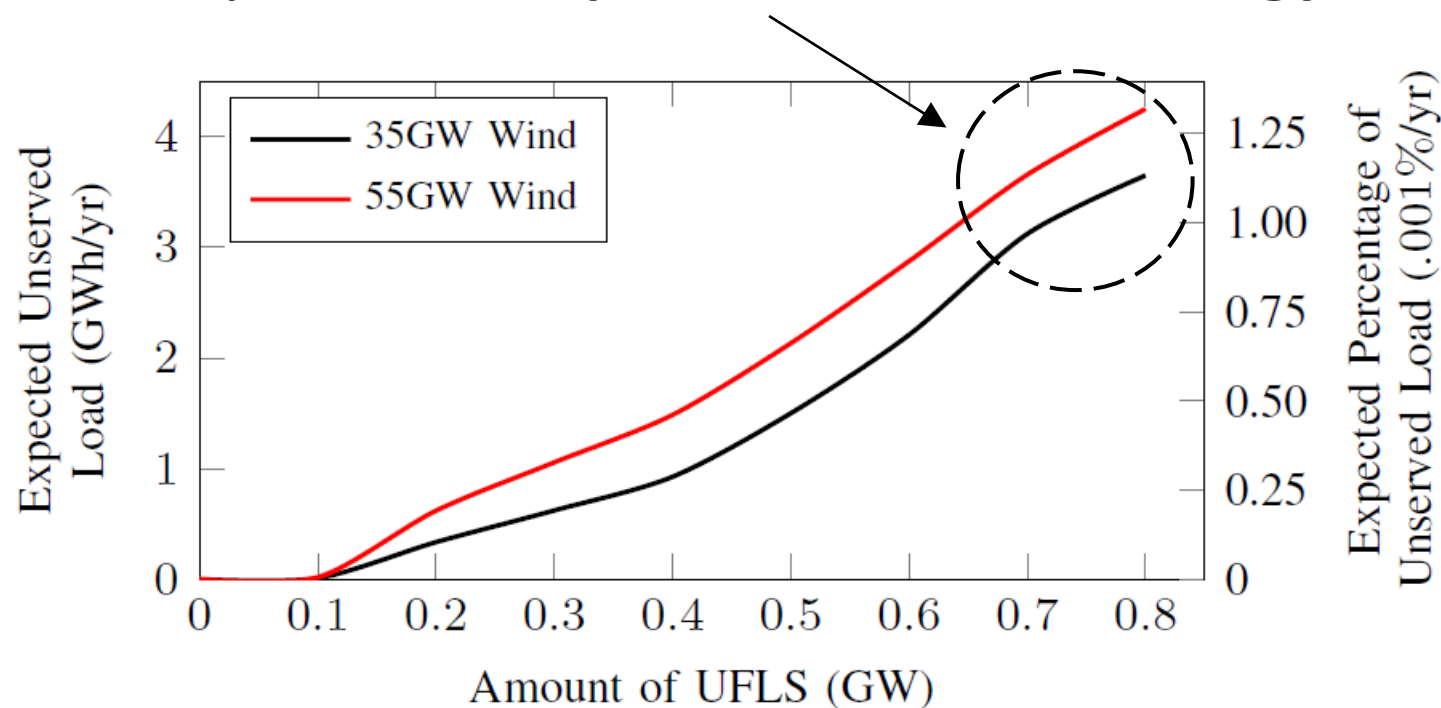
**UFLS 'accepted' (not necessarily activated)**



# Results: risk of UFLS for largest loss

The previous results come from a **risk neutral optimisation**:  
the expected cost is minimised

However, this still **provides high levels of reliability**:  
only **0.001% expected unserved energy**



Assumption for **outage rate**  
of large nuclear:  
**1.8 occurrences/yr**

(historical data shows that  
this assumption is even  
somewhat conservative)

# Communication requirements with UFLS relays

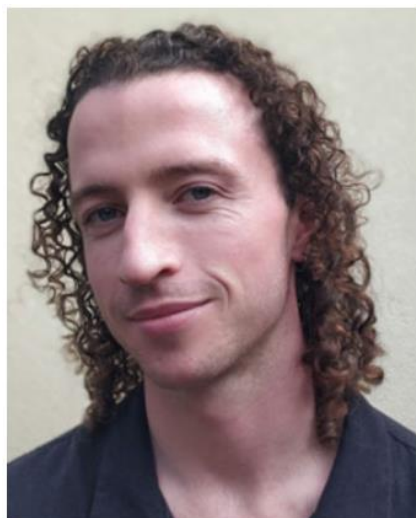
- Previous results assume that **UFLS relay settings can be updated every hour**: a communication network is needed for this
- This framework is **also compatible with traditional UFLS schemes** that have **no communication with relays**
  - In this case, **savings** from the UFLS service **decrease by up to £180m/year** for Great Britain



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# Thank you for your attention!



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