

{ordr}: Toward Tidy Principles for Matrix-Decomposed Data

New Developments in Graphing Multivariate Data

Section on Statistical Graphics • Joint Statistical Meetings 2022

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Acknowledgments

Development

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Discussion

Joyce Robbins (Columbia)

Applications

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Land

Potano tribe \subset Timucua people

Resources

UConn
HEALTH



Slideshow

remark.js (Ole Petter Bang) + xaringan (Yihui Xie)
Catlab.jl (Evan Patterson &al)
Flaticon.com

Prerequisites

Singular value decomposition

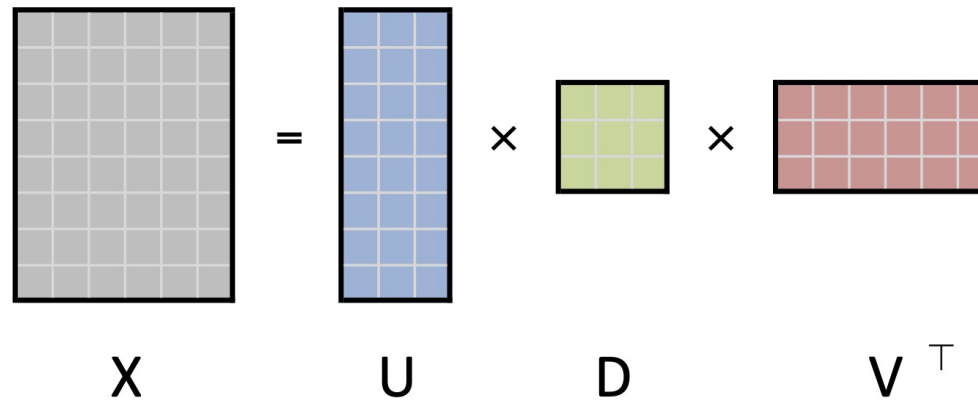
1. Data matrix $X_{n \times p} \in \mathbb{R}^{n \times p}$

2. SVD into **inertia** and rotation matrices of left and right **singular vectors**:

$$X = U_{n \times k} D_{k \times k} V_{p \times k}^\top$$

3. Low-dimensional approximation via first r **ordinates**:

$$X \approx U_r D_r V_r^\top$$



Biplots

Principal coordinates $F = UD$ or $G = VD$ approximate the geometry of the rows or columns of X :

- Distances $\|f_{j\bullet} - f_{i\bullet}\|$ approximate distances $\sqrt{(x_{j1} - x_{i1})^2 + \dots + (x_{jp} - x_{ip})^2}$
- Inner products $\frac{1}{n} g_{i\bullet} \cdot g_{j\bullet}$ approximate covariances $\text{cov}(x_{\bullet i}, x_{\bullet j})$
 - Cosines $\cos(\arg(g_{i\bullet}, g_{j\bullet}))$ approximate correlations $\text{cor}(x_{\bullet i}, x_{\bullet j})$

Standard coordinates U or V pair with principal coordinates to recover the values of X :

- Inner products $f_{i\bullet} \cdot v_{j\bullet}$ and $u_{i\bullet} \cdot g_{j\bullet}$ approximate entries x_{ij}

Biplots superimpose row and column coordinates with shares (a, b) of inertia:

$$\begin{bmatrix} U & D^a \\ V & D^b \end{bmatrix} \in \mathbb{R}^{(n+p) \times r}$$

Biplots

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$$\begin{bmatrix} U & D^a \\ V & D^b \end{bmatrix} \in \mathbb{R}^{(n+p) \times r}$$

Pick (at most) **two out of three**:

1. Approximate row geometry
2. Approximate column geometry
3. Approximate measured values

Pitch: Principal components analysis

PCA of Anderson's iris data

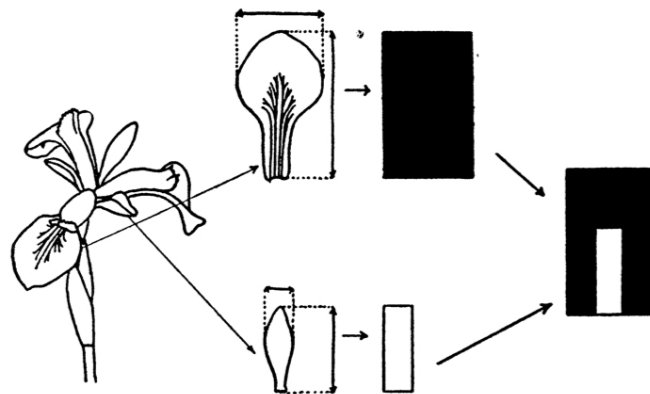
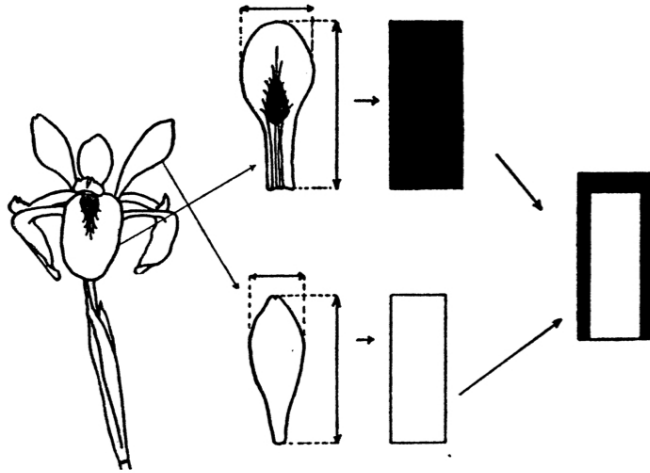


Fig. 8. Diagram illustrating how petal length and width, and sepal length and width are combined to form an ideograph. Above, *Iris virginica*; below, *I. versicolor*.

```
head(iris)
```

```
## Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1 5.1 3.5 1.4 0.2 setosa
## 2 4.9 3.0 1.4 0.2 setosa
## 3 4.7 3.2 1.3 0.2 setosa
## 4 4.6 3.1 1.5 0.2 setosa
## 5 5.0 3.6 1.4 0.2 setosa
## 6 5.4 3.9 1.7 0.4 setosa
```

```
summary(iris)
```

```
## Sepal.Length Sepal.Width Petal.Length Petal.Width
## Min. :4.300 Min. :2.000 Min. :1.000 Min. :0.100
## 1st Qu.:5.100 1st Qu.:2.800 1st Qu.:1.600 1st Qu.:0.300
## Median :5.800 Median :3.000 Median :4.350 Median :1.300
## Mean :5.843 Mean :3.057 Mean :3.758 Mean :1.199
## 3rd Qu.:6.400 3rd Qu.:3.300 3rd Qu.:5.100 3rd Qu.:1.800
## Max. :7.900 Max. :4.400 Max. :6.900 Max. :2.500
## Species
## setosa :50
## versicolor:50
## virginica :50
##
##
##
```


PCA of Anderson's iris data

```
(pca <- prcomp(iris[, 1:4]))
```

```
## Standard deviations (1, ..., p=4):  
## [1] 2.0562689 0.4926162 0.2796596 0.1543862  
##  
## Rotation (n x k) = (4 x 4):  
##           PC1      PC2      PC3      PC4  
## Sepal.Length 0.36138659 -0.65658877 0.58202985 0.3154872  
## Sepal.Width  -0.08452251 -0.73016143 -0.59791083 -0.3197231  
## Petal.Length 0.85667061 0.17337266 -0.07623608 -0.4798390  
## Petal.Width 0.35828920 0.07548102 -0.54583143 0.7536574
```

```
(pca_ord <- ordinate(iris, prcomp, cols = 1:4))
```

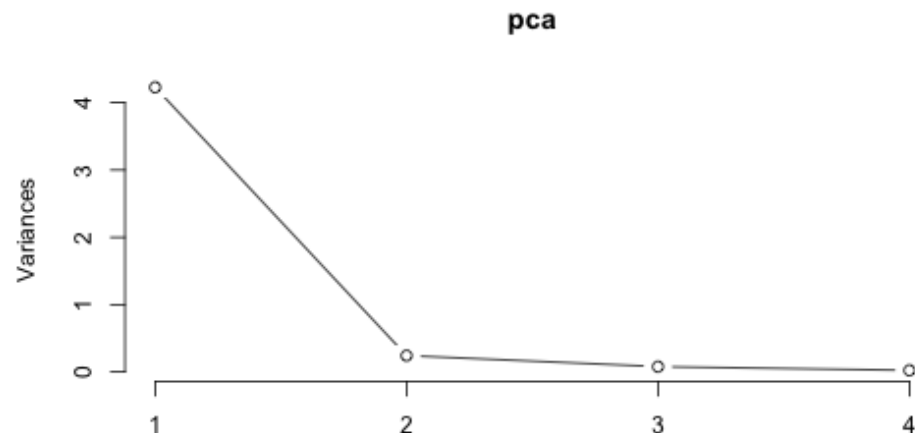
```
## # A tbl_ord of class 'prcomp': (150 x 4) x (4 x 4)'  
## # 4 coordinates: PC1, PC2, ..., PC4  
## #  
## # Rows (principal): [ 150 x 4 | 1 ]  
##   PC1    PC2    PC3 ... | Species  
##   <dbl> <dbl> <dbl> ... | <fct>  
## 1 -2.68 -0.319 0.0279   | 1 setosa  
## 2 -2.71 0.177 0.210 ... | 2 setosa  
## 3 -2.89 0.145 -0.0179   | 3 setosa  
## 4 -2.75 0.318 -0.0316   | 4 setosa  
## 5 -2.73 -0.327 -0.0901   | 5 setosa  
## # ... with 145 more rows  
## # i Use `print(n = ...)` to see more rows  
## #  
## # Columns (standard): [ 4 x 4 | 2 ]  
##   PC1    PC2    PC3 ... | .name      .center  
##   <dbl> <dbl> <dbl> ... | <chr>      <dbl>  
## 1 0.361 -0.657 0.582   | 1 Sepal.Length 5.84  
## 2 -0.0845 -0.730 -0.598 ... | 2 Sepal.Width 3.06  
## 3 0.857 0.173 -0.0762  | 3 Petal.Length 3.76  
## 4 0.358 0.0755 -0.546   | 4 Petal.Width 1.20
```

PCA of Anderson's iris data

```
summary(pca)
```

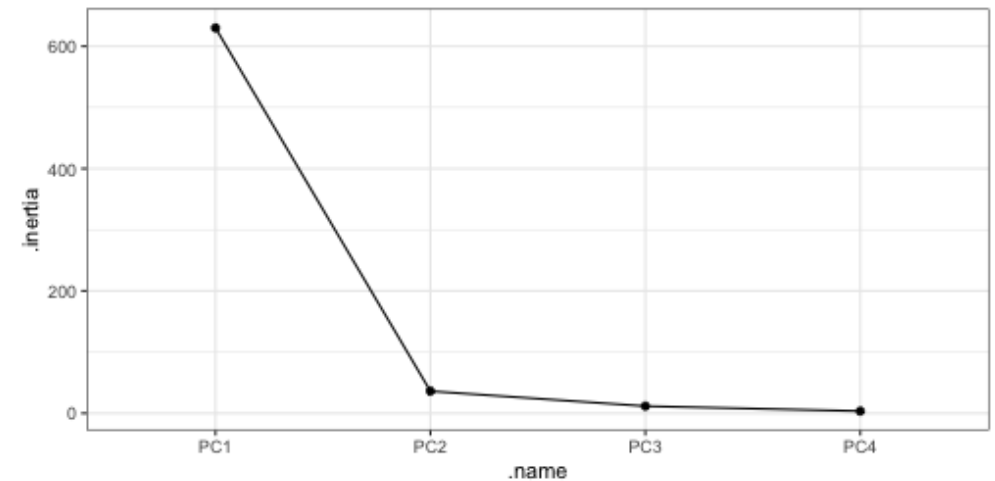
```
## Importance of components:  
##  
## Standard deviation      PC1      PC2      PC3      PC4  
## Proportion of Variance 0.9246 0.05307 0.0171 0.00521  
## Cumulative Proportion  0.9246 0.97769 0.9948 1.00000
```

```
screplot(pca, type = "lines")
```



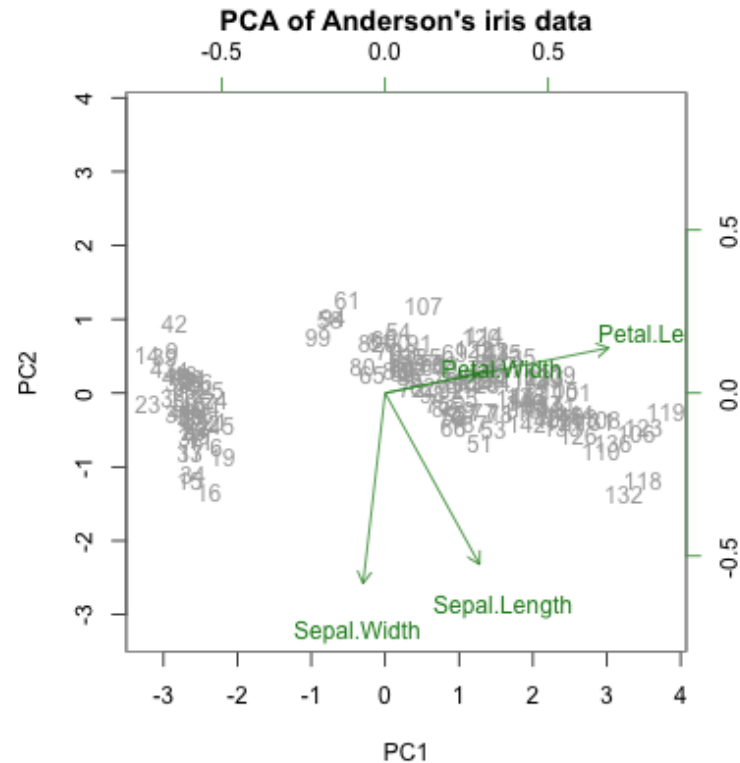
```
tidy(pca_ord) %>% print() %>%  
  ggplot(aes(x = .name, y = .inertia, group = 1)) +  
  geom_line() + geom_point()
```

```
## # A tibble: 4 × 4  
##   .name .sdev .inertia .prop_var  
##   <fct> <dbl>   <dbl>   <dbl>  
## 1 PC1   2.06    630.    0.925  
## 2 PC2   0.493   36.2    0.0531  
## 3 PC3   0.280   11.7    0.0171  
## 4 PC4   0.154    3.55   0.00521
```

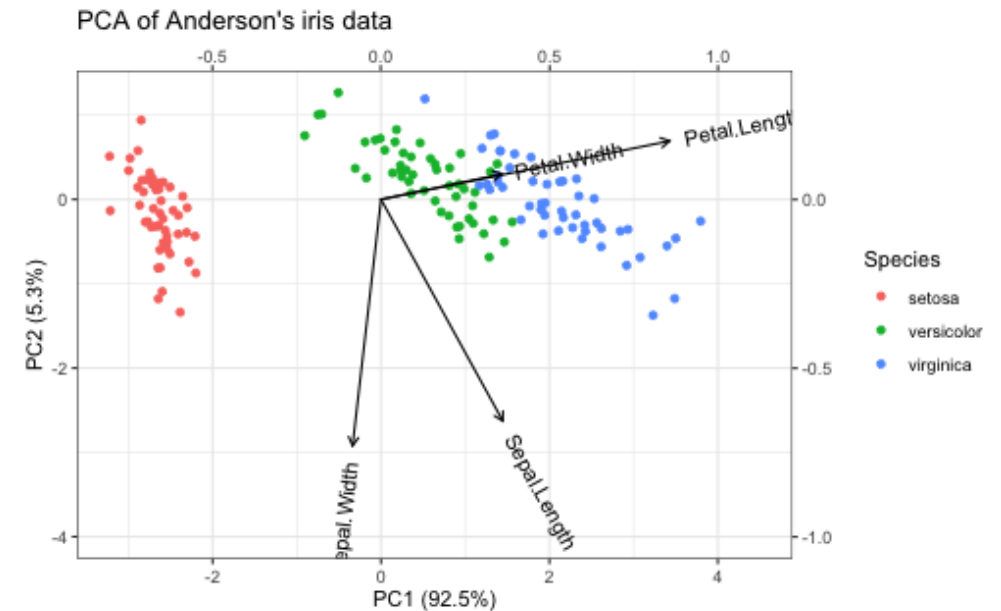


PCA of Anderson's iris data

```
biplot(pca, scale = 0, col = c("darkgrey", "forestgreen")  
main = "PCA of Anderson's iris data")
```



```
pca_ord %>% confer_inertia("rows") %>%  
ggbiplot(aes(label = .name),  
sec.axes = "cols", scale.factor = 4) +  
geom_rows_point(aes(color = Species)) +  
geom_cols_vector() + geom_cols_text_raduate() +  
expand_limits(x = c(NA, 4.5), y = c(-4, NA)) +  
ggtitle("PCA of Anderson's iris data")
```

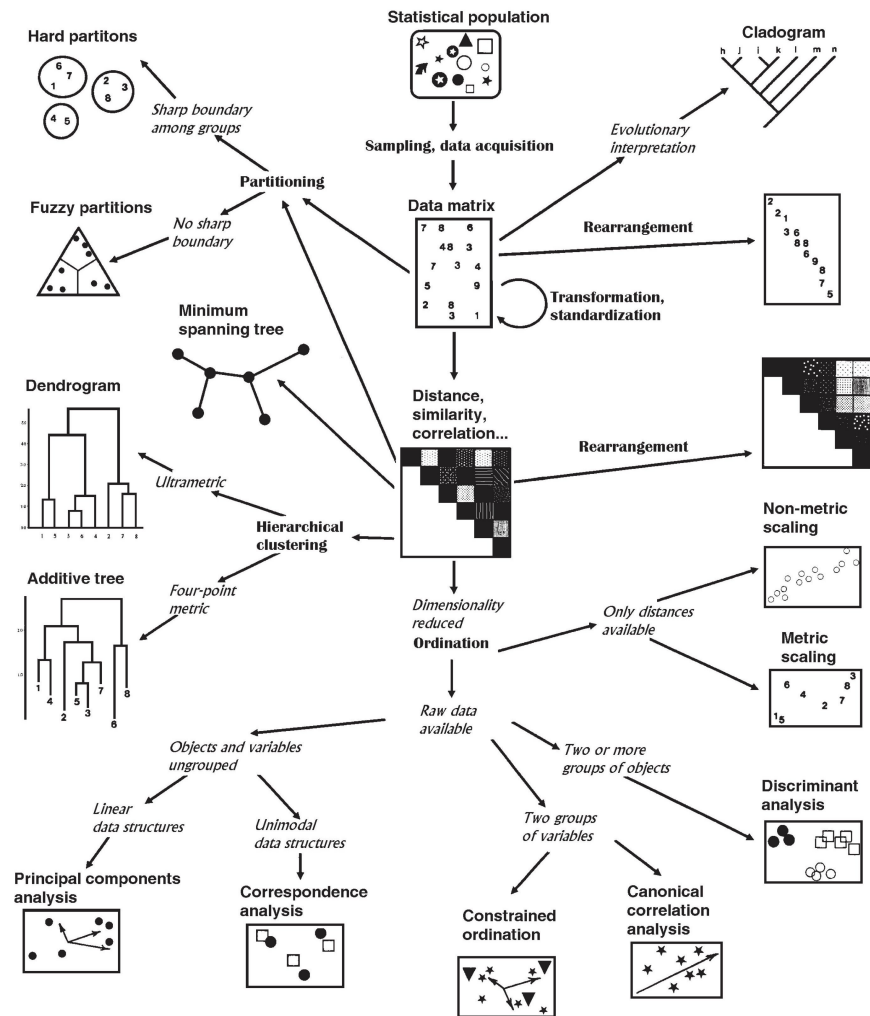


Motivation

Ordination

"[A]ny technique that extracts artificial variables in order to reduce the dimensionality of the data is referred to as ordination."¹

		model	
		unsupervised	supervised
data	discrete	clustering	classification
	continuous	dimension reduction	regression



Statement of need

R is replete with ordination methods!

CRAN Task View: Multivariate Statistics

Maintainer: Paul Hewson

Contact: Paul.Hewson at plymouth.ac.uk

Version: 2014-09-19

CRAN Task View: Analysis of Ecological and Environmental Data

Maintainer: Gavin Simpson

Contact: ucfagls at gmail.com

Version: 2014-05-31

... but they are

- **specialized:** unweildy or unintuitive inspection
- **heterogeneous:** diverse, dissimilar conventions
- **standalone:** not designed to be interoperable

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- **heterogeneous:** diverse, dissimilar conventions
- **standalone:** not designed to be interoperable

The tidyverse strives to be

- **human-centered:** supports data analysis conducted by humans
- **consistent:** ensures that learning transfers between packages
- **composable:** enables modular data exploration and study design
- **inclusive:** is developed and informed by a broad community of users



Statement of purpose

*The {ordr} package leverages a **unifying framework** for matrix decomposition models and the **philosophy, conventions, and popularity** of the tidyverse in order to more **naturally** and **efficiently** integrate ordination analyses into **common** data science workflows.*

Pitch: Correspondence analysis

CA of Snee's hair and eye color data

The data in Table 3 are the observed frequencies of hair color (black, brunette, red, blond) and eye color (brown, blue, hazel, green) of 592 subjects. These data were collected, as part of a class project, by students in

TABLE 3
HAIR COLOR - EYE COLOR DATA

	Hair Color				
Eye Color	Black	Brunette	Red	Blond	Total
Brown	68 .309*	119 .541	26 .118	7 .032	220 1.000
Blue	20 .093	84 .391	17 .079	94 .437	215 1.000
Hazel	15 .161	54 .581	14 .150	10 .108	93 1.000
Green	5 .078	29 .453	14 .219	16 .250	64 1.000

*Proportion of total

an elementary statistics course taught by the author at the University of Delaware. The chi-squared statistic for Table 3 is 138.29 (9 df, $p < .01$), indicating a significant correlation between hair color and eye color. In this problem it is of interest to determine which of the eye colors are producing the nonhomogeneity. The eigenvalue-eigenvector analysis (Table 4) indicated that the first two eigenvalues accounted for approximately 97 percent of the variation. The coordinates of

```
(haireye <- as.data.frame(rowSums(HairEyeColor, dims = 2L)))
```

```
##           Brown Blue Hazel Green
## Black      68   20   15    5
## Brown     119   84   54   29
## Red        26   17   14   14
## Blond       7   94   10   16
```

```
summary(HairEyeColor)
```

```
## Number of cases in table: 592
## Number of factors: 3
## Test for independence of all factors:
##           Chisq = 164.92, df = 24, p-value = 5.321e-23
##           Chi-squared approximation may be incorrect
```

CA of Snee's hair and eye color data

```
(ca <- MASS::corresp(haireye, nf = 2L))
```

```
## First canonical correlation(s): 0.4569165 0.1490859
##
## Row scores:
##           [,1]      [,2]
## Black -1.1042772  1.4409170
## Brown -0.3244635 -0.2191109
## Red   -0.2834725 -2.1440145
## Blond  1.8282287  0.4667063
##
## Column scores:
##           [,1]      [,2]
## Brown -1.0771283  0.5924202
## Blue   1.1980612  0.5564193
## Hazel -0.4652862 -1.1227826
## Green  0.3540108 -2.2741218
```

```
(ca_ord <- ordinate(haireye,
                    model = MASS::corresp, nf = 2L))
```

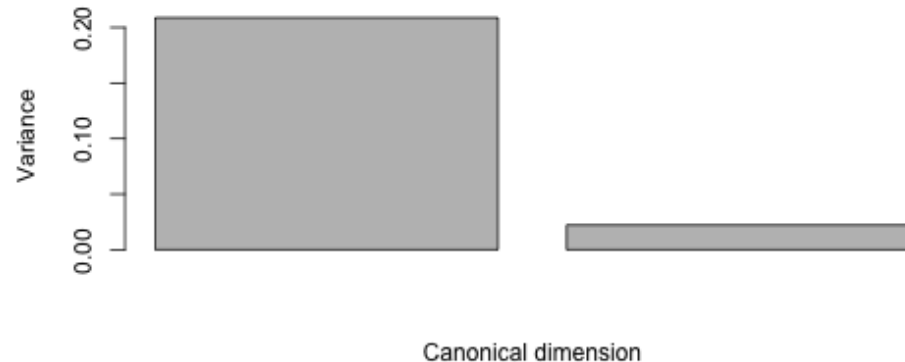
```
## # A tbl_ord of class 'correspondence': (4 x 2) x (4 x 2)'
## # 2 coordinates: Can1 and Can2
## #
## # Rows (standard): [ 4 x 2 | 1 ]
##   Can1  Can2 | .name
##      |      | <chr>
## 1 -1.10  1.44 | 1 Black
## 2 -0.324 -0.219 | 2 Brown
## 3 -0.283 -2.14 | 3 Red
## 4  1.83   0.467 | 4 Blond
## #
## # Columns (standard): [ 4 x 2 | 1 ]
##   Can1  Can2 | .name
##      |      | <chr>
## 1 -1.08  0.592 | 1 Brown
## 2  1.20  0.556 | 2 Blue
## 3 -0.465 -1.12 | 3 Hazel
## 4  0.354 -2.27 | 4 Green
```

CA of Snee's hair and eye color data

```
summary(ca)
```

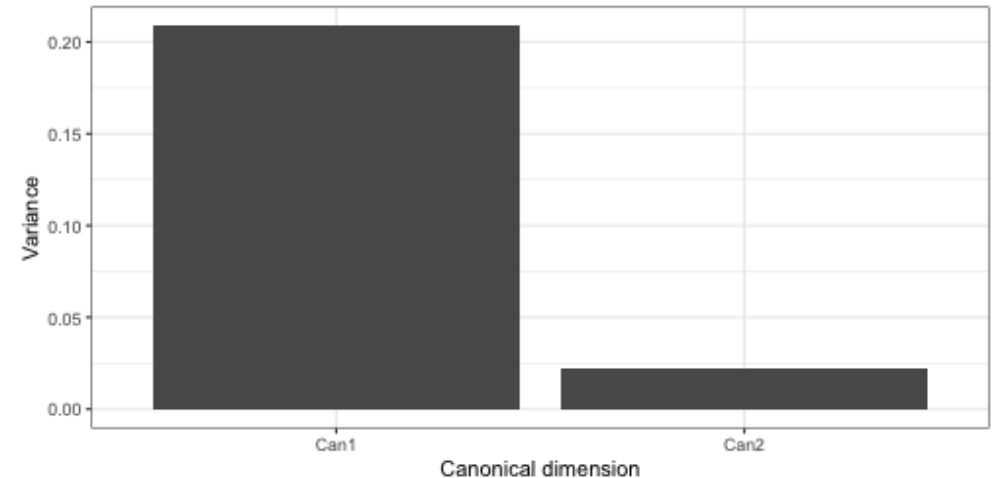
```
##          Length Class  Mode
## cor         2    -none- numeric
## rscore      8    -none- numeric
## cscore      8    -none- numeric
## Freq       16    -none- numeric
```

```
barplot(ca$cor^2,
        xlab = "Canonical dimension", ylab = "Variance")
```



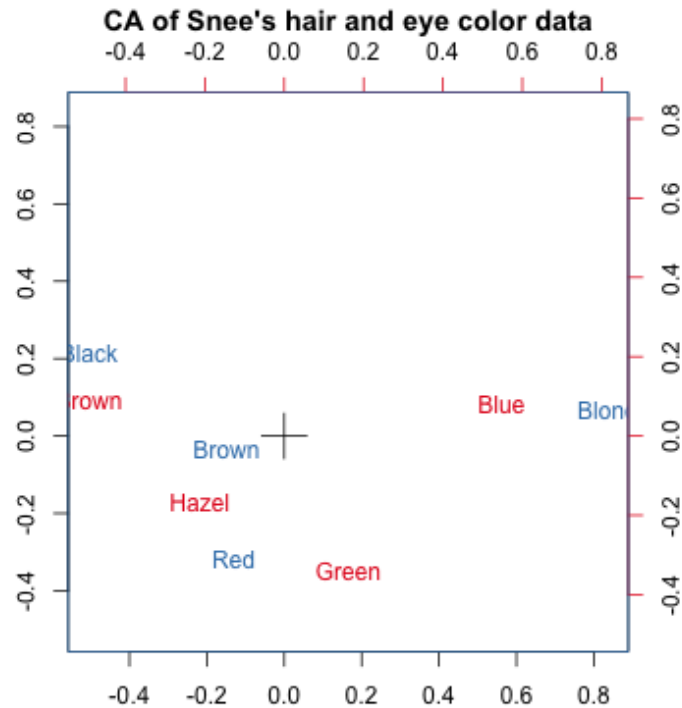
```
tidy(ca_ord) %T>% print() %>%
  ggplot(aes(x = .name, y = .cor^2)) +
  geom_col() +
  labs(x = "Canonical dimension", y = "Variance")
```

```
## # A tibble: 2 × 4
##   .name .cor .inertia .prop_var
##   <fct> <dbl> <dbl> <dbl>
## 1 Can1  0.457  0.209  0.904
## 2 Can2  0.149  0.0222 0.0962
```

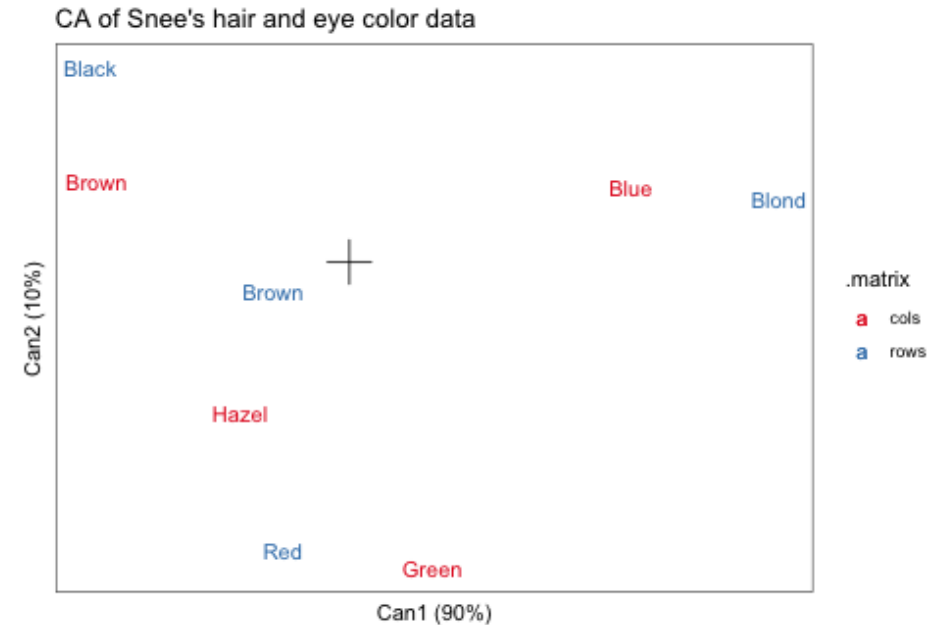


CA of Snee's hair and eye color data

```
biplot(ca, type = "symmetric",  
       col = c("#377eb8", "#e41a1c"),  
       main = "CA of Snee's hair and eye color data")
```



```
ca_ord %>% confer_inertia("symmetric") %>%  
  ggbiplot(aes(label = .name, color = .matrix)) +  
  scale_color_brewer(type = "qual", palette = "Set1") +  
  theme_biplot() + geom_origin() +  
  geom_rows_text() + geom_cols_text() +  
  ggtitle("CA of Snee's hair and eye color data")
```



Design

Principles

{ordr} strives for a coherent grammar² that is



accessible

- easy to learn and straightforward to advance
- couples easily with other data science tools



opinionated

- foregrounds the unity of supported techniques
- rewards good practice, relieves choice paralysis



extensible

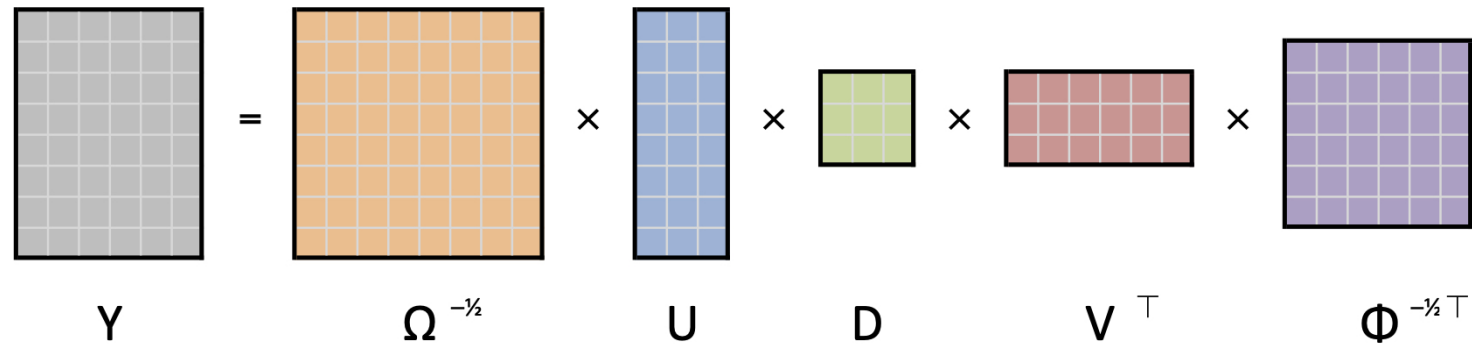
- relies on a small set of core generics
- borrows conventions from widely-used tools

Inspiration

A general approach to ordination techniques:³

1. **Preprocess data** (centering; double-centering): $X \rightsquigarrow Y$
2. **Generalized SVD** (weights; sphering):

$$Y = (\Omega^{-1/2} U) D (\Phi^{-1/2} V)^T$$



3. **Biplot**, with $a + b = 1$ (row-principal; column-principal; symmetric):

$$F = \Omega^{-1/2} U D^a, \quad G = \Phi^{-1/2} V D^b$$

Core generics

Engine

For each supported model class, **recover**:

- left & right matrix factors (singular vectors)

$$U, V$$

- inertia and its distribution unto the factors

$$D = \text{diag}(d_1, \dots, d_k), (a, b)$$

- supplementary elements

$$U D = X V, X' V, \text{ etc.}$$

- metadata about model components

Core generics

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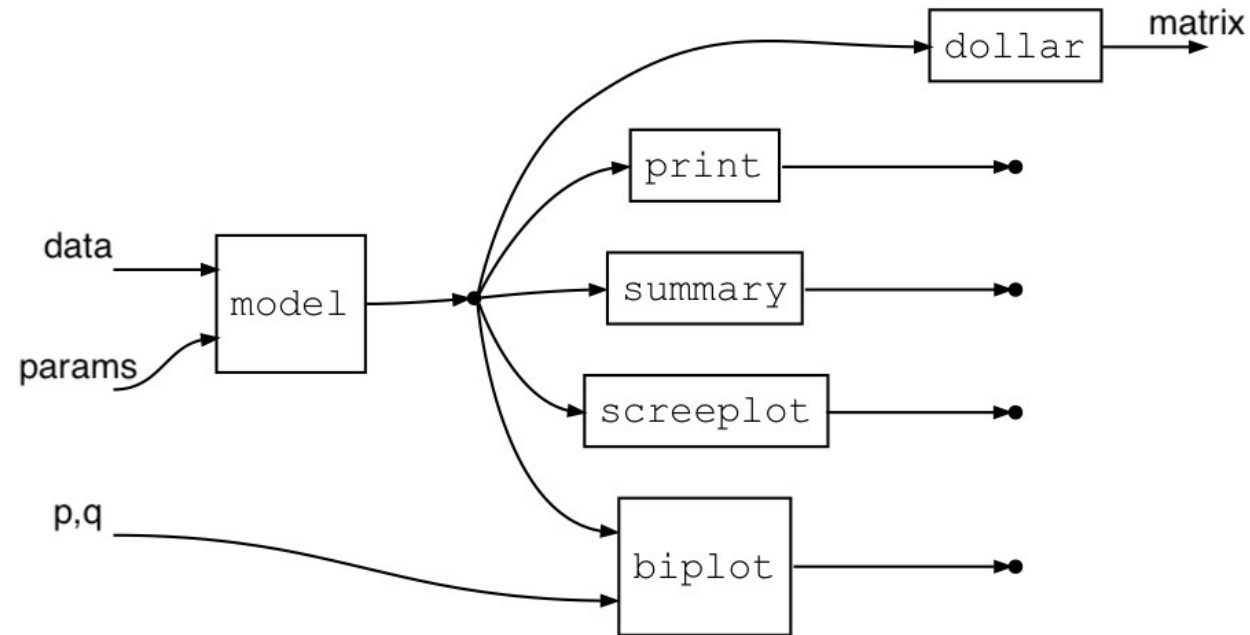
- metadata about model components

Dashboard

Via the wrapper class `'tbl_ord'`, **enable**:⁴

- clear & consistent formatting via `{tibble}`
- re-distribution of inertia
- negations of axes
- annotation of components via `{dplyr}`
- summaries for further analysis via `{broom}`
- grammatical construction of biplots via `{ggplot2}`
- workflows via `{magrittr}` (or `|>` if one must)

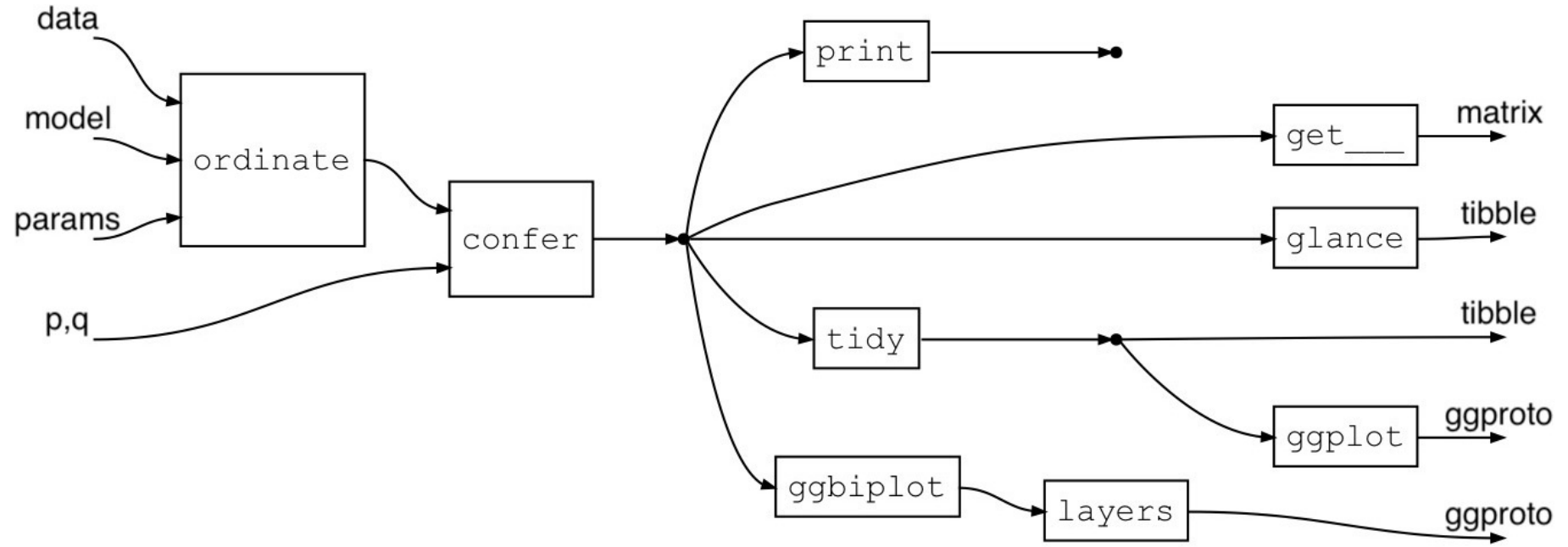
Base R workflow



Limitations

- idiosyncratic fit function and output class
- retrievable model components are nonstandard
- model summaries often have no class or methods
- (bi)plots offer limited customization and annotation

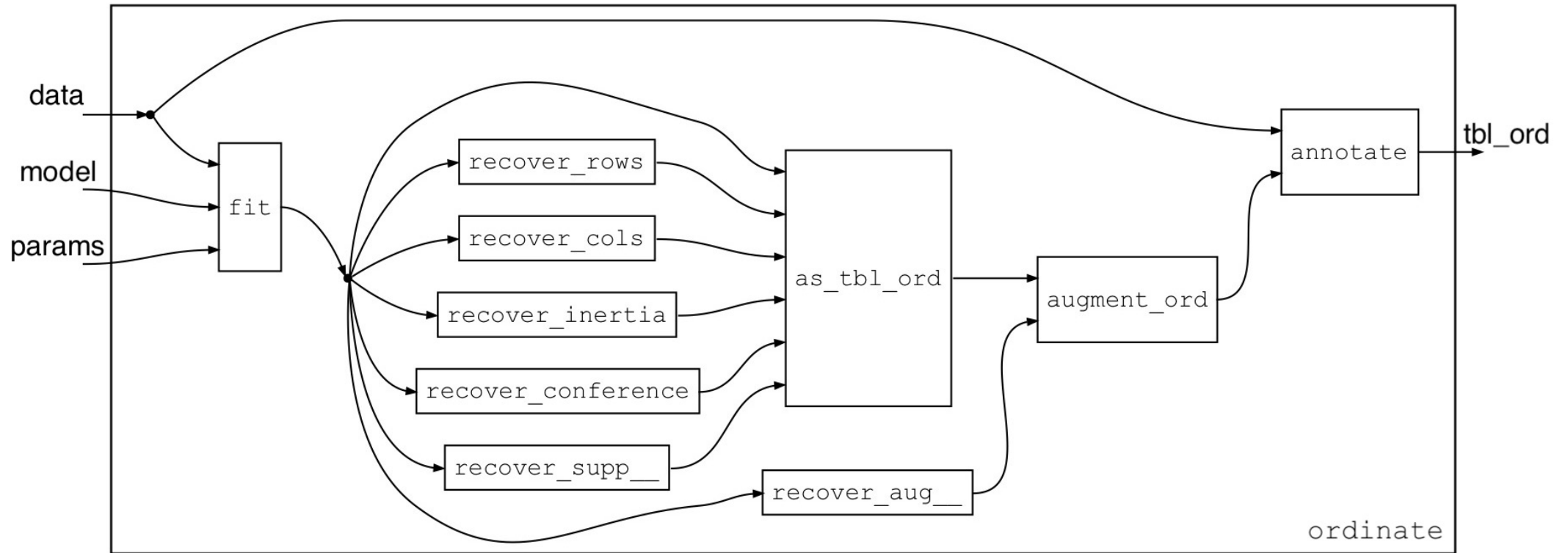
{ordr} workflow: Dashboard



Differences

- unified fit function and modifiable wrapper class
- retrieval methods for standard components
- model summaries are returned as data frames
- biplots can be layered

{ordr} workflow: Engine



Wrapper `'tbl_ord'`

- connects underlying models to unified functions by way of recovery methods

Decorator `augment_ord()`

- annotates recovered model components with recovered metadata

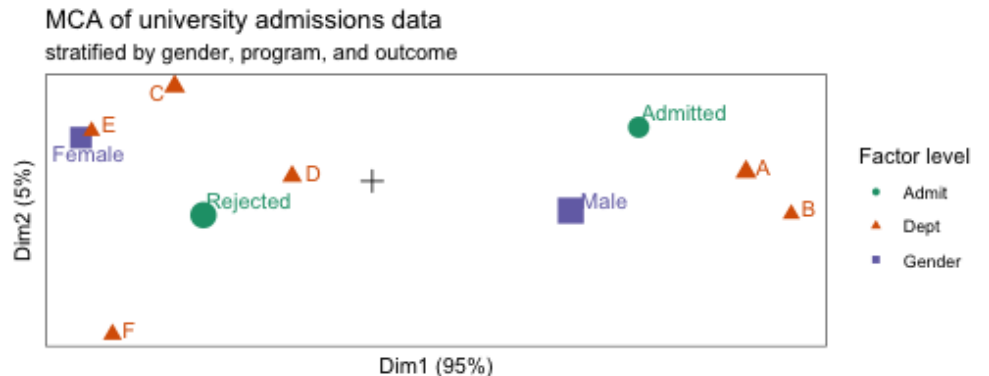
Gallery

Gallery: Multiple correspondence analysis of university admissions data

```
ca::mjca(UCBAdmissions) %>%  
  as_tbl_ord() %>% augment_ord() %>%  
  print() -> admissions_mca
```

```
## # A tbl_ord of class 'mjca': (4526 x 2) x (10 x 2)'  
## # 2 coordinates: Dim1 and Dim2  
## #  
## # Rows (standard): [ 4526 x 2 | 4 ]  
##   Dim1 Dim2 | .name .mass .dist  
##   | <chr> <dbl> <dbl>  
## 1 3.33 2.68 | 1 1 0.000221 0.00672  
## 2 3.33 2.68 | 2 2 0.000221 0.00672  
## 3 3.33 2.68 | 3 3 0.000221 0.00672  
## 4 3.33 2.68 | 4 4 0.000221 0.00672  
## 5 3.33 2.68 | 5 5 0.000221 0.00672  
## # ... with 4,521 more rows, and  
## # 1 more variable:  
## # .inertia <dbl>  
## # i Use `print(n = ...)` to see more rows, and `colnames()` to  
## #  
## # Columns (standard): [ 10 x 2 | 6 ]  
##   Dim1 Dim2 | .name .factor .level .mass  
##   | <chr> <chr> <chr> <dbl>  
## 1 1.08 0.975 | 1 Admi... Admit Admit... 0.129  
## 2 -0.681 -0.617 | 2 Admi... Admit Rejec... 0.204  
## 3 -1.18 0.786 | 3 Gend... Gender Female 0.135  
## 4 0.802 -0.536 | 4 Gend... Gender Male 0.198
```

```
admissions_mca %>%  
  confer_inertia("colprincipal") %>%  
  ggbiplot() + theme_biplot() + geom_origin() +  
  geom_cols_point(aes(color = .factor, shape = .factor,  
                      size = .mass)) +  
  geom_cols_text_repel(aes(label = .level, color = .facto  
                          show.legend = FALSE) +  
  scale_color_brewer(palette = "Dark2") +  
  scale_size_area(guide = "none") +  
  labs(color = "Factor level", shape = "Factor level") +  
  ggtitle("MCA of university admissions data",  
          "stratified by gender, program, and outcome")
```

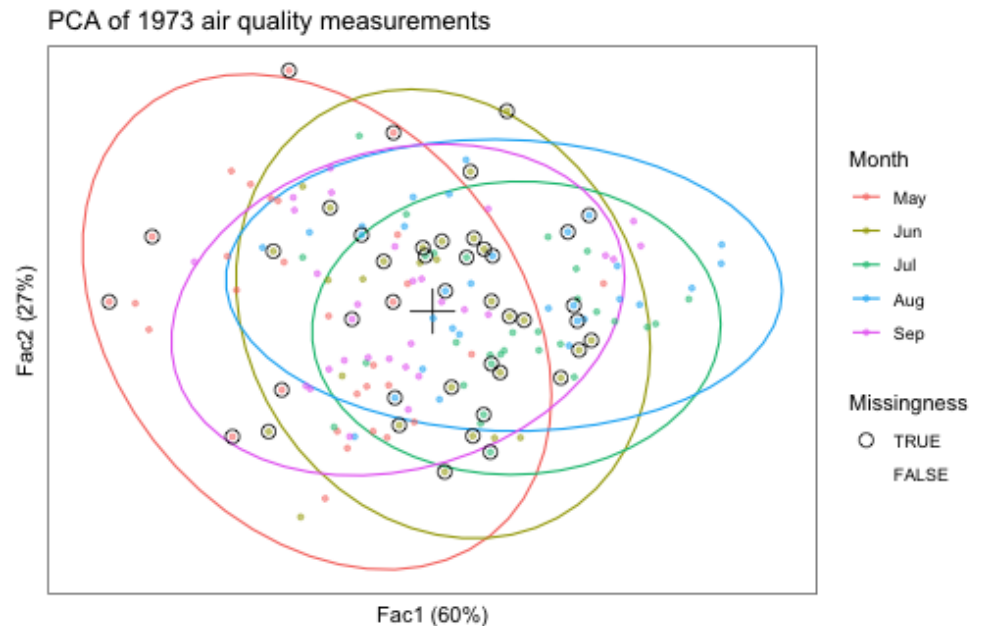


Gallery: NIPALS of (incomplete) air quality data

```
ordinate(airquality, seq(4L), ade4::nipals, nf = 3L) %>%  
  mutate_rows(  
    Month = factor(month.abb[Month], levels = month.abb),  
    Missingness = apply(is.na(airquality[, 1:4]), 1L, any  
  ) %>%  
  print() -> airqual_nipals
```

```
## # A tbl_ord of class 'nipals': (153 x 3) x (4 x 3)'  
## # 3 coordinates: Fac1, Fac2, Fac3  
## #  
## # Rows (principal): [ 153 x 3 | 4 ]  
##   Fac1   Fac2   Fac3 | .name Month   Day Missingn...1  
##   <dbl> <dbl> <dbl> | <chr> <fct> <int> <lgl>  
## 1 -0.305  0.334 -1.25 | 1 1    May     1 FALSE  
## 2 -0.426  0.930 -0.501 | 2 2    May     2 FALSE  
## 3 -1.27  -0.0592  0.279 | 3 3    May     3 FALSE  
## 4 -1.16  -1.46  -1.44 | 4 4    May     4 FALSE  
## 5 -3.41   0.906  -0.280 | 5 5    May     5 TRUE  
## # ... with 148 more rows, and  
## #   abbreviated variable name  
## #     'Missingness'  
## # i Use `print(n = ...)` to see more rows  
## #  
## # Columns (standard): [ 4 x 3 | 1 ]  
##   Fac1   Fac2   Fac3 | .name  
##   <dbl> <dbl> <dbl> | <chr>  
## 1  0.582  0.0175  0.104 | 1 Ozone
```

```
airqual_nipals %>%  
  ggbiplot() + theme_biplot() + geom_origin() +  
  stat_rows_ellipse(aes(color = Month)) +  
  geom_rows_point(aes(color = Month), size = 1, alpha = .  
  geom_rows_point(aes(shape = Missingness), size = 3) +  
  scale_shape_manual(values = c(`TRUE` = 1L, `FALSE` = NA  
  ggtitle("PCA of 1973 air quality measurements")
```

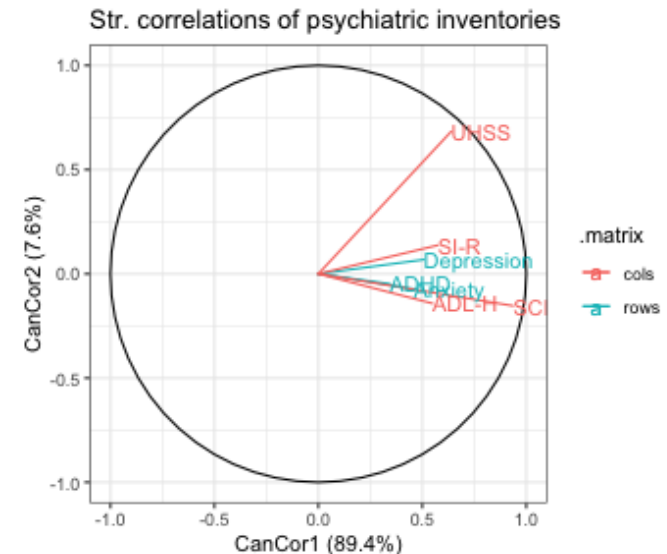


Gallery: Canonical correlation analysis of psychiatric inventories

```
cca_ord <- cancor_ord(pred, resp, scores = TRUE)
(cca_ord <- augment_ord(as_tbl_ord(cca_ord)))
```

```
## # A tbl_ord of class 'cancor_ord': (322 x 3) x (324 x 3)'
## # 3 coordinates: CanCor1, CanCor2, CanCor3
## #
## # Rows (standard): [ 322 x 3 | 3 ]
##   CanCor1  CanCor2  CanCor3 | .name      .center .element
##   <dbl>    <dbl>    <dbl> | <chr>      <dbl> <chr>
## 1  0.00146 -0.00494 -0.00306 | 1 Anxiety   18.9 active
## 2  0.00264  0.00507 -0.000169 | 2 Depression 20.7 active
## 3  0.00143 -0.000979  0.00371 | 3 ADHD      38.0 active
## 4 -0.0307  0.00214  0.0151 | 4 <NA>      NA score
## 5  0.0263  0.148    -0.0476 | 5 <NA>      NA score
## # ... with 317 more rows
## # i Use `print(n = ...)` to see more rows
## #
## # Columns (standard): [ 324 x 3 | 3 ]
##   CanCor1  CanCor2  CanCor3 | .name      .center .element
##   <dbl>    <dbl>    <dbl> | <chr>      <dbl> <chr>
## 1 -0.000433 -0.00240 -0.00560 | 1 SI-R      65.4 active
## 2  0.0208    -0.0303  -0.0176 | 2 ADL-H     2.13 active
## 3  0.00154   -0.000812  0.00120 | 3 SCI      100. active
## 4  0.00247   0.0136   0.00318 | 4 UHSS     30.0 active
## 5 -0.0510   -0.169   -0.0889 | 5 1        NA score
## # ... with 319 more rows
## # i Use `print(n = ...)` to see more rows
```

```
cca_ord %>% confer_inertia("rows") %>%
  ggbiplot(aes(label = .name, color = .matrix)) +
  geom_unit_circle() +
  geom_rows_vector(elements = "structure", arrow = NULL) +
  geom_cols_vector(elements = "structure", arrow = NULL) +
  geom_rows_text(elements = "structure", hjust = "outward") +
  geom_cols_text(elements = "structure", hjust = "outward") +
  expand_limits(x = c(-1, 1), y = c(-1, 1)) +
  ggtitle("Str. correlations of psychiatric inventories")
```

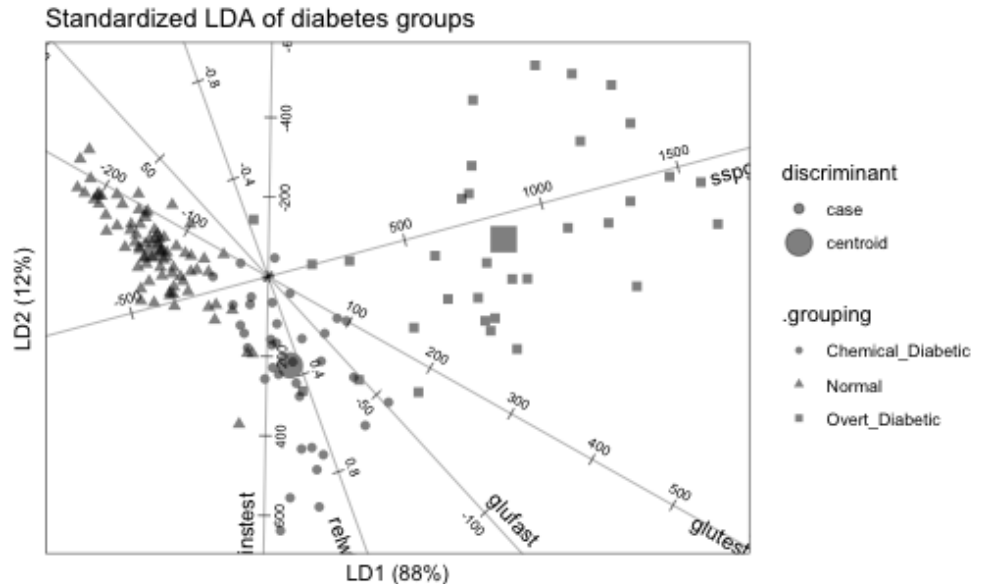


Gallery: Linear discriminant analysis of diabetes data

```
MASS::lda(group ~ ., heplots::Diabetes) %>%
  as_tbl_ord() %>% augment_ord() %>%
  mutate_rows(discriminant = ifelse(
    .element == "active", "centroid", "case"
  )) %>%
  print() -> diabetes_lda
```

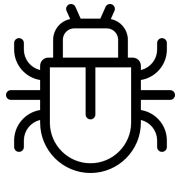
```
## # A tbl_ord of class 'lda': (148 x 2) x (5 x 2)'
## # 2 coordinates: LD1 and LD2
## #
## # Rows (principal): [ 148 x 2 | 6 ]
##   LD1    LD2 | .name .prior .counts .grou...1
##   <dbl> <dbl> | <chr> <dbl> <int> <chr>
## 1 -1.75  0.400 | 1 Norm... 0.524    76 Normal
## 2  0.340 -1.38  | 2 Chem... 0.248    36 Chemic...
## 3  3.66  0.580 | 3 Over... 0.228    33 Overt_...
## 4 -1.72  0.663 | 4 1      NA      NA Normal
## 5 -2.85  1.30  | 5 2      NA      NA Normal
## # ... with 143 more rows, 2
## # more variables:
## #   .element <chr>,
## #   discriminant <chr>, and
## #   abbreviated variable name
## #   `1.grouping`
## # i Use `print(n = ...)` to see more rows, and `colnames()` to
## #
## # Columns (standard): [ 5 x 2 | 2 ]
```

```
diabetes_lda %>% confer_inertia(1) %>%
  ggbiplot() + theme_biplot() +
  geom_rows_point(aes(shape = .grouping, size = discriminant
    alpha = .5) +
  geom_cols_axis(aes(label = .name),
    color = "#888888", num = 8L,
    text_size = 2.5, label_dodge = .02) +
  ggtitle("Standardized LDA of diabetes groups")
```



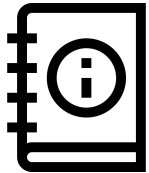
Wrap

Needs



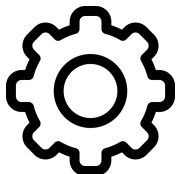
Engagement

- bug & need reports
- use cases
- code contributions



Documentation

- how to use `{ordr}` with **new model classes**
- how to use **new plot layers** with `ggbiplot()`



Features

- quality measures
- predictive biplots⁵

Welcome

Install `ordr`, and optionally methods for additional S3 classes:

```
remotes::install_github("corybrunson/ordr")  
remotes::install_github("corybrunson/ordr.extra")
```

Thank you!

- [1] Podani J • 2000 • *Introduction to the Exploration of Multivariate Biological Data* • <http://ramet.elte.hu/~podani/books.html>
- [2] Wilkinson L • 2005 • *The Grammar of Graphics* • <https://link.springer.com/book/10.1007/0-387-28695-0>
- [3] Greenacre M • 1984 • *Theory and applications of correspondence analysis* • <http://www.carme-n.org/>
- [4] Pedersen TL • 2022 • {tidygraph}: A Tidy API for Graph Manipulation • <https://CRAN.R-project.org/package=tidygraph>
- [5] Gower JC, Lubbe SG, le Roux NJ • 2011 • *Understanding Biplots* • <https://www.wiley.com/go/biplots>