

Unit - IV  
CHOPPER CONTROLLED DC MOTOR DRIVES

→ Choppers may be classified according to the no. of quadrants of the  $V_a$ - $I_a$  diagram in which they are capable of operating. By various combination of connections it is possible to realize any combination of output voltage and current polarity.

Control of Separately excited DC Motor :-

@ Modulating Control :-

→ Generally transistor choppers are preferred over thyristor because they can

be operated at a much higher frequency (2.5 to 10 kHz) than thyristors (upto 1 kHz)

But because of lower voltage and current ratings of transistors, use of transistors is restricted to 200 kW.

→ For higher ratings, thyristor choppers are used.

→ A transistor chopper controlled separately excited motor drive is shown in fig

A thyristor chopper is obtained when transistor is replaced by a thyristor with a forced commutation circuit.

→ Transistor  $T_y$  is operated periodically with period  $T$  and remains on for a

duration  $T_{ON}$ . present day choppers operate at a frequency which is high enough

to ensure continuous conduction. waveform of motor terminal voltage  $V_a$  and

current  $I_a$  for continuous conduction as shown below.

→ When  $0 \leq t \leq T_{ON}$ , transistor is turned ON. Hence Motor terminal voltage is 'V', Therefore the operation is described by

$$i_a R_a + L_a \left( \frac{di_a}{dt} \right) + E_b = V, \quad 0 \leq t \leq T_{ON}$$

In this interval, armature current increases from  $i_{a1}$  to  $i_{a2}$ . Since motor is connected to the source during this interval, it is called duty interval

→ At  $t = T_{ON}$ ,  $T_y$  is turned off. Motor current freewheels through the diode

$D_f$  and the motor terminal voltage is zero during the interval  $T_{ON} \leq t \leq T$ .

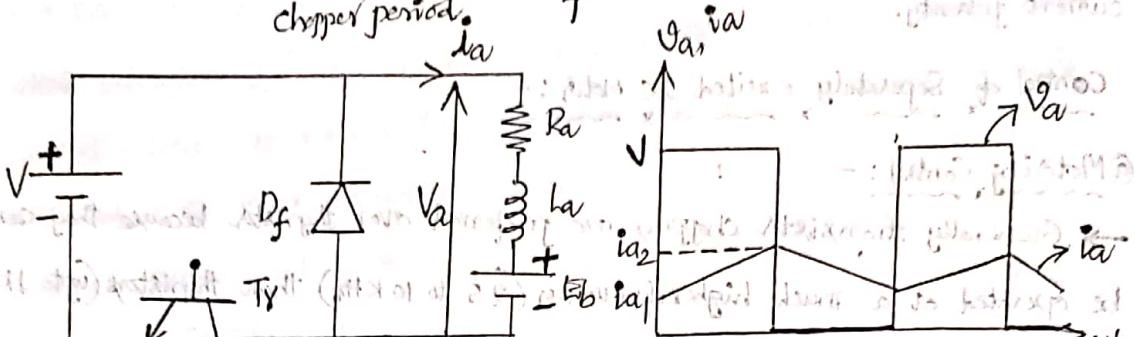
Motor operation during this interval known as freewheeling interval and is described by

$$i_a R_a + L_a \left( \frac{di_a}{dt} \right) + E_b = 0, \quad T_{ON} \leq t \leq T$$

Motor current decreases from  $i_{a2}$  to  $i_{a1}$  during this interval

→ Ratio of duty interval ' $T_{ON}$ ' to chopper period 'T' is called duty ratio (or) duty cycle ( $\delta$ ). Thus

$$\delta = \frac{\text{Duty interval}}{\text{Chopper period}} = \frac{T_{ON}}{T}$$



### Chopper Control of Separately Excited Motor

→ Average output Voltage  $V_a = \frac{1}{T} \int_0^{T_{ON}} V dt = V \left( \frac{T_{ON}}{T} \right) = \delta V$

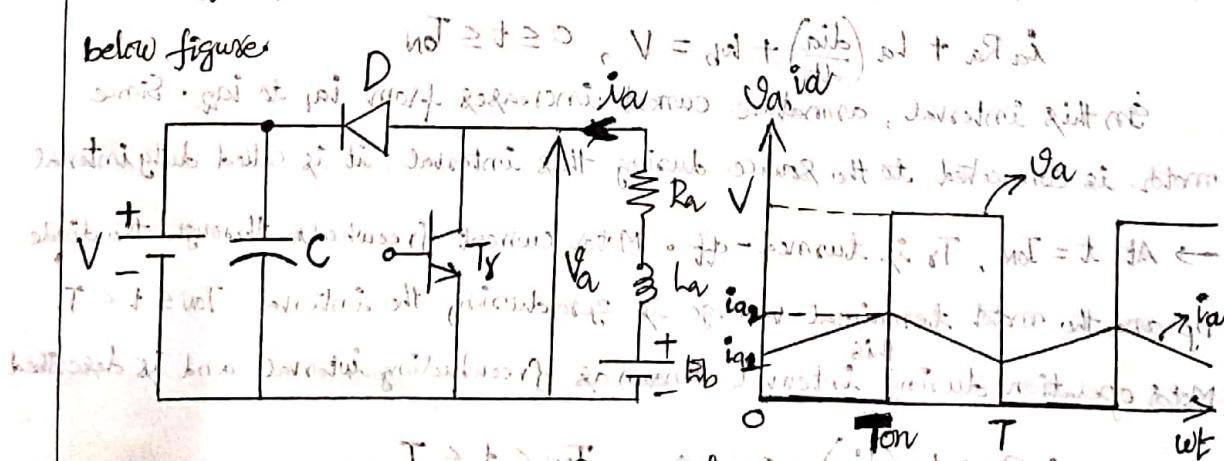
$$\text{Armatures current } I_a = \frac{V_a - E_b}{R_a} = \frac{\delta V - E_b}{R_a}$$

The steady state speed equation is given by

$$\omega = \frac{SV}{K} - \left( \frac{R_a}{K^2} \right) \gamma$$

$$\boxed{\omega = \frac{SV}{K} - \left( \frac{R_a}{K^2} \right) \gamma}$$

Regenerative Braking: → Inherent to alternators but not to DC motors  
→ chopper for regenerative braking and corresponding waveforms are shown in below figure.



Regenerative Braking of Separately excited motor by chopper control

→ When  $T_r$  is ON,  $i_a$  increases from  $i_{a1}$  to  $i_{a2}$ . The mechanical energy converted into electrical by the motor, now working as a generator, partly increases the stored magnetic energy in armature circuit inductance and remainder  $i_a$  dissipated in armature resistor and transistor.

→ When  $T_r$  is OFF, armature current flows through diode 'D' and the source 'V' and the current reduces from  $i_{a2}$  to  $i_{a1}$ . The stored energy and energy supplied by machine is fed to the source.

→ The interval  $0 \leq t \leq T_{ON}$  is called energy storage interval  
 $T_{ON} \leq t \leq T$  is called duty interval

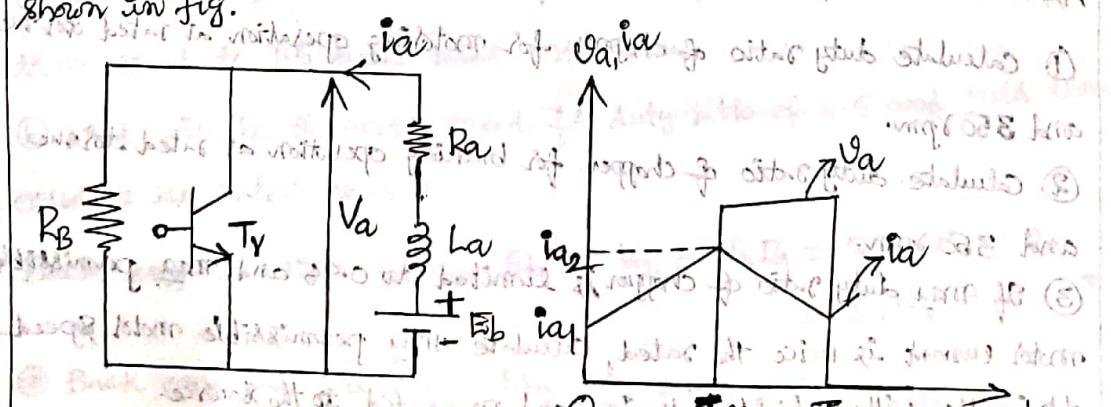
→ The duty ratio is given by

$$S = \frac{\text{Duty interval}}{\text{(2 - Chopper period)}} = \frac{T_{ON}}{T} = \frac{T_{ON}}{T - T_{ON}}$$

$$\rightarrow V_a = \frac{1}{T} \int_{T_{ON}}^T V dt = SV$$

$$\rightarrow I_a = \frac{E_b - V_a}{R_a} = \frac{E_b - SV}{R_a}$$

Dynamic Braking: Dynamic braking circuit and its waveforms are shown in fig.



Dynamic Braking of Separately excited motor by chopper control

→ During the interval  $0 \leq t \leq T_{ON}$ ,  $i_a$  increases from  $i_{a1}$  to  $i_{a2}$ . A part of the generated energy is stored in inductance and the rest is dissipated in  $R_B$  and  $T_R$ .

→ During the interval  $T_{ON} \leq t \leq T$ ,  $i_a$  decreases from  $i_{a2}$  to  $i_{a1}$ . The energies generated and stored in inductance are dissipated.

The effective value of braking resistance  $R_B$  and therefore controls its effective value. If  $i_a$  is assumed to be stepless DC, then energy consumed by  $R_B$  during a cycle of chopper operation is

$$\rightarrow W = I_a^2 R_B (T - T_{ON})$$

→ Average power consumed by  $R_B$

$$P = \frac{W}{T} = \frac{I_a^2 R_B (T - T_{ON})}{T} = I_a^2 R_B (1 - \delta)$$

$$\rightarrow \text{Effective Value of } R_{BE} = \frac{P}{I_a^2} = R_B (1 - \delta) \quad \text{where, } \delta = \frac{T_{ON}}{T}$$

The above equation shows that the effective value of braking resistor can be changed steplessly from 0 to  $R_B$  as controlled from 1 to 0. As the speed falls,  $\delta$  is increased steplessly to brake the motor at a constant torque. A 230V, 960 rpm and 200A separately excited DC motor has an armature resistance of 0.02Ω. The motor is fed from a chopper which provides both motoring and braking operations. The source has a voltage of 230V.

Assume continuous conduction.

① calculate duty ratio of chopper for motoring operation at rated torque and 350 rpm.

② calculate duty ratio of chopper for braking operation at rated torque and 350 rpm.

③ if max duty ratio of chopper is limited to 0.95 and max permissible motor current is twice the rated, calculate max permissible motor speed obtainable without field weakening and power fed to the source.

④ if motor field is also controlled in ③, calculate field current as a fraction of its rated value for a speed of 1200 rpm.

$$E_{b1} = V_a - I_a R_a = 230 - 200 \times 0.02 = 226 \text{ V at } 960 \text{ rpm}$$

$$\textcircled{1} \quad E_{b2} = \frac{N_2}{N_1} \times E_{b1} = \frac{350}{960} \times 226 = 82.4 \text{ V}$$

$$V_{a2} = E_{b2} + I_a R_a = 82.4 + 200 \times 0.02 = 86.4 \text{ V}$$

$$(1/\text{Duty ratio}) = \frac{V}{V_{a2}} \Rightarrow S = \frac{V_{a2}}{V} = \frac{86.4}{230} = 0.376 \text{ or } 37.6\%$$

$$\textcircled{2} \quad V_{a3} = E_{b3} - I_a R_a = 82.4 - 200 \times 0.2 = 78.4 \text{ V}$$

$$S = \frac{V_{a3}}{V} = \frac{78.4}{230} = 0.34 \text{ or } 34\% \text{ (2-1)} = (2 + 34) \text{ or } 134\%$$

$$\textcircled{3} \quad V_{a4} = SV = 0.95 \times 230 = 218.5 \text{ V}$$

$$E_{b4} = V_{a4} + I_a R_a = 218.5 + (2 \times 200 \times 0.02) = 226.5 \text{ V}$$

$$\text{Max permissible motor speed} = \frac{226.5}{226} \times 960 = 962 \text{ rpm}$$

Neglect the losses in the chopper, power fed to the source.

$$P = V_a I_a = 218.5 \times (2 \times 200) = 87.4 \text{ kW}$$

$$\textcircled{4} \quad \phi \propto \frac{1}{N} \quad \text{Assuming linear magnetic circuit}$$

$$\frac{\phi_2}{\phi_1} = \frac{N_1}{N_2} \Rightarrow \phi \propto I_f \Rightarrow \frac{\phi_2}{\phi_1} = \frac{N_1}{N_2} = \frac{1200}{1200} = 0.8$$

A 230V, 1200 rpm, 15A separately excited motor has an armature resistance of 1.2Ω. Motor is operated under dynamic braking with chopper control. Braking resistance has a value of 2Ω.

① Calculate duty ratio of chopper for motor speed of 1000 rpm and braking torque equal to 1.5 times rated motor torque. Note that motor torque is proportional to current.

② What will be the motor speed for duty ratio of 0.5 and motor torque equal to its rated torque?

$$\textcircled{1} \quad \text{Back emf at } 1200 \text{ rpm, } E_{b1} = V_a - I_a R_a = 230 - 15 \times 1.2 \\ = 212 \text{ V}$$

$$\textcircled{2} \quad \text{Back emf at } 1000 \text{ rpm, } E_{b2} = \frac{N_2}{N_1} \times E_{b1} = \frac{1000}{1200} \times 212 \\ = 176.66 \text{ V}$$

$$R_{BE} = R_B(1 - s)$$

$$R_{BE} = \frac{P}{I_a^2} = \frac{V_a I_a'}{I_a^2} = \frac{V_a}{I_a} = \frac{E_b - I_a R_a}{I_a} = \frac{E_b - I_a R_a}{I_a}$$

$$R_{BE} = \frac{176.66}{1.5 \times 15} - 1.2 = 6.65$$

$$6.65 = 20(1 - s) \Rightarrow (1 - s) = 0.3325 \Rightarrow s = 0.6675$$

$$\textcircled{b} \quad R_{BE} = \frac{E_b - I_a R_a}{I_a} \Rightarrow E_b = R_{BE} I_a + I_a R_a$$

$$E_{b_3} = I_a (R_{BE} + R_a) = I_a [(1-s) R_B + R_a] = \frac{R_{BE}}{s} = \frac{6.65}{0.6675} = 2$$

$$E_{b_3} = 15 [(1 - 0.5) 20 + 1.2] = 168 \text{ V}$$

$$N_3 = \frac{E_{b_3}}{E_b} \times N_1 = \frac{(168)}{212} \times 1200 = 950.94 \text{ rpm} = 951 \text{ rpm}$$

(2008) Q A 220V, 190A DC Series motor has armature and field resistance of 0.03 and 0.02 ohms respectively. Running on no-load as a generator with field winding connected to a separate source, it gave following magnetization characteristic at 500 rpm.

Field current (A)	40	80	120	160	200
Terminal voltage (V)	52	108	148	176	189

Motor is controlled by a chopper in dynamic braking with va braking resistance of 2 ohms.

- (a) calculate motor speed for an duty ratio of 0.6 and motor current of 160A  
 (b) what will be the motor speed for a duty ratio of 0.75 and motor torque equal to half of rated torque?  
 (c) calculate torque at 100% load at 50% duty ratio

$$T = \frac{C_1 I_f - C_2 R_a}{R_a} = \frac{C_1 I_f}{R_a} = \text{constant}$$

$$V = C_3 I_f + C_4$$

$$C_3 = \frac{C_1}{R_a}$$

$$C_4 = \frac{C_1 R_a}{R_a}$$

- ⑥ A 220V, 70A DC Series motor has combined resistance of armature and field of 0.12Ω. Running on load with the field winding connected to a separate source it gave following magnetization characteristics at 600 rpm:

Field current (A)	10	20	30	40	50	60	70	80
Terminal Voltage (V)	64	118	150	170	184	194	202	210

Motor is controlled by a chopper, with a source voltage = 220V, calculate

- ① Motor speed for a duty ratio of 0.6 and motor current of 60A.
- ② Torque for a speed of 600 rpm and duty ratio of 0.65

A) ①  $V_{a2} = 8V = 132V$

$$E_{b2} = V_{a2} - I_{a2} R = 132 - 60 \times 0.12 = 124.8V = 2V$$

From Magnetization characteristics for  $I_a = 60A$ ,  $E_{b2} = 194V$  at 600 rpm.

$$\text{For } 194V \rightarrow 600 \text{ rpm} \quad N = \frac{600 \times 124.8}{194} = 386 \text{ rpm}$$

②  $V_a = E_b + I_a R_a = 8V$

$$E_b + I_a (0.12) = 0.65 \times 220 = 143$$

$$0.12 I_a = 143 - E_b \quad \text{①}$$

The above equation is a non-linear equation and can be solved

by Trial and error. From Magnetization characteristics

For  $I_a = 70A$ ,  $E_b = 202V$  for 600 rpm

$$600 \text{ rpm} \rightarrow 202V$$

$$\Rightarrow E_b = 400 \times 202 = 134.66V$$

$$20(100+51.0) + 400 \rightarrow E_b \quad \leftarrow 40(600+51) + V = 134.66$$

put  $E_b = 134.66V$  and  $I_a = 70A$  in equation ①

$$0.12 I_a = 8.4, \quad 143 - E_b = 8.34, \quad \therefore L.H.S \approx R.H.S$$

These values balances the equation Hence  $E_b = 134.66$  holds good

$$\gamma = \frac{E_b I_a}{w} = \frac{134.66 \times 70}{\frac{2\pi \times 400}{60}} = 225 \text{ Nm.}$$

- (Q) A DC Series motor of above example is now controlled in regenerative braking by a chopper with a source voltage of 220V.
- (a) Calculate motor speed for a duty ratio of 0.5 and motor braking torque equal to the rated motor torque.
- (b) Calculate maximum allowable motor speed for a max. permissible current of 70A and max. permissible duty ratio of 0.95
- (c) What resistance must be inserted in armature circuit for the drive to run at 1000 rpm without exceeding armature current beyond 70A?
- (d) To what extent the no. of turns in field winding should be reduced to run the motor at 1000 rpm without exceeding the armature current beyond 70A.

$$V_{220} = V_d = \text{f} \cdot V \quad (1)$$

(a)  $V_a = 8V_d = 0.5 \times 220 = 110V$

$$E_b = V_a + I_a R_a = 110 + 70 \times 0.12 = 118.4V$$

for  $I_a = 70A$ ,  $E_b = 202V$  for 600 rpm

$$\frac{202}{118.4} = \frac{2.451}{118.4} \rightarrow N = \frac{118.4}{202} \times 600 = 351.7 \text{ rpm}$$

(b)  $V_a = 8V_d = 0.95 \times 220 = 209V$

$$E_b = V_a + I_a R_a = 209V$$

for  $I_a = 70A$ ,  $E_b = 202V$  for 600 rpm

$$\frac{202}{209} = \frac{2.451}{209} \rightarrow N = \frac{209}{202} \times 600 = 645.7 \text{ rpm}$$

(c) for  $I_a = 70A$ ,  $E_b = 202V$  for 600 rpm

$$600 \text{ rpm} \rightarrow 202V \quad E_b = \frac{1000}{600} \times 202 = 336.67V$$

$$V_{220} = 2.451 \times \frac{1000}{600} \rightarrow E_b = \frac{2.451}{600} \times 202 = 8.12V$$

$$E_b = V_a + (R_a + R_{ext}) I_a \Rightarrow 336.67 = 0.95 \times 220 + (0.12 + R_{ext}) 70$$

$$0.12 + R_{ext} = 1.82 \Rightarrow R_{ext} = 1.7V$$

(d) It is assumed that even after changing field turns  $R_a = 0.12 \Omega$

$$E_b = 8V_d + I_a R_a = 0.95 \times 220 + 70 \times 0.12 = 217.4 \text{ for } 1000 \text{ rpm}$$

$$1000 \text{ rpm} \rightarrow 217.4 \text{ V}$$

$$600 \text{ rpm} \rightarrow E_b = \frac{600}{1000} \times 217.4 = 130.44 \text{ V}$$

Fraction to which the no. of turns in the field are reduced =  $\frac{E_{b2}}{E_{b1}}$

$$= \frac{130.44}{202} = 0.646$$

Q) A DC Series motor of above example is now controlled in dynamic braking.

Available chopper provides a variation in duty ratio from 0.1 to 0.9

(a) Calculate braking resistor so that max. braking speed at the armature current of 70A will be 800 rpm.

(b) Also calculate the max. available motor torque for a speed of 87 rpm with braking resistance as calculated in (a)

(c) For 70A,  $E_b = 202 \text{ V}$  for 600 rpm

$$600 \text{ rpm} \rightarrow 202 \text{ V}$$

$$800 \text{ rpm} \rightarrow E_b = \frac{800}{600} \times 202 = 269.33 \text{ V}$$

$$R_{BE} = \frac{E_b}{I_a} - R_a = \frac{269.33}{70} - 0.12 = 3.73 \Omega$$

For a given value of  $R_B$ , max. value of  $R_{BE}$  is obtained at min. value of 'S'

$R_{BE} = R_B(1 - S_{min})$

$$3.73 = R_B(1 - 0.1) \Rightarrow R_B = 4.14 \Omega$$

(b) For a given speed, torque will be maximum when duty ratio is maximum

Total Armature circuit resistance at max. duty ratio,  $S_{max}$

$$R_T = R_B(1 - S_{max}) + R_a = 4.14(1 - 0.9) + 0.12 = 0.534 \Omega$$

$$E_b = I_a R_T \quad \text{and} \quad 217.4 = 214 \times 0.534$$

Equation 1 must be satisfied for a speed of 87 rpm.

(c) A 230V, 960 rpm, 200A separately excited DC motor has an armature resistance of 0.02 Ω. The source voltage = 230V. It is operated in dynamic braking with chopper control with a braking resistor of 2 Ω

(1) calculate duty ratio of chopper for a motor speed of 600 rpm and braking torque of twice the rated value.

- ② What will be the motor speed for a duty ratio of 0.6 and motor torque equal to twice its rated torque.

(A) ①  $E_b \text{ at } 600 \text{ rpm} = \frac{600}{960} \times 226 = 141.25 \text{ V}$

$$R_{B5} = (1-S)R_B = \frac{E}{I_a} - R_a$$

$$(1-S) \times 2 = \frac{141.25}{2 \times 200} - 0.02 \Rightarrow S = 0.83$$

②  $E = I_a [(1-S)R_B + R_a] = 2 \times 200 [(1-0.6) \times 2 + 0.02] = 328 \text{ V}$

$$\text{Speed} = \frac{328}{226} \times 960 = 1393.3 \text{ rpm}$$

(\*) Trying various values of  $I_a$  and the value of corresponding

$E$  (at 87 rpm = 26.68 V) obtained from magnetization

characteristics gave an approximate solution of  $I_a = 50 \text{ A}$

$$\text{At } 50 \text{ A}, K_a \phi = \frac{184}{600 \times \left(\frac{2\pi}{60}\right)} = 2.928$$

$$T = (K_a \phi) I_a = 2.928 \times 50 = 146.4 \text{ Nm}$$

- (Q) A dc shunt motor takes a current of 50 A on a 440 V supply which runs at a speed of 1000 rpm with  $R_a = 0.5 \Omega$  &  $R_{sh} = 100 \Omega$ . A chopper is used to control the speed of the motor in the range of 400-800 rpm having a constant torque. The on-period of the chopper is 2 ms with its field supply voltage from 440 V. Determine the range of frequencies of the chopper.

(A)  $E_b \text{ at } 1000 \text{ rpm} = 440 - 456 \times 0.5 = 414.4 \text{ V}$ ,  $I_f = \frac{440}{100} = 4.4 \text{ A}$

①  $E_b \text{ at } 400 \text{ rpm} = \frac{400}{1000} \times 415 = 166.8 \text{ V}$ ,  $I_a = 50 - 4.4 = 45.6 \text{ A}$

$$V = 166.8 + 456 \times 0.5 = 189.68 \text{ V}$$
,  $f = \frac{V_0}{V} = \frac{189.68}{440} = 0.431 = \frac{T_{on}}{T} = f_{on}$

$$f_1 = \frac{0.431}{T_{on}} = \frac{0.431}{2 \times 10^{-3}} = 215.5 \text{ Hz}$$

②  $E_b \text{ at } 800 \text{ rpm} = 333.76 \text{ V}$

$$V = 333.76 + 456 \times 0.5 = 356.56 \text{ V}$$

$$f = \frac{356.56}{440} = 0.81 = \frac{T_{off}}{T} \Rightarrow f_2 = \frac{0.81}{2 \times 10^{-3}} = 405 \text{ Hz}$$

Range of freq is  $215.5 \text{ Hz} \leq f \leq 405 \text{ Hz}$