

David Maloney

ME 221 Applied Thermodynamics
Fall 2010

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D.44

A fuel oil has the following specifications:

$$H/C = 1.7$$

$$MW = 200 \text{ kg/kmol}$$

$$LHV_{\text{liquid}} = 42.5 \times 10^3 \text{ kJ/kg}$$

$$\text{Heat of vaporization} = 230 \text{ kJ/kg}$$

- Find the thermodynamically representative formula for the fuel, C_xH_y
- Find the **stoichiometric** air-to-fuel ratio, A/F_{st} .
- Find the heat of formation of **liquid** fuel oil (kJ/kmol)
- Find the heat of formation of **gaseous** fuel oil (kJ/kmol)

$$C_xH_y = C_{14.6}H_{24.82}$$

$$C_{14.6}H_{24.82} + a(O_2 + 3.76N_2) = bH_2O + 14.6CO_2 + dN_2$$

$$200 = 12(x) + 1(1.7x)$$

$$O_2: a = \frac{b}{2} + 14.6 \quad a = 20.81$$

$$H: 24.82 = 2b$$

$$\left(\frac{A}{F}\right)_{st} = \frac{20.81(4.76)(29)}{200} = 14.36$$

$$\bar{h}_{f,CxHy}^\circ: LHV = \sum_R n_i \bar{h}_i^\circ - \sum_P n_i \bar{h}_i^\circ$$

$$42.5 \times 10^3 \frac{\text{kJ}}{\text{kg}} (200 \text{ kg/kmol}) = \bar{h}_{f,CxHy}^\circ - 14.6 \bar{h}_{f,H_2O}^\circ - 12.41 \bar{h}_{f,H_2O}^\circ$$

$$8.5 \times 10^4 \frac{\text{kJ}}{\text{kmol}} = \bar{h}_{f,CxHy}^\circ - 14.6(-393,520) - 12.41(-241,820)$$

$$\bar{h}_{f,CxHy,l}^\circ = -246,378 \frac{\text{kJ}}{\text{kmol}}$$

$$\bar{h}_{f,CxHy,g}^\circ: \bar{h}_{f,l}^\circ = \bar{h}_{f,g}^\circ - \bar{h}_{fg}$$

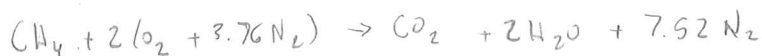
$$\bar{h}_{f,g}^\circ = -246,378 + 230(200)$$

$$\bar{h}_{f,g}^\circ = -184,700$$



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D.45 A constant volume vessel is charged with a stoichiometric mixture of methane and air. The total pressure is 0.1 MPa and the temperature is 298 K before combustion. Combustion then occurs and the products are cooled to 1000 K. Assume complete combustion. Determine the final pressure and the heat released in kJ per kmol of fuel.



$$-Q = \sum_p n_i (\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_i - \sum_R n_i (\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_i$$

$$Q = (\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{CO}_2} + 2(\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{H}_2\text{O}}$$

$$+ 7.52(\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{N}_2} - (\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{CH}_4}$$

$$- 2(\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{O}_2} - 7.52(\bar{h}_f^\circ + \Delta\bar{h} - R_u T)_{\text{N}_2}$$

Prod	$\bar{h}_f^\circ$	$\Delta\bar{h} < 1000 \text{ K} >$	R
CO ₂	-393,520	42769 - 9364	
H ₂ O	-241,820	35852 - 9904	
N ₂	0	31359 - 8682	
CH ₄	-74850	0	6
O ₂	X	0	0
N ₂	X	0	0

$$\bar{Q} = -368429 - 448312 + 108235 + 77328 + 2479 + 18631$$

$$\bar{Q} = -6.1 \times 10^5 \text{ kJ/kmol f}$$

$$P_f = \frac{n_f R_u T_f}{V} \quad P_i = \frac{n_i R_u T_i}{V} \quad P_f = P_i \left(\frac{n_f}{n_i} \right) \left(\frac{T_f}{T_i} \right)$$

$$n_f = 1 + 2 + 7.52 = 10.52 \quad n_i = 1 + 2(4.76) = 10.52$$

$$P_f = 0.1 \text{ MPa} \left(\frac{10.52}{10.52} \right) \left(\frac{1000}{298} \right)$$

$$P_f = 0.336 \text{ MPa}$$

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D.42 Propane, C_3H_8 , and air undergo rich combustion ($\phi > 1$) and produce products consisting of CO_2 , CO , H_2O , H_2 and N_2 . Using a **dry gas analysis**, the following product composition is measured:

Product	Volume Percent
CO_2	11.41%
CO	3.355%

For these conditions, find:

- The **stoichiometric** fuel-to-air ratio, F/A_{st} , for propane (C_3H_8).
- The **actual** fuel-to-air ratio, F/A_{act} , given the species and product concentrations shown above.
- The **equivalence ratio**.
- If 5 kg of fuel are consumed, how much mass of water (kg) is produced in the actual combustion reaction?

$$a) C_3H_8 + a(O_2 + 3.76N_2) \rightarrow bCO_2 + cH_2O + dN_2 +$$

$$C: 3 = b \quad O_2: a = b + \frac{1}{2}c \quad \frac{F}{A}_{st} = \frac{(12(3) + 8)}{5(4.76)(29)} = \boxed{.0638}$$

$$H_2: 4 = c \quad a = 3 + \frac{1}{2}c = 5$$

$$b) aC_3H_8 + b(O_2 + 3.76N_2) \rightarrow 11.41CO_2 + 3.355CO + cH_2 + 3.76bN_2 + eH_2O$$

$$C: 3a = 11.41 + 3.355 \quad a = 4.922$$

$$H_2: 4a = c + e \quad e = 19.688 - c$$

$$O_2: b = 11.41 + \frac{3.355}{2} + \frac{e}{2} =$$

$$\frac{F}{A_{act}} = \frac{a(44)}{22.9(29)(4.76)} = \boxed{.0701}$$

dry analysis: $11.41 + 3.355 + e + 3.76b = 100$

$$\phi = \frac{F/A_{act}}{F/A_{st}} = \frac{.0701}{.0638} = \boxed{\phi = 1.10}$$

$$c = 1.12 \quad e = 18.57$$

$$b = 27.37$$

$$\frac{5 \text{ kg}}{44 \text{ kg/kmol}} = .1136 \text{ kmol} \quad \frac{18.57 \text{ kmol } H_2O}{4.922 \text{ kmol } C_3H_8} \Rightarrow .4544 \text{ kmol } H_2O (18 \text{ kg/kmol}) = \boxed{7.715 \text{ kg } H_2O}$$

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BOOK PROBLEM



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D.43 Ethanol (C_2H_6O) is used to fuel an engine. The engine operates slightly rich ($\phi > 1.0$). A dry exhaust gas analysis is made with the following mole fraction results:

$$y_{CO} = 0.0489$$

$$y_{CO_2} = 0.1177$$

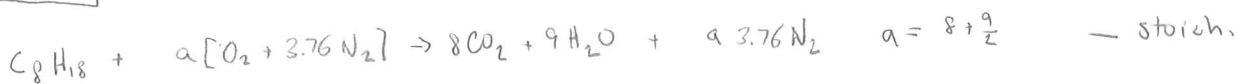
Other combustion products include H_2O , N_2 and H_2 .

- Find the balanced, stoichiometric reaction for 1 kmol of ethanol.
- Find the balanced, actual reaction for 1 kmol of ethanol.
- Find the fuel to air ratio for the actual reaction
- Find the equivalence ratio

15.59

find $\bar{Q}$

$$C_2H_6O \quad 25^\circ C, \quad \bar{h}_f^\circ = -208,450 \quad \text{kJ/kmol}$$



$$\bar{Q} = \sum N_P (\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_P - \sum N_R (\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_R$$

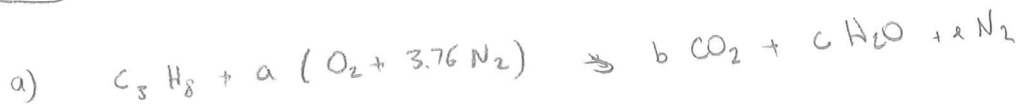
$$= 8(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{CO_2} + 9(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{H_2O} + 94(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{N_2} + 12.5(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{O_2} \\ - (\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{C_2H_6O} - 25(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{O_2} - 94(\bar{h}_f^\circ + \bar{h} - \bar{h}_o)_{N_2}$$

$$= 8(-393,520 + 19,029 - 9364) + 9(-241,820 + 17,887 - 9904) + (12.5)(0 + 15,708 - 8682) + (94)(0 + 15,469 - 8669) \\ - 1(-208,450) - 0 - 0$$

$$\bar{Q} = -4,239,880 \text{ kJ/kmol } C_2H_6O$$

$$Q = \frac{\bar{Q}}{m_{fuel}} = \frac{(-4,239,880 \text{ kJ/kmol})}{114 \text{ kg/kmol}} = \boxed{-37,200 \text{ kJ/kg } C_2H_6O}$$

D 40 | C_3H_8 equivalence ratio 0.9



$$\begin{aligned} C: 3 &= b & b &= 3 \\ H: 8 &= 2c & c &= 4 \\ O: 2a &= 2b + c & & \\ N_2: 3.76a &= d & d &= 18.8 \\ & & a &= 5 \end{aligned}$$



MW $C_3H_8 = 36 + 8$ Air = 29

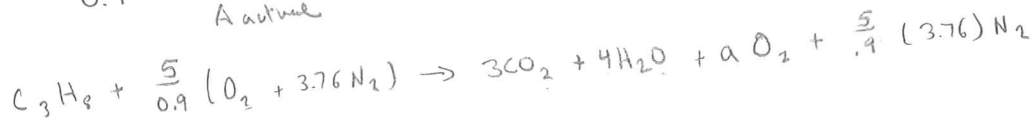
$$\frac{F}{A_{st}} = \frac{(36 + 8)}{5(4.76)(29)} = \boxed{.0638}$$

b) find actual combustion reaction

$$\phi = .9 =$$

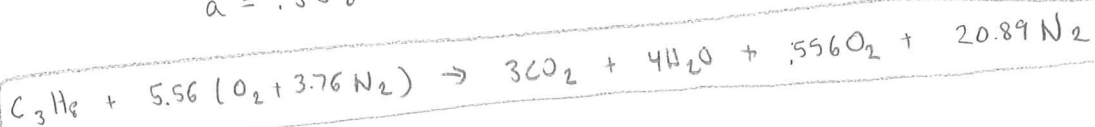
$$\frac{F/A_{actual}}{F/A_{st}} = \frac{(F/\phi)_{st}}{(A/\phi)_{actual}}$$

$$0.9 = \frac{A_{st}}{A_{actual}} \quad A_{act} = \frac{A_{st}}{0.9}$$



$$O_2: \frac{5}{.9} = 3 + 2 + a$$

$$a = .556$$



D. 41 | Natural gas $C_n H_{3.8n} N_{0.1n}$ MW=18

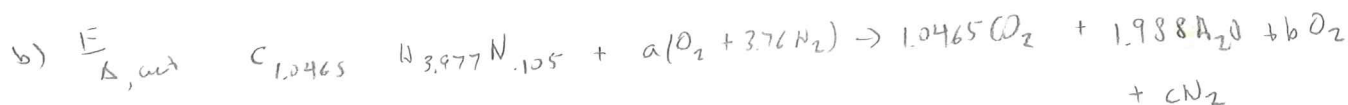
dry gas analysis $y_{O_2} = 0.1$

a) $\frac{F}{A}_{st} \quad C_n H_{3.8n} N_{0.1n} \Rightarrow 12n + 3.8n + 14(0.1)n = 18 \quad n = 1.0465$



$$O_2 \text{ bal: } a = 1.0465 + \frac{1}{2} \left(\frac{3.977}{2} \right) = 2.04$$

$$\frac{F}{A}_{st} = \frac{18}{2.04(4.76)(29)} = \boxed{.0639}$$



$$N_2: c = \frac{1}{2}(.105) + 3.76a$$

$$O_2: a = 1.0465 + \frac{1}{2}(1.988) + b \Rightarrow a = 2.0405 + b$$

$$y_{O_2} = \frac{b}{(1.0465 + b + 3.76a + \frac{1}{2}(.105))} = 0.1$$

$$b = 0.1(1.0465 + b + 7.672 + 3.76b + .0525)$$

$$0.9246 = .8771 \Rightarrow b = 1.674, a = 3.714$$

$$\frac{F}{A}_{act} = \frac{18}{(3.714)(4.76)(29)} = .0351$$

c) m_{CO_2} for 1 kg Nat-gas $1 \text{ kg } C_x H_y N_z \left(\frac{1 \text{ kmol fuel}}{18 \text{ kg}} \right) \left(\frac{1.0465 \text{ kmol } CO_2}{1 \text{ kmol fuel}} \right) \left(\frac{44 \text{ kg } CO_2}{1 \text{ kmol } CO_2} \right)$

$$m_{CO_2} = \boxed{2.558 \text{ kg}}$$

David Maloney

15-20, 25

(75% extra air)

10

20) Propane C_3H_8 & air complete combustion. find A/F ratio



balance:

C: $3 = b$

H₂: $8 = 2c$

O₂: $a = b + \frac{1}{2}c$ $a = 3 + \frac{1}{2}(4) = 5$

N₂ $3.76a = d$ $d = 1.33$

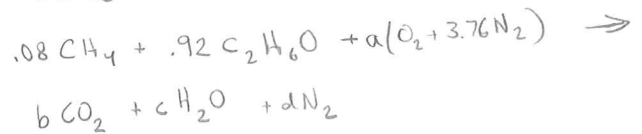
mw	
$C_3H_8 = 36 + 8 = 44$	$CO_2 = 44$
air = 29	$H_2O = 18$
$(A/F)_{stoich} = \frac{29(5)(4.76)}{3(44)} = 15.69$	

$(A/F)_{actual} = 1.75(15.69) = \boxed{27.46}$

25)

CH_4	mw 16	mf .2	y _i .08
C_2H_6O	46	.8	.92
mix	40		

balance



C: $.08 + .92(2) = b$ $b = 1.92$

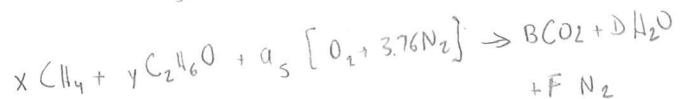
H₂: $.08(2) + .92(6) = 2c$ $c = 2.92$

O: $.92 + 2a = 2b + c$ $a = 2.92$

find A/F ratio = $\frac{2.92(4.76)(29)}{(.08 + .92)(40)} = 10.25$

$\dot{M}_{fuel} = 31 \text{ kg/s}$

$\dot{M}_{air} = 10.25(31) = 318 \text{ kg/s}$



C:	$x + 2y = b$	$b = 1.582$	$x = .4$
H	$4x + 6y = 2d$	$d = 2.582$	$y = .5818$
O	$2a_s + y = 2b + d$	$f = 9.708$	$a_s = 2.582$
N ₂	$3.76a_s = f$		

$A/F = \frac{(2.582)(4.76)(29)}{(.4182)(12 + 4) + (.5818)(24 + 6 + 16)} = 10.64 \frac{\text{kg A}}{\text{kg F}}$

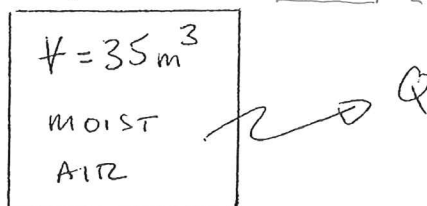
$\dot{M}_{air} = A/F \dot{M}_{fuel} = 10.64(31) = \boxed{330 \text{ kg/s}}$

- D.39 Air and water vapor are contained in a constant volume vessel with a volume of 35 m^3 at 150 kPa , 120°C and a relative humidity of 9.548% (state 1). This system is cooled at a constant total volume until the temperature reaches 20°C . T_2

$$PV = mRT$$

$$Pv = RT$$

$$v = \frac{RT}{P}$$



- Find the partial pressure of the water vapor at state 1, P_{v1} .
- Find the temperature at which condensation begins.
- Find the mass of the vapor at state 1, m_{v1} .
- Find the mass of the vapor at state 2, m_{v2} . You may assume that any volume taken up by the liquid water at this state is negligible (i.e. the volume of the water vapor-air mixture at state 2 is still 35 m^3).
- Find the total heat transfer for the system between state 1 and state 2.

$$a) \quad \phi = .09548 = \frac{P_v}{P_g(T_1)} \quad P_g(T_1) = 198.67 \Rightarrow P_{v1} = 18.97 \text{ kPa}$$

$$b) \quad T_{DP}: \quad v_{v1} = v_g \quad v_{v1} = \frac{R_v T_1}{P_{v1}} = \frac{.4615(120+273)}{18.97} \quad v_{v1} = 9.561 \text{ m}^3/\text{kg} \Rightarrow T_{DP} = 55^\circ\text{C}$$

$$c) \quad m_{v1} = \frac{P_{v1} V}{R_v T_1} = \frac{18.97(35)}{.4615(393)} = 3.661 \text{ kg}$$

$$d) \quad m_{v2}: \quad P_{v2} = P_{sat}(20^\circ\text{C}) = 2.339 \quad \frac{P_{v2} V}{R_v T_2} = \frac{2.339(35)}{.4615(293)} = .6054 \text{ kg}$$

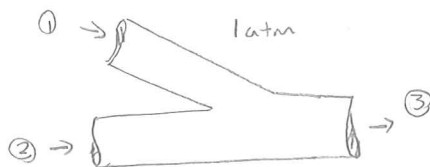
$$e) \quad Q = m_{v2} u_{v2} + m_{a2} u_{a2} - m_{v1} u_{v1} + m_a (u_2 - u_1)$$

$$.6054(2402) + 3.056(83.91) - 3.661(2529) + 40.66(0.718)(-100)$$

$$m_a = \frac{P_a V}{R_a T_1} = \frac{(150-18.97)(35)}{.2870(393)} = 40.66 \text{ kg}$$

$$Q = -10470 \text{ kJ}$$

14.107



① 32°C	② 12°C	③
$\phi = 40\%$	$\phi = 90\%$	ω_3
$\dot{V} = 20 \text{ m}^3/\text{min}$	$\dot{V} = 25 \text{ m}^3/\text{min}$	ϕ_3
$h = 62 \text{ kJ/kg}$	$h = 32 \text{ kJ/kg}$	T_3
$\omega_1 = .0123 \text{ kg/kg}$	$\omega_2 = .008$	$\dot{V} = ?$
$v_1 = .88 \text{ m}^3/\text{kg}$	$v_2 = .818$	

$$\dot{Q} - \dot{W} = \dot{m}_{a3} h_{a3} + \dot{m}_{v3} h_{v3} - \dot{m}_{a1} h_{a1} - \dot{m}_{v1} h_{v1} - \dot{m}_{a2} h_{a2} - \dot{m}_{v2} h_{v2}$$

$$\dot{m}_{a3} (h_3 + \omega_3 h_3) - \dot{m}_{a1} (h_1 + \omega_1 h_1) - \dot{m}_{a2} (h_2 + \omega_2 h_2)$$

Cons. mass: $\dot{m}_{a3} = \dot{m}_{a1} + \dot{m}_{a2}$ $\dot{m}_{v3} = \dot{m}_{v2} + \dot{m}_{v1}$ $\dot{m}_{a3} \omega_3 = \dot{m}_{a2} \omega_2 + \dot{m}_{a1} \omega_1$

$$\omega_3 = \frac{\dot{m}_{a2} \omega_2 + \dot{m}_{a1} \omega_1}{\dot{m}_{a3}} \quad \dot{m}_{a1} = \frac{\dot{V}_1}{v_1} = \frac{20 \text{ m}^3/\text{min} (1 \text{ min}/60 \text{ s})}{.88 \text{ m}^3/\text{kg}} = .3788 \text{ kg/s}$$

$$\dot{m}_{a2} = \frac{25}{.818 (60)} = .5094 \text{ kg/s} \quad \dot{m}_{a3} = .8882 \text{ kg/s}$$

$$\omega_3 = .0097$$

$$\phi_3 = \frac{p_{v3}}{p_3 - p_{v3}} \quad p_3 - T_3 = 2.339 \text{ Chart.}$$

$$.3788 ((62)(1 - .012) + .5094 (32)(1 - .008) = .8882 (h_3 (1 - .0097)))$$

$$h_3 = 44.76 \text{ kJ/kg dry air} \quad T_3 = 20^\circ \text{C}$$

$$\phi_3 = 65\%$$

$$v_3 = .845 \text{ m}^3/\text{kg dry air}$$

$$.845 (.8882) = .7505 \text{ m}^3/\text{s} \Rightarrow 45.03 \text{ m}^3/\text{min}$$

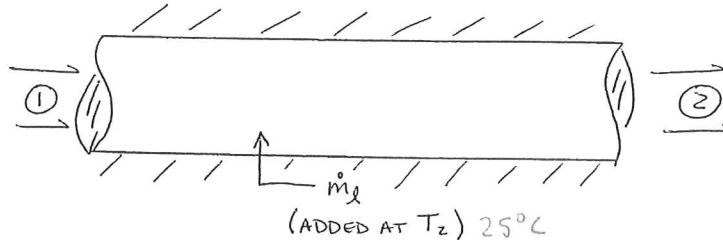
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D.37 Hot air at 40 °C with 10% relative humidity passes through an adiabatic evaporative cooler. Water is added as the air passes through a series of wicks and the mixture exits at 25 °C.

$$\begin{aligned} T_1 &= 40^\circ\text{C} \\ P_1 &= 100 \text{ kPa} \\ \phi_1 &= 0.1 \end{aligned}$$



$$\begin{aligned} P_2 &= P_1 \\ T_2 &= 25^\circ\text{C} \\ \phi_2 &= ? \end{aligned}$$

- Find the humidity ratio at state 1, ω_1
- Find the humidity ratio leaving the evaporative cooler, at state 2, i.e. ω_2
- Find the relative humidity leaving the evaporative cooler, at state 2, i.e. ϕ_2
- Find the mass flow rate of the liquid water added relative to the flow of dry air, i.e. $\frac{\dot{m}_l}{\dot{m}_{\text{air}}}$

$$a) \quad \phi = \frac{P_v}{P_g} \quad P_g(40^\circ\text{C}) = 7.385 \Rightarrow P_v = .7385 \quad \omega_1 = .622 \left(\frac{.7385}{100 - .7385} \right) = .004628$$

$$b) \quad \dot{Q} = \dot{m}_A h_{A2} + \dot{m}_V h_{V2} - \dot{m}_A h_{A1} - \dot{m}_V h_{V1} - \dot{m}_l h_l$$

$$h_{A2} - h_{A1} + \omega_2 h_{V2} - \omega_1 h_{V1} - \frac{\dot{m}_l}{\dot{m}_A} h_l$$

$$0 = h_{A2} - h_{A1} + \omega_2 (h_{V2} - h_l) - \omega_1 (h_{V1} - h_l)$$

$$1.005(25 - 40) + \omega_2 () - .004628(2574 - 104.8)$$

$$\begin{aligned} \dot{m}_l &= \dot{m}_{V2} - \dot{m}_{V1} & h_l &= 104.8 \\ \frac{\dot{m}_l}{\dot{m}_A} &= \omega_2 - \omega_1 & h_{V1} &= 2574 \\ & & h_{V2} &= 2547 \end{aligned}$$

$$\omega_2 = .01085$$

$$c) \quad \phi_2 = \frac{P_v}{P_g(T_2)} \quad \frac{P_v}{100 - P_v} = \frac{\omega}{.622} \quad P_v = (100 - P_v)(.01744) \Rightarrow 1.744 = .P_v(1.01744) \quad P_v = 1.714$$

$$P_g(25) = 3.170 \Rightarrow \phi = 23.21\%$$

Ans:

$$\phi = .5047$$

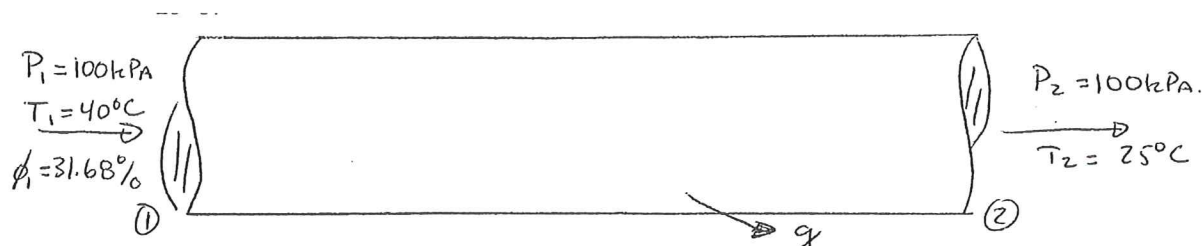
$$d) \quad \frac{\dot{m}_l}{\dot{m}_A} = \omega_2 - \omega_1 = .01085 - .004628 = .00622$$

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D.38

A flow of moist air at 100 kPa, 40 °C and a relative humidity of 31.68% enters a constant pressure, steady flow device. This moist air is cooled in the device to an exit temperature of 25°C.



- Find the humidity ratio, ω_1 , of the entering flow. (kg vapor per kg dry air)
- Find the dew point temperature given the inlet conditions. Will water condense?
- Find the humidity ratio, ω_2 , of the exiting flow. (kg vapor per kg dry air)
- Find the specific heat transfer (kJ/kg dry air) required to cool the flow from the entering conditions to the exiting conditions.

$$a) \quad \omega_1 = 0.622 \phi \left(\frac{P_v}{P - P_v} \right) \quad \begin{matrix} P_g < 40^\circ\text{C} > = 7.385 \\ P_A = 100 \text{ kPa} \end{matrix} \quad P_v = \phi P_g = 2.3396 \quad \boxed{\omega_1 = .0149}$$

$$b) \quad T_{DP} = P_{Sat} = P_v = \boxed{20^\circ\text{C}} \quad \boxed{\text{Will not condense}}$$

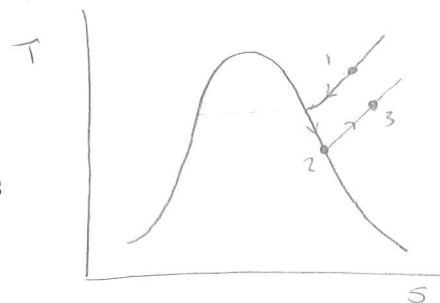
$$c) \quad \omega_2 = \omega_1 = \boxed{.0149}$$

$$d) \quad \dot{Q} - \dot{W} = \dot{m}_{a_2} h_{a_2} + \dot{m}_{v_2} h_{v_2} - \dot{m}_{a_1} h_{a_1} - \dot{m}_{v_1} h_{v_1}$$

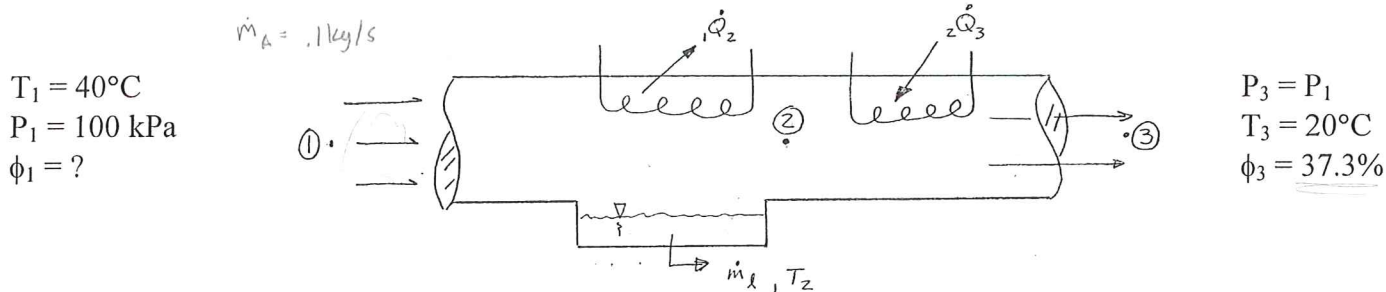
$$\frac{\dot{Q}}{\dot{m}_a} = (h_{a_2} - h_{a_1} + \omega(h_{v_2} - h_{v_1}))$$

$$q = 1.005(25 - 40) + .0149(1.8723)(25 - 40)$$

$$\boxed{q = -15.49 \frac{\text{kJ}}{\text{kg}} \text{ dry air}}$$



- D.35 A dehumidifying/heating unit operates at a steady state as shown below. The inlet conditions are 40°C , 100 kPa . The dry air mass flow rate is 0.1 kg/s . The moist air then passes over a cooling coil and some water is condensed. The condensate leaves the unit at T_2 at $\dot{m}_l = 0.00288\text{ kg/s}$. The moist air then passes through a heating unit, exiting at 20°C , 100 kPa and 37.3% relative humidity.



- Find the humidity ratio at state 3, ω_3
- Find the temperature of the moist air at state 2 (leaving the dehumidifier and entering the heater).
- Find the humidity ratio entering the unit, state 1. ω_1
- Find the relative humidity entering the unit, state 1.
- Find the rate of heat transfer across the entire unit, $\dot{Q}_3$ (kJ/s).

$$a) \omega_3 = .622 \left(\frac{P_{V_3}}{P - P_{V_3}} \right) \quad \phi = .373 = \frac{P_{V_3}}{P_g(T_3)} \quad P_g(T_3) = 2.3392 \quad P_{V_3} = .8725$$

$$\omega_3 = .00548$$

$$b) T_2 = T_{sat}(P_{V_2}) = T_{wher} P_3 = P_g$$

$$T_2 = 15^\circ\text{C}$$

$$\dot{Q}_{in} = \dot{m}_{A2} h_{A2} + \dot{m}_{V2} h_{V2} + \dot{m}_l h_l - \dot{m}_A h_{A1} - \dot{m}_V h_{V1}$$

$$\dot{m}_l = \dot{m}_{V1} - \dot{m}_{V3}$$

$$\frac{\dot{Q}_{in}}{\dot{m}_A} = h_{A2} + \omega_2 h_{V2} + \frac{\dot{m}_l}{\dot{m}_A} h_l - h_{A1} - \omega_1 h_{V1}$$

$$\frac{\dot{m}_l}{\dot{m}_A} = \omega_1 - \omega_3$$

$$\omega_1 = \frac{.00288}{.1} + .00548 = .03428$$

c)

$$d) \phi_1 = \frac{P_{V1}}{P_g(T_1)}$$

$$P_g(T_1) = 7.3851$$

$$\phi_1 = 70.72\%$$

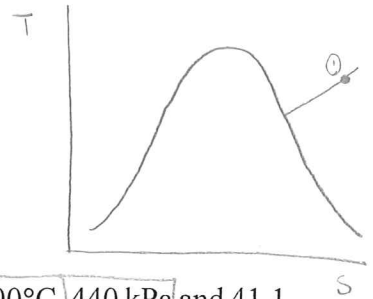
$$.03428 = \frac{P_V}{P - P_V} (.622)$$

$$(100 - P_V) .05511 = P_V$$

$$P_V = 5.223$$

$$100 (.05511) = 1.05511 P_V$$

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D.36 A closed rigid tank having a volume of 3 m^3 initially contains moist air at 100°C , 440 kPa and 41.1% relative humidity. Neglect the volume of any liquid that might be present in your calculations below.

- Find the temperature at which condensation begins as the tank is cooled.
- If the tank is cooled to 80°C , determine the final tank pressure (kPa). (Assume no condensation) $\rightarrow 353 \text{ K}$
- If the tank is cooled to 20°C , determine the mass of water condensed out.

$$a) \quad \phi = 41.1\% \quad \text{Before sat, } P_v = \text{const} \quad .411 = \frac{P_{v1}}{P_{s(T_1)}} = \frac{P_{v1}}{101.4 \text{ kPa}} \Rightarrow P_{v1} = 41.68 \text{ kPa}$$

$$T_{\text{DP}} = 76.75^\circ\text{C}$$

$$b) \quad P = P_v + P_a = \frac{m_v R_v T}{V_1} + \frac{m_a R_a T}{V_1}$$

$$= \frac{.7264 (.4615)(353 \text{ K})}{3} + \frac{11.16 (.2870)(353)}{3}$$

$$m_v = \frac{P_v V}{R_v T} = \frac{41.68 (3 \text{ m}^3)}{.4615 (373 \text{ K})} = .7264 \text{ kg}$$

$$m_a = \frac{P_a V}{R_a T} = \frac{(440 - 41.68) (3)}{.2870 (373)} = 11.16 \text{ kg}$$

$$P_{(80^\circ\text{C})} = 416.3 \text{ kPa}$$

$$c) \quad P_{s(20^\circ\text{C})} = 2.3392 \text{ kPa} \quad \phi = 1 \Rightarrow P_v = 2.339$$

$$m_v = \frac{P_v V}{R_v T} = \frac{2.339 (3)}{.4615 (293)} = .05189$$

$$m_v - m_{v1} = m_l = .7264 - .05189$$

$$m_l = .6745 \text{ kg}$$

▷ 35 (continued)

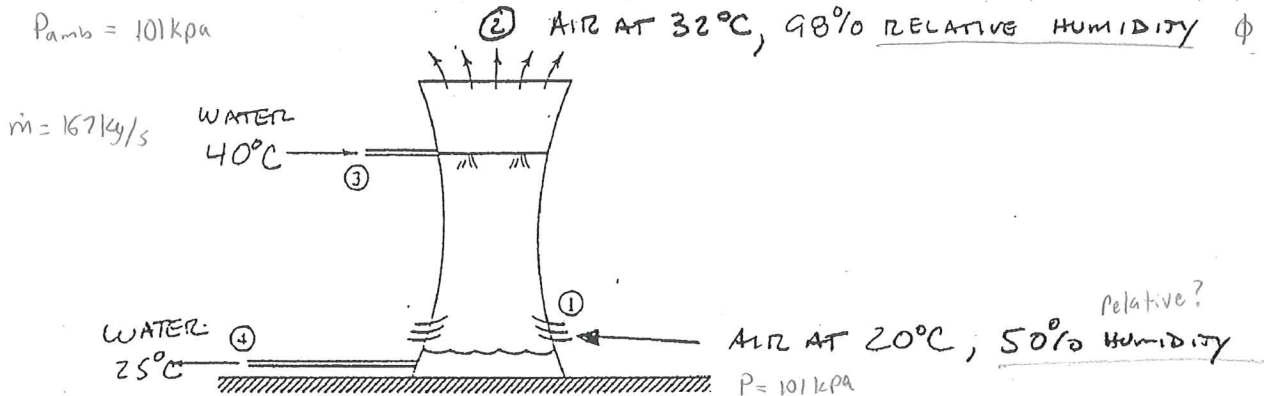
$$\frac{\dot{Q}_{in}}{\dot{m}_a} = (h_{A2} - h_{A1}) + \frac{\dot{m}_g h_g}{\dot{m}_a} + \omega_3 h_{v3} - \omega_1 h_{v1}$$

$$+ c_{p_A}(T_2 - T_1) +$$

$$\dot{Q}_{in} = \left[1.005(20 - 40) + \frac{.00288(2102)}{.1} + .00548(2537) - .03428(2574) \right] 0.1$$
$$[-20.1 + .6054 + 13.90 - 88.24] 0.1$$

$$\dot{Q} = -9.383 \text{ kW/s}$$

D.34 A "cooling tower" is used to remove heat from the condenser water of a power plant. Water enters at point 3 at 167 kg/s and 40°C and is sprayed in the upward flowing air. Liquid water is collected and leaves the system at point 4 at 25°C. The inlet air conditions at point 1 and outlet air conditions at point 2 are given. You may assume the tower is adiabatic and ambient pressure is 101 kPa. Also, treat the water vapor as an ideal gas.



- Find the humidity ratio at points 1 and 2 (i.e. ω_1 and ω_2).
- Find the mass flow rate of dry air through the cooling tower. You may assume constant specific heats for air.
- Find the mass flow of water that leaves at point 4.

$$a) \quad \omega_1 = .622 \left(\frac{P_v}{P - P_v} \right) \quad \omega_2 = \phi \cdot .622 \frac{P_g}{P_a} \quad \phi = .98, P_a = .02(101)$$

$$P_v = (0.5) P_{sat, < 20^\circ \text{C} >} = .5(1.17) \Rightarrow \omega_1 = .622 \left(\frac{1.17}{101 - 1.17} \right) = \boxed{0.0073}$$

$$(.98) P_{sat, < 32^\circ \text{C} >} \quad \omega_2 = .622 \left(\frac{4.66}{101 - 4.66} \right) = \boxed{0.03}$$

$$\dot{m}_A = \dot{m}_{A_2} = \dot{m}_a$$

$$b) \quad \dot{Q} - \dot{W} = \dot{m}(h_o - h_{in}) = [\dot{m}_{A_2} h_{A_2} + \dot{m}_{v_2} h_{v_2} + \dot{m}_{l_4} h_{l_4} - \dot{m}_{l_3} h_{l_3} - \dot{m}_{A_1} h_{A_1} - \dot{m}_{v_1} h_{v_1}] \frac{1}{\dot{m}_A}$$

$$0 = C_{pA} (T_2 - T_1) + \frac{\dot{m}_{v_2}}{\dot{m}_A} h_{v_2} + \frac{\dot{m}_{l_4}}{\dot{m}_A} h_{l_4} - \frac{\dot{m}_{l_3}}{\dot{m}_A} h_{l_3} - \frac{\dot{m}_{v_1}}{\dot{m}_A} h_{v_1}$$

$$h_{v_2} = h_g < T_2 > = 2560$$

$$h_{v_1} = h_g < T_1 > = 2538$$

$$h_{l_4} = h_f < T_4 > = 104.8$$

$$h_{l_3} = h_f < T_3 > = 167.5$$

$$\dot{m}_{l_4} + \dot{m}_{v_2} = \dot{m}_{l_3} + \dot{m}_{v_1} \quad \frac{\dot{m}_{l_4}}{\dot{m}_a} = \frac{\dot{m}_{l_3}}{\dot{m}_a} + (\omega_1 - \omega_2)$$

$$0 = C_{pA} (T_2 - T_1) + \omega_2 h_{v_2} - \omega_1 h_{v_1} + (\omega_1 - \omega_2) h_{l_4} + \frac{\dot{m}_{l_3}}{\dot{m}_a} (h_{l_4} - h_{l_3})$$

$$\frac{\dot{m}_{l_3}}{\dot{m}_a} = 1.084$$

$$c) \quad \dot{m}_{l_4} = \dot{m}_{l_3} + \dot{m}_a (\omega_1 - \omega_2)$$

$$= 167 + 154.1 (.0073 - .03)$$

$$\dot{m}_a = \frac{1}{1.084} (167) = \boxed{154.1 \text{ kg/s}}$$

$$\dot{m}_{l_4} = 163.5 \text{ kg/s}$$

14.33

$$P = 100 \text{ kPa}$$

$$T_2 = T = 22^\circ\text{C} \text{ (dry bulb)}$$

$$T_1 = T_{wb} = 16^\circ\text{C}$$

$$\omega_1 = \frac{c_p(T_2 - T_1) + \omega_2 h_{f,2}}{h_g(T_1) - h_f(T_{2s})}$$

$$\omega_2 = .622 \left(\frac{P_{g,2}}{P_2 - P_{g,2}} \right) = \frac{(.622)(1.819)}{(100 - 1.819) \text{ kPa}} = .01152$$

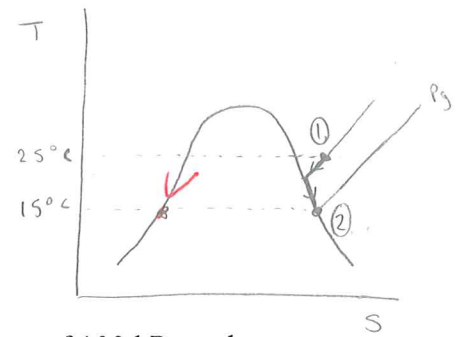
$$\omega_1 = \frac{(1.005)(16 - 22) + (.01152)(2463)}{(2541 - 67.17)} = 9.03 \times 10^{-3}$$

$$b) \quad \phi_1 = \frac{\omega_1 P_1}{(.622 + \omega_1) P_{g,1}} = \frac{9.03 \times 10^{-3} (100 \text{ kPa})}{(.622 + .0091)(2.645)} = 0.541$$

$$c) \quad P_{v,1} = \phi_1 P_{g,1} = \phi_1 P_{sat}(T_2) = .541 (2.645) = 1.432 \text{ kPa}$$

$$T_{dp} = T_{sat}(P_{v,1}) = 12.3^\circ\text{C}$$

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ME 221 Applied Thermodynamics
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D.33 The moist air in a 150 m³ vessel has a temperature of 25°C, pressure of 100 kPa and a relative humidity of 53.8%. Assume water vapor behaves as an ideal gas.

- Find the dew point temperature.
- Find the humidity ratio.
- If the temperature is cooled to 10°C at constant pressure, calculate the amount of water condensed.
- Sketch the process described in c) on a T-S diagram, showing the initial and final states as well as the path.

P_v partial pressure of vapor
 P_A partial pressure of dry air = $P - P_v$
 P_g saturation pressure

a) $\phi = \frac{\omega P_A}{.622 P_g} = .538$ $P_g = 3.1698$ $P = 100 \text{ kPa} = P_A + P_v$

$T_{DP} = T \text{ where } P_v = P_{sat} < 25^\circ\text{C} >$ $P_v = .538(3.1698) = 1.705 \text{ kPa}$

$T_{DP} = 15^\circ\text{C}$

b) $\omega = 0.622 \frac{P_v}{P_A} = 0.622 \left(\frac{1.705}{100 - 1.705} \right) = .01079 = \omega_1$

c) $\phi_2 = 100\%$ $10^\circ\text{C} < T_{DP}$ $P_{v2} = P_g(T_2) = 1.2281 \text{ kPa}$

$\omega_2 = .622 \frac{P_{v2}}{P_A} = .622 \left(\frac{1.228}{100 - 1.228} \right) = .00773 = \omega_2$

$m_l = m_a(\omega_1 - \omega_2)$ $m_a = \frac{P_A V_1}{R_A T_1} = \frac{(100 - 1.705)(150)}{(0.287)(298)} = 172.4 \text{ kg}$

$\Rightarrow m_l = 172.4(.01079 - .00773)$

$m_l = .5275 \text{ kg}$

T
 Dupont?

14.28

air 25°C $\phi = .65$ Windows drop to 10°C

$$P_g = 3.1698 \quad .65 = \frac{P_v}{P_g} \Big|_{T,P} \Rightarrow P_v = 2.060 \text{ kPa}$$

$$T_{DP} = T_{\text{wet}} \quad P_g = 2.060 \text{ kPa}$$

$$17.5^{\circ} < T_{DP} < 21.1^{\circ}\text{C} \quad \text{Yes, moisture will condense}$$

$$10^{\circ} < T_{DP}$$

ME 221 Applied Thermodynamics
Fall 2010

D.32 A tank has two sides initially separated by a diaphragm. Side A contains 1 kg of water and side B contains 1.2 kg of air, both initially at 20°C, 100 kPa. The diaphragm is broken and the entire tank is heated to 600°C by the ambient which is at 700°C (i.e. the heat transfer comes from a source at a constant 700°C). You may assume that air is an ideal gas with constant specific heats evaluated at 300K. However, use the steam tables for water.

② $600^\circ\text{C} = 873\text{K}$

1 kg H_2O

1.2 kg air

- Determine the volume of the entire tank.
- Find the final total pressure (hint: this is the sum of the partial pressures)
- Find the heat transfer into the tank.
- Find the total entropy generation.

a) $V_{\text{H}_2\text{O}} = 0.001002 (1\text{kg}) = 0.001\text{m}^3$ $V_{\text{air},1} = \frac{m R_{\text{air}} T_1}{P_1} = \frac{.2870 (1.2) (293)}{100} = 1.010\text{m}^3$

$V_{\text{total}} \approx 1.01\text{m}^3$

b) $P_{\text{total}} = \sum P_i$ $\frac{m_i R_i T}{V} = (\text{Air}) \frac{1.2 (.2870) (873)}{1.01\text{m}^3} = 297.7\text{ kPa}$
 $(\text{Water}) \frac{(1) (.4615) (873)}{(1.01)} = 398.9\text{ kPa}$ $\left. \vphantom{\frac{m_i R_i T}{V}} \right\} P_2 = 696.6\text{ kPa}$

c) $Q_{\text{in}} = u_2 - u_1 = \sum m_i c_{p,i} (\Delta T) =$

air, $1.2\text{kg} (.717) (600 - 20^\circ\text{C}) = 499.0\text{ kJ}$
 $\text{H}_2\text{O}, \Delta u = 1\text{kg} (3299 - 83.91) = 3215\text{ kJ}$ $\left. \vphantom{\Delta u} \right\} Q_{\text{in}} = 3715\text{ kJ}$

d) $S_2 - S_1 = \int \frac{dQ}{T} + S_{\text{gen}}$ $\frac{Q}{T} = \frac{3715}{(700 + 273)} = 3.818 \frac{\text{kJ}}{\text{K}}$

$(S_2 - S_1)_{\text{air}} = c_p \ln\left(\frac{T_2}{T_1}\right) - R \ln\left(\frac{P_2}{P_1}\right) = 1.005 \ln\left(\frac{873}{293}\right) - .2870 \ln\left(\frac{696.7}{100}\right) = .783 \frac{\text{kJ}}{\text{kg}\cdot\text{K}} (1.2\text{kg})$

$(S_2 - S_1)_{\text{H}_2\text{O}} = \left. \begin{array}{l} S_2 = 8.458 \\ S_1 = .2965 \end{array} \right\} (\Delta S_{\text{H}_2\text{O}}) = 8.162 \frac{\text{kJ}}{\text{kg}\cdot\text{K}} (1\text{kg})$

$(S_2 - S_1)_{\text{total}} = 9.102 \frac{\text{kJ}}{\text{K}} - 3.818$

$S_{\text{gen}} = (S_2 - S_1) - \frac{Q}{T} = 5.284 \frac{\text{kJ}}{\text{K}}$

Text ρ 14.41

$$m_A, m_V? \quad V = 240 \text{ m}^3 \quad P = 98 \text{ kPa} \quad T = 23^\circ\text{C} \quad \phi = 50\% = \frac{P_V}{P_g} = \frac{\omega P_A}{.622 P_g}$$

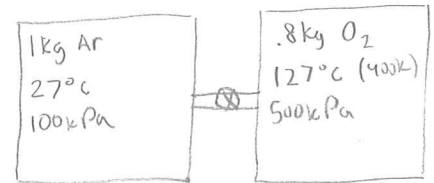
$$P_g = P_{\text{sat}}(23^\circ\text{C}) = 2.811 \text{ kPa}$$

$$P_V = .5 P_g = 1.41 \text{ kPa}$$

$$P_A = P - P_V = 98 - 1.41 = 96.59$$

$$m_A = \frac{P_A V}{R_A T} = \frac{(96.59)(240)}{(.287)(296)} = \boxed{272.9 \text{ kg}}$$

$$m_V = \frac{P_V V}{R_V T} = \frac{1.41 \text{ kPa} (240)}{.4615 (296)} = \boxed{2.47 \text{ kg}}$$



D.30 One kg of argon at 27°C, 100 kPa, is contained in a rigid tank connected by a valve to another rigid tank containing 0.8 kg of O₂ at 127°C, 500 kPa. The valve is opened and the gasses are allowed to mix, reaching equilibrium at 77°C. Given MW_{Ar} = 40 kg/kmol and MW_{O₂} = 32 kg/kmol, determine:

- The volume of each tank (m³)
- The final pressure (kPa)
- The heat transfer to or from the system during the process (kJ). Assume constant specific heats.
- The entropy change of the argon (kJ/K)

$$a) \quad PV = nRT \quad V_{Ar} = \frac{8.314(300)}{100 \text{ kPa}} \left(\frac{1 \text{ kg}}{40 \text{ kg/kmol}} \right) = \boxed{.6236 \text{ m}^3}$$

$$V_{O_2} = \frac{8.314(400)}{500 \text{ kPa}} \left(\frac{.8}{32} \right) = \boxed{.1663 \text{ m}^3} \quad V_{total} = \underline{.7899}$$

$$b) \quad P_{mix} = m R_{mix} T \quad R_{mix} = \sum m_i R_i = \frac{1}{1.8} (.2081) + \frac{.8}{1.8} (.2598) = .2311$$

$$P_{mix} = \frac{1.8 \text{ kg} (.2311 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}) (77 + 273) \text{ K}}{.7899 \text{ m}^3} = \boxed{184.3 \text{ kPa}}$$

$$c) \quad Q - W = u_2 - u_1 = m c_v (T_2 - T_1) = 1 \text{ kg} (.3122) (77 - 27) + .8 \text{ kg} (.658) (77 - 127)$$

$$\boxed{Q = -10.71 \text{ kJ}}$$

$$d) \quad S_2 - S_1 = C_p \ln \left(\frac{T_2}{T_1} \right) - R \ln \left(\frac{P_2}{P_1} \right) =$$

$$= .5203 \ln \left(\frac{350}{300} \right) - .2081 \ln \left(\frac{184(.5)}{100} \right)$$

$$\boxed{\Delta S_{Ar} = .0976 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}} \quad * (1 \text{ kg})$$

$$\text{where } P_{2,Ar} = \left[\frac{1}{40 \text{ kg/kmol}} / \left(\frac{1}{40} + \frac{.8}{32} \right) \right] P_2$$

David Maloney

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ME 221 Applied Thermodynamics
Fall 2010

D.31 An insulated rigid tank is divided into two compartments by a partition. One compartment contains 7 kg of oxygen (O_2) gas at $40^\circ C$ and 100 kPa and the other compartment contains 4 kg of nitrogen (N_2) gas at $20^\circ C$ and 150 kPa. The partition is removed and the gases are allowed to mix. Assume ideal gas behavior and constant specific heats.

- Determine the final mixture temperature (K)
- Find the total volume of the tank (m^3)
- Find the final system pressure (kPa)
- Find the entropy generated in the process (kJ/K)

$$R_{O_2} = .2598 \quad C_{p_{O_2}} = .918$$

$$R_{N_2} = .2968 \quad C_{p_{N_2}} = 1.039$$

$$Q - W = \Delta U = m_{O_2} C_{v_{O_2}} (T_2 - T_1) + m_{N_2} C_{v_{N_2}} (T_2 - T_1)$$

$$7 \text{ kg} (.658) (T_2 - 313) + 4 \text{ kg} (.743) (T_2 - 293) = 0 \Rightarrow 7.578 T_2 - 2313 = 0$$

$$T_2 = 305.2 \text{ K}$$

$$V_{O_2} = \frac{m R_{O_2} T}{P} = \frac{7 \text{ kg} (.2598) (40 + 273)}{100} = 5.692 \text{ m}^3$$

$$V_{N_2} = \frac{4 \text{ kg} (.2968) (293)}{150} = 2.319 \text{ m}^3$$

$$V_{\text{total}} = 8.011 \text{ m}^3$$

$$P_2 = \frac{m R_{\text{mix}} T}{V}$$

$$R_{\text{mix}} = \sum m_i R_i = \frac{7(.2598) + 4(.2968)}{7+4} = .2733$$

$$= \frac{11(.2733)(305.2)}{8.011} \Rightarrow P_2 = 114.5 \text{ kPa}$$

$$(S_2 - S_1)_{O_2} = C_p \ln \left(\frac{T_2}{T_1} \right) - R \ln \left(\frac{P_2}{P_1} \right) = .918 \ln \left(\frac{305.2}{313} \right) - .2598 \ln \left(\frac{69.3}{100} \right) = (.07211) (7.89)$$

$$(S_2 - S_1)_{N_2} = 1.039 \ln \left(\frac{305.2}{298} \right) - .2968 \ln \left(\frac{45.3}{150} \right) = (.3982) (4 \text{ kg})$$

$$(S_2 - S_1) = .5048 + 1.593 = 2.098$$

$$\frac{Q}{T_0} = 0 \Rightarrow S_2 - S_1 = S_{\text{gen}} = 2.098 \frac{\text{kJ}}{\text{K}}$$

$$P_{2, N_2} = \left(\frac{.143}{.219 + .143} \right) (114.6) = 69.3$$

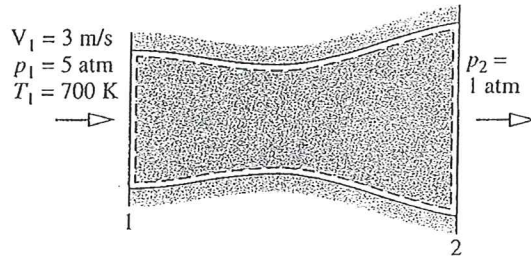
$$P_{2, O_2} = \left(\frac{.219}{.219 + .143} \right) (114.6) = 45.3$$

David Maloney

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ME 221 Applied Thermodynamics
Fall 2010

- D.29 A gas mixture consisting of CO_2 (mole fraction, $y_{\text{CO}_2} = 0.8$) and O_2 (mole fraction, $y_{\text{O}_2} = 0.2$) enters a test section and expands isentropically. The inlet conditions, state 1, have $P_1 = 500 \text{ kPa}$ (5 atm), $T_1 = 700 \text{ K}$ and $V_1 = 3 \text{ m/s}$. At the exit, state 2, the pressure is 100 kPa (1 atm). Assume constant specific heats evaluated at 300 K .



- a) Find the mass fraction of each gas
b) Find the final temperature (T_2)
c) Find the exit velocity, V_2 (m/s).

$$MW_{\text{mix}} = (0.8)(44.01) + (0.2)(32.0) = 41.61$$

$$m_{f_i} = \frac{y_i MW_i}{MW_{\text{mix}}} = \frac{0.8(44.01)}{41.61} = \boxed{0.846} \quad MW_{\text{O}_2} = \frac{0.2(32.0)}{41.61} = \boxed{0.153}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{k-1}{k}} \quad k = \frac{C_p}{C_v} \quad C_{p,\text{mix}} = \sum m_{f_i} C_{p_i} = 0.846(0.846) + (0.153)(0.918) = 0.8561$$

$$C_{v,\text{mix}} = \sum m_{f_i} C_{v_i} = 0.846(0.657) + (0.153)(0.658) = 0.6565$$

$$k = 1.304$$

$$T_2 = 700 \left(\frac{1}{5}\right)^{\frac{0.304}{1.304}} = \boxed{481.0 \text{ K}}$$

$$\Delta E = 0 \quad \left(h_1 + \frac{V_1^2}{2}\right) = \left(h_2 + \frac{V_2^2}{2}\right) \Rightarrow V_2 = \sqrt{2 \left[h_1 - h_2 + \frac{V_1^2}{2}\right]}$$

$$h_1 - h_2 = C_p (T_1 - T_2) = 0.8561 (700 - 481) = 187.5 \frac{\text{kJ}}{\text{kg}}$$

$$\frac{V_1^2}{2} = \frac{(3 \text{ m/s})^2}{2} \frac{1 \text{ kJ/kg}}{1000 (\text{m/s})^2} = 0.0045 \text{ kJ/kg}$$

$$V_2 = \sqrt{2 \left(187.5 + 0.0045\right) \frac{\text{kJ}}{\text{kg}} \left(\frac{1000 \text{ m}^2/\text{s}^2}{\text{kJ/kg}}\right)}$$

$$\boxed{V_2 = 612.4 \text{ m/s}}$$

David McIlwain

ME 221 Applied Thermodynamics
Fall 2010

Week D23

D.28

A mixture of 60% helium and 40% nitrogen, by volume, enters a turbine at 1 MPa, and 800 K. The mass flow rate of the mixture is 2 kg/s. The adiabatic turbine has an exit pressure of 100 kPa. Assume the turbine has an isentropic efficiency of 85%. Find the actual turbine power (kW) and the actual exit temperature (K). Assume constant specific heats.

$$\eta_T = .85$$

$$\dot{Q}_T - \dot{W}_T = \dot{m}(h_2 - h_1) = \dot{m} C_{p,mix} (T_2 - T_1)$$

$$\dot{W}_T = \dot{m} C_{p,mix} (T_1 - T_2) \quad T_{2s} = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}}$$

$$\bar{C}_{p,mix} = \sum_i y_i = (0.6)(8.193)(4) + 4(1.039)(28) = 24.1 \text{ kJ/kmol}\cdot\text{K}$$

$$k = \frac{\bar{C}_p}{\bar{C}_v} \quad \bar{C}_p - \bar{C}_v = R_u \quad \frac{\bar{C}_p}{\bar{C}_p - R_u} = k = \frac{24.1}{24.1 - 8.314} = 1.527 \checkmark$$

$$\dot{m} \dot{W}_{mix} = \sum_i y_i \dot{m} \dot{W}_i = (0.6)(4) (0.4)(28) = 13.6 \text{ kg/kmol}$$

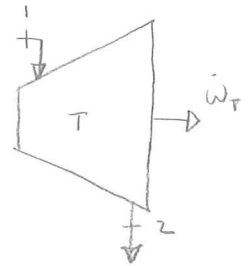
$$C_{p,mix} = \frac{24.1 \text{ kJ/kmol}\cdot\text{K}}{13.6 \text{ kg/kmol}} = 1.772 \text{ kJ/kg}\cdot\text{K}$$

$$T_{2s} = 800 \left(\frac{100}{1000} \right)^{\frac{1.527}{1.527}} = 361.4 \text{ K}$$

$$\dot{W}_{Ts} = 2 \frac{\text{kg}}{\text{s}} (1.772 \frac{\text{kJ}}{\text{kg}\cdot\text{K}}) (800 - 361.4) = 1554 \text{ kW}$$

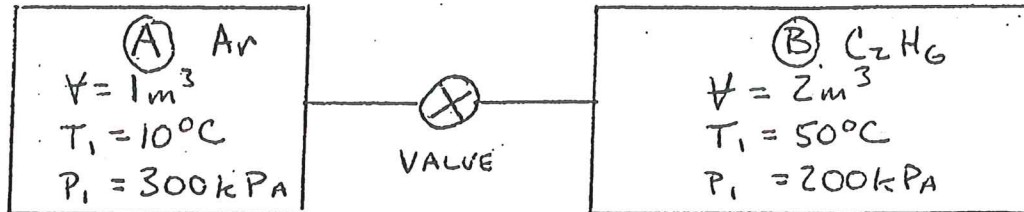
$$\dot{W}_{TA} = (.85) \dot{W}_{Ts} = \boxed{1321 \text{ kW}}$$

$$\dot{m} C_{p,mix} (T_1 - T_{2A}) = 2 \frac{\text{kg}}{\text{s}} (1.772 \frac{\text{kJ}}{\text{kg}\cdot\text{K}}) (800 - T_{2A}) \quad \boxed{T_{2A} = 427 \text{ K}}$$



ME 221 Applied Thermodynamics
Fall 2010

- D.27 Two insulated tanks A and B are connected by a valve as shown in the sketch below. Tank A has a volume of 1 m^3 and initially contains argon (Ar) at 300 kPa and 10°C . Tank B has a volume of 2 m^3 and initially contains ethane (C_2H_6) at 200 kPa and 50°C . The valve is opened and remains open until the resulting gas mixture comes to a uniform state. Assume constant specific heats.



- Find the final temperature of the gas mixture.
- Find the final tank pressure.

$$a) \quad 0 = U_2 - U_1 = M_{\text{Ar}} (u_{\text{Ar},2} - u_{\text{Ar},1}) + M_{\text{C}_2\text{H}_6} (u_{\text{C}_2\text{H}_6,2} - u_{\text{C}_2\text{H}_6,1})$$

$$= M_{11} C_{V,11} (T_2 - T_{1,1}) + M_{11} C_{V,11} (T_2 - T_{1,2})$$

$$M_{\text{Ar}} = \frac{P_{\text{Ar},1} V_{\text{Ar}}}{R_{\text{Ar}} T_{\text{Ar}}} = \frac{300(1)}{(0.2081)(283)} = 5.094 \text{ kg}$$

$$M_{\text{C}_2\text{H}_6} = \frac{P_1 V}{R T_1} \text{ C}_2\text{H}_6 = \frac{(200)(2)}{(0.2765)(323)} = 4.479 \text{ kg}$$

$$0 = (5.094 \text{ kg})(0.3122 \frac{\text{kJ}}{\text{kg K}})(T_2 - 283 \text{ K}) + (4.479 \text{ kg})(1.490)(T_2 - 323 \text{ K})$$

$$\Rightarrow T_2 = 315.3 \text{ K}$$

$$b) \quad P_2 = \frac{M_{\text{tot}} R_{\text{tot}} T_2}{V_2} \quad V_2 = 3 \text{ m}^3 \quad R_{\text{tot}} = \sum m f_i R_i = \left(\frac{5.094}{9.573}\right)(0.2081) + \frac{4.479}{9.573}(0.2765)$$

$$M_{\text{tot}} = 5.094 + 4.479 = 9.573 \text{ kg}$$

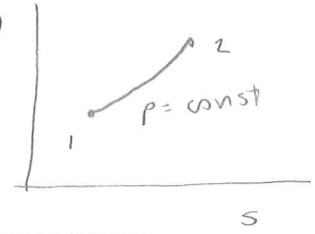
$$P_2 = \frac{(9.573)(0.240)(315.3)}{3 \text{ m}^3} = 241.6 \text{ kPa}$$

David Mulawey

$$R_{mix} = \sum_i m_{fi} R_i = (.3077)(\quad) + .4231(\quad) + .2692(\quad)$$

$$= .3193$$

(10)



ME 221 Applied Thermodynamics
Fall 2010

D.26 A mixture of ideal gases in a container consists of 50% CH₄, 25% CO₂ and 25% N₂ by volume. The gas mixture has a total mass of 12 kg and is initially at 293 K. The fixed mass mixture is then heated, **at constant pressure**, to 673 K. For this problem assume constant specific heats.

- Find the molecular weight of the mixture.
- Find the mass fraction of each species.
- Find C_p for the mixture (kJ/kgK)
- Find C_v for the mixture (kJ/kgK)
- Find the total heat transfer, Q, required to heat the mixture from 293 K to 673 K at constant pressure for the mixture. (kJ)
- Find the total work, W, during this heating process. (kJ)

$$\frac{m_i}{m_{total}} = \frac{y_i \cdot MW_i}{MW_{total}}$$

$$a) MW = \sum_i y_i MW_i = (.5)(16.043) + (.25)(44.01) + (.25)(28.013)$$

$$MW = \boxed{26.03 \frac{kg}{kmol}} \quad \text{total mols } n = \frac{12 kg}{26.03 \frac{kg}{kmol}} = .4610 kmol$$

$$b) m_{fi} = \frac{m_i}{m_{total}} = \frac{(.5)(16.043)}{26.03} = \boxed{.3079} = m_{fCH_4} \quad m_{fCO_2} = \frac{(.25)(44)}{26} = \boxed{.4231}$$

$$m_{fN_2} = \frac{(.25)(28)}{(26)} = \boxed{.2692}$$

$$c) C_{p,mix} = \sum_i m_{fi} C_{pi} = .3077(25.37 \frac{kJ}{kg}) + .4231(.846 \frac{kJ}{kg}) + .2692(1.039)$$

$$\boxed{C_{p,mix} = 1.331 \frac{kJ}{kg}}$$

$$d) \sum_i m_{fi} C_{vi} = .3077(1.7354) + .4231(.657) + .2692(.743)$$

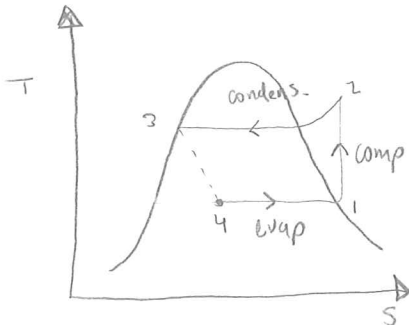
$$\boxed{C_{v,mix} = 1.0123}$$

$$e) Q_2 = u_2 - u_1 + w_2 = h_2 - h_1 = C_p(T_2 - T_1) = 1.331(673 - 293) = 505.8(12 kg) = \boxed{6070 kJ}$$

$$w_2 = Q_2 - (u_2 - u_1) \Rightarrow C_v(T_2 - T_1) = .9621(673 - 293) = 365.6$$

$$W = 140.2 \frac{kJ}{kg}(12 kg) = \boxed{1496 kJ}$$

11.16, 11.19

11.16) 134a ideal refrigeration cycle .12-.7 MPa $\dot{m} = .05 \text{ kg/s}$ 

① sat vapor

$P = .12 \text{ MPa}$

$T = -22.32^\circ\text{C}$

$S = .9478$

$h = 236.97$

② SHV

$P = .7 \text{ MPa}$

$S = .9478$

$h = 273.7$

③ sat liq

$P = .7 \text{ MPa}$

$h = 88.82$

④

$P = .12 \text{ MPa}$

$h = 88.82$

$$h_2 = \begin{matrix} 268.9 & .9313 \\ 278.6 & .9641 \end{matrix} \quad h_2 = 273.7$$

a) $\dot{q}_L$ & $P_{\text{compressor}}$ b) $\dot{q}_H$ & COP

$$\dot{q}_2 - \dot{w}_2 = h_2 - h_1, \quad \dot{w}_2 = h_1 - h_2 = 236.97 - 273.7$$

$$\dot{w}_{12} = \dot{m}(h_1 - h_2) = \boxed{-1.837 \text{ kW}} \quad \text{means work into system}$$

$$\boxed{\dot{w}_c}$$

$$\dot{q}_3 - \dot{w}_3 = h_3 - h_2 = 88.82 - 273.7 =$$

$$\dot{q}_L = \dot{q}_1 = \dot{m}(h_1 - h_4) = .05(237.0 - 88.82) = \boxed{7.409 \text{ kW}} \quad \dot{Q}_L$$

$$\dot{q}_H = \dot{q}_3 = \dot{m}(h_3 - h_2) = .05(88.82 - 273.7) = \boxed{-7.44 \text{ kW}} \quad \text{heat out of system}$$

$$\boxed{\dot{Q}_H}$$

$$\text{COP} = \frac{\dot{Q}_L}{\dot{w}_{in}} = \frac{7.409}{1.837} = \boxed{4.033}$$

David Maloney

10

ME 221 Applied Thermodynamics
Fall 2010

Due MON 10-25

D.25 A 100 m^3 storage tank contains fuel gases at 20°C and a total pressure of 100 kPa . The gases consist of methane (CH_4), propane (C_3H_8), and butane (C_4H_{10}). A test shows that the partial pressure of the methane is 15 kPa and that of the propane is 65 kPa .

- Find the mole fraction for each of the three species.
- Find the mass of each of the three species in the tank.
- Find the mass fraction of each of the three species.
- Find C_p for the mixture. (kJ/kgK)

$$a) \quad P_i = y_i P_T \quad y_i = \frac{P_i}{P_T} \quad P_{\text{C}_4\text{H}_{10}} = 100 - 15 - 65 = 20 \text{ kPa}$$

$$y_{\text{CH}_4} = .15 \quad y_{\text{C}_3\text{H}_8} = .65 \quad y_{\text{C}_4\text{H}_{10}} = .20$$

$$b) \quad m_i = n_i (MW_i) \quad n_i = y_i n_{\text{total}} \quad n_{\text{total}} = \frac{P_T V}{R_u T} = \frac{100 \text{ kPa} (100 \text{ m}^3)}{(8.314) \frac{\text{kJ}}{\text{kmol}} (293 \text{ K})} = 4.105 \text{ kmol}$$

$$m_{\text{CH}_4} = .15 (4.105) (16 \frac{\text{kg}}{\text{kmol}}) = 9.852 \text{ kg}$$

$$m_{\text{C}_3\text{H}_8} = .65 (4.105) (44) = 117.4 \text{ kg}$$

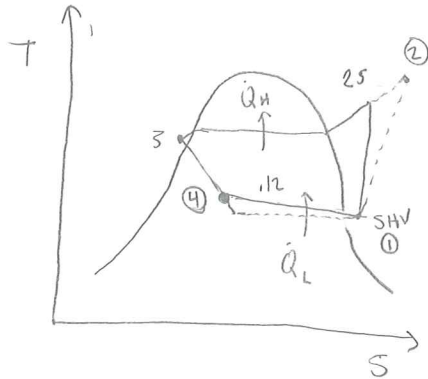
$$m_{\text{C}_4\text{H}_{10}} = 47.6 \text{ kg}$$

$$c) \quad m_{fi} = \frac{m_i}{m_{\text{total}}} \Rightarrow \begin{aligned} m_{f\text{CH}_4} &= .0563 \\ m_{f\text{C}_3\text{H}_8} &= .671 \\ m_{f\text{C}_4\text{H}_{10}} &= .272 \end{aligned}$$

$$d) \quad C_p = \sum m_{fi} C_{pi} = .0563(2.2537) + .671(1.6794) + .272(1.7164) = 1.721 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

11.19

134a



① SHV

$$P = .14 \text{ MPa}$$

$$T = -10^\circ\text{C}$$

$$h = 246.4$$

$$s = .9724$$

②

$$P = .7 \text{ MPa}$$

$$T = 50^\circ\text{C}$$

$$h = 288.5$$

③

$$T = 24^\circ\text{C}$$

$$P = .65 \text{ MPa}$$

$$h = 85.26$$

④

$$P = .15 \text{ MPa}$$

$$h = 85.26$$

$$\dot{m} = .12 \text{ kg/s}$$

$$a) \dot{q}_L = ? \quad \dot{w}_{\text{comp}}$$

$$b) \eta_{\text{isen},c} = ?$$

$$c) \text{COP} = ?$$

$$a) \dot{q}_L = \dot{m} (h_1 - h_4) = .12 (246.4 - 85.26) = \boxed{19.34 \text{ kW}}$$

$$\dot{w}_{\text{comp}} = \dot{m} (h_2 - h_1) = (246.4 - 288.5) \cdot .12 = \boxed{5.052 \text{ kW}} \quad \text{work in}$$

$$b) h_{2s}: s_{2s} = s_1 = .9724 \quad h = (\text{interpolate}) \quad 281.2 \text{ kJ/kg}$$

$$\eta_{\text{isen}} = \frac{281.2 - 246.4}{288.5 - 246.4} = \boxed{82.66 \%}$$

$$c) \text{COP} = \frac{q_L}{w_{\text{in}}} = \frac{19.34}{5.052} = \boxed{\text{COP} = 3.828}$$

10

ME 221 Applied Thermodynamics & 13.33
Fall 2010

D.24 A gas mixture contains 5 kg of O₂, 8 kg of N₂ and 10 kg of CO₂. Find (a) the mass fraction of each component, (b) the mole fraction of each component, and (c) the average molar mass and gas constant of the mixture.

a) $m_{f, O_2} = .2174 \quad m_{f, N_2} = .3478 \quad m_{f, CO_2} = .4348$

$$y_{O_2} = \frac{n_{O_2}}{n}$$

$$O_2: 32.00 \text{ kg/kmol}$$

$$5 \text{ kg} / 32 = .1563 \text{ kmol}$$

$$n_{\text{total}} = .6691 \text{ kmol}$$

$$N_2: 28.01 \text{ kg/kmol}$$

$$8 \text{ kg} / 28.01 = .2856 \text{ kmol}$$

$$CO_2: 44.01 \text{ kg/kmol}$$

$$10 / 44.01 = .2272 \text{ kmol}$$

b) $y_{O_2} = .1563 / .6691$

$$y_{O_2} = .2336$$

$$y_{N_2} = .4268$$

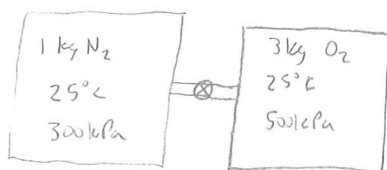
$$y_{CO_2} = .3396$$

c) $MW_{\text{avg}} = 34.38 \frac{\text{kg}}{\text{kmol}}$

$$R = \frac{R_u}{MW} = \frac{8.314}{34.38} = .242 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

13-33)

rigid tank



$$T_{\text{final}} = 25^\circ\text{C}$$

$$V_{\text{final}} = ? \quad P_{\text{final}} = ?$$

$$N_2: m = 28.013 \frac{\text{kg}}{\text{kmol}}$$

$$O_2: m = 32.00 \frac{\text{kg}}{\text{kmol}}$$

$$R_{N_2} = .2968$$

$$R_{O_2} = .2598$$

$$300 \text{ kPa} = 1 \text{ kg} (.2968) (25 + 273) \Rightarrow V = .2948 \text{ m}^3$$

$$500 \text{ kPa} = 3 \text{ kg} (.2598) (298) \Rightarrow V = .4645 \text{ m}^3$$

$$V_{\text{tot}} = .7593$$

$$R_{\text{final}} = \frac{R_u}{M_w} \quad M_w = \sum_i y_i M_{wi} =$$

$$y_{N_2} = \frac{\frac{1}{28.01} (n)}{\left(\frac{1}{28.01} + \frac{3}{32.00} \right)} = .2758$$

$$M_{w_{N_2}}$$

$$M_{w_{O_2}}$$

$$y_{O_2} = \frac{\frac{3}{32.00}}{.1295} = .7242$$

$$\left. \begin{aligned} N_{N_2} &= \frac{1 \text{ kg}}{28.01 \text{ kg/kmol}} = .03571 \text{ kmol} \\ N_{O_2} &= \frac{3 \text{ kg}}{32.00 \text{ kg/kmol}} = .09375 \text{ kmol} \end{aligned} \right\} N_m = .1295 \text{ kmol}$$

$$P_{\text{final}} = \frac{N R_u T}{V} = \frac{.1295 (8.314) (298)}{.7593}$$

$$P_{\text{final}} = 422.2 \text{ kPa}$$

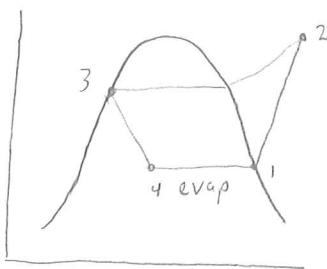
10, (100%)

ME 221 Applied Thermodynamics
Fall 2010

D.23

The air conditioner in your car is modeled with a vapor compression refrigeration cycle using R-134a. Refrigerant enters the compressor at 200 kPa and is compressed to 1200 kPa, 60°C. Note that the compressor can be considered adiabatic but not reversible. The required compressor input is 1.5 kW. Assume saturated vapor entering the compressor and a saturated liquid leaving the condenser.

- Sketch the T-S diagram for this cycle, labeling the states and assumptions for each of the four processes.
- Find the mass flow rate of the refrigerant. (kJ/kg)
- Find the capacity of the system (i.e. the heat transfer rate through the evaporator). (kW)



- (1-2) adiabatic, not rev.
(2-3) constant P heat rejection
(3-4) constant h throttling
(4-1) $\dot{w}=0$, const P, T heat addition

① Sat. Vap.

$P=200 \text{ kPa}$
 $h=244.5$

②

$P=1.2 \text{ MPa}$
 $T=60^\circ\text{C}$
 $h=289.6$

③ sat. liquid

$P=1.2 \text{ MPa}$
 $T=$
 $h=117.8$

④

$h=h_3=117.8$

b) ${}_1w_2 = (h_1 - h_2) = -45.1 \text{ kJ/kg}$

$\dot{m}_1 w_2 = \dot{w} = 1.5 \text{ kW}$

$\dot{m} = .0333$

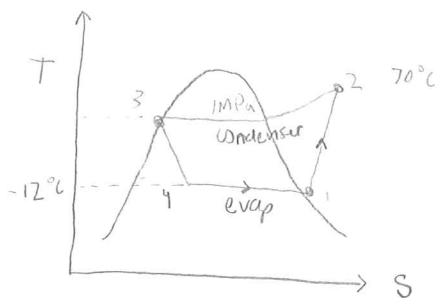
c) ${}_1q_4 = (h_1 - h_4) = 244.5 - 117.8 = 126.7 \text{ kJ/kg}$

$\dot{q}_4 = \dot{m} {}_1q_4 = 4.219 \text{ kW}$

ME 221 Applied Thermodynamics
Fall 2010

D22. A refrigerator using R-134a as the working fluid has a minimum temperature of -12°C and a maximum pressure of 1 MPa. The actual adiabatic (non-isentropic) compressor exit temperature is 70°C . Assume no pressure loss in the heat exchangers and a cycle with saturated vapor entering the compressor and a saturated liquid leaving the condenser.

- Sketch the T-S diagram for this refrigeration cycle, labeling the states.
- Find the specific heat transfer from the cold space. (kJ/kg)
- Find the specific heat transfer from the hot space. (kJ/kg)
- Find the required refrigerant mass flow rate for 1 ton of cooling. (kg/s)



① Sat. Vapor
 $P = 185.37$
 $T = -12^\circ\text{C}$
 $S = 0.93911$
 $h = 243.3$

②
 $P = 1 \text{ MPa}$
 $T = 70^\circ\text{C}$
 $h = 303.9$

③ Sat. liquid
 $P = 1 \text{ MPa}$
 $T =$
 $h = 107.3$

④
 $P =$
 $T = -12^\circ\text{C}$
 $h = 107.3$

b) $q_L = q_{1-4} = h_1 - h_4 = (243.3 - 107.3) = 136.1 \text{ kJ/kg}$

c) $q_H = q_{2-3} = h_3 - h_2 = (107.3 - 303.9) = -196.6 \text{ kJ/kg}$

d) 1 ton = 3.52 kW

$\dot{m} \left(136.1 \frac{\text{kJ}}{\text{kg}} \right) = 3.52 \text{ kW}$

$\dot{m} = 0.0259 \text{ kg/s}$

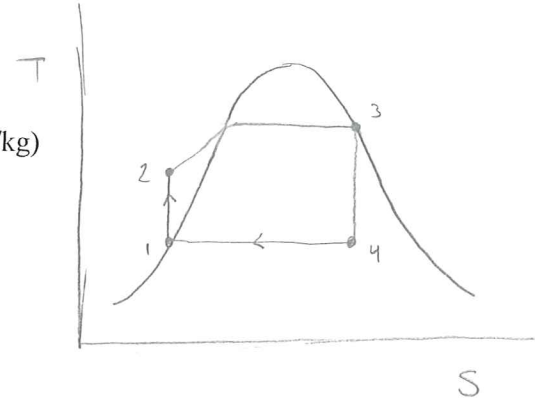
David Maloney

10

ME 221 Applied Thermodynamics
Fall 2010

D.21 A steam power generation system operates using a Rankine cycle. The water leaves the boiler as a saturated vapor at 3.5 MPa. The working fluid leaves the turbine and enters the condenser at 10 kPa. The pump has an isentropic efficiency of 80% and the turbine has an isentropic efficiency of 85%. Both can be considered adiabatic. You may assume a constant pressure boiler and condenser.

- Find the **actual** specific pump work. (kJ/kg)
- Find the **actual** specific turbine work (kJ/kg)
- Find the **actual** specific heat rejected from the condenser (kJ/kg)



sat liq		sat vapor	
①	②	③	④
$P = 10 \text{ kPa}$	$P = 3.5 \text{ MPa}$	$P = 3.5 \text{ MPa}$	$P = 10 \text{ kPa}$
$x = 0$		$h = 2803$	$s_s = 6.124$
		$s = 6.124$	

$$q_2 - w_2 = h_2 - h_1 = v \Delta P$$

$$a) \quad w_2 = \frac{1}{\eta_{isen}} (0.001014)(10 - 3500) = \boxed{-4.424 \text{ kJ/kg}}$$

$$q_4 - w_4 = h_4 - h_3$$

$$b) \quad 6.124 = .6492 + x_{4s}(7.4996) = x_{4s} = .7300 \Rightarrow h_4 = 191.8 + (.73)(2392) = 1938$$

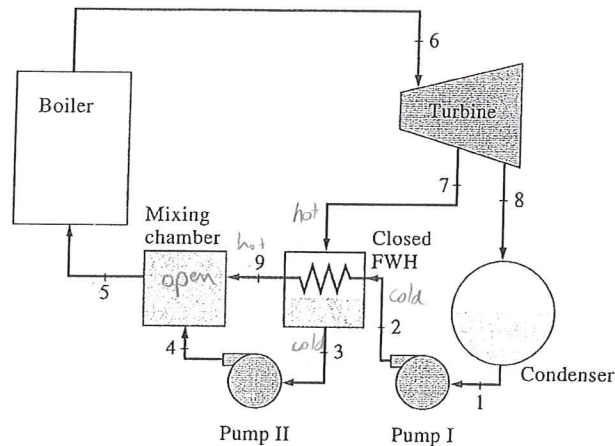
$${}_3w_4 = \eta_s(h_3 - h_4) = (2803 - 1938) \cdot .85 = \boxed{735.3 \text{ kJ/kg}}$$

$$c) \quad q_1 - w_1 = h_1 - h_4 = 191.81 - 2068 = \boxed{-1876 \text{ kJ/kg}}$$

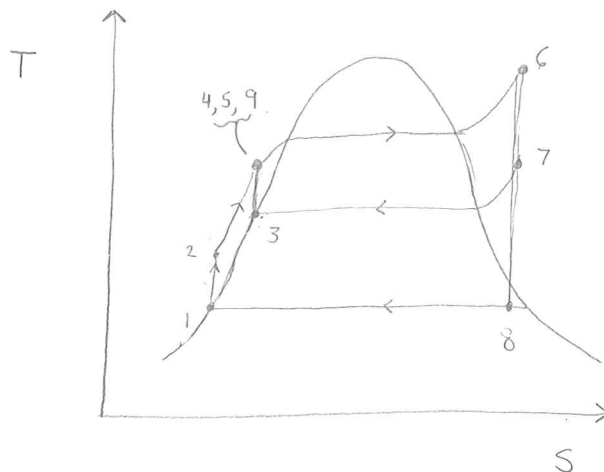
$$h_4 \text{ actual} = h_3 - {}_3w_4 = 2803 - 735.3 = 2068$$

ME 221 Applied Thermodynamics
Fall 2010

- D.20 A steam power system operates using a Rankine cycle with one closed feed water heater. The steam leaves the boiler at 5 MPa, 900 °C and expands isentropically to the condenser temperature of 45 °C. Steam is extracted at 1 MPa for the feed water heater (state 7). Assume isentropic pumps and turbine and saturated liquid entering the pumps (state 1 and 3). Also assume state 4, 5 and 9 are the same and at a temperature of 200 °C. You may also assume a constant pressure boiler and condenser and an adiabatic FWH. Do not interpolate in the steam tables, simply choose the state with the closest values.



- Sketch the T-S diagram, labeling the states.
- Find the quality entering the condenser (i.e. x_8).
- Find the specific pump work for pump 1 (kJ/kg)
- Find the specific pump work for pump 2 (kJ/kg)
- Find an **expression** (not a value) for the turbine work per kg of steam through the boiler (i.e. $\frac{\dot{W}_T}{\dot{m}_6}$). Your answer should be in terms of enthalpies and the fraction y , where $y = \frac{\dot{m}_7}{\dot{m}_6}$.
- Find the fraction of steam, y , extracted for the FWH relative to the steam in the boiler (i.e. $\frac{\dot{m}_7}{\dot{m}_6}$).



David Maloney

D.19

① Sat. liquid
 $P = 10 \text{ kPa}$
 $h = 191.8$

② $P = .5 \text{ MPa}$
 $h = 192.3$

Sat. liq.
 ③ $P = .5 \text{ MPa}$
 $S =$
 $x = 0$
 $h = 640.1$

Sat. liquid
 ④ $P = 8 \text{ MPa}$
 $S =$

⑤ $P = 8 \text{ MPa}$
 $T = 500^\circ\text{C}$
 $S = 6.727$
 $h = 3400$

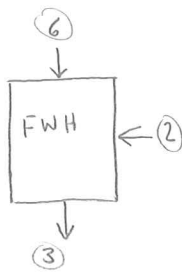
⑥ $P = .5 \text{ MPa}$
 $S = 6.727$
 $x = .9813$
 $h = 2717$

⑦ $P = 10 \text{ kPa}$

b) find $w_2 = v(P_1 - P_2) = .001010(10 - 500) = \boxed{-.4949}$

c) find x_6 : $S_5 = S_6$ $6.727 = 1.560 + x(4.960)$ $\boxed{x_6 = .9813}$

d) find $\frac{\dot{m}_6}{\dot{m}_5}$



$$\dot{m}_6 h_6 + \dot{m}_2 h_2 = \dot{m}_3 h_3$$

$$\dot{m}_5 = \dot{m}_3$$

$$h_6 = 670.4 + .9813(2086) = 2717$$

$$h_2 = h_1 - w_2 = 191.8 + .4949 = 192.3$$

$$h_3 : h_f < .5 \text{ MPa} = 640.1$$

$$\dot{m}_6 = \dot{m}_2 \left(\frac{640.1 - 192.3}{2717 - 640.1} \right) = .2156 \dot{m}_2 \quad \left. \vphantom{\dot{m}_6} \right\} \frac{\dot{m}_6}{\dot{m}_3} = \frac{.2156 \dot{m}_2}{1.2156 \dot{m}_2}$$

$$\dot{m}_3 = 1.2156 \dot{m}_2$$

$$\frac{\dot{m}_6}{\dot{m}_5} = \boxed{.1773} \text{ part of total steam in boiler goes to FWH}$$

— T/S on first page —

David Maloney

10.58

$\eta_{s, \text{turbine}} = 90\%$ before & after steam extraction pt.

Set by

① $P = 20 \text{ kPa}$
 $h = 251.4$

② $P = 3000 \text{ kPa}$
 $h = 254.5$

③ $P = 3000 \text{ kPa}$
 $T = 179.9^\circ\text{C}$
 $h = 763.5$

④ $P = 3000 \text{ kPa}$
 $T = 350^\circ\text{C}$
 $h = 3116$
 $s = 6.745$

⑤ $P = 1000 \text{ kPa}$
 $h = 2852$
 $s = 6.745$

⑥ $P = 20 \text{ kPa}$
 $s_{ss} = 6.745$
 $x = 0$
 $h = 2222$

⑦ $P = 1000 \text{ kPa}$ $T = 179.9^\circ\text{C}$
 $x = 0$
 $h = 762.5$ w_{pump}

$$w_2 = v(P_1 - P_2) = 0.001017(20 - 3000) = -3.030 \text{ kJ/kg}$$

$$h_2 = h_1 + 3.030 = 254.5$$

$$h_{ss} = \frac{2328}{2943} \frac{6.696}{6.927} 6.745 \text{ interpolate } h_{ss} = 2852$$

state 6 - $6.745 = .8320 + x(1.7075) \Rightarrow x = .8357$

$$h_6 = 251.4 + (.8357)(2358) = 2222$$

$$\eta_T = \frac{h_4 - h_5}{h_4 - h_{ss}} \therefore h_5 = h_4 - \eta_T(h_4 - h_{ss}) = 3116 - (.9)(3116 - 2852) = 2878 \text{ kJ/kg}$$

$$\eta_T = \frac{h_4 - h_6}{h_4 - h_{ss}} \therefore h_6 = 3116 - (.9)(3116 - 2222) = 2311 \text{ kJ/kg}$$

$$h_3 \approx h_7 \quad \dot{m}_5 h_5 + \dot{m}_2 h_2 = \dot{m}_7 h_7 + \dot{m}_3 h_3$$

$$\dot{m}_5 = \dot{m}_7$$

$$\dot{m}_2 = \dot{m}_3$$

$$\dot{m}_5(h_5 - h_7) = \dot{m}_3(h_3 - h_2)$$

divide by $\dot{m}_3$

$$y = \left(\frac{h_3 - h_2}{h_5 - h_7} \right) = .2406$$

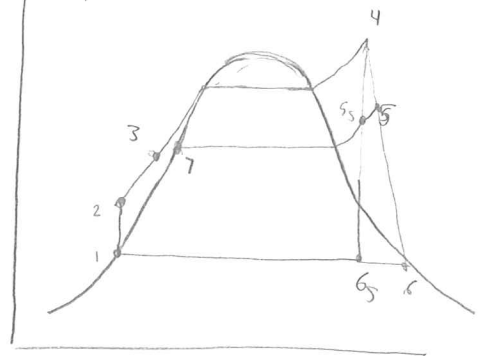
$$w_T = h_4 - h_5 + 1 - y(h_5 - h_6) = 668.5 \text{ kJ/kg } w_T$$

$$\dot{q}_{in} = h_4 - h_3 = 2353 \text{ kJ/kg}$$

$$\eta_{th} = \frac{w_{net}}{\dot{q}_{in}} = \frac{668.5 - 3.03}{2353} = \boxed{.2829}$$

$$w_T = ? \quad \dot{q}_{in} = ?$$

$$w_P = ?$$



Cale madsen

sat liq	comp liq	ext liq	comp liq	ext liq
①	②	③	④	⑤
$P = 9.595 \text{ MPa}$	$P = 5 \text{ MPa}$	$P = 1 \text{ MPa}$	$P = 5 \text{ MPa}$	$P = 1 \text{ MPa}$
$T = 45^\circ\text{C}$	$T =$	$T = 179.9^\circ\text{C}$	$T = 200^\circ\text{C}$	$T = 200^\circ\text{C}$
$S = .6386$	$S = .6386$	$S = 2.138$	$S = 2.138$	$S = 2.138$
$h = 188.4$	$h = 183.4$	$h = 762.5$	$h \approx 369.9$	$h \approx 369.9$
			$x = .9732$	$x = .9732$
			$T = 45^\circ\text{C}$	$T = 200^\circ\text{C}$
			$P = 9.595$	$P =$
			$S = 7.962$	$S = 2.138$
			$h = 852.3$	$h =$

$$b) S_g = S_f + x(S_{fg}) \quad 7.962 = .6386 + x(7.5247) \Rightarrow x = .9732$$

$$c) \dot{m}_2 - \dot{m}_1 = h_2 - h_1 = v_d P = .001010 (5000 - 9.595) \Rightarrow \dot{m}_2 = -5.040 \text{ kJ/kg}$$

$$d) \dot{m}_4 - \dot{m}_3 = v_d P = .001127 (5000 - 1000) \Rightarrow \dot{m}_4 = -4.508 \text{ kJ/kg}$$

$$e) \frac{\dot{W}_T}{\dot{m}_6} = \frac{c\dot{W}_7 + \dot{W}_8}{\dot{m}_6} = \frac{\dot{m}_7(h_6 - h_7) + \dot{m}_8(h_8 - h_7)}{\dot{m}_6} = \frac{\dot{m}_7(h_6 - h_7) + (1-y)(h_6 - h_8)}{\dot{m}_6} = \frac{y(h_8 - h_7) + h_6 - h_8}{\dot{m}_6}$$

$$f) \frac{\dot{m}_7}{\dot{m}_6} (h_9 - h_2) = \dot{m}_7 (h_3 - h_7) \Rightarrow \frac{\dot{m}_7}{\dot{m}_6} = \frac{(h_9 - h_2)}{h_3 - h_7 + h_9 - h_2} = \frac{(852.3 - 193.5)}{762.5 - 369.9 + (\quad)}$$

$$h_2 - h_1 = +5.040$$

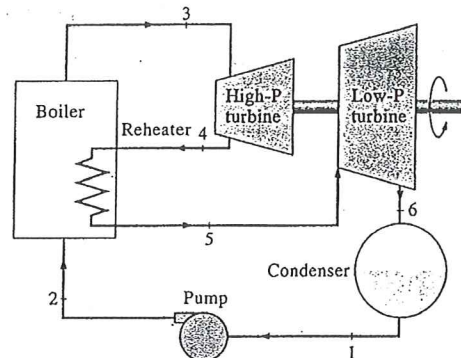
$$h_2 = h_1 + 5.040 = 193.48$$

$$\frac{\dot{m}_7}{\dot{m}_6} = .2892$$

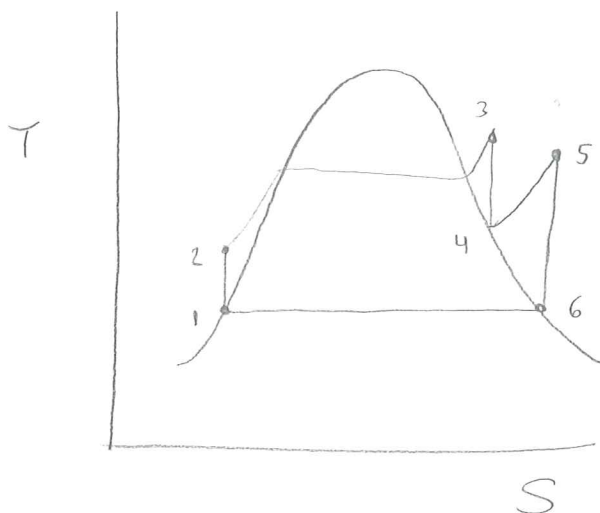
ask about h_3 & $\dot{W}_3$

ME 221 Applied Thermodynamics
Fall 2010

- D.18 A steam power system operates using a Rankine cycle with reheat. The steam leaves the boiler at 6 MPa, 450 °C and expands isentropically to 0.6 MPa where it is reheated at constant pressure to 400 °C. The steam is further expanded to 15 kPa at which point it enters the condenser. Assume a isentropic pump and turbine and saturated liquid entering the pump. You may also assume a constant pressure boiler and condenser.

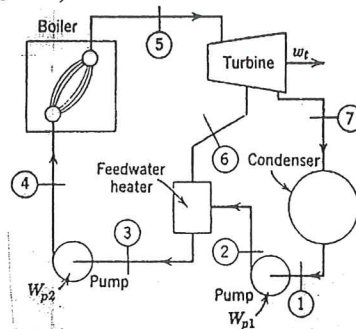


- Find the quality after the high pressure turbine (i.e. x_4).
- Find the quality after the low pressure turbine (i.e. x_6).
- Find the specific pump work (kJ/kg)
- Find the **total** specific turbine work (kJ/kg)
- Find the **total** specific heat into the boiler (kJ/kg)

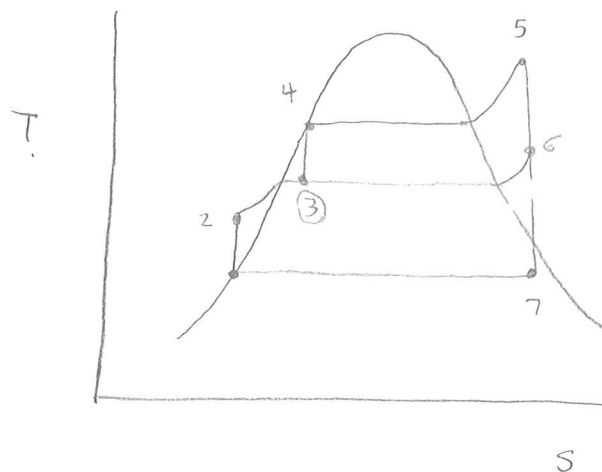


ME 221 Applied Thermodynamics
Fall 2010

- D.19 An ideal (i.e. isentropic pumps and turbine) steam power system operates on a Rankine cycle with regeneration using an open feedwater heater. Steam enters the turbine at 8 MPa and 500 °C and enters the condenser at 10 kPa. A portion of the steam is extracted from the turbine at 0.5 MPa for use in the open feedwater heater. Assume an adiabatic feedwater heater and that the feedwater leaving to pump 2 is a saturated liquid (i.e. $x_3 = 0$). Also assume a saturated liquid leaving the condenser (i.e. $x_1 = 0$).



- Sketch the T-S diagram, labeling the states.
- Find the specific work of pump 1. (kJ/kg)
- Find the quality of the bleed steam into the FWH (i.e. x_6)
- Find the fraction of steam extracted for the FWH relative to the steam in the boiler (i.e. $\frac{\dot{m}_6}{\dot{m}_5}$).



$$\begin{aligned}\dot{m}_6 h_6 + \dot{m}_2 h_2 &= (\dot{m}_2 + \dot{m}_6) h_3 \\ \dot{m}_6 h_6 - \dot{m}_6 h_3 &= \dot{m}_2 h_3 - \dot{m}_2 h_2 \\ \dot{m}_6 (h_6 - h_3) &= \dot{m}_2 (h_3 - h_2) \\ \dot{m}_6 &= \dot{m}_2 \frac{(h_3 - h_2)}{(h_6 - h_3)}\end{aligned}$$

David Maloney

D18.

① Sat. liq
 $P = 15 \text{ kPa}$
 $h = 225.9$

② $P = 6 \text{ MPa}$
 $h = 232.1$

③ $P = 6 \text{ MPa}$
 $T = 450^\circ\text{C}$
 $S = 6.722$
 $h = 3303$

④ $P = 0.6 \text{ MPa}$
 $S = 6.722$
 $x = .9923$
 $h = 3024$

⑤ $P = 0.6 \text{ MPa}$
 $T = 420^\circ\text{C}$
 $S = 7.710$
 $h = 3271$

⑥ $P = 15 \text{ kPa}$
 $S = 7.710$
 $h = 2501$
 $x = .9590$

a) find x_4 :

$$s = s_f + x s_{fg}$$
$$6.722 = 1.9308 + x(4.8285) \Rightarrow x_4 = .9923$$

b) find x_6 : $7.710 = .7549 + x 7.2522 \Rightarrow x_6 = .9590$

c) find w_{pump} : $w_2 = v(P_1 - P_2) = v_{\text{sat}}(15 \text{ kPa})$

$$= .001014(15 - 6000) \Rightarrow w_2 = -6.224 \text{ kJ/kg}$$

d) find $w_{T, \text{Total}}$ isentropic $q_4 - w_4 = h_4 - h_3$

$$h_4 = h_f + x h_{fg} = 670.38 + .9923(2086) = 3024$$

$$h_6 = h_f + x h_{fg} = 225.9 + .9590(2372) = 2501$$

$${}_3w_4 + {}_5w_6 = h_3 - h_4 + h_5 - h_6 = 1049 \text{ kJ/kg}$$

$$q_{\text{total, boiler}} = h_2 - h_3 + h_4 - h_5$$

$$h_2 = h_1 - w_2 = 225.9 + 6.224 = 232.1$$

$$q_{\text{total into boiler}} = 2548 \text{ kJ/kg}$$

David Malauey

10.105

$\dot{m}_8 = ?$
 $\eta_{th} = ?$

① $P = 15 \text{ kPa}$

② $P = 600 \text{ kPa}$

sat. liq.
③ $P = 600 \text{ kPa}$
 $T =$
 $h = 670.4$

④ $P = 10 \text{ MPa}$
 $T =$
 $h = 680.75$

⑤ $P = 10 \text{ MPa}$
 $T = 500^\circ\text{C}$
 $h = 3375$
 $s = 6.5995$

⑥ $P = 1 \text{ MPa}$
 $S = 6.600$
 $h = 2784$

⑦ $P = 1 \text{ MPa}$
 $T = 500^\circ\text{C}$
 $S = 7.764$
 $h = 3479$

⑧ $P = 0.6 \text{ MPa}$
 $S = 7.764$

⑨ $P = 15 \text{ kPa}$
 $T =$
 $x = 96.5$

$W_2 = v_2 P = (.001014)(600 - 15) = .5915 \text{ kJ/kg}$

$W_4 = v_4 P = (.001101)(10,000 - 600) = 10.35 \text{ kJ/kg}$

$h_4 = h_3 + W_4 = 680.73$

$S_4 = S_f + x S_{fg} \Rightarrow x_4 = \frac{7.764 - .7549}{7.252} = .9665$

$\begin{cases} \dot{m}_8 h_8 + \dot{m}_2 h_2 = \dot{m}_3 h_3 \\ y(h_8) + (1-y)h_2 = h_3 \end{cases}$

$y = \frac{\dot{m}_8}{\dot{m}_3} \Rightarrow$

$y = \frac{h_2 - h_2}{h_8 - h_2} = \frac{670.38 - 226.5}{3310 - 226.5}$

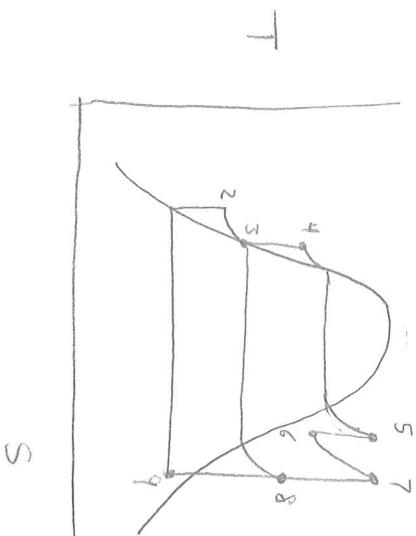
$y = .144$

$q_{in, net} = h_5 - h_4 + h_2 - h_6 = 3390 \text{ kJ/kg}$

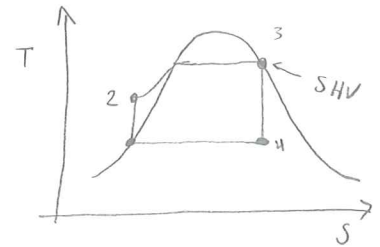
$\dot{q}_{out} = (1-y)(h_9 - h_1) = 1963 \text{ kJ/kg}$

$\eta_{th} = 1 - \frac{\dot{q}_{out}}{\dot{q}_{in}} = 1 - \frac{1963}{3390}$

$= \frac{1427}{3390} = 42.1\%$



David Malawey

REGRADER
7

+ 10.25

ME 221 Applied Thermodynamics
Fall 2010

D.17 Consider a steam power plant operating on the ideal Rankine cycle. The steam enters the turbine at 3 MPa and 350 °C and is condensed in the condenser at a pressure of 10 kPa. Assume isentropic pump and turbine. Determine:

- The thermal efficiency of the plant at the given conditions.
- The thermal efficiency if the steam is superheated to 600 °C instead of 350 °C.
- The thermal efficiency if the boiler pressure is raised to 15 MPa while the turbine inlet is maintained at 600°C.

??
0 n

Be sure to comment on the impact of the change in b) and c) on the turbine inlet and/or outlet conditions.

① $P = 10 \text{ kPa}$

② $P = 3 \text{ MPa}$

③ $P = 3 \text{ MPa}$

④ $P = 10 \text{ kPa}$

$T = 350^\circ\text{C}$

$S = 6.7450$

$$\eta_{th} = \frac{w_{net}}{q_{in}} = \frac{w_p + w_T}{q_{in}} \quad (1-2) \quad q_{2-1} = w_2 = h_2 - h_1 = -\int v dp$$

$v_1 (P_2 - P_1)$

$$v_1 = v_{sat} = 0.001010 \text{ m}^3/\text{kg} \quad (3000 - 10)$$

$w_2 = -3.020 \text{ kJ/kg}$

$$w_T: \quad w_4 = h_3 - h_4 = 3116.1 - 2136.02$$

$w_4 = 980.1 \text{ kJ/kg}$

$$S_4 = 6.7450 = .6492 + x(7.4996) \Rightarrow x = .8128 \Rightarrow h_4 = 191.81 + (.8128)2392.1$$

$q_3: \text{ const. } p \text{ no shaft work}$

$q_3 = h_3 - h_2$

$$h_2 = h_1 - w_p = 191.81 + 3.02$$

$h_2 = 194.83$

$q_3 = 2921$

$\eta_{th} = 33.45\%$

$$\begin{aligned} \text{b) } T_3 &= 600^\circ\text{C} \\ S_3 &= 7.5103 \\ h_3 &= 3683 \end{aligned}$$

$$\begin{aligned} w_2 &= -3.020 \\ h_4 &= 2380 \\ x_4 &= .9149 \end{aligned}$$

$w_4 = 1303 \text{ kJ/kg}$

$q_3 = h_3 - h_2 = 3683 - 194.83$

$q_3 = 3488$

$\eta_{th} = 37.27\%$

c) $P_2 = P_3 = 15 \text{ MPa}$ (barely SHV)

$S_3 = 5.444$

$h_3 = 2893$

$x_4 = .6393$

$h_4 = 1721$

$h_1 = 191.81$

$$w_2 = 0.001010 \text{ m}^3/\text{kg} ((15000 - 10) = -15.14$$

$w_4 = h_3 - h_4 = 972 \text{ kJ/kg}$

$q_3 = h_3 - h_2 = h_3 - (h_1 - w_p)$

$$\begin{aligned} h_3 &= 3582.3 \\ S_3 &= 6.6775 \\ \Rightarrow h_4 &= 2115.7 \end{aligned}$$

? -3

David Maloney

10.25/

Rankine cycle

net $\dot{w}_{out} = 45 \text{ MW}$

① $P = 10 \text{ kPa}$
 $T =$
 $h = 191.81$

② $P = 7 \text{ MPa}$
 $h = 198.9$

③ SHV
 $P = 7 \text{ MPa}$
 $T = 500^\circ\text{C}$
 $S = 6.800$
 $h = 3411$

④ $P = 10 \text{ kPa}$
 $h = 2154$
 $x =$
 $S = 6.800$

cooling water 4-1 2000 kg/s

4) $\frac{S}{6.800} = .6492 + x \cdot 7.4996 \Rightarrow x = .8202$

$h_4 = 191.81 + .8202(2392.1) \quad h_4 = 2154 \text{ kJ/kg}$

$\eta_{th} = \frac{w_{net}}{q_3} = \frac{w_2 + w_4}{q_3}$

$w_2 = h_1 - h_2 = v(P_1 - P_2) = .00101(10 - 7000)$

$w_2 = -7.060 \text{ kJ/kg}$

$w_4 = h_3 - h_4 = 1257$

$q_3 = h_3 - h_2 \quad h_2 = h_1 - w_2 = 198.9$

$q_3 = 3212 \text{ kJ/kg}$

$\eta_{th} = 38.92 \%$

$\dot{w}_{net} = \dot{m}_{steam} (w_2 + w_4)$

$45,000 = \dot{m}(1250)$

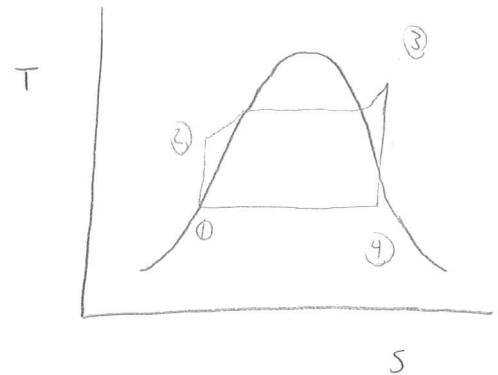
$\dot{m} = 36 \text{ kg/s}$

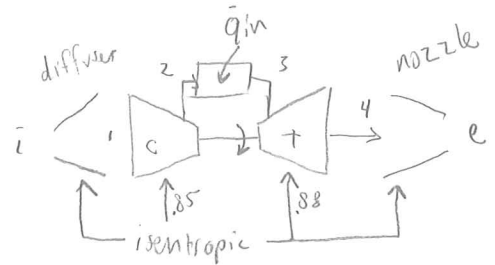
$q_1 = h_1 - h_4 = -1962 \text{ kJ/kg}$

$\dot{m} \Delta h = \dot{q} = 70640 \text{ kJ/s}$

$\frac{70640 \text{ kJ/s}}{2000 \text{ kg/s}} = 35.32 \text{ kJ/kg}$

$\frac{35.32 \text{ kJ/kg}}{C_p \text{ water } 4.18 \text{ kJ/kg}} = 8.450^\circ\text{C}$





D.16 Air at 22 kPa, 220 K, and 250 m/s enters a turbojet engine in flight at an altitude of 10,000 m. The pressure ratio across the compressor is 12. The turbine inlet temperature is 1240 K and the pressure at the nozzle exit is 22 kPa. The diffuser and nozzle processes are isentropic, the compressor and turbine have isentropic efficiencies of 85 and 88 %, respectively. There is negligible pressure drop through the combustor. Assuming constant specific heats and $P_{4s} = P_4$ (at the turbine exit), determine

- The pressures and temperatures at states 1 through 4.
- The velocity at the exit of the nozzle, V_e .

$$\begin{array}{llllll}
 \textcircled{1} & T = 251.1 & \textcircled{2} & T = 556.5 \text{ K} & \textcircled{3} & T = 1240 \text{ K} & \textcircled{4} & T = 971.2 \text{ K} & \textcircled{i} & P = 22 \text{ kPa} & \textcircled{e} & P = 22 \text{ kPa} \\
 & P = 34.41 \text{ kPa} & & P = P_3 = 412.9 \text{ kPa} & & P = 412.9 \text{ kPa} & & P = 130.7 & & T = 220 \text{ K} & & V = 250 \text{ m/s} \\
 & & & & & & & & & & & S
 \end{array}$$

$$h_1 = h_i$$

$$T_1 c_p = T_i c_p + \frac{V^2}{2} \Rightarrow T_1 = T_i + \frac{V^2}{2c_p} = 220 \text{ K} + \frac{250^2}{1.005(2)} \frac{\text{m}^2/\text{s}^2}{\text{J/kg}} = 251.1 \text{ K}$$

$$P_1 = P_i \left(\frac{T_1}{T_i} \right)^{\frac{k}{k-1}} = 22 \text{ kPa} \left(\frac{251.1}{220} \right)^{\frac{1.4}{0.4}} = 34.41 \text{ kPa}$$

$$(1-2) \text{ isentropic: } \cancel{h_2} - \cancel{h_1} = h_2 - h_1, \quad w_2 = c_p(T_1 - T_2), \quad \eta_T = \frac{w_{\text{isen}}}{w_{\text{act}}} = \frac{(251.1 - 510.7)}{(251.1 - T_2)} = 0.85$$

$$T_{2s} = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = 251.1 (12)^{\frac{0.4}{1.4}} = 510.72 \quad T_2 = 556.5 \text{ K}$$

$$P_2 = 12 P_1 = 412.9 \text{ kPa}$$

$$(3-4) \text{ for isentropic case: } -w_c = w_T, \quad \cancel{h_4} - \cancel{h_3} = h_4 - h_3, \quad w_4 = c_p(T_3 - T_4), \quad \eta_c = \frac{w_c}{w_T} = \frac{(-w_{12})}{w_4}$$

$$\eta_T (-w_2) = c_p(T_3 - T_4) = c_p(T_2 - T_1), \quad T_4 = 892.7$$

$$P_4 = P_3 \left(\frac{T_4}{T_3} \right)^{\frac{k}{k-1}} = 412.9 \left(\frac{892.7}{1240} \right)^{\frac{1.4}{0.4}} = 130.7 \text{ kPa}$$

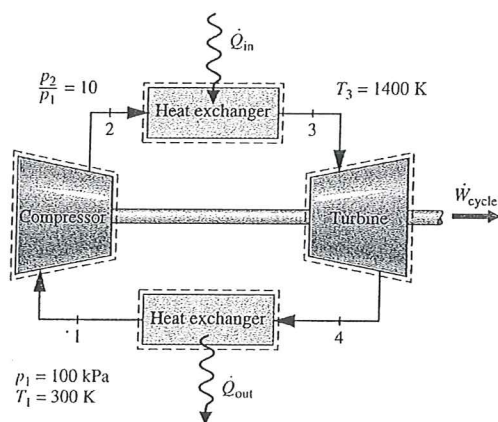
$$T_4 = T_e + \frac{V_e^2}{2c_p}, \quad V_e = \sqrt{(T_4 - T_e) 2c_p}, \quad T_e = T_4 \left(\frac{P_e}{P_4} \right)^{\frac{k-1}{k}} = 892.7 \left(\frac{22}{130.7} \right)^{\frac{0.4}{1.4}} = 559 \text{ K}$$

$$= \sqrt{(892.7 - 559)(2 \cdot 1.0035)(1000)}$$

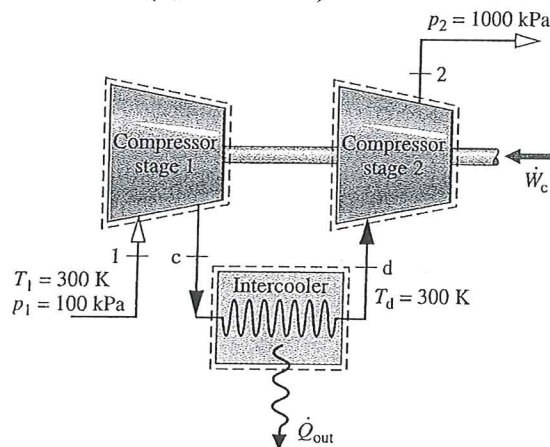
$$V_e = 868 \text{ m/s}$$

ME 221 Applied Thermodynamics
Fall 2010

- D.13 Air enters the compressor of an ideal air-standard Brayton cycle at 100 kPa and 300K. The compressor pressure ratio is 10. The turbine inlet temperature is 1400 K. Assume isentropic compressor and turbine. Assume constant specific heats (i.e. $C_v = 0.717$ kJ/kgK, $C_p = 1.004$ kJ/kgK, $k = 1.4$).



- Find the temperature after the compressor. (K).
- Find the temperature after the turbine. (K)
- Find the specific compressor work (kJ/kg)
- Find the cycle thermal efficiency.
- A two-stage compressor is now used with an intercooler between the two stages of compression. Stage 1 compresses the air to 300 kPa (i.e. $P_c = 300$ kPa) and stage 2 compresses the air to the final pressure of 1000 kPa ($P_2 = 1000$ kPa):



The intercooler, which is a simple heat exchanger, can be assumed to be a constant pressure device which cools the compressed air to $T_d = 300$ K. Find the **total** required work for this two stage compressor (kJ/kg).

D.13

$$a) \quad T_2 = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = 300 \text{ K} (10)^{0.4/1.4} = \boxed{579.2 \text{ K}} \quad T_2$$

$$b) \quad T_4 = T_3 \left(\frac{P_4}{P_3} \right)^{\frac{k-1}{k}} = 1400 \text{ K} (1/5)^{0.4/1.4} = \boxed{725.1 \text{ K}} \quad T_4$$

$$c) \quad W_c = h_1 - h_2 = c_p (T_1 - T_2) = 1.004 (300 - 579.2) = \boxed{-280.3 \text{ kJ/kg}}$$

$$d) \quad \eta_{th} = \frac{W_{net}}{q_{in}} \quad h_3 - h_4 = c_p (T_3 - T_4) \quad W_r = 1.004 (1400 - 725.1) = 677.6 \text{ kJ/kg}$$

$$q_{in} = h_3 - h_2 = 1.004 (1400 - 579.2) = 824.1 \text{ kJ/kg}$$

$$= \frac{677.6 - 280.3}{824.1} = 0.482 \quad \boxed{\eta_{th} = 48.2\%}$$

e) 2-stage compression

$$W_c = W_{c1} + W_{c2} = c_p [(T_1 - T_c) + (T_d - T_c)]$$

$$T_c = T_1 \left(\frac{P_c}{P_1} \right)^{\frac{k-1}{k}} = 300 \left(\frac{300}{100} \right)^{0.4/1.4} = 410.6 \text{ K}$$

$$T_d = T_d \left(\frac{P_2}{P_d} \right)^{\frac{k-1}{k}} = 300 \left(\frac{1000}{300} \right)^{0.4/1.4} = 423.2 \text{ K}$$

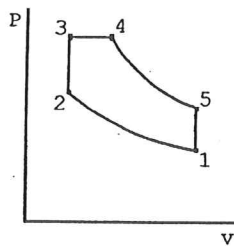
$$W_{c, tot} = 1.004 \text{ kJ/kg} (300 - 410 + 300 - 423.2)$$

$$\boxed{W_{c, tot} = -234.7 \text{ kJ/kg}}$$

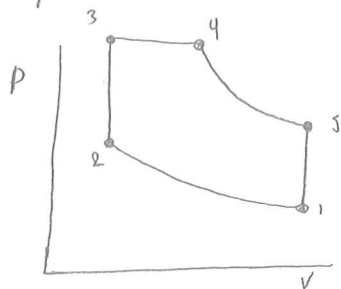
ME 221 Applied Thermodynamics
Fall 2010

D.12

An engine is to be modeled with an ideal “dual” cycle using air as the working fluid. The dual cycle is one where the first part of the energy addition is modeled as constant volume and the second part as constant pressure. Assume that $2/3$ of the energy is input as constant volume ($q_{23} = 2/3 q_{in}$) and $1/3$ of the energy at constant pressure ($q_{34} = 1/3 q_{in}$). The conditions at the beginning of the compression process (state 1) are 90 kPa and 293 K. The engine has a compression ratio of 7 and the temperature at state 3 is 2900 K. Assume ideal gas behavior and **constant specific heats** evaluated at 300K.



- Find the temperature and pressure at the end of compression (K)
- Find the temperature after the constant pressure heat addition, T_4 (K)
- Find the temperature after expansion, T_5 (K)
- Find the thermal efficiency



(1-2) isentropic

(2-3) const V q_{in} (3-4) const P q_{in}

(4-5) isentropic exp.

$$2q_3 = \frac{2}{3} q_{in}$$

$$3q_4 = \frac{1}{3} q_{in}$$

$$k = 1.4$$

$$r = 7 = \frac{V_2}{V_1}$$

$$C_p = 1.005$$

$$C_v = .718 \text{ kJ/kg}\cdot\text{K}$$

① $P_1 = 90 \text{ kPa}$
 $T_1 = 293 \text{ K}$

② $P_2 = 1372 \text{ kPa}$
 $T_2 = 638.1 \text{ K}$

③ $P_3 = 6235 \text{ kPa}$
 $T_3 = 2900 \text{ K}$

④ $P_4 =$
 $T_4 = 3708 \text{ K}$

⑤ $P_5 =$
 $T_5 = 1878 \text{ K}$

$$(1-2) \quad \frac{P_1}{P_2} = \left(\frac{V_2}{V_1}\right)^k \quad \frac{90}{P_2} = \left(\frac{1}{7}\right)^{1.4} \quad P_2 = 1372.08 \text{ kPa}$$

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{k-1} \quad \frac{293}{T_2} = \left(\frac{1}{7}\right)^{0.4} \quad T_2 = 638.1 \text{ K}$$

$$(2-3) \quad 2q_3 - \cancel{2q_3} = u_3 - u_2 = C_v(T_3 - T_2) = .718(2900 - 638.1)$$

$$2q_3 = 1624 \text{ kJ/kg}$$

$$P_3 = \frac{mRT_3}{V_3} = \frac{P_2 T_3}{T_2} = \frac{(1372)(2900)}{638.1} = P_3 = 6235 \text{ kPa}$$

$$3q_4 = \frac{1}{2} 2q_3 = 812.0 \text{ kJ/kg}$$

(3-4)

$$3q_4 - \cancel{3q_4} = (u_4 - u_3)$$

$$3q_4 - \cancel{3q_4} = u_4 - u_3 \quad 3q_4 = h_4 - h_3$$

$$3q_4 = C_p(T_4 - T_3) \quad 812.0 = 1.005(T_4 - 2900) \Rightarrow T_4 = 3708 \text{ K}$$

(4-5)

$$\frac{V_4}{V_5} = \frac{V_4}{V_3} \cdot \frac{V_3}{V_5} \Rightarrow T_5 = T_4 \left(\frac{T_4}{T_3} \cdot \frac{1}{r} \right)^{k-1}$$

$$T_5 = 3708 \left(\frac{3708}{2900} \cdot \frac{1}{7} \right)^{0.4} \Rightarrow T_5 = 1878 \text{ K}$$

$$\eta_{th} = \frac{W_{net}}{q_{in}} = \frac{1W_2 + 3W_4 + 4W_5}{q_{in}} = \frac{2q_3 + 3q_4 + 5q_1}{1624 + 812.0} = \frac{1624 + 812.0 - 1138 \text{ kJ/kg}}{1624 + 812.0}$$

$$5q_1 = C_v(T_1 - T_5) = .718(293 - 1878) = -1138 \text{ kJ/kg}$$

$$\boxed{\eta_{th} = 53.3\%}$$

D10 ✓

D9 ✓

D8

D7 ✓

D6 ✓ otto, var specific heats

D5 ✓

D4 ✓

D3 ✓

D2

D1

Stirling:

- const T compression (1-2)

$$w_2 = q_2 = \int p dv$$

$$= RT_1 \ln \left(\frac{v_2}{v_1} \right)$$

Test Notes—Hour Exam I D-problems 1-12 ?

Definitions:

$$h = u + Pv$$

$$c_p = (\partial h / \partial T)_p, \quad c_v = (\partial u / \partial T)_v, \quad k = c_p / c_v$$

$$Tds = du + Pdv = dh - vdP$$

Ideal Gas Relations:

$$Pv = RT, \quad R = \bar{R} / MW \quad (\bar{R} = 8.314 \text{ kJ/kmol-K}, \text{ MW} = \text{molecular weight})$$

h, u, c_p, c_v = functions of temperature only

$$du = c_v dT, \quad dh = c_p dT \quad (\text{any process})$$

$$s_2 - s_1 = s_{T2}^o - s_{T1}^o - R \ln \left(\frac{P_2}{P_1} \right); \quad \frac{v_2}{v_1} = \left(\frac{v_{r,T2}}{v_{r,T1}} \right)_{s=\text{constant}}$$

$$s_2 - s_1 = c_p \ln \left(\frac{T_2}{T_1} \right) - R \ln \left(\frac{P_2}{P_1} \right) \quad (\text{constant specific heats})$$

$$s_2 - s_1 = c_v \ln \left(\frac{T_2}{T_1} \right) + R \ln \left(\frac{v_2}{v_1} \right) \quad (\text{constant specific heats})$$

Isentropic Processes (constant specific heats):

$$Pv^k = \text{Constant}$$

$$\frac{P_1}{P_2} = \left(\frac{v_2}{v_1} \right)^k = \left(\frac{T_1}{T_2} \right)^{\frac{k}{k-1}}, \quad \frac{T_1}{T_2} = \left(\frac{v_2}{v_1} \right)^{k-1} = \left(\frac{P_1}{P_2} \right)^{\frac{k-1}{k}}, \quad \frac{v_1}{v_2} = \left(\frac{T_2}{T_1} \right)^{\frac{1}{k-1}} = \left(\frac{P_2}{P_1} \right)^{\frac{1}{k}}$$

Polytropic Processes

$$Pv^n = \text{Constant} \quad {}_1w_2 = \left(\frac{R}{1-n} \right) (T_2 - T_1)$$

Fixed Mass Systems:

$$\delta Q - \delta W = dE$$

$${}_1Q_2 - {}_1W_2 = E_2 - E_1$$

$$E = 1/2 m v^2 + mgz + U$$

$$W = \int P dV$$

$$S_2 - S_1 = \int_1^2 \frac{\delta Q}{T} + S_{\text{gen}}$$

$$x = (u - u_o) + P_o(v - v_o) - T_o(s - s_o)$$

$$W_{\text{REV}} = m(x_1 - x_2)$$

Open Systems:

$$\frac{dE_{\text{cv}}}{dt} = \dot{Q}_{\text{cv}} - \dot{W}_{\text{cv}} + \dot{m}_{\text{in}} \left(h + \frac{V^2}{2} + gz \right)_{\text{in}} - \dot{m}_{\text{out}} \left(h + \frac{V^2}{2} + gz \right)_{\text{out}}$$

If isentropic: $w = \int_0^i v dP$

Memorize

$$\frac{dS_{\text{cv}}}{dt} = \sum_{\text{in}} \dot{m}_{\text{in}} s_{\text{in}} - \sum_{\text{out}} \dot{m}_{\text{out}} s_{\text{out}} + \sum \frac{\dot{Q}_i}{T_i} + \dot{S}_{\text{GEN}}$$

Max power/work = ΔX

Actual power = $\dot{m} \Delta h$

$$\psi = (h - h_o) - T_o(s - s_o) + 1/2 V^2$$

$$\dot{W}_{\text{REV}} = \sum \dot{m}_i \psi_i - \sum \dot{m}_e \psi_e$$

$${}_2q_3 = h_3 - h_2 \text{ (const P. work)}$$

Efficiencies:

$$\eta_{\text{MAX}} = 1 - \frac{T_L}{T_H}$$

$$\eta_{\text{th}} = \frac{W_{\text{ACT}}}{\text{Energy}_{\text{IN}}} \text{ (1st Law Efficiency)}; \quad \eta_{\text{II}} = \frac{W_{\text{ACT}}}{W_{\text{REV}}} \text{ (2nd Law Efficiency)}$$

$$\eta_{\text{isen,t}} = \frac{W_{\text{ACT}}}{W_{\text{ISEN}}} = \frac{(h_1 - h_2)_{\text{ACT}}}{(h_1 - h_2)_{\text{ISEN}}}$$

$$\eta_{\text{isen,p}} = \eta_{\text{isen,c}} = \frac{W_{\text{ISEN}}}{W_{\text{ACT}}} = \frac{(h_1 - h_2)_{\text{ISEN}}}{(h_1 - h_2)_{\text{ACT}}}$$

memorize:

otto,
const $c_{v,p}$ $\rightarrow \eta_{\text{th}} = 1 - \frac{1}{r^{k-1}}; \quad \text{MEP} = \frac{W_{\text{NET}}}{V_1 - V_2}$

David Maloney
9.98J

Brayton Cycle, $r = 12$

total Q_{in} needed = ?

① $T = 300K$

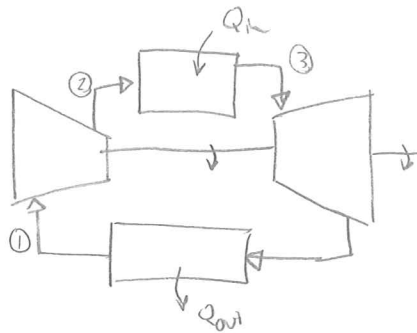
② $T_2 =$

③ $T = 1000K$

$C_p = 1.005$

$C_v = .718$

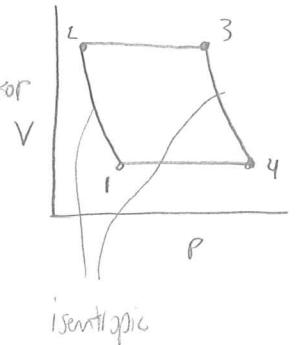
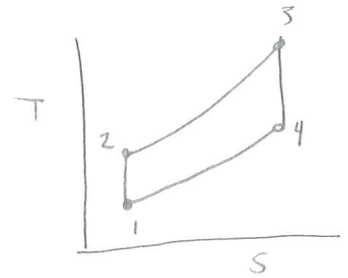
$w_{2/1}^0 = C_p$



$\dot{W}_{out} = 70 MW$

a) 100% efficiency turbine/compressor

b) 85% efficiency



$$T_{2s} = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{(k-1)}{k}} = 300 (12)^{\frac{.4}{1.4}} = 610.2 K$$

$$T_{4s} = T_3 \left(\frac{P_4}{P_3} \right)^{\frac{(k-1)}{k}} = 1000 \left(\frac{1}{12} \right)^{\frac{.4}{1.4}} = 491.7 K$$

$$w_{s, cin} = h_{2s} - h_1 = C_p (T_{2s} - T_1) = (1.005)(610.2 - 300K) = 311.75 \frac{kJ}{kg}$$

$$w_{s, Tout} = h_3 - h_{4s} = 1.005 (1000 - 491.7) = 510.84 \frac{kJ}{kg}$$

$$w_{s, net out} = 510.84 - 311.75 = 199.1 \frac{kJ}{kg}$$

$$\dot{m}_s = \frac{\dot{W}_{net out}}{w_{s, net out}} = \frac{70,000 \frac{kJ}{s}}{199.1 \frac{kJ}{kg}} = \boxed{352.0 \frac{kg}{s}}$$

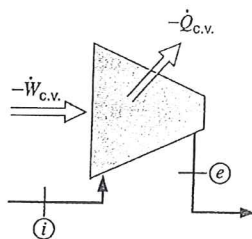
$$w_{a, net out} = w_{a, T, out} = -w_{a, cin} = \eta_t w_{s, T, out} - w_{s, cin} / \eta_c$$

$$= .85 (510.84) - 311.75 / .85 = 67.5 \frac{kJ}{kg}$$

$$\dot{m}_a = \frac{\dot{W}_{net out}}{w_{a, net, out}} = \frac{70,000 \frac{kJ}{s}}{67.5 \frac{kJ}{kg}} = \boxed{1037 \frac{kg}{s}}$$

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- D.4 Air enters a compressor at 100 kPa and 25 °C. The air is compressed to 1 MPa where it exits the compressor at 540 K. The compressor is hotter than the ambient surroundings due to the compression process. Hence 50 kJ of heat per kg of air is transferred to the ambient which is at a temperature of 25 °C. Assume ideal gas behavior and **constant specific heats** evaluated at 300K.



- Find the **actual** compressor work given the measured states
- Find the **minimum** required work into the compressor given the measured states
- Find the 2nd Law efficiency (i.e. exergy based efficiency) of the compressor.
- Another method to define the performance of this compressor would be relative to an isentropic device. Find the isentropic exit temperature of the compressor given the same inlet conditions.
- Find the isentropic efficiency

$$a) \dot{Q}_2 - \dot{W}_2 = \Delta U$$

$$-50 \frac{\text{kJ}}{\text{kg}} - \dot{W}_2 = C_v (T_2 - T_1) = 1.005 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (540 - 25 + 273)^\circ \text{K}$$

$$\boxed{W = -293.21 \frac{\text{kJ}}{\text{kg}}}$$

$$b) \text{ Minimum work} = \Delta \psi = \psi_2 - \psi_1 = h - h_o - T_o (S - S_o)$$

$$= 293.21 - 298 \left[1.005 \ln \left(\frac{540}{298} \right) - 0.2870 \ln \left(\frac{1000}{100} \right) \right] = 293.21 + (18.89) = \boxed{-262.1 \text{ kJ/kg}}$$

$$c) \frac{W_{\text{act}}}{W_{\text{min}}} = \eta_{\text{II}} = \boxed{89.4\%}$$

placed here to show work will be in.

$$d) \frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} \quad T_2 = 298 (10)^{\frac{1.4-1}{1.4}} \quad \boxed{T_2 = 575.35 \text{ K}}$$

$$e) W_{\text{isentropic}} = 1.005 (575.4 - 298) = 278.8 \text{ kJ/kg}$$

$$\eta_s = \frac{278.8}{293.21} = \boxed{95.08\%}$$

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D.5 A mixture of gasoline and air has an energy release upon combustion of approximately 2800 kJ/kg of the mixture. To approximate an actual spark ignition engine using such a mixture, consider an Otto cycle that has a heat addition of 2800 kJ/kg of air, a compression ratio of 7 and a pressure and temperature at the beginning of the compression process of 90 kPa and 10°C. Assume ideal gas behavior and **constant specific heats** evaluated at 300K.

- Find the maximum pressure and temperature in the cycle (kPa, K).
- Find the thermal efficiency of the cycle.
- Find the net specific work from the cycle (kJ/kg)
- Find the mean effective pressure for the cycle (kPa)

① 90 kPa ② $P = 1372 \text{ kPa}$ ③ $P = 10.05 \text{ MPa}$ ④
 283°K $T = 616 \text{ K}$ $T = 4516$ $T = 2074 \text{ K}$

isotropic compression $r = 7 = \frac{v_1}{v_2}$ $T_2 = T_1 (r)^{k-1}$ $T_2 = 283(7)^{1.4-1}$

$P_2 = P_1 \left(\frac{v_1}{v_2} \right)^k = 90(7)^{1.4} =$

heat addt. const. v. ${}_2Q_3 = 2800 \text{ kJ/kg}$ No work $\Delta h = 2800 \text{ kJ/kg} = C_v(T_3 - T_2)$

$2800 = .718(T_3 - 616)$

a) $T_3 = 4516 \text{ K}$ $PV = mRT$ $\frac{P_2}{T_2} = \frac{P_3}{T_3}$ $P_3 = 10.058 \text{ MPa}$

b) $\eta_{th} = \frac{w_{net}}{q_{in}}$ $w_{net} = w_2 + w_3 + w_4$ isentropic expansion $\frac{T_3}{T_4} = \left(\frac{v_4}{v_3} \right)^{k-1}$ $T_4 = 4516 / 7^{1.4-1}$
 $= C_v(T_1 - T_2 + T_3 - T_4) = .718() = 1514.26 \text{ kJ/kg}$

$\eta_{th} = \frac{1514}{2800} = 54.08\%$

c) $w_{net} = 1514.26 \text{ kJ/kg}$

d) $MEP = \frac{w_{net}}{v_1 - v_2} = \frac{1514.26 \text{ kJ/kg}}{.9025 - .1289 \text{ m}^3/\text{kg}}$

$MEP = 1957$

$Pv = RT$
 $v_1 = .2867(283) \frac{\text{kJ}}{\text{kg} \cdot \text{K}} = .81427 \text{ m}^3/\text{kg}$
 $v_2 = .2867(616) = .17673 \text{ m}^3/\text{kg}$
 $.9025 - .1289$

$.9025 - .1289$

D10

① $T = 283 \text{ K}$
 $P = 90 \text{ kPa}$

② $T = 616.34 \text{ K}$
 $P = 1372 \text{ kPa}$

③ $T = 3123 \text{ K}$
 $P_3 =$
 $V_3 =$

④ $T = 1219 \text{ K}$

⑤ $T = 424.4$
 $P = 90 \text{ kPa}$

$r = 7 \quad \frac{V_1}{V_2}$
 $\frac{V_4}{V_3} = 1.5 \quad \frac{V_1}{V_2}$

(1-2) isentropic compression

$$T_2 = T_1 \left(\frac{V_1}{V_2} \right)^{\gamma-1} = 283 (7)^{0.4} = 616.34 \text{ K}$$

$$P_2 = P_1 \left(\frac{V_1}{V_2} \right)^{\gamma} = 90 (7)^{1.4} = 1372 \text{ kPa}$$

$$q_{1-2}^0 = w_2 = u_2 - u_1$$

$$w_2 = u_2 - u_1 = C_v (T_2 - T_1)$$

$$w_2 = .718 (616.34 - 283)$$

$$w_2 = -239.34 \text{ kJ/kg}$$

(2-3) const $\dot{q}_{in}$ $q_{in}^0 = u_3 - u_2 = C_v (T_3 - T_2) = .718 (T_3 - 616) \Rightarrow T_3 = 3123 \text{ K}$
 (1830 kJ/kg)

(3-4) isent. expansion

$$\frac{T_3}{T_4} = \left(\frac{V_4}{V_3} \right)^{\gamma-1}$$

$$T_4 = \frac{3123}{[1.5(7)]^{0.4}}$$

$$T_4 = 1219 \text{ K}$$

d) expansion work (3-4) isentropic

$$q_{3-4}^0 = w_4 = u_4 - u_3 = C_v (T_4 - T_3) = .718 (1219 - 3123)$$

$$w_4 = -1367 \text{ kJ/kg}$$

e) $P_4 = \frac{P_3}{\left(\frac{V_4}{V_3} \right)^{\gamma}}$
 $= 6953 (1.5(7))^{-(1)(1.4)}$

$$P_4 = 258.5 \text{ kPa}$$

$$\frac{V_4}{V_3} = 1.5(7)$$

$$Pv = RT$$

$$V_2 = V_3 = \frac{RT_2}{P_2} = \frac{.2870 (616.34)}{1372} = .1289$$

$$P_3 = \frac{.2870 (3123)}{.1289} = 6953 \text{ kPa}$$

f) $T_5 = ?$ const volume heat rejection (4-5)

$$q_{4-5} = C_v (T_5 - T_4)$$

$$Pv = RT$$

$$T_5 = \frac{P_5 V_4}{R} = \frac{P_1 R T_4}{R P_4} = \frac{90 (1219)}{258.5}$$

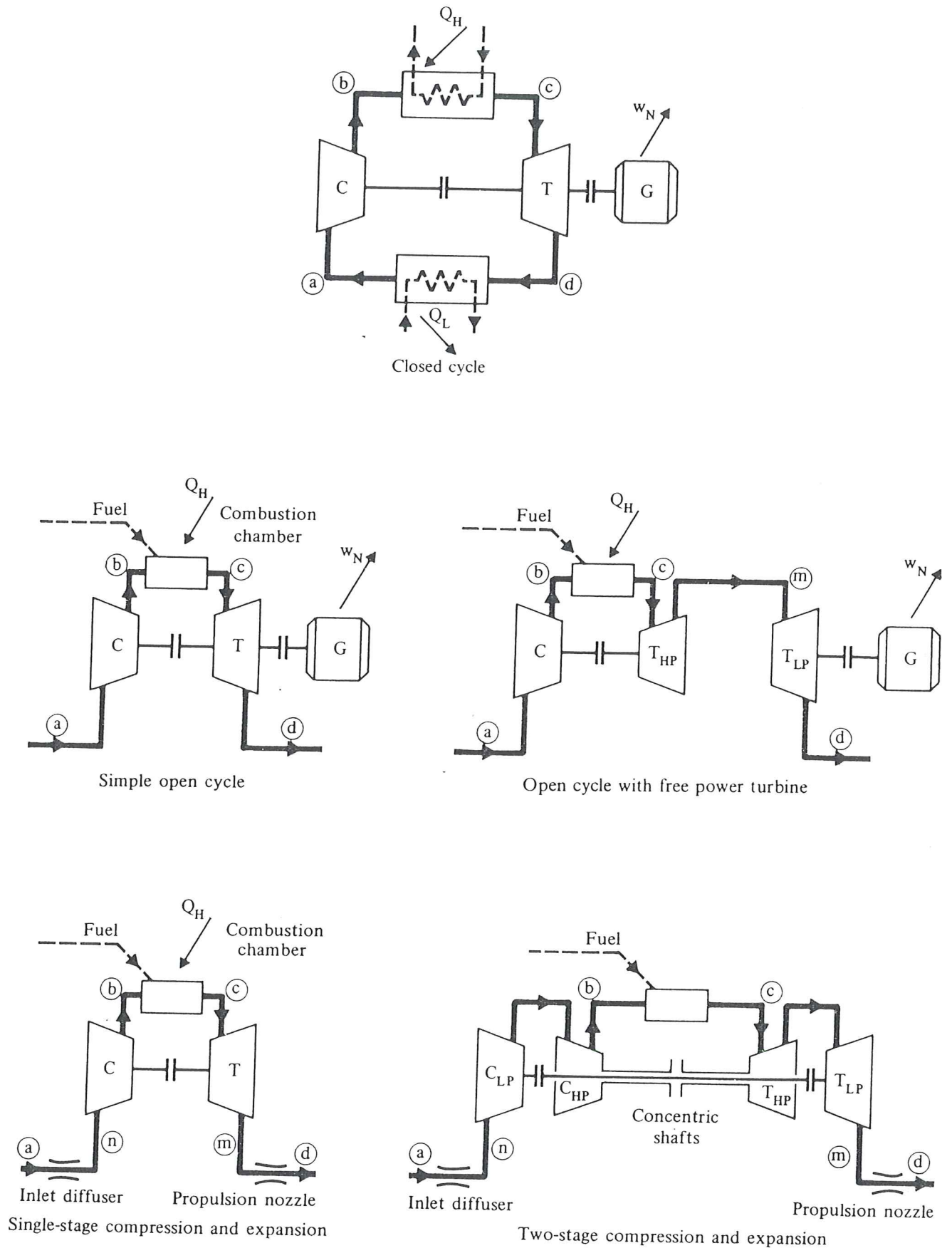
$$T_5 = 424.4 \text{ K}$$

$$V_4 = \frac{R T_4}{P_4}$$

g) find work during const pressure process $w = \int p dv$ $sw_i = \int_1^5 p dv$

$${}_5w_1 = 90 (V_1 - V_5) = 90 (.9025 - 1.353)$$

$${}_5w_1 = -40.55$$



Turbo-jet propulsion cycles

FIG. 1.36 Variations of the Brayton cycle.

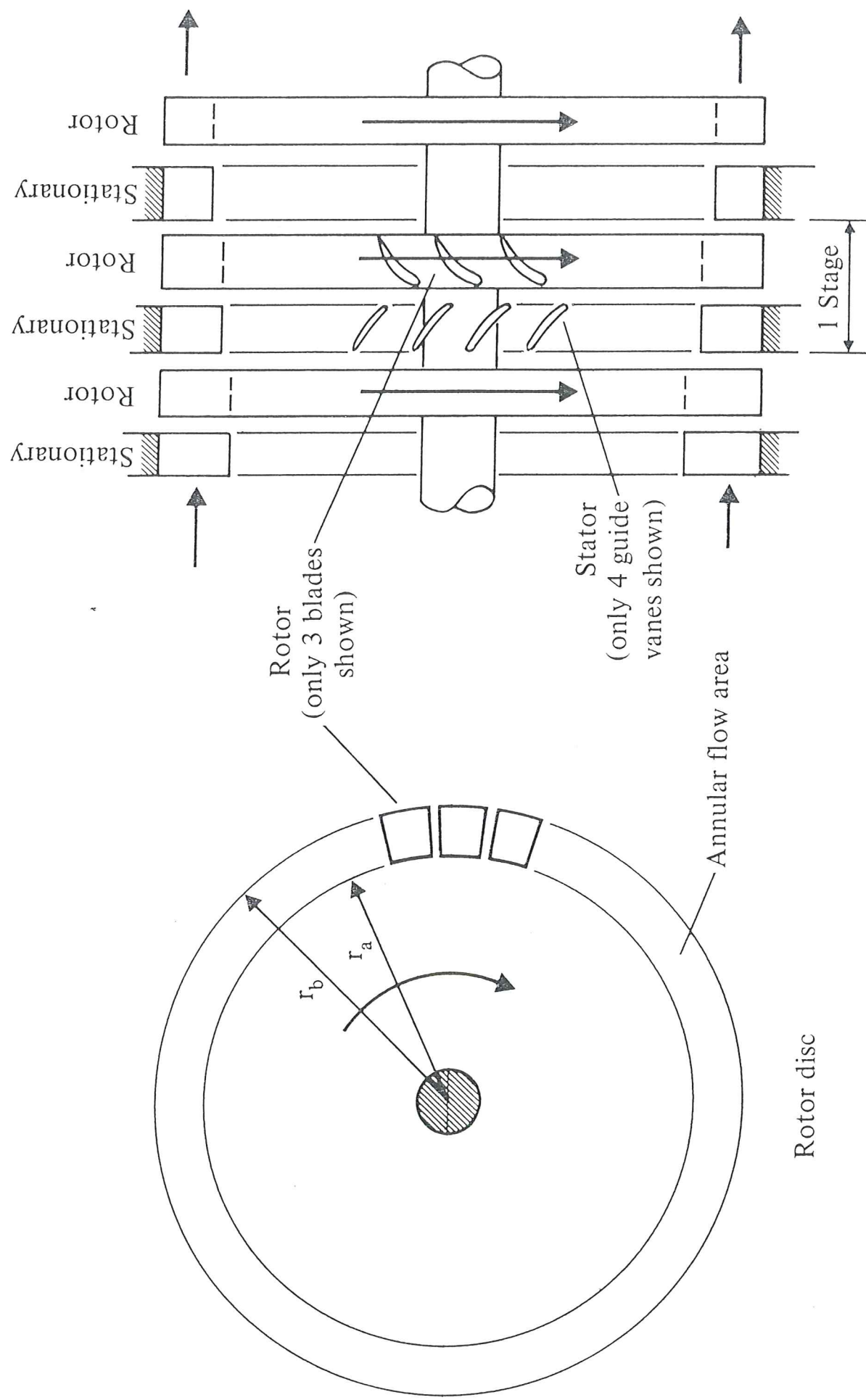
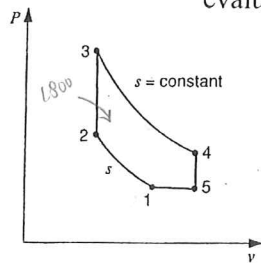


FIG. 3.37 An axial-flow compressor (schematic).

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D.10

A Miller cycle can be used to model an engine that has a longer expansion process than the compression process, as shown in the pressure-volume diagram below. This difference in compression and expansion ratios can be achieved using variable valve timing such as in the Toyota hybrid system. For the problem below using air, the inlet temperature and pressure at state 1 are 283 K and 90 kPa , respectively. The constant volume heat input is 1800 kJ/kg . The compression ratio (i.e. V_1/V_2) is 7 whereas the expansion ratio (i.e. V_4/V_3) is 1.5 times larger, i.e. $V_4/V_3 = 1.5(V_1/V_2)$. Assume ideal gas behavior and **constant specific heats** evaluated at 300 K .



Process 1-2 and 3-4 are isentropic

Process 5-1 is constant pressure

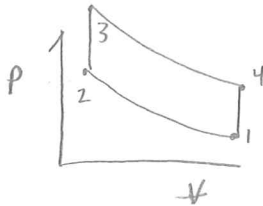
- Find the temperature at the end of compression and the compression work, ${}_1w_2$ ✓
- Find the temperature after the constant volume heat addition, T_3 ✓
- Find the temperature after expansion, T_4
- Find the expansion work, ${}_3w_4$
- Find the pressure after expansion, i.e. P_4
- Find the temperature after the constant volume heat rejection process, i.e. T_5
- Find the work during the constant pressure process, state 5 to state 1. (kJ/kg)

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D.11

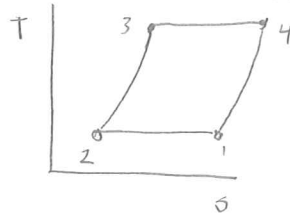
An ideal Stirling cycle uses 0.12 kg of air as the working fluid. The lower temperature at which energy is exchanged is 300 K while the upper temperature is 2000 K. Air is at 150 kPa at the beginning of compression and the peak pressure is 3 MPa. Assume that an ideal regenerator is used. Determine a) the energy captured and supplied by the regenerator, b) the net work from the cycle, c) the thermal efficiency of the cycle. Assume constant specific heats.

① $T = 300 \text{ K}$
 $P = 150 \text{ kPa}$



② $T = 300 \text{ K}$

③ $T = 2000 \text{ K}$
 $P = 3 \text{ MPa}$



④ $T =$

$m = 0.12 \text{ kg}$

$q_{reg} = q_{23}$

$R_{air} = .2870$

$c_v = .718$

$c_p = 1.005$

(1-2) isothermal compression $q_2 - w_2 = u_2 - u_1 = 0 \quad (T_2 = T_1)$

$q_2 = w_2 = \int P dv \quad P = \frac{RT}{v} \quad q_2 = RT \int \frac{dv}{v} = RT \ln\left(\frac{v_2}{v_1}\right) = RT \ln\left(\frac{P_1 T_3}{P_2 T_3}\right)$

$= (.287)(300) \ln\left(\frac{150 \cdot 2000}{300 \cdot 3000}\right) = -94.59 \text{ kJ/kg}$

(2-3) $w_3 = 0$ const. & heat addition

$q_3 = u_3 - u_2 = c_v (T_3 - T_2) = .718 (2000 - 300)$

$q_3 = 1221 \text{ kJ/kg} \leftarrow x (.12 \text{ kg})$

$Q_3 = 146.5 \text{ kJ}$

isothermal expansion

(3-4) $q_4 = w_4 = RT_3 \ln\left(\frac{v_4}{v_3}\right) = RT_3 \ln\left(\frac{T_1 P_3}{P_1 T_3}\right) = .287 (2000) \ln\left(\frac{300 \cdot 3000}{150 \cdot 2000}\right) = 630.6 \text{ kJ/kg}$

(4-1) const. & heat rejection

$q_1 = c_v (T_1 - T_4) = .718 (300 - 2000) = -1221 \text{ kJ/kg}$

$w_{net} = m(w_2 + w_4) = .12 \text{ kg} (-94.59 + 630.6) = 64.32 \text{ kJ}$

$\eta_{th} = \frac{w_{net}}{q_{in}} = \frac{64.32 \text{ kJ}}{(630.6)(.12 \text{ kg})} = 85\%$

David Maloney 9-16-16

HW #1
9

ME 221 Applied Thermodynamics
Fall 2010

D.6 A spark ignition engine is to be modeled using an ideal Otto cycle. The working fluid, air, is at 95 kPa and 290 K before compression. The compression ratio is 9 and the maximum temperature is 2000 K. For the calculations below **use variable specific heats** (Do not interpolate, enter the table by choosing the value in the table closest to your calculated value).

- Find the pressure and temperature at the end of compression.
- Find the required heat input into the cycle on a specific basis.
- Find the net specific work from the cycle.
- Find the cycle thermal efficiency
- Find the maximum pressure in the cycle as predicted by the model.

① $p_1 = 95 \text{ kPa}$ ② $p = 1995$ ③ $p =$ ④ $p =$ $r = 9 = \frac{v_1}{v_2}$
 $T = 290 \text{ K}$ $T = 620 \text{ K}$ $T = 2000 \text{ K}$ $T = 1100 \text{ K}$

a) isentropic compression $\frac{v_2}{v_1} = \frac{1}{9} = \left(\frac{v_{R, T_2}}{v_{R, T_1}} \right)$ $\frac{v_{R, T_2}}{676.1} = 96.59 \Rightarrow T_2 = 620 \text{ K}$

$0 = S_{T_2}^\circ - S_{T_1}^\circ - R \ln \left(\frac{p_2}{p_1} \right) \Rightarrow \left(\frac{2.54175 - 1.66802}{.2870} \right) = \frac{p_2}{p_1} \Rightarrow p_2 = 1995 \text{ kPa}$

b) $\dot{q}_{\text{const heat addition}}$

$q_3 = u_3 - u_2 = (1678.7 - 450.09) \frac{\text{kJ}}{\text{kg}} \Rightarrow q_3 = 1229 \text{ kJ/kg}$

c) isentropic expansion $w_{\text{net}} = q_3 + q_4 \Rightarrow v_{r3} = f(T_3) = 2.776$
 $v_{r4} = 7(2.776) = 19.432 \Rightarrow T_4 = 1100 \text{ K}$ $u_4 = 845.33$
 $w_{\text{net}} = 1229 \frac{\text{kJ}}{\text{kg}} + (206.91 - 845.33) \frac{\text{kJ}}{\text{kg}} = 590.58 \frac{\text{kJ}}{\text{kg}}$

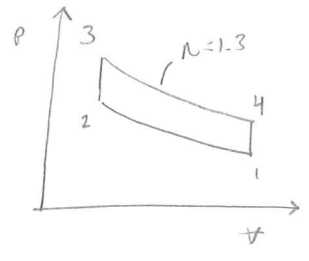
d) $\eta_{\text{th}} = \frac{w_{\text{net}}}{q_{\text{in}}} = \frac{590.58}{1229} = 48.05\%$

e) $p_{\text{max}} = p_3$ $\frac{p_2 v_2}{R T_2} = \frac{p_3 v_3}{R T_3}$ $p_3 = \frac{1995}{620} (2000) \Rightarrow p_3 = 6435 \text{ kPa}$

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- D.7 An Otto cycle is to be used to model an engine cycle. All assumptions of the ideal Otto cycle are to be applied except a **polytropic process** with $n = 1.3$ will be used for the **expansion process**. The conditions at the beginning of compression are $T_1 = 333$ K, $P_1 = 90$ kPa and the compression ratio is 8. The energy input into the cycle during the constant volume process is 2000 kJ/kg. Assume constant specific heats.

- Find the temperature (K) and pressure (kPa) after compression
- Find the peak temperature of the cycle. (K)
- Find the temperature at the end of the expansion process. (K)
- Find the expansion work (kJ/kg)
- Find the **net** heat transfer for the cycle (kJ/kg)



① $P = 90 \text{ kPa}$
 $T = 333 \text{ K}$

② $P = 1654 \text{ kPa}$
 $T = 765 \text{ K}$

③ $T = 3554 \text{ K}$

④

a) isentropic compression $T_2 = T_1 \left(\frac{v_1}{v_2} \right)^{\gamma-1} = 333 \text{ K} (8)^{0.4} = \boxed{765 \text{ K}}$
 $P_2 = P_1 \left(\frac{v_1}{v_2} \right)^{\gamma} = 90 \text{ kPa} (8)^{1.4} = \boxed{1654 \text{ kPa}}$

b) $q_{\text{in}} = u_3 - u_2 = C_v (T_3 - T_2)$ $T_3 = \frac{q_{\text{in}}}{C_v} + T_2 = \frac{2000}{.717} + 765 = \boxed{3554 \text{ K}}$

c) polytropic expansion

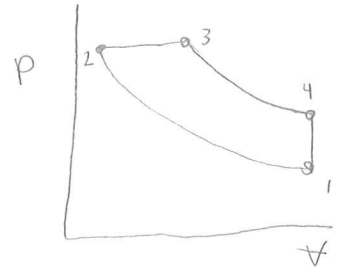
$P_3 v_3^n = P_4 v_4^n$ $\frac{P_4}{P_3} = \left(\frac{v_3}{v_4} \right)^n = \left(\frac{1}{r} \right)^n$ $P_3 = \frac{R T_3}{v_3}$ $P_4 = \frac{R T_4}{v_4}$
 $\frac{T_4}{T_3} = \left(\frac{v_3}{v_4} \right)^{n-1} = \left(\frac{1}{r} \right)^{n-1}$ $T_4 = 3554 \text{ K} \left(\frac{1}{8} \right)^{0.3} = \boxed{1905 \text{ K}}$

d)

e) $q_{\text{net}} = w_{\text{net}} = w_2 + w_4$ $q_2 = u_2 - u_1 = C_v (T_2 - T_1) \Rightarrow w_2 = .717 \frac{\text{kJ}}{\text{kg K}} (333 - 765)$
 $w_2 = -309.7 \frac{\text{kJ}}{\text{kg}}$ $q_{\text{net}} = 1578 - 309.7 = \boxed{1268 \frac{\text{kJ}}{\text{kg}}}$

d)

Polytropic expansion $w_4 = \left(\frac{R}{1-n} \right) (T_4 - T_3) = \frac{.287 \text{ kJ/kg K}}{(1-1.3)} (1905 - 3554 \text{ K}) = \boxed{1578 \frac{\text{kJ}}{\text{kg}}}$



D.8 The processes within an engine are to be modeled using an ideal Diesel cycle with a compression ratio of 14.84. The cylinder has a volume of 0.0005 m^3 before compression (state 1). At this state (state 1) the temperature is 300 K and the mass of air is 0.001 kg . Energy, equivalent to 1.386 kJ , is added to this ideal Diesel cycle as heat addition. For the calculations below **use variable specific heats** (Do not interpolate, enter the table by choosing the value in the table closest to your calculated value).

- Find the temperature and pressure at the end of compression (K, kPa)
- Find the temperature after the heat addition (K)
- Find the temperature after expansion (K)
- Find the total heat rejected from the cycle (kJ)
- Find the thermal efficiency of the cycle

① $V = 0.0005 \text{ m}^3$
 $T = 300 \text{ K}$
 $P = 172 \text{ kPa}$

② $V = 3.37 \text{ E-}5$
 $T_2 = 840 \text{ K}$
 $P_2 = 7154 \text{ kPa}$

③ $T = 2000 \text{ K}$

④ $T = 1140 \text{ K}$
 $U = 880.35$

a) $P_2 = \frac{mRT_2}{V_2} = \frac{0.001 \text{ kg} (0.287 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}) (300 \text{ K})}{0.0005 \text{ m}^3} = 172.2 \text{ kPa}$
 $\frac{1}{14.84} = \frac{V_{R,T_2}}{V_{R,T_1} 6.21.2} \quad P_2 = \frac{0.001 \text{ kg} (0.287) (840)}{3.37 \text{ E-}5}$

(1-2) isentropic compression

b) (2-3) const p heat addition $q_3 = h_3 - h_2 \quad h_3 = 866.08 \text{ kJ/kg} (0.001 \text{ kg}) + 1.386 = 2252 \text{ kJ/kg}$
 $T_3 = 2000 \text{ K}$

c) isentropic expansion $V_{R_4} = V_{R_3} \left(\frac{T_3}{T_4} \right) \quad T_4 = 1140 \text{ K}$

d) $q_{12} = u_1 - u_4 = 214.07 - 880.35 = -511 \text{ kJ/kg} (0.001 \text{ kg}) = \boxed{0.667 \text{ kJ}}$ heat rejected

e) $\eta_{th} = \frac{h_3 - h_2 - (u_4 - u_1)}{(h_3 - h_2)} = \frac{1386 \text{ kJ/kg} - (880 - 214)}{1386}$

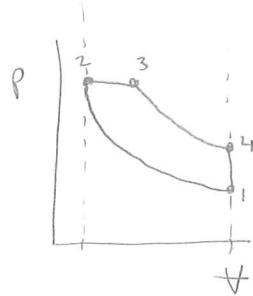
$\eta_{th} = 51.9\%$

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D.9

At the beginning of compression in an ideal diesel cycle, $T = 300 \text{ K}$, $P = 100 \text{ kPa}$. After combustion (heat addition) is complete, $T = 1800 \text{ K}$. The cycle has a compression ratio of 18.11. Assume ideal gas behavior but **do not assume constant specific heats** (i.e. use variable specific heats).

- Find the temperature after compression
- Find the energy into the cycle
- Find the temperature at the end of the expansion process.
- Find the thermal efficiency.



① $T = 300 \text{ K}$
 $P = 100 \text{ kPa}$
 $h = 300.19$
 $u = 214.07$

② $T = 900 \text{ K}$
 $P =$
 $h = 932.93$
 $u = 674.58$

③ $T = 1800 \text{ K}$
 $P =$
 $h = 2003.3$
 $u =$

④ $T = 876 \text{ K}$
 $u = 661.13$

$r = 18.11$

(1-2) isentropic compression

$$\frac{V_2}{V_1} = \frac{V_{r, T_2}}{V_{r, T_1}} = \frac{1}{18.11} = \frac{1}{621.2}$$

$T_2 = 900 \text{ K}$

(2-3) const. P $q_{in} = h_3 - h_2 = 2003.3 - 932.93$

$q_3 = 1070.4 \frac{\text{kJ}}{\text{kg}}$

(3-4) isentropic expansion

$$r \left(\frac{T_2}{T_3} \right) = \frac{V_{r, T_2}}{V_{r, T_3}} = \frac{V_{r, T_2}}{V_{r, T_3}} = 3.994 (18.11)^{\frac{1}{2}}$$

$T_4 = 876 \text{ K}$

$$\eta_{th} = \frac{w_{net}}{q_3} = \frac{h_3 - h_2 - u_4 - u_1}{h_3 - h_2}$$

$h_3 - h_2 = 2003.3 - 932.9 = 1070.4 \frac{\text{kJ}}{\text{kg}}$

$u_4 - u_1 = 661.13 - 214.07 = 447.06 \frac{\text{kJ}}{\text{kg}}$

$\eta_{th} = 58.2 \%$

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D.3 An adiabatic turbine operates using air at a flow rate of 5 kg/s. Air enters the turbine at 550 kPa and 425 K. The measured conditions of the air leaving the turbine are 100 kPa and 325 K. Take ambient temperature to be 298 K and pressure to be 100 kPa. Assume constant specific heats for air at 300 K.

- Find the exergy flow of the state entering the turbine.
- Find the actual power from the turbine.
- Find the maximum power that could be extracted from the turbine given the measured inlet and exit states.
- Find the first law (thermal) and second law efficiencies.
- Find the exit temperature if the turbine was isentropic, assuming the same exit pressure.

$$a) \psi = (h - h_0) - T_0 (s - s_0) + \frac{V^2}{2} + \frac{gz}{2}$$

$$= (426.35 - 298.18) -$$

$$C_p (\Delta T) - T_0 \left[c_p \ln \frac{T_1}{T_0} - R \ln \frac{P_1}{P_0} \right] = 1.005 (127) - 298 \left[1.005 \ln \left(\frac{425}{278} \right) - .287 \ln \left(\frac{550}{100} \right) \right]$$

$$\psi_1 = 167.117 \frac{\text{kJ}}{\text{kg}} (5 \text{ kg/s}) = \boxed{835.58 \text{ kW}}$$

$$b) \dot{W}_{\text{actual}} = \dot{Q} - \dot{W} = \dot{m} \Delta h \quad -\dot{W} = \dot{m} C_p \Delta T = 1.005 (425 - 325)$$

$$\dot{W} = 502.5 \frac{\text{kJ}}{\text{s}} \text{ kW}$$

$$c) \Delta \psi = C_p (T_1 - T_2) + T_0 \left(c_p \ln \frac{T_1}{T_2} - R \ln \frac{P_1}{P_2} \right)$$

$$= 1.005 (425 - 325) - 298 \left[1.005 \ln \left(\frac{425}{325} \right) - .287 \ln \left(\frac{550}{100} \right) \right]$$

$$= (100.5 + 65.458) \text{ kJ/kg}$$

$$= \boxed{829.79 \text{ kW}} \text{ maximum power that could be ext. (} \dot{W}_{\text{rev}} \text{)}$$

$$d) \eta_I = \frac{\dot{W}_{\text{out}}}{\dot{Q}_{\text{in}}} = \frac{502.5}{2135.6} \quad \dot{Q}_{\text{in}} = \dot{m} C_p (T_{\text{in}}) = 5 \text{ kg/s} \cdot 1.005 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (425 \text{ K})$$

$$\eta_I = .2353$$

$$\eta_{II} = \frac{502.5}{829.79} = \boxed{\eta_{II} = .606}$$

$$e) S_1 - S_2 = 0 \quad c_p \ln \frac{T_1}{T_2} = R \ln \frac{P_1}{P_2}$$

$$1.005 \ln \left(\frac{425}{T_2} \right) = .287 \ln \left(\frac{550}{100} \right)$$

$$\ln () = .4868$$

$$\frac{425}{T_2} = 1.627$$

$$\boxed{T_2 = 261 \text{ K}}$$

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- D2. Air enters a steady flow turbine at 1600 K, 3000 kPa and the measured conditions at the exit are 1000 K and 100 kPa. The ambient temperature is 298 K. a) What is the maximum work that could be extracted out of this turbine? (kJ/kg). b) What would be the work output if the turbine was assumed adiabatic? For both parts, assume ideal gas behavior but **do not assume constant specific heats** (i.e. use variable specific heats).

$$W_{max} = \Delta \psi$$

$$\psi_1 = (h_1 - h_o) - T_o (s_1 - s_o)$$

$$h(1600) - h(298)$$

$$\psi_1 = (1757.57 - 298.18) - 298 (\quad) = 913.97$$

$$1000K \quad \psi_2 = (1046.04 - 298.18) - 298 (\quad) =$$

$$s_1 - s_2 = s_1^o - s_2^o - R \ln \frac{p_1}{p_2} = 3.52364 - 2.96770 - .287 \ln \left(\frac{3000}{100} \right)$$

$$s_1 - s_2 = -.4207 \text{ kJ/kgK}$$

$$\Delta h - T_o \Delta s$$

$$711.53 - (298 \cdot -.4207)$$

a) $W_{max} = 836.90 \text{ kJ/kg}$

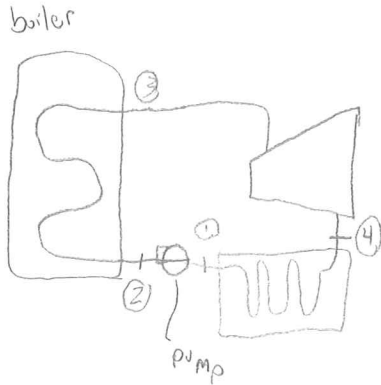
b) $\dot{Q} = \dot{W}_2 = \Delta E_{internal}$

$$-W = h_2 - h_1 =$$

$$W = 711.53 \text{ kJ/kg}$$

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10-17) Rankine Cycle



$$\dot{w}_{\text{pump}} = (v \Delta P) \dot{m}$$

$$= .001017 (3,000 - 30) (50 \text{ kg/s})$$

$$\dot{w}_{\text{pump}} = 158.90 \text{ kW}$$

$$\dot{m} = 50 \text{ kg/s}$$

$$\dot{w}_{\text{turbine}} = ?$$

$$\dot{w}_{\text{pump}} = ?$$

shv

$$① P = 30 \text{ kPa}$$

$$T =$$

$$h = 251.42$$

$$v = .001017$$

$$② P = 3 \text{ MPa}$$

$$T =$$

$$③ P = 30 \text{ kPa}$$

$$T = 700^\circ\text{C}$$

$$h = 3912.2$$

$$s = 7.7590$$

$$④ P = 30 \text{ kPa}$$

$$T = 69.09$$

$$h = 2621.8$$

$$s = 7.7590$$

$$s_3 = s_4$$

$$s_4 = s_f(30 \text{ kPa}) + x s_{fg}(30 \text{ kPa})$$

$$7.759 = .9441 + x(6.8234)$$

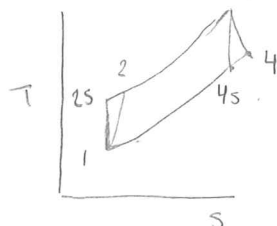
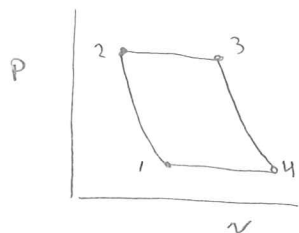
$$x_4 = .9988$$

$$h_4 = 289.27 + .9988(2335.3) = 2621.8$$

$$\dot{w}_{\text{turbine}} = \dot{m} (h_3 - h_4) = \boxed{64,520 \text{ kJ/s}}$$

D.14 A simple gas turbine system is to be modeled using a Brayton cycle. Air enters the compressor at 100 kPa and 300 K. The compressor has a pressure ratio of 10 and an isentropic efficiency of 85% (i.e. $\eta_c = 0.85$). Due to flow losses in the combustor the air enters the turbine at 950 kPa and 1400 K. The turbine has an exit pressure of 100 kPa and an isentropic efficiency of 88% (i.e. $\eta_T = 0.88$). Assume constant specific heats. (i.e. $C_v = 0.717 \text{ kJ/kgK}$, $C_p = 1.004 \text{ kJ/kgK}$).

- Sketch the T-s diagram for the entire system including both the isentropic and actual states for the compressor and turbine. Label the states.
- Find the actual compressor work (kJ/kg).
- Find the actual turbine work (kJ/kg).
- Find the heat transfer into the combustor (kJ/kg)



isentropic
(1-2) isent. comp. $\dot{Q}_2 - \dot{Q}_1 = \dot{m}(h_2 - h_1)$
 $T_2 = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = 300 (10)^{\frac{1.4}{1.4}} = 579.2 \text{ K}$

① 100 kPa
300 K

② 1000 kPa

(579.2 K) isent.

③ 950 kPa

1400 K

④ 100 kPa

$$\eta_c = 0.85 = \frac{w_{cs}}{w_c} = \frac{\dot{m}(h_1 - h_2)_s}{\dot{m}(h_1 - h_2)_{\text{actual}}}$$

$$0.85 = \frac{C_p(T_1 - T_2)_{\text{isent}}}{\dot{w}_{\text{actual}}} =$$

$$\dot{w}_{\text{actual}} = \frac{(-280.3)(1.004)}{0.85}$$

$$w_{\text{compressor}} = 388.0 \frac{\text{kJ}}{\text{kg}}$$

$$T_4 = T_3 \left(\frac{P_4}{P_3} \right)^{\frac{k-1}{k}}$$

$$T_4 = 1400 \left(\frac{100}{950} \right)^{\frac{1.4}{1.4}} = 735.8 \text{ K}$$

$$\Rightarrow w_{Ts} = C_p(T_3 - T_{4s}) = 666.8 \frac{\text{kJ}}{\text{kg}}$$

$$w_{t,\text{act}} = \eta_T w_{Ts} = 0.88(666.8) = 586.8 \frac{\text{kJ}}{\text{kg}}$$

$$w_T =$$

$$q_{\text{in}} = h_3 - h_2 = C_p(T_3 - T_2)$$

$$w_{c,\text{act}} = C_p(T_1 - T_2)$$

$$T_2 = T_1 - \frac{w_{c,\text{act}}}{C_p} = 300 - \frac{-329.3}{1.004} = 628.5 \text{ K}$$

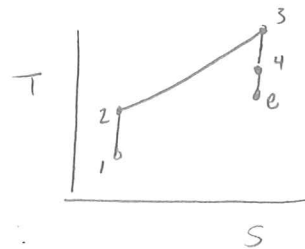
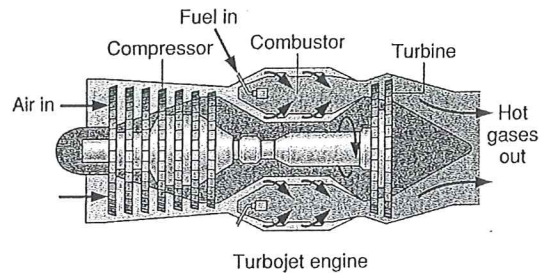
$$q_{\text{in}} = 1.004(1400 - 628.5)$$

$$q_{\text{in}} = 774.6 \frac{\text{kJ}}{\text{kg}}$$

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- D.15 Air enters the compressor of turbo-jet engine, modeled as an ideal air-standard Brayton cycle, at 85 kPa and 270 K. The turbine inlet temperature is 1200 K and the turbine inlet pressure is 800 kPa. Assume an isentropic compressor, turbine and exit nozzle. The ambient pressure is 80 kPa. Assume constant specific heats (i.e. $C_v = 0.717$ kJ/kgK, $C_p = 1.004$ kJ/kgK, $k = 1.4$).



- Find the temperature after the compressor. (K)
- Find the specific compressor work (kJ/kg)
- Find the temperature of the flow exiting the turbine (**before** the nozzle) (K)
- Find the pressure of the flow exiting the turbine (**before** the nozzle) (kPa)
- Find the temperature of the flow **after** the nozzle assuming it exits at ambient pressure. (K)
- Find the exit velocity. (m/s)

a) T_2 : $T_1 = 270$ K $P_1 = 85$ kPa $P_2 = P_3 = 800$ kPa $T_2 = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = 270 \left(\frac{800}{85} \right)^{\frac{1.4}{1.4}}$

$T_2 = 512.3$ K

b) $w_c = C_p (T_2 - T_1)$ $w_c = 1.004 (512.3 - 270) = -243.3$ kJ/kg w_c

c) T_4 : $w_c = -w_T = 243.3$ kJ/kg $= C_p (T_3 - T_4) = 1.004 (1200 - T_4)$

$T_4 = 957.7$ K

d) Find P_4 : $P_4 = P_3 \left(\frac{T_4}{T_3} \right)^{\frac{k}{k-1}} = 800 \left(\frac{957.7}{1200} \right)^{\frac{1.4}{1.4}} = 363.2$ kPa $= P_4$

e) T_e : $T_e = T_4 \left(\frac{P_e}{P_4} \right)^{\frac{k-1}{k}} = 957.7 \left(\frac{80}{363.2} \right)^{\frac{1.4}{1.4}} = 621.6$ K isentropic nozzle

f) v_e : $h_4 = h_e + \frac{v_e^2}{2}$ $C_p (T_4 - T_e) = \frac{v_e^2}{2} = 1.004 (957.7 - 621.6)$

$v_e = 821.5$ m/s

David Maloney

9

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- D1. Air in a piston/cylinder arrangement undergoes a **polytropic expansion process** (i.e. $Pv^n = \text{constant}$) with $n = 1.5$. Initially the air is at 3 MPa and 3000 K (i.e. state 1) and the gas expands to 1 MPa (state 2). Assume ideal gas behavior and **constant specific heats** evaluated at 300K. Assume ambient (or dead state) conditions of 298 K and 100 kPa.
- a) Find the temperature at state 2. (K)
 - b) Find the **expansion work** given the polytropic expansion from state 1 to state 2. (kJ/kg)
 - c) Find the **heat transfer** given the work and states 1 and 2 (kJ/kg).
 - d) Find the **maximum work** that could be extracted out of this process between states 1 and 2. (kJ/kg)
 - e) If the air was expanded **isentropically** from the given T and P at state 1 to the pressure at state 2 (i.e. 1 MPa), find the expansion work. (kJ/kg)

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D1

$PV^{1.5} = \text{const.}$ Ideal gas behavior, constant $C_p, C_v, < 300\text{K}>$

① $P_1 = 3\text{MPa}$

$T_1 = 3000\text{K}$

② $P_2 = 1\text{MPa}$

Surf $T = 298\text{K}$

$P = 100\text{kPa}$

Air $k = 1.4$

$R = .287$

$C_v = .718 < 300\text{K}>$

a) $T_2 = ?$ $\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}}$ $T_2 = 3000 \left(\frac{1}{3}\right)^{\frac{(1.5-1)}{(1.5)}}$
 $= \boxed{2080\text{K}}$

b) $W_{\text{expansion}}$ given polytropic exp. from state 1 to 2

$W_b = \frac{P_2 V_2 - P_1 V_1}{1-n} = \frac{.287(2080-3000)}{1-1.5} = \boxed{528.08 \text{ kJ/kg}}$ W_b work done by system

$PV = RT$

$V_1 = \frac{.287(3000)}{3000} = .287 \text{ m}^3/\text{kg}$ $V_2 = \frac{.287(2080)}{1000} = .5970 \text{ m}^3/\text{kg}$ $V_0 =$

c) $q_2 - w_2 = (u_2 - u_1) = C_v (T_2 - T_1)$

$q_2 = 528.08 \text{ kJ/kg} + .718(2080 - 3000)$

$q_2 = \boxed{-132.48 \text{ kJ/kg}}$ heat into system

d) $W_{\text{max available}} = X_1 - X_2 = u - u_0 + P_0 (v - v_0) - T_0 (s - s_0)$

$u - u_0 = C_v (T - T_0) = .718(2080 - 3000) = -660.56$

$P_0 (v - v_0) = 100(.5970 - .287) = 31.0$

$T_0 (s - s_0) = 298(-.054) = -16.09$

$s_1 - s_0 = C_p \ln \frac{T}{T_0} - R \ln \frac{P_1}{P_0} = 1.005 \ln \left(\frac{3000}{298}\right) - .287 \ln \left(\frac{3000}{100}\right) = 1.345 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$

$s_2 - s_0 = C_p \ln \frac{T_2}{T_0} - R \ln \frac{P_2}{P_0} = 1.005 \ln \left(\frac{2080}{298}\right) - .287 \ln \left(\frac{2080}{100}\right) = 1.291$

$s_2 - s_1 = -0.054$

$X_1 - X_2 = +660 + 31.0 - 30.99 = \boxed{660.2 \text{ kJ/kg}}$ $W_{\text{available}}$ State 1 $\rightarrow$ State 2

c)

Isentropic expansion

$w_2 = ?$

$$k = .287 + 1.400$$

$$T_1 = 3000 \text{ K}$$

$$P_1 = 3000 \text{ Pa} \quad P_2 = 1000 \text{ K}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}}$$

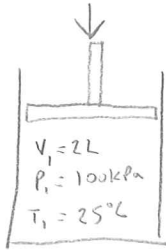
$$T_2 = 3000 \left(\frac{1}{3} \right)^{\frac{1.4}{1.4}} = 2191.8$$

$$Q_{in} - W_{out} = \Delta U$$

$$W = \frac{k R T_1}{k-1} \left(\left| \frac{P_2}{P_1} \right|^{\frac{k-1}{k}} - 1 \right) = \frac{1.4 (.278)(3000)}{0.4} \left[\left(\frac{1}{3} \right)^{\frac{1.4}{1.4}} - 1 \right] = \boxed{-786.38 \frac{\text{kJ}}{\text{kg}}}$$

David Malawuy

8.33)



② $P_2 = 600 \text{ kPa}$
 $T = 150^\circ\text{C}$

$W_{\text{useful}, \text{in}} = 1.2 \text{ kJ}$

① dead state
 ϕ air initial & final

$X_{\text{initial}} =$

$R = .287 \text{ kPa} \cdot \text{m}^3 / \text{kg} \cdot \text{K}$

$C_{p, \text{avg}} = 1.009$

$C_{v, \text{avg}} = .722 \text{ kJ/kg} \cdot \text{K}$

$100 \text{ kPa}, 25^\circ\text{C}$

$$m = \frac{P_1 V_1}{R T_1} = \frac{600 (2 \text{ L})}{.287 (25 + 273)} = 0.00234 \text{ kg}$$

$$\frac{P_2 V_2}{T_2} = \frac{P_1 V_1}{T_1} \quad V_2 = \frac{T_2}{T_1} \left(\frac{P_1}{P_2} \right) V_1 = \frac{423 \text{ K} \cdot 100 \text{ kPa}}{298 \text{ K} \cdot 600 \text{ kPa}} (2 \text{ L}) = .473 \text{ L} \quad V_2 = .473 \text{ L}$$

$$S_2 - S_0 = C_{p, \text{avg}} \ln \frac{T_2}{T_0} - R \ln \frac{P_2}{P_0} = 1.009 \ln \frac{423 \text{ K}}{298 \text{ K}} - .287 \ln \frac{600}{100 \text{ kPa}} = -.1608 \text{ kJ/kg} \cdot \text{K}$$

$$\begin{aligned} X_2 = \Phi_2 &= m [C_{v, \text{avg}} (T_2 - T_0) - T_0 (S_2 - S_0)] + P_0 (V_2 - V_0) \\ &= .00234 [.722 (423 - 298) - 298 (-.1608)] + 100 (.000473 - .002) \\ &= \boxed{0.171 \text{ kJ}} \end{aligned}$$

b) min work input $X_{\text{dest}} = 0 \quad X_{\text{in}} - X_{\text{out}} = \Delta X_{\text{system}}$

$$W_{\text{rev}, \text{in}} = X_2 - X_1 = 0.171 - 0 = \boxed{0.171 \text{ kJ}}$$

c) 2nd law efficiency $\eta_{\text{II}} = \frac{W_{\text{rev}, \text{in}}}{W_{\text{u}, \text{in}}} = \frac{.171 \text{ kJ}}{1.2 \text{ kJ}} = \boxed{14.3\%}$

ME 221 Applied Thermodynamics
Fall 2010

- D1. Air in a piston/cylinder arrangement undergoes a **polytropic expansion process** (i.e. $Pv^n = \text{constant}$) with $n = 1.5$. Initially the air is at 3 MPa and 3000 K (i.e. state 1) and the gas expands to 1 MPa (state 2). Assume ideal gas behavior and **constant specific heats** evaluated at 300K. Assume ambient (or dead state) conditions of 298 K and 100 kPa.
- a) Find the temperature at state 2. (K)
 - b) Find the expansion **work** given the polytropic expansion from state 1 to state 2. (kJ/kg)
 - c) Find the **heat transfer** given the work and states 1 and 2 (kJ/kg).
 - d) Find the **maximum work** that could be extracted out of this process between states 1 and 2. (kJ/kg)
 - e) If the air was expanded **isentropically** from the given T and P at state 1 to the pressure at state 2 (i.e. 1 MPa), find the expansion work. (kJ/kg)

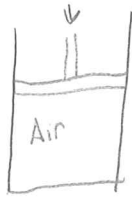
David Maloney

Thermo II

10

7.93, 7.128, 8.22

7.93



reversible
adiabatic
(isentropic)

$$R = .287 \text{ kJ/kg} \cdot \text{K}$$

$$k = 1.4$$

$$T_1 = 290 \text{ K}$$

Const.
Specific
Heats

$$a) T_2 = T_1 \left(\frac{P_2}{P_1} \right)^{(k-1)/k} = 290 \text{ K} \left(\frac{800 \text{ kPa}}{100 \text{ kPa}} \right)^{(1.4-1)/1.4} = \boxed{525.3 \text{ K}}$$

$$T_{avg} = \frac{290 + 525.3}{2} = 407.7 \quad C_{v, avg} = .727 \text{ kJ/kg} \cdot \text{K}$$

$$E_{in} - E_{out} = \Delta E_{sys} \quad W = \Delta U = m(u_2 - u_1) \equiv m C_v (T_2 - T_1)$$

$$W_{in} = (C_{v, avg} (T_2 - T_1)) = (.727)(525.3 - 290) \text{ K} = \boxed{W = 171.1 \text{ kJ/kg} \text{ into System}}$$

Variable
Specific
Heats

$$b) T_f: \quad T_1 = 290 \text{ K} \rightarrow P_1 = 1.2311$$

$$u_1 = 206.91 \text{ kJ/kg}$$

$$P_{r2} = \frac{P_2}{P_1} P_{r1} = \frac{800 \text{ kPa}}{100 \text{ kPa}} (1.2311) = 9.849$$

$$\boxed{T_2 = 522.4 \text{ K}}$$

$$u_2 = 376.16 \text{ kJ/kg}$$

$$W = u_2 - u_1 = 376.16 - 206.91 \text{ kJ/kg} = \boxed{169.25 \text{ kJ/kg} \text{ Work in}}$$

7.128

$$\dot{E}_{in} = \dot{E}_{out} \text{ (Steady)}$$

$$\textcircled{1} P = 3 \text{ MPa}$$

$$T = 400^\circ \text{C}$$

$$h = 3231.7$$

$$s = 6.9235$$

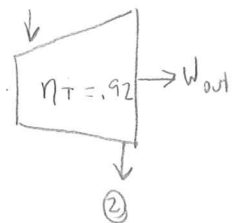
$$\textcircled{2} P = 30 \text{ kPa} \text{ adiabatic}$$

$$s = 6.9235$$

$$x_2 = \frac{s_2 - s_f}{s_{fg}} = \frac{6.9235 - .9441}{6.8234} = .8763$$

$$h_2 = 289.27 + (.8763)(2335.3) = 2335.7$$

①



$$\dot{W}_{out} = \eta_T \dot{W}_{s, out} = \eta_T \dot{m} (h_1 - h_{2s}) = .92 (2 \text{ kg/s}) (3231.7 - 2335.7) \text{ kJ/kg}$$

$$\boxed{\dot{W}_{out} = 1649.2 \text{ kW}}$$

David Maloney

HW #

8.22/

$$E = 100 \text{ kJ thermal energy}$$

$$T = 800 \text{ K}$$

$$T_{\text{environment}} = 25^\circ\text{C} = 298 \text{ K}$$

$$W_{\text{net}} = \eta_{\text{th, net}} Q_{\text{in}}$$

$$\eta_{\text{th, net}} = 1 - \frac{T_c}{T_h} = 1 - \frac{298}{800} = .6275$$

$$W_{\text{net}} = (.6275)(100 \text{ kJ})$$

$$= \boxed{62.75 \text{ kJ}}$$

David Maloney

9-2-10

Thermo II h/w

10

5.78

① hot H₂O 80°C $\dot{m} = 0.5 \text{ kg/s}$ $P = 250 \text{ kPa}$ ② cold H₂O

20°C

 $P = 250 \text{ kPa}$

③ 42°C

 $P = 250 \text{ kPa}$ $h_1 = 335.02 \text{ (} h_f \text{ at } 80^\circ \text{)}$ $h_2 = 83.915 \text{ kJ/kg}$ $h_3 = 175.72 \text{ kJ/kg}$

↑

interpolated 40°, 45°

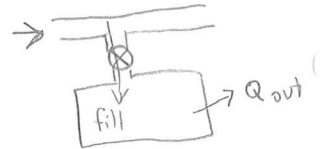
$$\dot{Q} - \dot{W} = \dot{m}(h)_{in} - \dot{m}(h)_{out} \quad (\text{Neglect P.E. \& K.E.})$$

$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$$

$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_1 h_3 + \dot{m}_2 h_3$$

$$\dot{m}_2 (h_2 - h_3) = \frac{\dot{m}_1 h_3 - \dot{m}_1 h_1}{(h_2 - h_3)} = \frac{0.5 \text{ kg/s} (175.72 - 335.02)}{(83.915 - 175.72)} = 0.869 \text{ kg/s} = \dot{m}_2$$

5.124

 $V = 2 \text{ m}^3$ $P_1 = 100 \text{ kPa}$ $T_1 = 22^\circ \text{C}$ $P_2 = 600 \text{ kPa}$ $T_2 = 77^\circ \text{C}$ $m \& Q = ?$ $R = 0.287 \text{ kPa} \cdot \text{m}^3 / \text{kg} \cdot \text{K}$ $P_i = 600 \text{ kPa}$ $T_i = 22^\circ \text{C}$ 

$$\dot{Q} - \dot{W} = \Delta E_{\text{system}}$$

$$\dot{Q}_{in} + \dot{m}_1 h_i = \dot{m}_2 u_2 - \dot{m}_1 u_1$$

$$\left. \begin{aligned} m_1 &= \frac{P_1 V}{R T_1} = \frac{100 \text{ kPa} \cdot 2 \text{ m}^3}{0.287 \text{ kPa} \cdot \text{m}^3 / \text{kg} \cdot \text{K} \cdot 295 \text{ K}} = 2.362 \text{ kg} \\ m_2 &= \frac{P_2 V}{R T_2} = \frac{600 \text{ kPa} \cdot 2 \text{ m}^3}{0.287 \text{ kPa} \cdot \text{m}^3 / \text{kg} \cdot \text{K} \cdot 350 \text{ K}} = 11.946 \text{ kg} \end{aligned} \right\} \Rightarrow m_i = 9.584 \text{ kg}$$

$$\dot{Q}_{in} = -\dot{m}_1 h_i + \dot{m}_2 u_2 - \dot{m}_1 u_1 = -9.584(295.17) + (11.946)(250.02) - (2.362)(210.49)$$

$$\boxed{Q = -339 \text{ kJ}} \quad \text{heat leaves system}$$

7.116

Sat. liquid 10 MPa	Sat. vapor 20 kPa
-----------------------	----------------------

work delivered by turbine?
work consumed by pump?

$$\Delta E_{cv} = 0 \quad \dot{E}_{in} = \dot{E}_{out} \quad W_{in} - Q_{in}$$

$$s_1 = s_2 \quad s_3 = s_4 \quad (\text{isentropic})$$

④

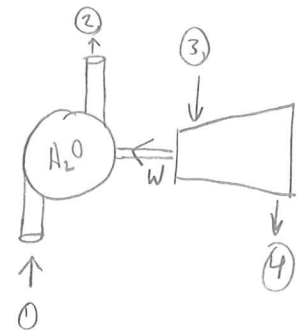
$$P = 20 \text{ kPa}$$

$$h = 2608.9 \text{ kJ/kg}$$

$$s = 7.9073$$

$$\textcircled{3} \quad P = 10 \text{ MPa}$$

$$h = 4707.2 \text{ kJ/kg}$$



$$\textcircled{1} \quad V = .001017 \text{ m}^3/\text{kg} \quad \dot{E}_{in} - \dot{E}_{out} = \Delta \dot{E}_{sys}$$

$$\dot{m} h_3 = \dot{m} h_4 + \dot{W}_{out}$$

$$\dot{W}_{out} = \dot{m} (h_3 - h_4)$$

$$w_{turbine} = h_3 - h_4 = 4707.2 - 2608.9 = 2098.3 \text{ kJ/kg} \quad \text{out of sys}$$

$$w_{pump, in} = \int_1^2 v dp = v_1 (P_2 - P_1) = .001017 \text{ m}^3/\text{kg} (10,000 - 20) \text{ kPa} \left(\frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) = 10.15 \text{ kJ/kg}$$

$$\frac{w_{turb, out}}{w_{pump, in}} = \frac{2098.3}{10.15} = 206.7$$

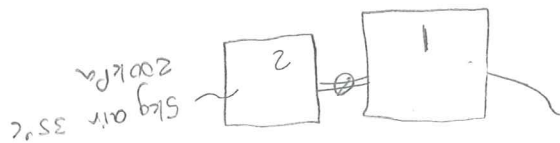
David Malaney
Thermo II 221

3.80, 3.84, 3.90

10

3.80

1 m³ air
25°C
500 kPa



$V_{\text{tank 2}} = ?$
 $P_2 = ?$

Air = 2870 kJ/kg · K
 $PV = mRT$

$$200 \text{ m}^3 = 5(2870)(35 + 273)$$

$$A = 2.21 \text{ m}^3$$

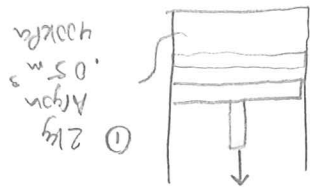
$$m_1 = \frac{PV}{RT_1} = \frac{500(1)}{2870(298)} = 5.846 \text{ kg}$$

$$A_{\text{total}} = 3.21 \text{ m}^3 \quad m_2 = 5.846 \text{ kg} + 5 \text{ kg}$$

$$T_2 = 20^\circ\text{C}$$

$$P_2 = \frac{mRT_2}{V_2} = \frac{10.846(2870)(293)}{3.21 \text{ m}^3} = 284.1 \text{ kPa}$$

3.84



② 2 kg
10 m³
 $P_2 = ?$

$$P_1 V_1 = P_2 V_2$$

$$PV = mRT$$

$$T_2 = T_1$$

$$400(.05) = P_2(.10) \Rightarrow P_2 = 200 \text{ kPa}$$

3.90

134a
Vapor,
 $P = 9 \text{ MPa}$
 $T = 70^\circ\text{C}$
 $R = .08149$

$$PV = mRT$$

$$\frac{V}{P} = \frac{RT}{P}$$

$$.03105 \text{ m}^3/\text{kg}$$

$$13.26\% \text{ error}$$

b)

$T_{cr} = 374.2 \text{ K}$
 $P_{cr} = 4.059$

$$\frac{P_r}{P} = \frac{P_{cr}}{P} = \frac{4.059}{9} = .222$$

$$T_r = \frac{T}{T_{cr}} = \frac{374.2}{374.2} = .917$$

$$V = ZV_{ideal}$$

$$= .895(.03105)$$

$$= .0278 \text{ m}^3/\text{kg}$$

$$1.4\% \text{ error}$$

c) superheated table $\Rightarrow .027413 \text{ m}^3/\text{kg}$

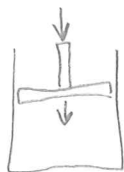
David Maloney (prof head)

Therm 2 8-31-10

10

4.81, 5.51, 5.54

4.81) ① 0.8 kg N_2
100 kPa
27°C



Polytropic $PV^{1.3} = \text{constant}$

$$P_1 V_1^{1.3} = P_2 V_2^{1.3} \quad \frac{P_1}{P_2} = \left(\frac{V_2}{V_1} \right)^{1.3} \quad \frac{P_1}{P_2} = (1.5)^{1.3}$$

② $V_2 = .5 V_1$

$Q = ?$

$W = ?$

$$P_1 V_1 = m R T_1$$

$$\frac{P_1 V_1}{T_1} = m R = \frac{P_2 V_2}{T_2}$$

$$T_2 = \frac{P_2 V_2}{P_1 V_1} T_1 = \frac{246.2}{100} (1.5) (27 + 273)$$

$$T_2 = 369.3 \text{ K}$$

boundary
work

$$W_2 = \int_1^2 P dV$$

$$\frac{P_2 V_2 - P_1 V_1}{1-n} = \frac{m R (T_2 - T_1)}{1-n} = \frac{.8 \text{ kg} \left(.2968 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \right) (369.3 - 300)}{1 - 1.3}$$

$W_b = -54.85$ means work goes into system

$$Q_2 - W_2 = \Delta U = m C_v (T_2 - T_1) = .8 \text{ kg} \left(.744 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \right) (69.3 \text{ K})$$

$C_{v, \text{avg}} = .744$

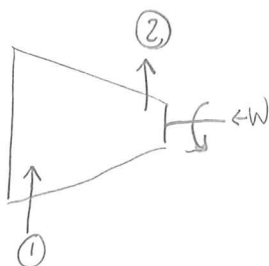
$$= 41.25 \text{ kJ}$$

$$Q_2 = -54.85 \text{ kJ} + 41.25 \text{ kJ}$$

$Q_2 = -13.60 \text{ kJ}$ means heat goes out of system

David Maloney
H/W continued...

Compressor



5.51) adiabatic compressor

① $\dot{V} = 10 \text{ L/s}$
120 kPa
20°C
Air

② 1000 kPa
300°C

W required = ?
power req'd = ?

$$h_2 - h_1 = C_p (T_2 - T_1) = 1.018 (280) = 285.0 \frac{\text{kJ}}{\text{kg}}$$

$$C_{p, \text{avg}} = C_p, 160^\circ\text{C} = 1.018 \text{ kJ/kg}\cdot\text{K}$$

$$\text{Control volume } \dot{Q} - \dot{W} = \dot{m} (\Delta h + \cancel{\Delta e} + \cancel{\Delta p})$$

$$\dot{m}: P_1 \dot{V}_1 = \dot{m} R T_1$$

$$\dot{m} = \frac{P_1 \dot{V}_1}{R T_1} = \frac{120 \text{ kPa} (0.01 \text{ m}^3/\text{s})}{0.287 \frac{\text{kPa}\cdot\text{m}^3}{\text{kg}\cdot\text{K}} (293 \text{ K})}$$

$$= 0.01427 \text{ kg/s}$$

$$\dot{Q} - \dot{W} = \dot{m} \Delta h$$

$$\dot{Q} - \dot{W} = 0.01427 \frac{\text{kg}}{\text{s}} 285.0 \frac{\text{kJ}}{\text{kg}}$$

$$\dot{Q} - \dot{W} = 4.067 \frac{\text{kJ}}{\text{s}}$$

adiabatic

$$\dot{W}_b = 4.067 \text{ kW work into system}$$

$$\dot{W} = 285.0 \frac{\text{kJ}}{\text{kg}} \text{ into sys.}$$

5.54) turbine

① 10 MPa
500°C

② 10 kPa
 $x = .9$

$\dot{M} = ?$

$$P = 5 \text{ MW} = 5000 \frac{\text{kJ}}{\text{s}}$$

$$\text{Tables: } h_1 = 3375.1 \text{ kJ/kg}$$

$$h_2 = h_f + .9 h_{fg} (10 \text{ kPa}) = 2344.7 \text{ kJ/kg}$$

$$E_{\text{in}} - E_{\text{out}} = \cancel{\Delta E}^0$$

$$\dot{Q} - \dot{W} = \dot{m} (\Delta h)$$

$$-5000 \frac{\text{kJ}}{\text{s}} = \dot{m} (h_2 - h_1)$$

$$\dot{m} = 4.852 \text{ kg/s}$$

David Maloney

ME 221 HW due 9-31-10

105

a) $\Delta - 26$ table $\Delta \bar{u} = \int_1^2 c_v(T) dt$ (Valid temperature range?)

4.63) $\Delta u = ?$ hydrogen, $\Delta \bar{u} = \int_1^2 \left[(29.11 - R_u) - .1916 \times 10^{-2} (T) + .4003 \times 10^{-5} (T^2) - .8704 \times 10^{-9} (T^3) \right] dt$
 $T_1 = 200 \text{ K}$
 $T_2 = 800 \text{ K}$
 $= 12,487 \text{ kJ/kmol} \left(\frac{1}{2.016 \text{ kg/mol}} \right)$
 $= \boxed{6194 \text{ kJ/kg}}$

b) $c_{v, \text{avg}} = c_v(500 \text{ K}) = 10.389 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$

$\Delta u = 10.389 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (800 \text{ K} - 200 \text{ K}) = \boxed{6233 \text{ kJ/kg}}$

c) $c_v = 10.183 \text{ kJ/kg} \cdot \text{K}$

$\Delta u = c_{v, RT} (T_2 - T_1) = 10.183 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (600 \text{ K}) = \boxed{6110 \frac{\text{kJ}}{\text{kg}}}$

4.29)

① H_2O sat. vapor 200°C $P = 1554.9 \text{ kPa}$

② sat liquid, 200°C $Q = ?$ $w_2 = ?$

$u_1 = 2594.2 \text{ kJ/kg}$ $u_2 = 850.46$ $\Delta u = 1743.7$

$v_1 = .12721$ $v_2 = .001157$

$w_2 = \int P dv = 1554.9 \left(.001157 - .12721 \right) = -196.0 \frac{\text{kPa} \cdot \text{m}^3}{\text{kg}} = \boxed{196.0 \frac{\text{kJ}}{\text{kg}}}$
 on into system

${}_1Q_2 - {}_1W_2 = E_2 - E_1$

${}_1Q_2 - 196.0 \frac{\text{kJ}}{\text{kg}} = 1743.7 \frac{\text{kJ}}{\text{kg}}$

$\boxed{{}_1Q_2 = 1940 \text{ kJ/kg}}$ heat is transferred out of system

4.42/

Steam	
A 2kg 1 MPa 300°C	B 3kg 150°C x = .5

①

② $P = 300 \text{ kPa}$ 5kg

$$v_A = 0.25797 \text{ m}^3/\text{kg} \Rightarrow 0.51598 \text{ m}^3$$

$$v_B = .5(.001091) + .5(.39248) = 0.196786 \text{ m}^3/\text{kg} (3\text{kg}) = 0.59036 \text{ m}^3$$

$$v_{\text{total}} = 1.106 \text{ m}^3 \quad v_{\text{total}} = 0.2212 \text{ m}^3/\text{kg}$$

$$v_f < 0.2212 < v_g \therefore \text{sat. mixture}$$

$$x \overset{v_g}{(.60582)} + (1-x) \overset{v_f}{(.001073)} = 0.2212$$

$$x v_g + v_f - x(v_f) = v$$

$$x(v_g - v_f) + v_f = v$$

$$\frac{0.2212 - 0.001073}{(.60582 - 0.001073)} = x = 0.3640$$

$$T_{\text{final}} = 133.52^\circ\text{C}$$

$$u_A = m(u) = 2\text{kg} (2793.7 \frac{\text{kJ}}{\text{kg}}) = 5587.4 \text{ kJ}$$

$$u_B = m(.5 u_f + .5 u_g) = 3[.5(631.66) + .5(2559.1)] = 4786.14 \text{ kJ}$$

$$\left. \begin{array}{l} 5587.4 \text{ kJ} \\ 4786.14 \text{ kJ} \end{array} \right\} = 10373.5 \text{ kJ}$$

$$u_{\text{final}} = m(u_f + x u_{fg}) = 5\text{kg} (561.11 + (.364) 1982.1) = 6412.97 \text{ kJ}$$

$$\Delta u = u_2 - u_1 = -3961 \text{ kJ}$$

$$Q_2 - \cancel{W_2} = \Delta u$$

no work

$$Q_2 = 3961 \text{ kJ out of system}$$