# Optimised Deep Learning - Jean Zay

## Hyperparameter Optimization

# HPO = Hyperparameter Optimisation

Hyperparameters ◂

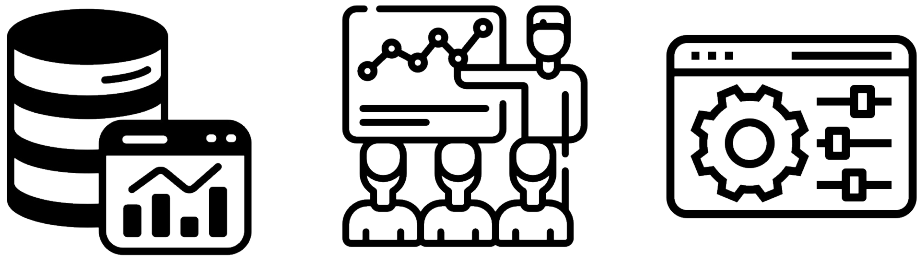
HPO ◂

Related Problems ◂

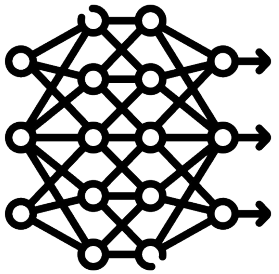
# Hyperparameters

In machine learning, a hyperparameter is **a parameter whose value is used to control the learning process**. By contrast, the values of other parameters (typically node weights) are derived via training.

## Hyperparameters

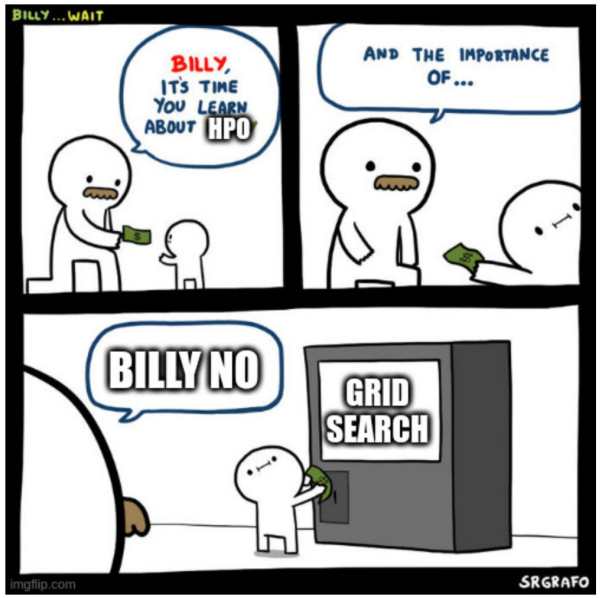


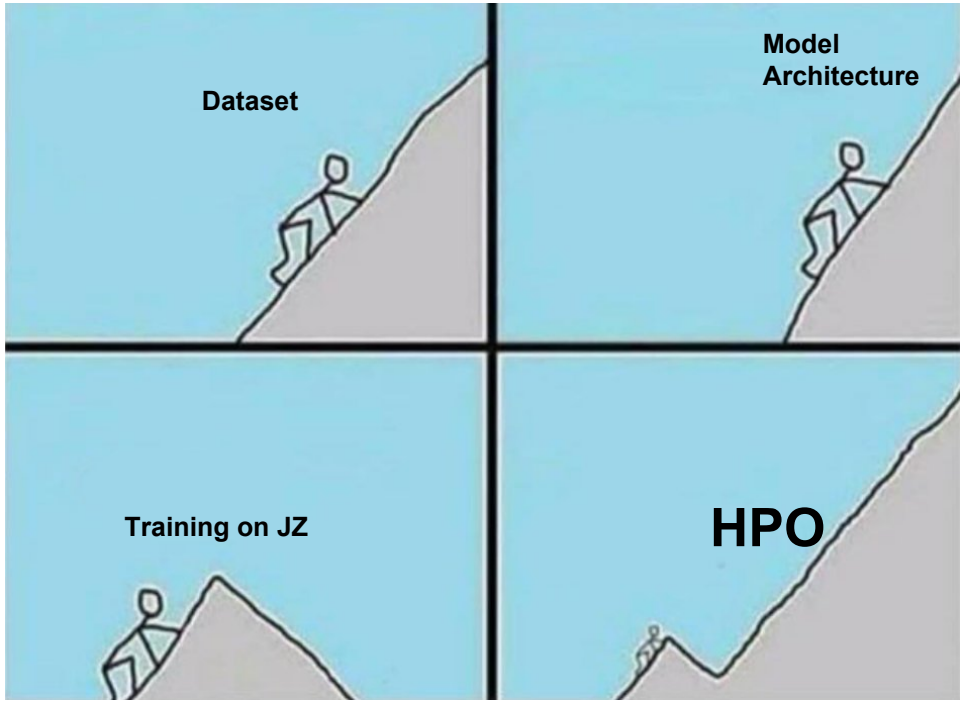
## Parameters



# HPO : Hyperparameter Optimisation

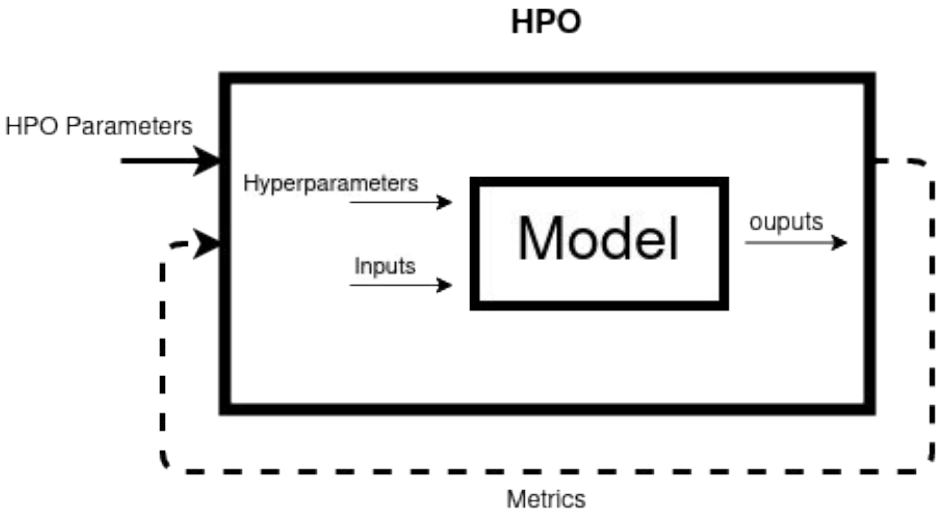
Machine learning algorithms are highly configurable by their hyperparameters.
**These parameters often substantially influence** the complexity, behavior, speed as well as other aspects of the learner, and their values must be selected with care in order to achieve optimal performance.
**Human trial-and-error to select these values is time-consuming, often somewhat biased, error-prone and computationally irreproducible.**

# HPO






Hyperparameter Optimization == Bi-Level optimization problem

# Search Algorithms / Samplers

**Basic ◂**

Manual, Grid Search, Random Search

**Bayesian Optimisation ◂**

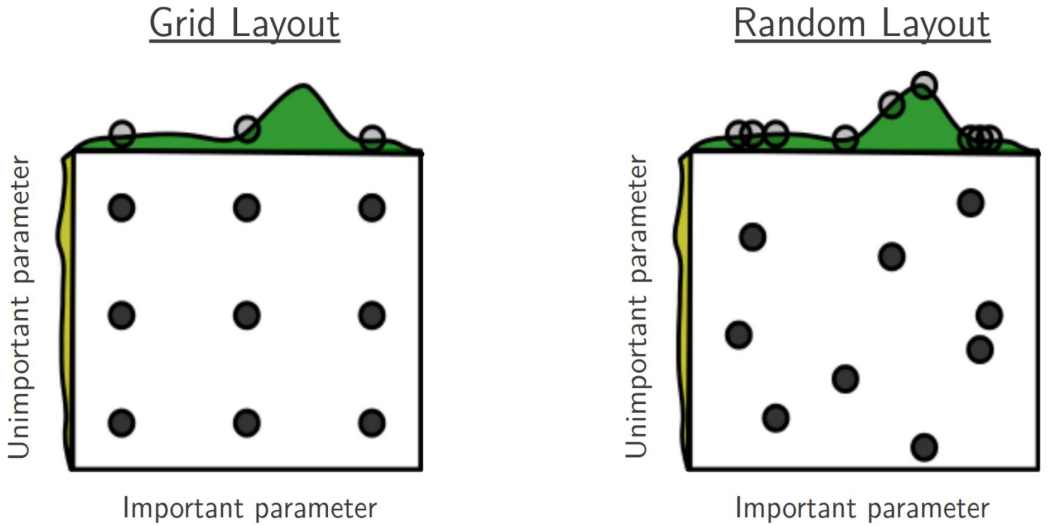
Tree-structured Parzen Estimator, Gaussian Process

**Heuristic ◂**

Genetic  Algorithm, Particle Swarm Optimization

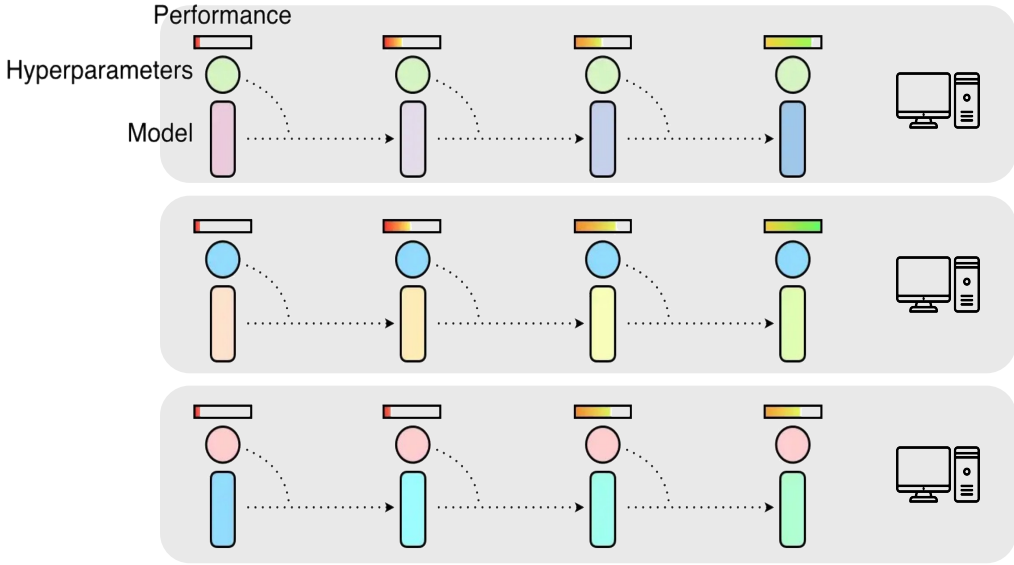
**Gradient-based Optimization ◂**

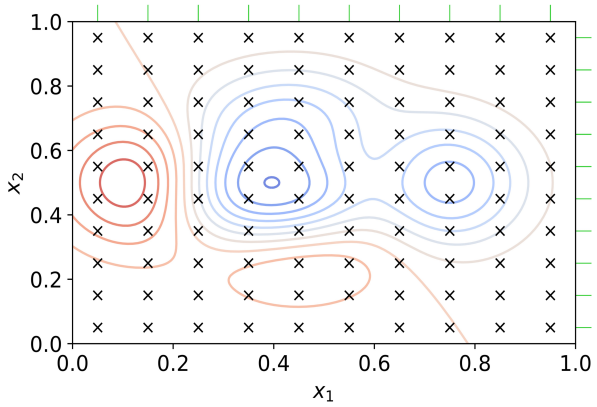
# Basic : Grid & Random Search

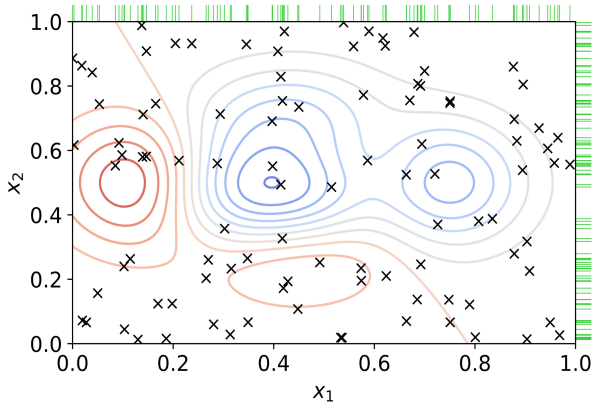






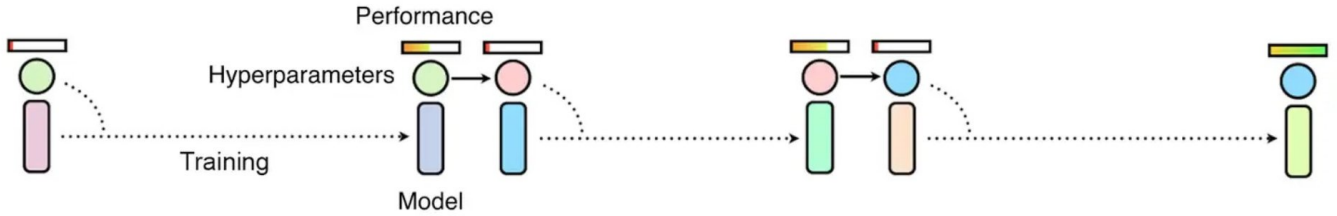


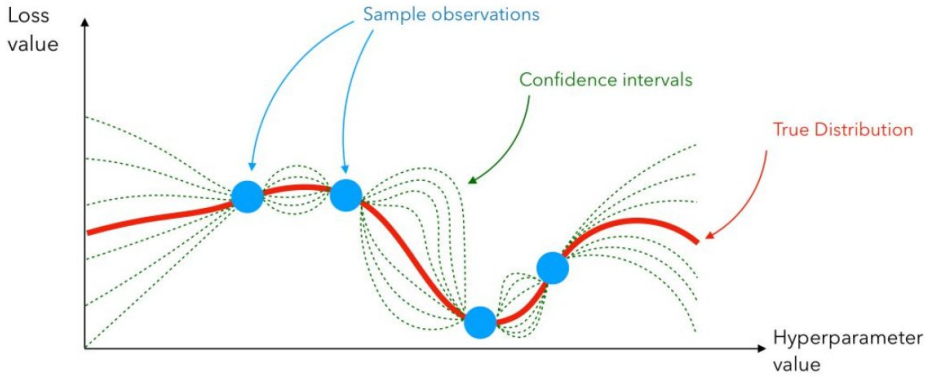



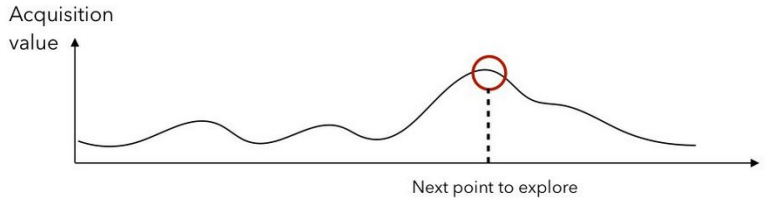

- Independent tests (which can be parallelized) which test a combination of hyperparameters.
- Very costly in resources and no guarantee of improved results.
- Random search is better for high dimensional space

# Bayesian Optimization : TPE & GP



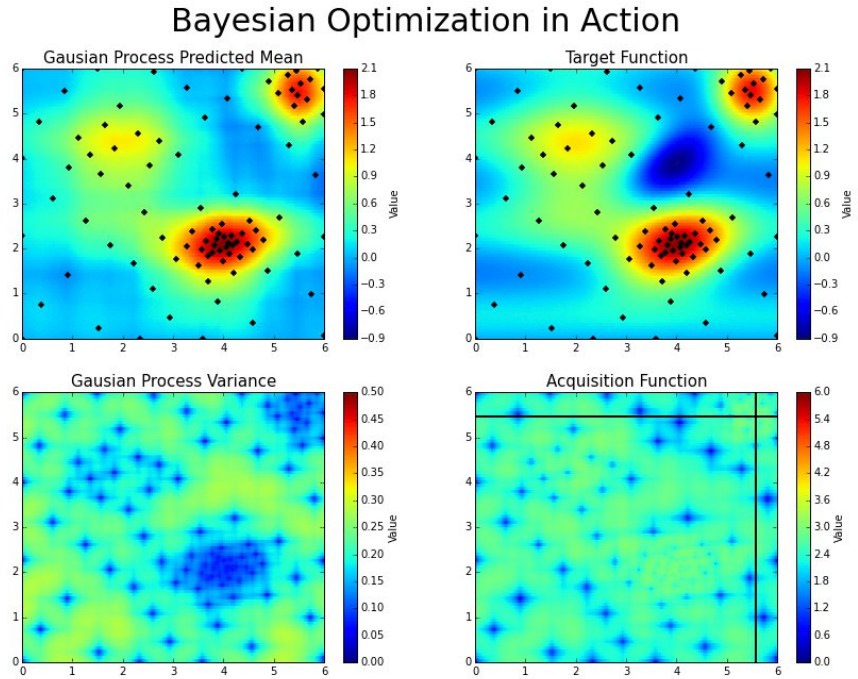




Expected metric score according to Hyper-parameters

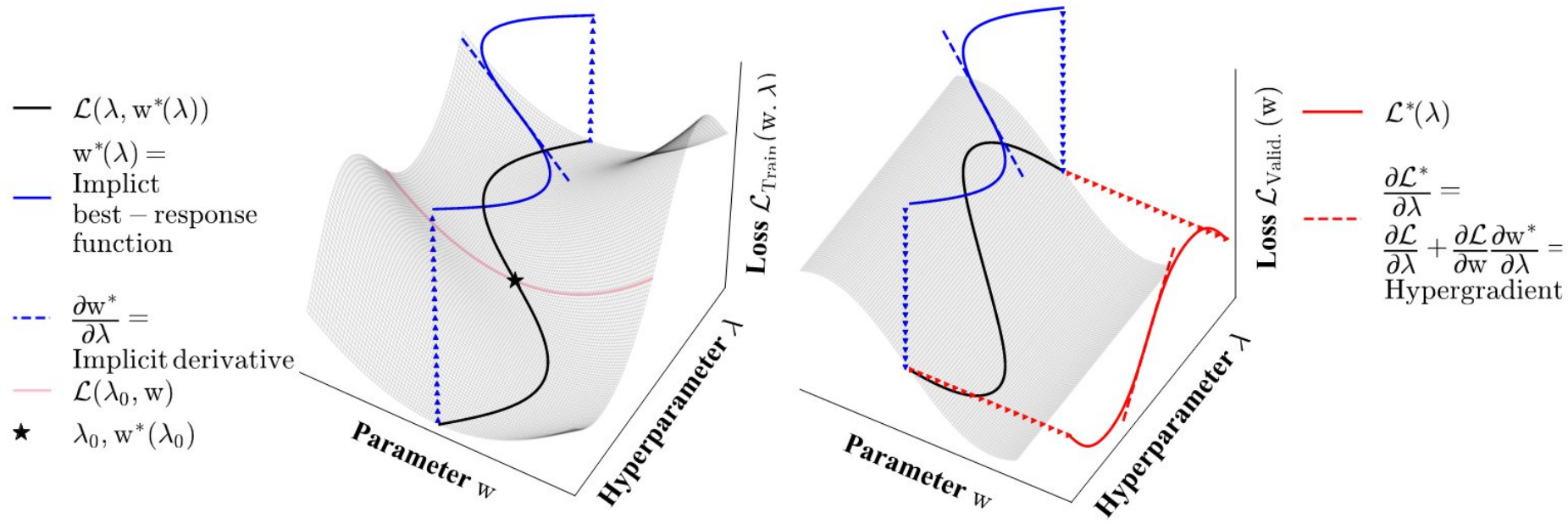



Maximize Acquisition function e.g. Expected Improvement

- Tree Parzen Estimator / Gaussian Process
- Sequential but allows to quickly find the global optimum.
- Proposes a new set of hyper parameters based on the scores obtained by the previous ones tested.



# Gradient-based optimization




**Optimizing Millions of Hyperparameters by Implicit Differentiation**
(https://arxiv.org/pdf/1911.02590.pdf)

- High dimensionality
- Bi-level optimisation

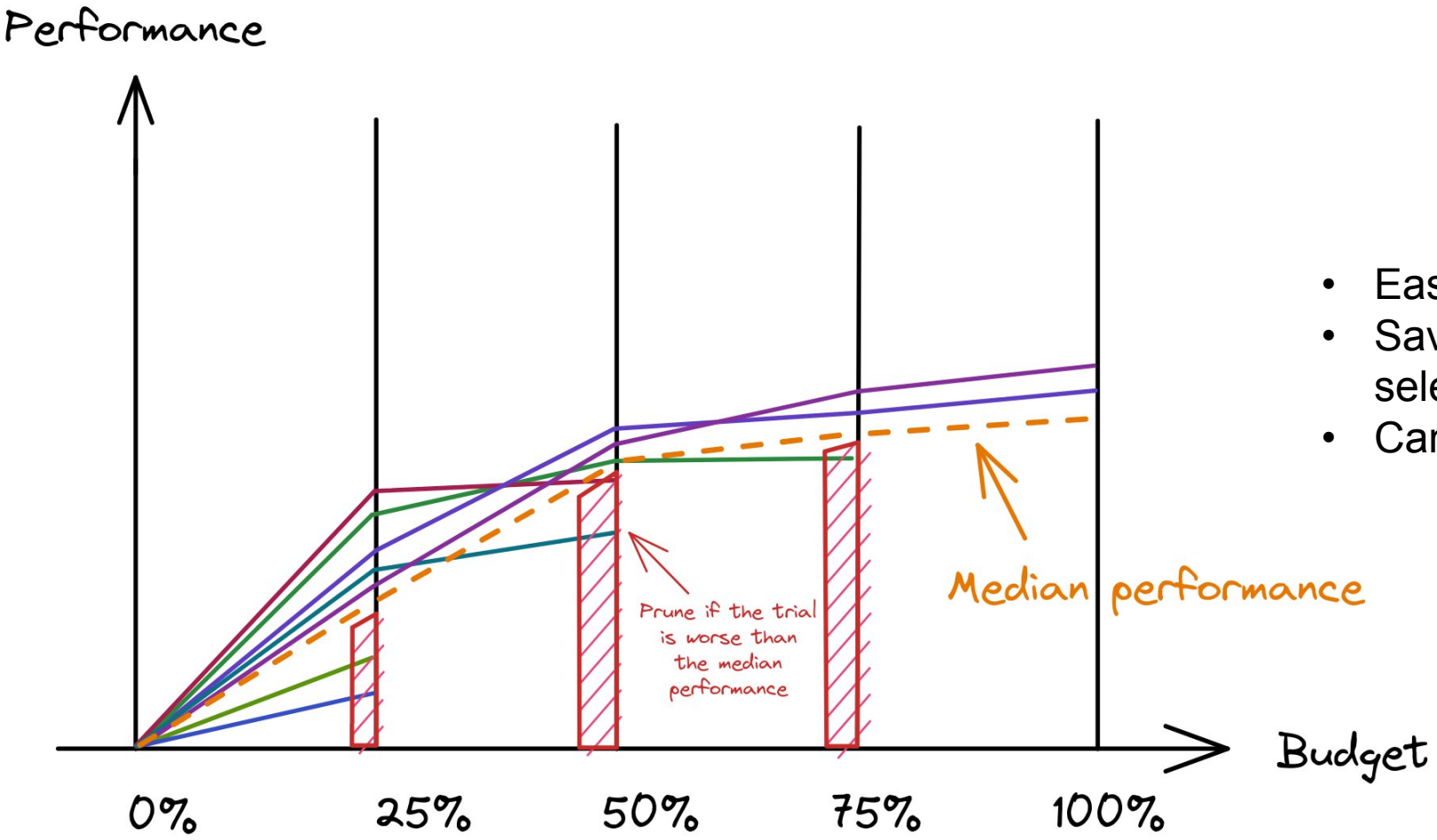
# Schedulers Algorithms / Pruners

Early Stopping ◂

SHA/ASHA ◂

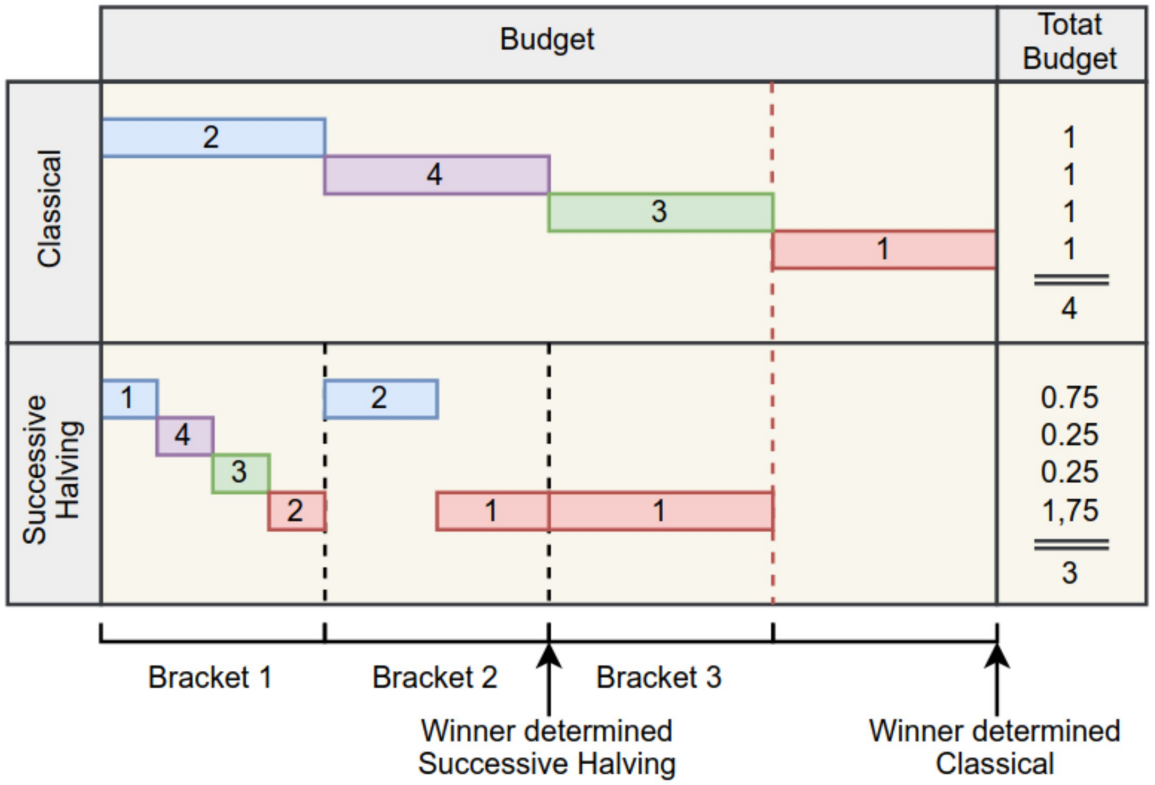
HyperBand ◂

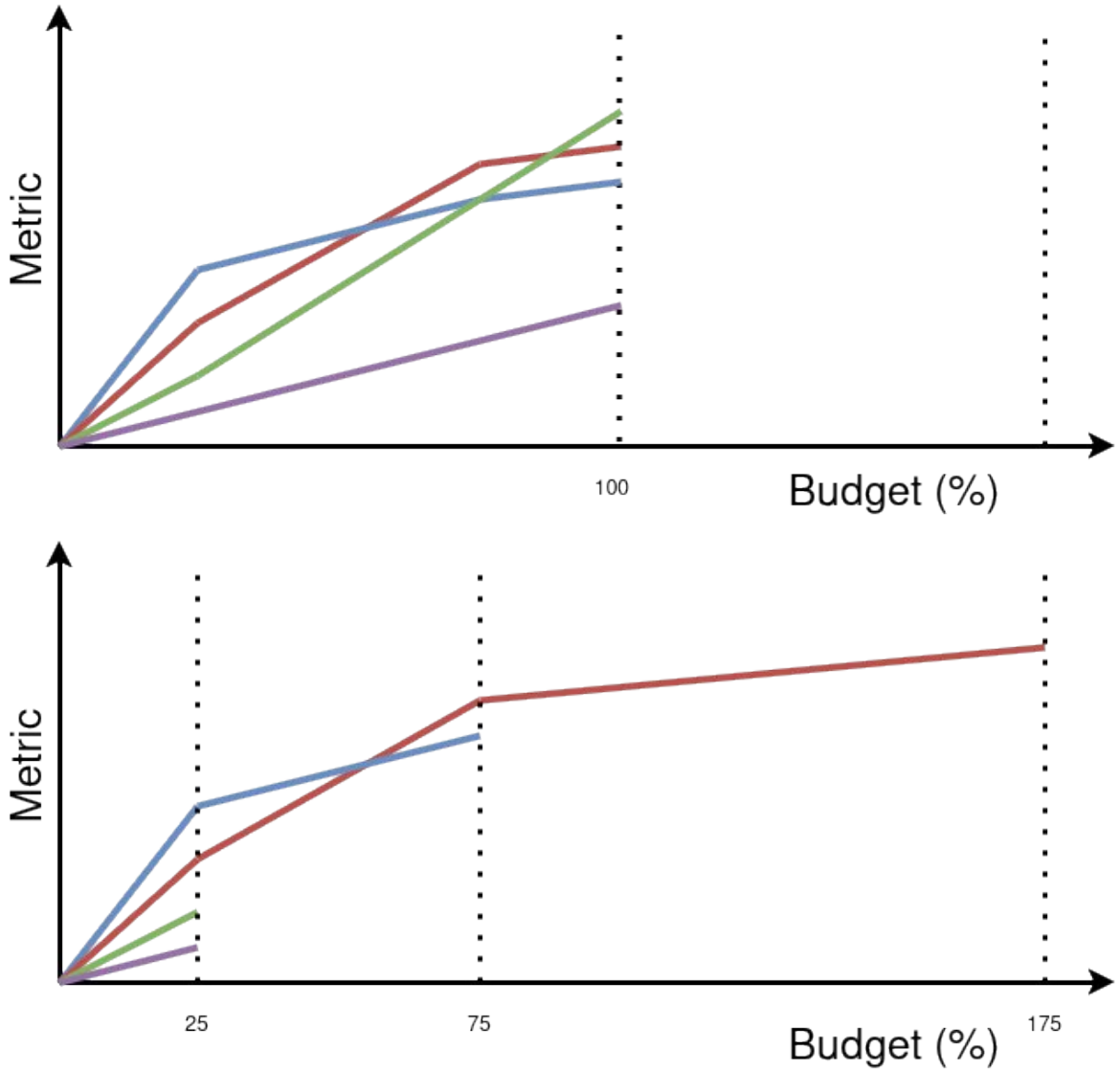
# Early Stopping




- Easy to implement
- Save ressources & make automatic selection
- Can be with acc%, time%, rank%, etc

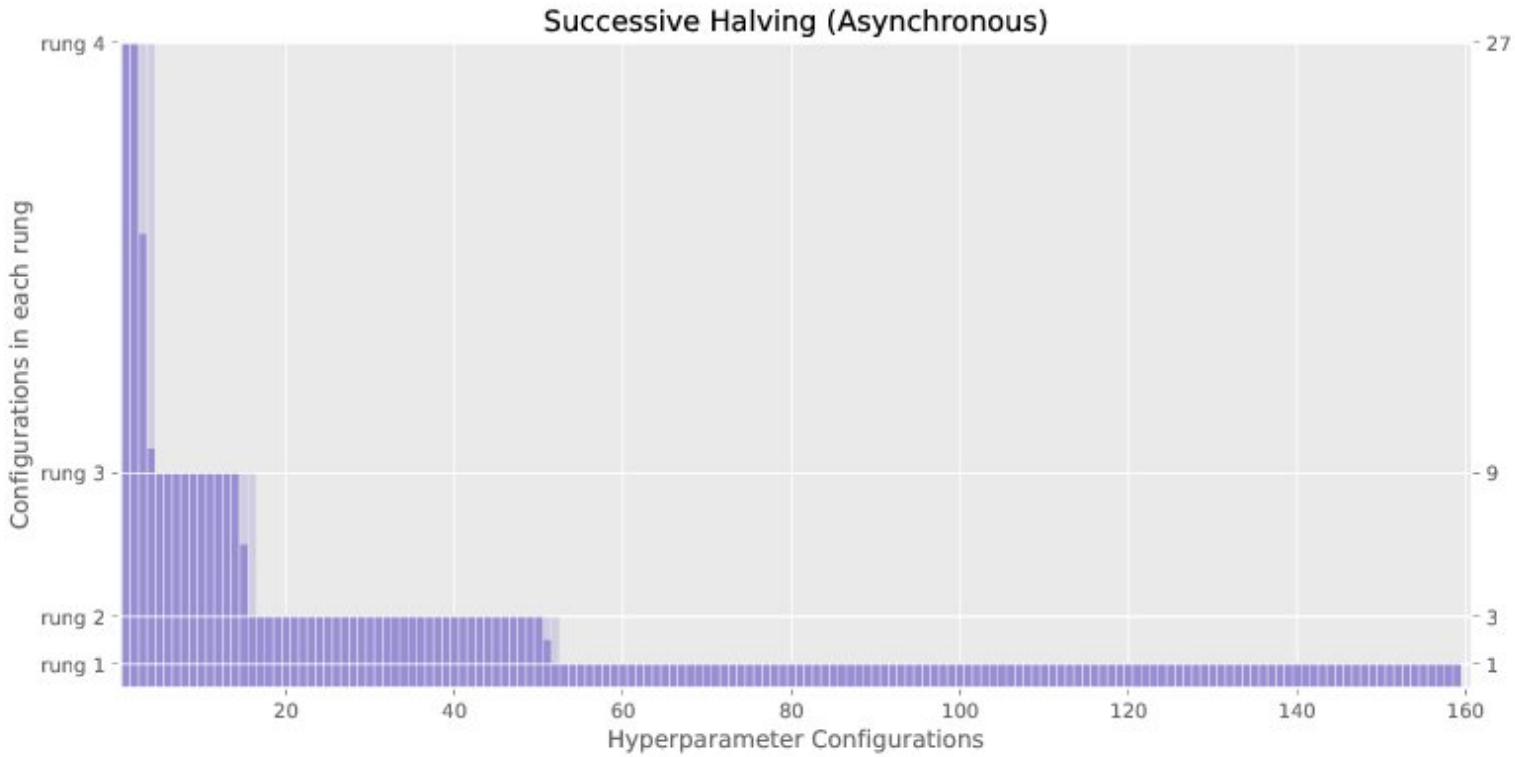
# SHA : Successive Halving Algorithm

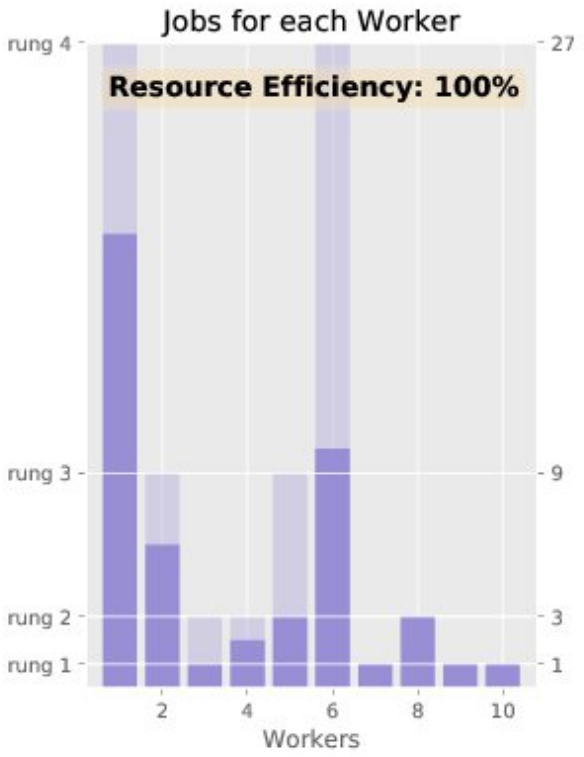



- For sequentials trials
- Works well with small or medium model -> Trials must be fast !

# ASHA


Successive Halving (Asynchronous)
rung 4
rung 3
rung 2
rung 1
27
9
3
1
Configurations in each rung
20
40
60
80
100
120
140
160
Hyperparameter Configurations


Jobs for each Worker
Resource Efficiency: 100%
rung 4
rung 3
rung 2
rung 1
27
9
3
1
2
4
6
8
10
Workers

# Hyperband

**Algorithm 1:** HYPERBAND algorithm for hyperparameter optimization.

**input** : $R$, $\eta$ (default $\eta = 3$)
**initialization** : $s_{\max} = \lfloor \log_\eta(R) \rfloor$, $B = (s_{\max} + 1)R$
**for** $s \in \{s_{\max}, s_{\max} - 1, \ldots, 0\}$ **do**
  $n = \lceil \frac{B}{R} \frac{\eta^s}{(s+1)} \rceil$, $r = R\eta^{-s}$
  // begin SUCCESSIVEHALVING with $(n, r)$ inner loop
  $T$ =get_hyperparameter_configuration($n$)
  **for** $i \in \{0, \ldots, s\}$ **do**
    $n_i = \lfloor n\eta^{-i} \rfloor$
    $r_i = r\eta^i$
    $L = \{\text{run\_then\_return\_val\_loss}(t, r_i) : t \in T\}$
    $T$ =top_k($T, L, \lfloor n_i/\eta \rfloor$)
  **end**
**end**
**return** *Configuration with the smallest intermediate loss seen so far.*

| | $s=4$ | | $s=3$ | | $s=2$ | | $s=1$ | | $s=0$ | |
|---|---|---|---|---|---|---|---|---|---|---|
| $i$ | $n_i$ | $r_i$ | $n_i$ | $r_i$ | $n_i$ | $r_i$ | $n_i$ | $r_i$ | $n_i$ | $r_i$ |
| 0 | 81 | 1 | 27 | 3 | 9 | 9 | 6 | 27 | 5 | 81 |
| 1 | 27 | 3 | 9 | 9 | 3 | 27 | 2 | 81 | | |
| 2 | 9 | 9 | 3 | 27 | 1 | 81 | | | | |
| 3 | 3 | 27 | 1 | 81 | | | | | | |
| 4 | 1 | 81 | | | | | | | | |

Table 1: Values of $n_i$ and $r_i$ for the brackets of HYPERBAND when $R = 81$ and $\eta = 3$.

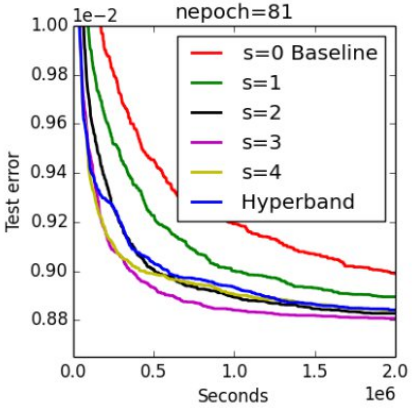
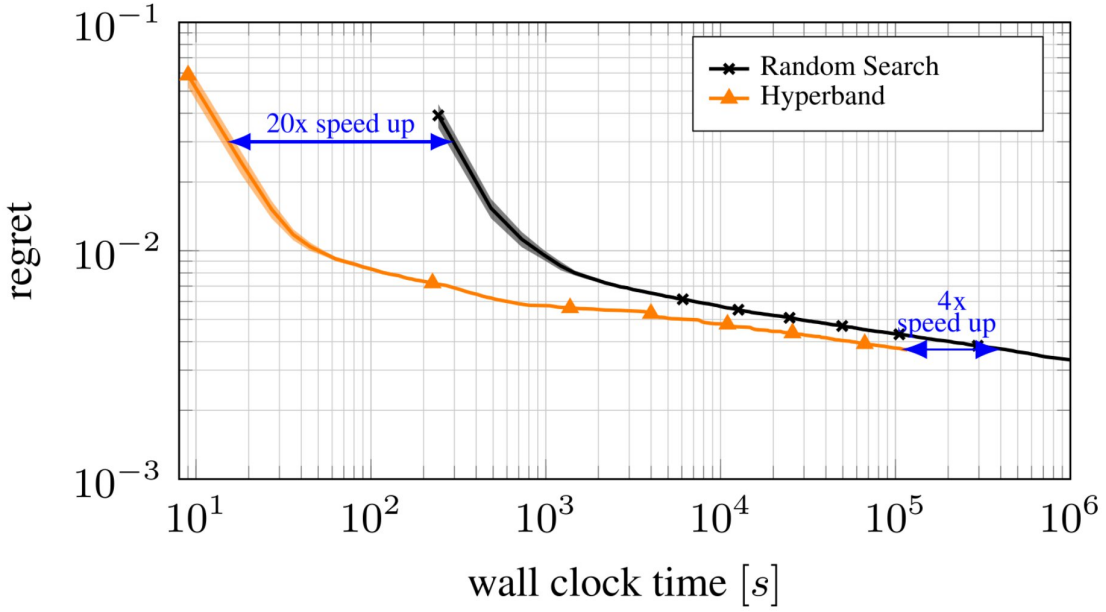



Figure 2: Performance of individual brackets $s$ and HYPERBAND.




- Repeatedly calls SuccessiveHalving but mitigate it's drawbacks
- Limited convergence

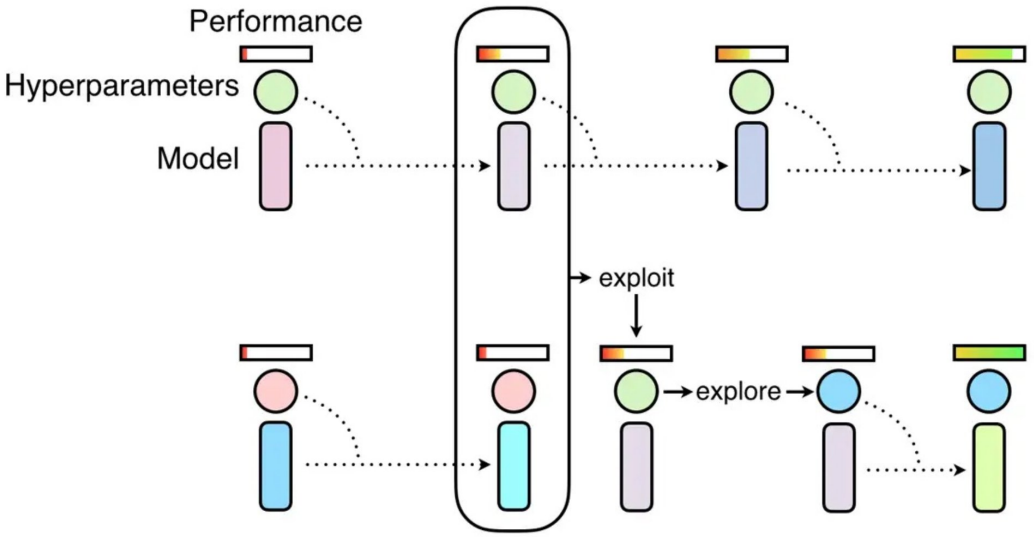
# Advanced Algorithms

*Hybrid time !*

PBT ◂

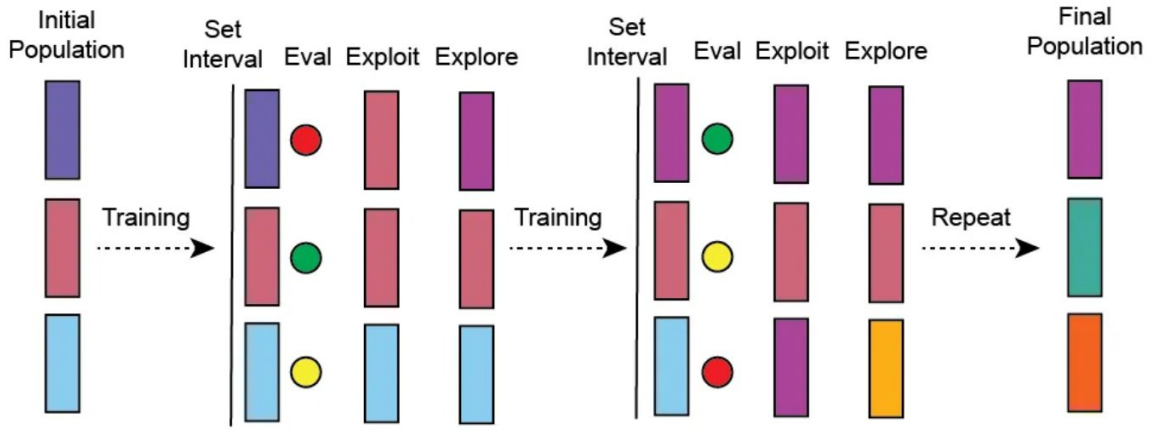
BOHB, DEHB ◂

# PBT : Population Based Training



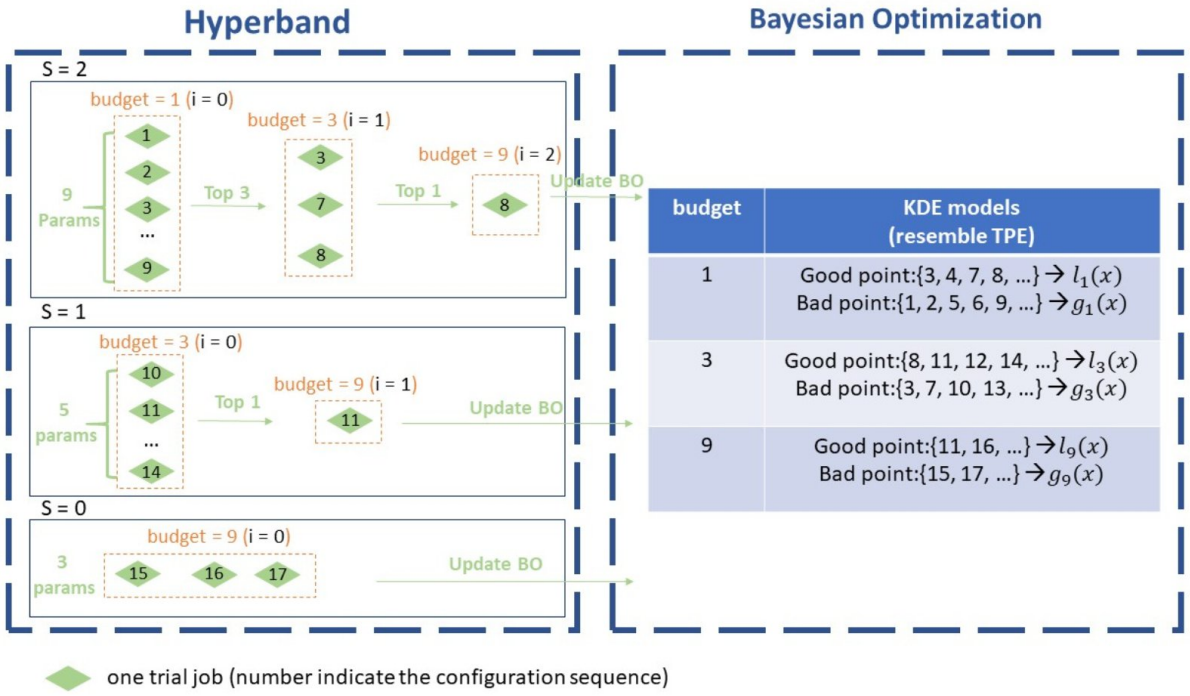

- Research and optimization of hyper parameters during training
- For large models with long and poorly parallelizable tests on a few machines.

- **Exploit** = Copy of the weights of the best model
- **Explore** = Bayesian Optimization



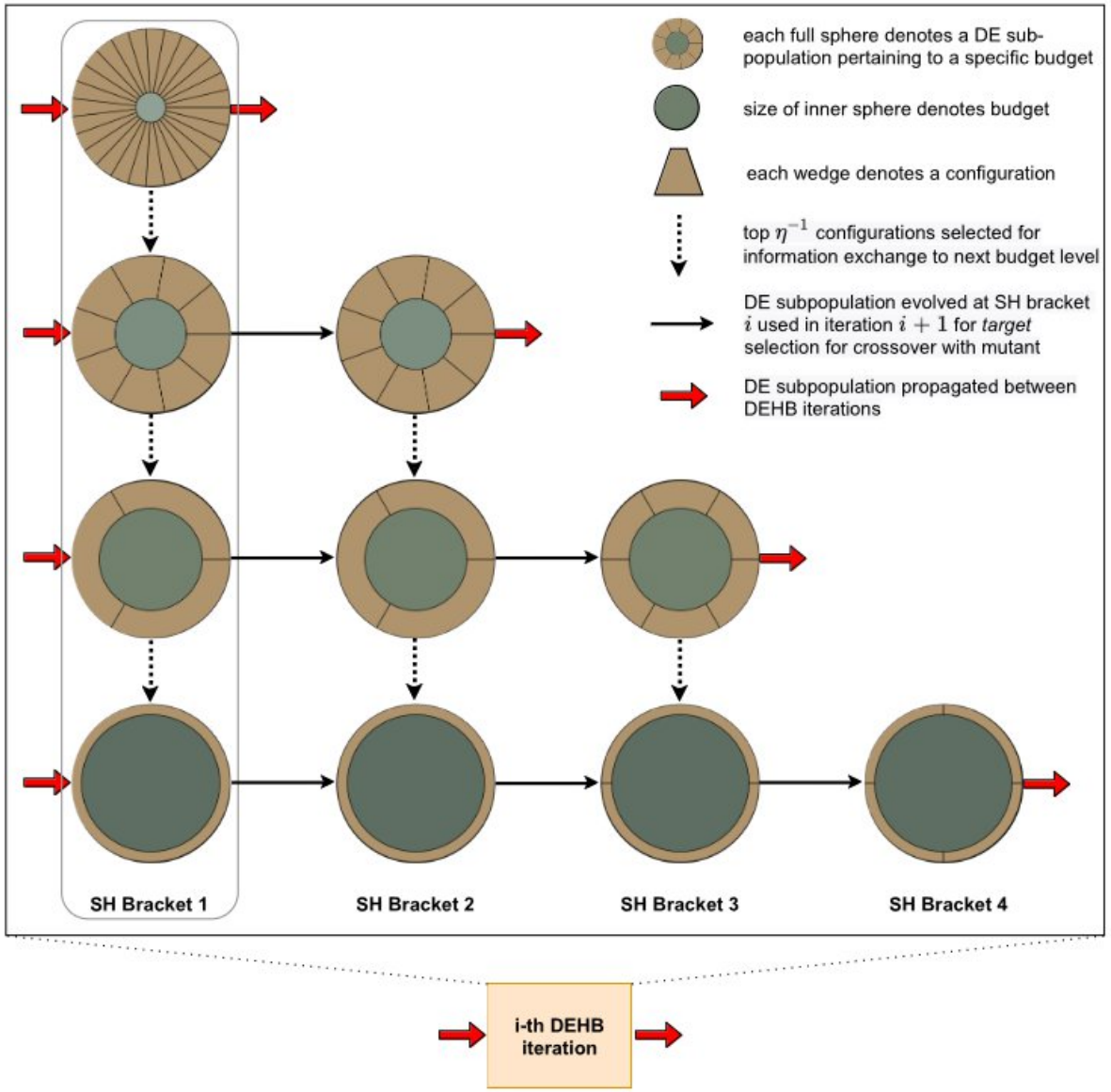
# BOHB, DEHB

## BOHB : Bayesian Optimization Hyperband

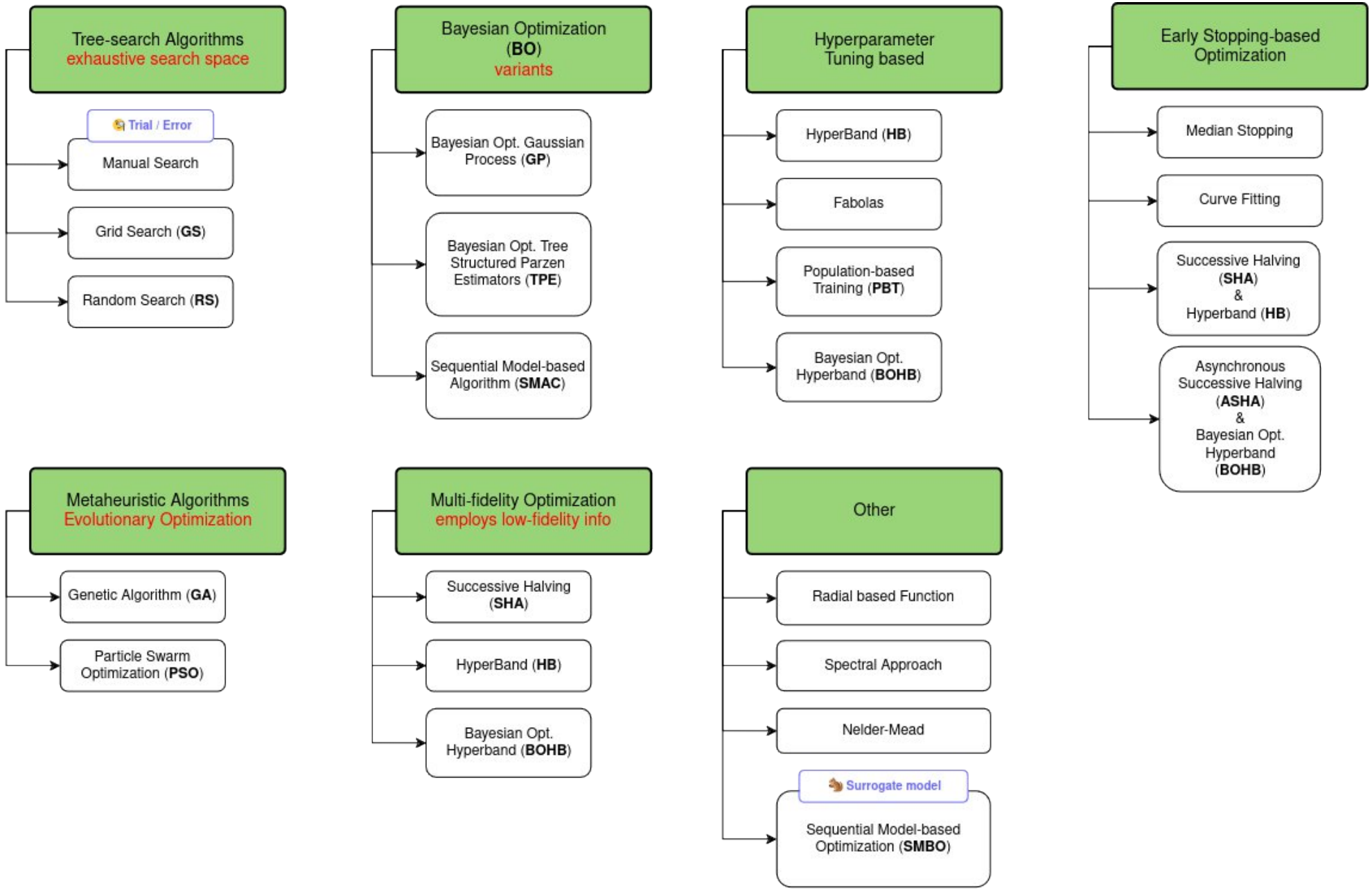



| budget | KDE models (resemble TPE) |
|---|---|
| 1 | Good point:{3, 4, 7, 8, ...}→ $l_1(x)$<br>Bad point:{1, 2, 5, 6, 9, ...}→ $g_1(x)$ |
| 3 | Good point:{8, 11, 12, 14, ...}→ $l_3(x)$<br>Bad point:{3, 7, 10, 13, ...}→ $g_3(x)$ |
| 9 | Good point:{11, 16, ...}→ $l_9(x)$<br>Bad point:{15, 17, ...}→ $g_9(x)$ |

## DEHB : Differential Evolution Hyperband



# Summary


Tree-search Algorithms
exhaustive search space
Trial / Error
Manual Search
Grid Search (GS)
Random Search (RS)
Bayesian Optimization
(BO)
variants
Bayesian Opt. Gaussian Process (GP)
Bayesian Opt. Tree Structured Parzen Estimators (TPE)
Sequential Model-based Algorithm (SMAC)
Hyperparameter Tuning based
HyperBand (HB)
Fabolas
Population-based Training (PBT)
Bayesian Opt. Hyperband (BOHB)
Early Stopping-based Optimization
Median Stopping
Curve Fitting
Successive Halving (SHA) & Hyperband (HB)
Asynchronous Successive Halving (ASHA) & Bayesian Opt. Hyperband (BOHB)
Metaheuristic Algorithms
Evolutionary Optimization
Genetic Algorithm (GA)
Particle Swarm Optimization (PSO)
Multi-fidelity Optimization
employs low-fidelity info
Successive Halving (SHA)
HyperBand (HB)
Bayesian Opt. Hyperband (BOHB)
Other
Radial based Function
Spectral Approach
Nelder-Mead
Surrogate model
Sequential Model-based Optimization (SMBO)

# Have the right tools

HPO frameworks ◂

Visualisation & Experiments Tracking ◂

# HPO Frameworks & tools


- Based on config file
- Easy to use
- Not only used for ML/DL

OPTUNA

- Work with an objective function
- Efficient Optimization Algorithms

RAY

tune

- Scalable HPO framework
- State of the art algorithms (PBT)
- Integrates with a wide range of additional HPO tools

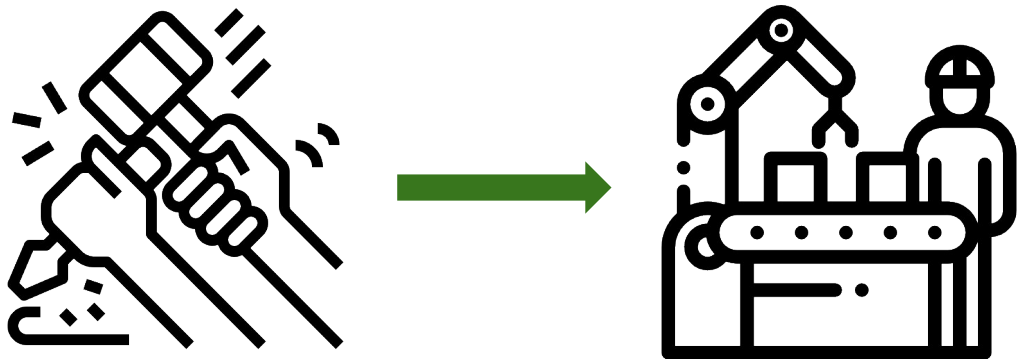
# Experiments tracking



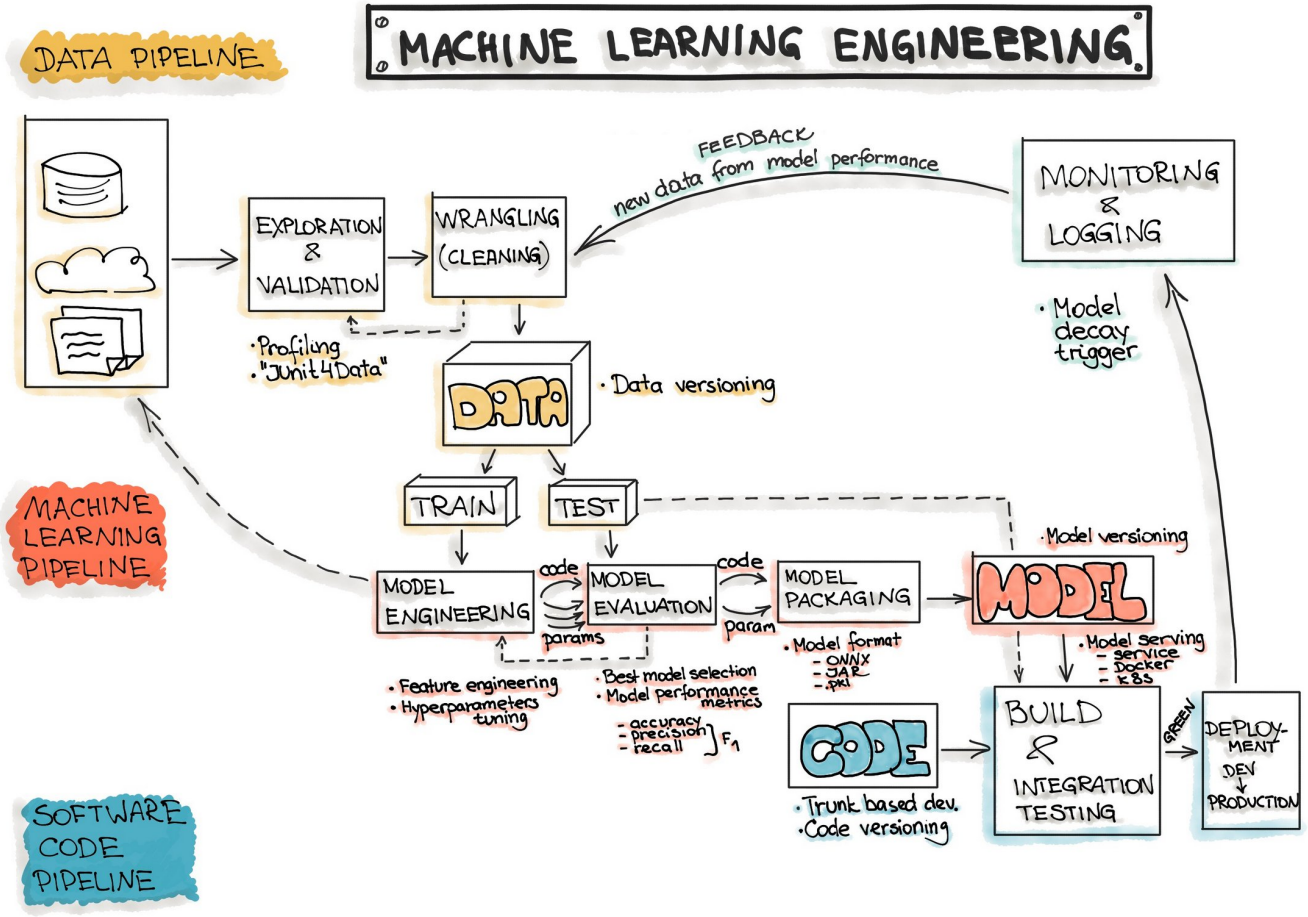
Advantages :

- allows you to save and order the results
- allows easy comparison and visualization of results
- provides all the information needed to reproduce the results

# HPO and MLOps



- As soon as our HPO requires a lot of resources (time, money or both) it is necessary to scale up and industrialize the experience process.
- Taking inspiration from MLOps processes and tools is a good start




https://ml-ops.org/content/end-to-end-ml-workflow

Kubeflow

mlflow™

# Sources


- Hyperparameter optimization: Foundations, algorithms, best practices, and open challenges (https://wires.onlinelibrary.wiley.com/doi/pdfdirect/10.1002/widm.1484)
- https://www.automl.org/
- Gradient-based Hyperparameter Optimization Over Long Horizons (https://openreview.net/pdf?id=6x8tcREIL2W)
- Seld-Tuning networks : Bilevel Optimization of Hyperparameters using structured best-response functions (https://openreview.net/pdf?id=r1eEG20qKQ)
- https://maelfabien.github.io/machinelearning/Explorium4/#
- https://towardsdatascience.com/a-novices-guide-to-hyperparameter-optimization-at-scale-bfb4e5047150#e813
- Population Based Training : https://www.deepmind.com/blog/population-based-training-of-neural-networks
- Hyper-Parameter Optimization: A Review of Algorithms and Applications : https://arxiv.org/pdf/2003.05689