



## Introduction

### Categorial Grammars & the Holy Trinity :

Logic	Computer Science	Linguistics
Propositional Constant	Base Type	Syntactic Category
Inference Rule	Term Rewrite	Phrase Formation
Axiom	Variable	Word
Provability	Type Inhabitation	Grammaticality
Deduction	Program Synthesis	Parsing

Standard pipeline:

parse surface form  $\implies$  convert to  $\lambda$   $\implies$  downstream task

This work:

parse deep  $\lambda$  form  $\implies$  downstream task

## Type Grammar

A **semantics-first, type-driven** grammar for the 21st century.

Combines:

- a linear functional core
- a set of residuated modalities

to capture:

- grammatical function-argument structures
- dependency-domain annotations ( $\leftarrow$  **new fancy feature!**)

- ✓ cooler than CCG!
- ✓ type checks!

**Grammatical Types** are inductively defined as:

$A, B := p$	# base categories, e.g. NP
$\diamond_d A$	# d-marked <b>complements</b> , e.g. $\diamond_{su} NP$
$A \multimap B$	# grammatical functions, e.g. $\diamond_{su} NP \multimap S$
$\square_d A$	# d-marked <b>adjuncts</b> , e.g. $\square_d (NP \multimap NP)$

**Inference Rules** assert grammaticality and provide recipes for compositional meaning assembly in the form of  $\lambda$  expressions:

$$\frac{}{x : A \vdash x : A} \text{id} \qquad \frac{(c \mapsto A) \in \mathcal{L}}{c : A \vdash c : A} \text{lex}$$

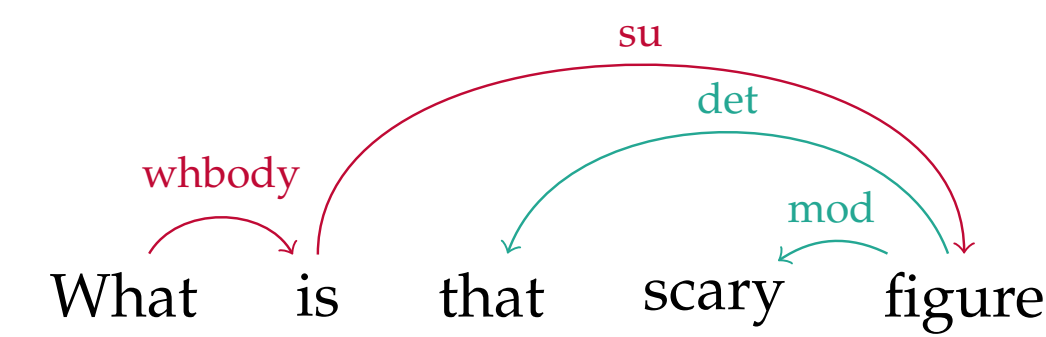
$$\frac{\Gamma \vdash s : A \multimap B \quad \Delta \vdash t : A}{\Gamma, \Delta \vdash st : B} \multimap E \qquad \frac{\Gamma, x : A \vdash s : B}{\Gamma \vdash \lambda x. s : A \multimap B} \multimap I$$

$$\frac{\Gamma \vdash s : \square_\delta A}{\langle \Gamma \rangle^\delta \vdash \blacktriangledown_\delta s : A} \square_\delta E \qquad \frac{\Gamma \vdash s : A}{\langle \Gamma \rangle^\delta \vdash \Delta_\delta s : \diamond_\delta A} \diamond_\delta I$$

## Proof Representations

### In Natural Deduction:

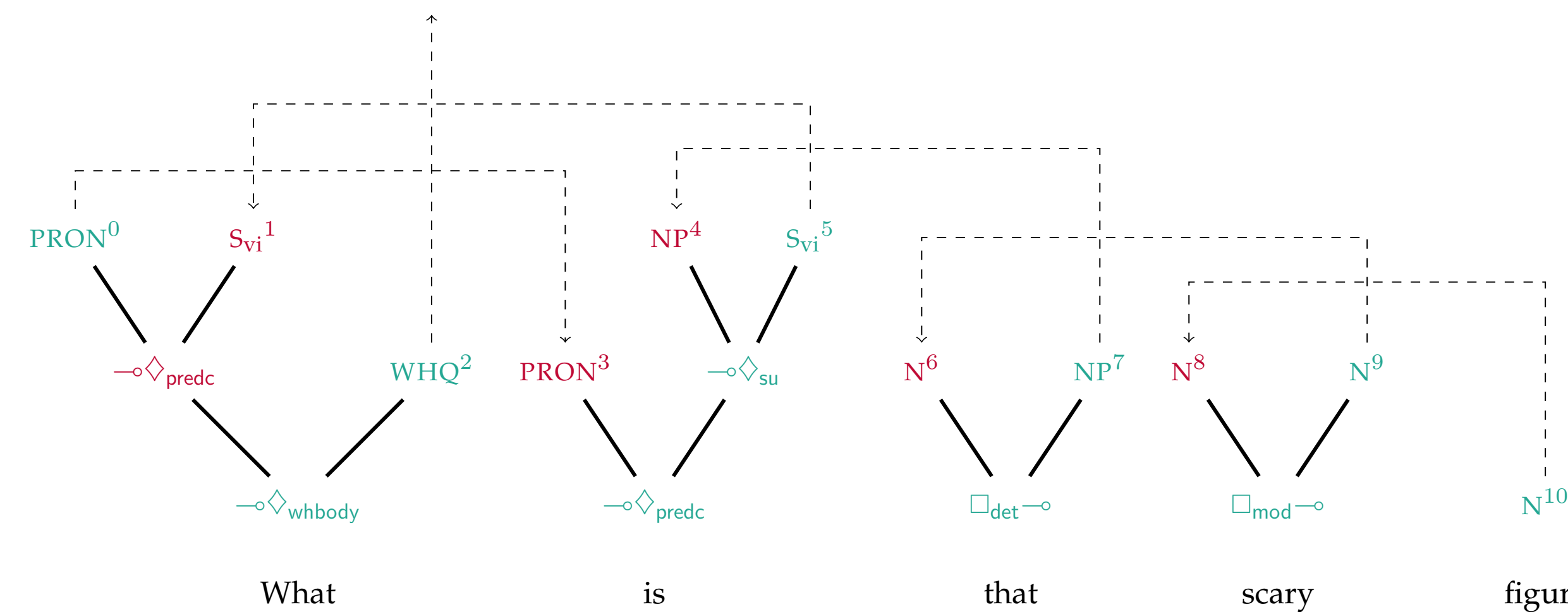
$$\frac{\frac{\frac{}{c_1 \vdash \diamond_{pred} PRON \multimap \diamond_{su} NP \multimap S VI} \text{lex} \quad \frac{}{x \vdash \diamond_{pred} PRON} \text{id}}{c_1, x \vdash \diamond_{su} NP \multimap S VI} \multimap E \quad \frac{\frac{\frac{}{c_2 \vdash \square_{det} (N \multimap NP)} \text{lex} \quad \frac{\frac{\frac{}{c_3 \vdash \square_{mod} (N \multimap N)} \text{lex} \quad \frac{\frac{}{c_4 \vdash N} \text{lex}}{c_3 \vdash \square_{mod} E}}{c_2 \vdash \square_{det} E}}{c_2 \vdash \square_{det} E} \multimap E}}{c_2 \vdash \square_{det} E, c_3 \vdash \square_{mod} E, c_4 \vdash N} \multimap E}}{c_1, x, \langle \langle c_2 \rangle^{det}, \langle c_3 \rangle^{mod}, c_4 \rangle^{su} \vdash S VI} \multimap I}}{c_0, \langle c_1, \langle \langle c_2 \rangle^{det}, \langle c_3 \rangle^{mod}, c_4 \rangle^{su} \rangle^{whbody} \vdash \diamond_{whbody} (\diamond_{pred} PRON \multimap S VI)} \multimap E} \diamond_{whbody} I$$



### a proof-tree

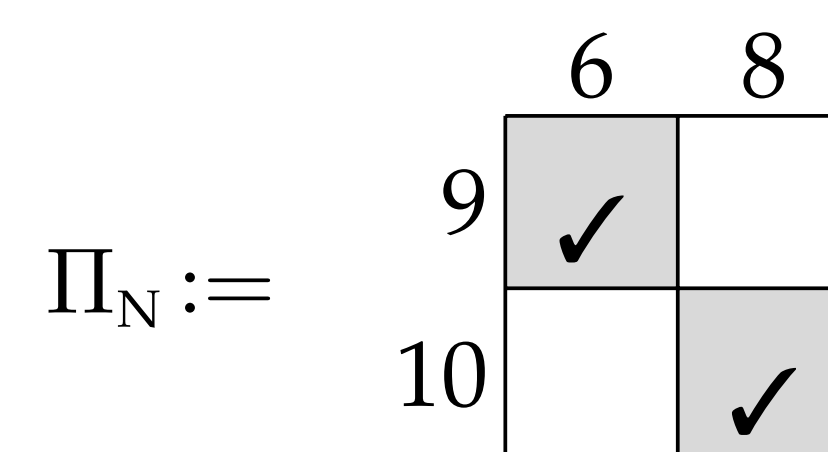
- ✓ clear computational interpretation
- ✓ trivial interface to a dependency tree
- ✓ correct by construction
- ✗ takes time to build (induction in *depth*)
- ✗ odd structure for ML (can't batch!)

### As a Proof Net:



### a proof-graph

- ✓ each type decomposed to a bicolor tree
- ✓ functional relations specified as a bijection
- ✓ fully parallel, easy to vectorize
- ✗ computationally intractable ( $n!$  combinations)
- ✗ requires formal verification



## System Architecture

### spind<sup>2</sup>λe

spind<sup>2</sup>λe parses into dependency-decorated  $\lambda$  expressions

A neat packaging of:

- a graph-based supertagger**
  - learns (word  $\mapsto$  type) mapping as a **graph generation task**
  - can correctly produce **new** types on demand
  - SOTA** across datasets (multi-framework, multi-lingual)
  - length-parallel, depth-linear decoding (i.e. **constant**)
- an OT-based proof search module**
  - learns proof search as a **node matching task**
  - fully parallel** in batch/depth/length
  - no iteration** (unlike shift-reduce)
- a mini type checker**
  - Python DSL to write/manipulate well-typed parses
  - handles proof net  $\longleftrightarrow$  nat. ded.  $\longleftrightarrow$   $\lambda$ -term conversions
  - asserts validity of neural output
  - user-friendly hooks

## Experiments

**Current implementation** trained/evaluated on *Æthel* (~70,000 proof-derivations of written Dutch):

parsability (some proof obtainable)	coverage (some proof obtained)
86.83	84.94
types correct (correct proof obtainable)	accuracy (correct proof obtained)
56.88	55.30

- faster & stricter than conventional parsers, just as accurate
- proof search bottlenecked by supertagging

## Try It Out/Read More



source code,  
installation instructions  
& usage examples



arXiv preprint