
diffsph
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DIFFSPH

1.1 diffsth package

1.1.1 Subpackages

diffsth.profiles package

Submodules

diffsth.profiles.analytics module

`diffsth.profiles.analytics.cobrA(t, rs, rh)`

Brightness H-function for the ‘constant’ top-hat source in the regime-A approximation

Parameters

- **t** – $D \sin(\theta)/r_h$, where θ (`theta`), r_h (`rh`) and D (`dist`) are defined below
- **theta** – angular radius in rad
- **rs** – scale radius
- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsth.profiles.analytics.cobrC(t, rs, rh)`

Brightness H-function for the ‘constant’ source in the regime-C approximation

Parameters

- **t** – $D \sin(\theta)/r_h$, where θ (`theta`), r_h (`rh`) and D (`dist`) are defined below
- **theta** – angular radius in rad
- **rs** – scale radius
- **rh** – diffusion radius parameter

`diffsth.profiles.analytics.cofdA(theta, rs, rh, dist)`

Flux-density H-function for the ‘constant’ top-hat source in the regime-A approximation

Parameters

- **theta** – angular radius in rad
- **rs** – scale radius

- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsph.profiles.analytics.cofdAmax(rs, rh, dist)`

Maximum value for the flux-density H-function for the ‘constant’ top-hat source in the regime-A approximation

Parameters

- **rs** – scale radius
- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsph.profiles.analytics.cofdC(theta, rs, rh, dist)`

Flux-density H-function for the ‘constant’ top-hat source in the regime-C approximation

Parameters

- **theta** – angular radius in rad
- **rs** – scale radius
- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsph.profiles.analytics.cofdCmax(rs, rh, dist)`

Maximum value for the flux-density H-function for the ‘constant’ top-hat source in the regime-C approximation

Parameters

- **rs** – scale radius
- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsph.profiles.analytics.psbrA(theta, rs, rh, dist)`

Brightness H-function for point sources in the regime-A approximation

Parameters

- **theta** – angular radius in rad
- **rs** – scale radius
- **rh** – diffusion radius parameter
- **dist** – distance to the source

`diffsph.profiles.analytics.psbrC(t, rh)`

Brightness H-function for point sources in the regime-C approximation Variable t is defined as

Parameters

- **t** – $D \sin(\theta)/r_h$, where θ (**theta**), r_h (**rh**) and D (**dist**) are defined below
- **theta** – angular radius in rad
- **rh** – diffusion radius parameter
- **dist** – distance to the source

diffsph.profiles.analytics.psfdC(theta, rh, dist)

Flux-density H-function for point sources in the regime-C approximation

Parameters

- **theta** – angular radius in rad
- **rh** – diffusion radius parameter
- **dist** – distance to the source

diffsph.profiles.analytics.psfdCmax(rh, dist)

Maximum value for the flux-density H-function for point sources in the regime-C approximation

Parameters

- **rh** – diffusion radius parameter
- **dist** – distance to the source

diffsph.profiles.analytics.sisbrA(t, sigmav, rh)

Brightness H-function for the singular isothermal source in the regime-A approximation

Parameters

- **t** – $D \sin(\theta)/r_h$, where θ (**theta**), r_h (**rh**) and D (**dist**) are defined below
- **theta** – angular radius in rad
- **sigmav** – velocity dispersion parameter
- **rh** – diffusion radius parameter
- **dist** – distance to the source

diffsph.profiles.analytics.sisbrC(t, sigmav, rh)

Brightness H-function for the singular isothermal source in the regime-C approximation

Parameters

- **t** – $D \sin(\theta)/r_h$, where θ (**theta**), r_h (**rh**) and D (**dist**) are defined below
- **theta** – angular radius in rad
- **sigmav** – velocity dispersion parameter
- **rh** – diffusion radius parameter
- **dist** – distance to the source

diffsph.profiles.hfactors module**diffsph.profiles.hfactors.D_factor(theta, dist, rad_temp, **kwargs)**

Generic “D” factor

Parameters

- **theta** – angular distance in rad units
- **dist** – distance to earth
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

D factor

`diffsph.profiles.hfactors.H_brightness(theta, dist, rh, hyp, rad_temp, regime, **kwargs)`

Generic emissivity halo/bulge function in the Regime “A”, “B” or “C” approximations

Parameters

- **theta** – angular distance in rad units
- **dist** – distance to earth
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: ‘wimp’ (**default**), ‘decay’ or ‘generic’)
- **halo_model** – DM halo model
- **rad_temp** – radial template
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

brightness halo/bulge function

`diffsph.profiles.hfactors.H_emissivity(r, rh, hyp, rad_temp, regime, **kwargs)`

Generic emissivity halo/bulge function in the Regime “A”, “B” or “C” approximations

Parameters

- **r** – galactocentric distance

- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic')
- **rad_temp** – radial template
- **regime** – regime of the approximation (upper/lower case a, b, c or I/II/III).

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

emissivity halo/bulge function

`diffsph.profiles.hfactors.H_fluxdens(theta, dist, rh, hyp, rad_temp, regime, **kwargs)`

Generic flux-density halo/bulge function in the Regime "A", "B" or "C" approximations

Parameters

- **theta** – angular distance in rad units
- **dist** – distance to earth
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic')
- **halo_model** – DM halo model
- **rad_temp** – radial template
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile

- **sigmav** – velocity dispersion parameter σ_v in the [*diffsph.profiles.templates.sis\(\)*](#) profile

Returns

flux density halo/bulge function

`diffsph.profiles.hfactors.H_fluxdens_approx(theta, dist, rh, hyp, rad_temp, regime, **kwargs)`

Generic flux-density halo/bulge function in the Regime “A”, “B” or “C” approximations (alternative formula)

Parameters

- **theta** – angular distance in rad units
- **dist** – distance to earth
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: ‘wimp’ (**default**), ‘decay’ or ‘generic’)
- **halo_model** – DM halo model
- **rad_temp** – radial template
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the [*diffsph.profiles.templates.hdz\(\)*](#) profile
- **beta** – exponent β in the [*diffsph.profiles.templates.hdz\(\)*](#) profile
- **gamma** – exponent γ in the [*diffsph.profiles.templates.hdz\(\)*](#) profile
- **alphaE** – parameter α_E in the [*diffsph.profiles.templates.enst\(\)*](#) profile
- **rc** – core radius parameter r_c in the [*diffsph.profiles.templates.cnfw\(\)*](#) profile
- **sigmav** – velocity dispersion parameter σ_v in the [*diffsph.profiles.templates.sis\(\)*](#) profile

Returns

flux density halo/bulge function

`diffsph.profiles.hfactors.Hem_A(r, rh, hyp, rad_temp, **kwargs)`

Generic emissivity halo/bulge function for Regime A

Parameters

- **r** – galactocentric distance
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: ‘wimp’ (**default**), ‘decay’ or ‘generic’)
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density

- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

emissivity halo/bulge function using the Regime-A approximation

`diffsph.profiles.hfactors.Hem_B(r, rh, hyp, rad_temp, **kwargs)`

Generic emissivity halo/bulge function for Regime B

Parameters

- **r** – galactocentric distance
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic')
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

emissivity halo/bulge function using the Regime-B approximation

`diffsph.profiles.hfactors.Hem_C(r, rh, hyp, rad_temp, **kwargs)`

Generic emissivity halo/bulge function for Regime C

Parameters

- **r** – galactocentric distance
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic')
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

emissivity halo/bulge function using the Regime-C approximation

`diffsph.profiles.hfactors.J_factor(theta, dist, rad_temp, **kwargs)`

Generic “J” factor

Parameters

- **theta** – angular distance in rad units
- **dist** – distance to earth
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

J factor

`diffsph.profiles.hfactors.halo_factor(n, rh, hyp, rad_temp, **kwargs)`

n-th order halo/bulge factor h_n for a given model (e.g. NFW, Einasto, Plummer, ...) Arguments ‘n’, ‘rh’, ‘hyp’ and ‘rad_temp’ are necessary. Remaining arguments depend on the adopted halo model.

Parameters

- **n** – order of the halo/bulge factor
- **rh** – diffusion halo/bulge radius
- **hyp (str)** – hypothesis: ‘wimp’ (**default**), ‘decay’ or ‘generic’)
- **rad_temp** – radial template

Keyword arguments

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

halo/bulge factor

diffsph.profiles.massmodels module

`diffsph.profiles.massmodels.D(tharcmin, galaxy, rad_temp, manual=False, **kwargs)`

Model-specific D factor in GeV/cm²

Parameters

- **tharcmin** – angular radius in arcmin
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile

- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

D factor

`diffsph.profiles.massmodels.Hbr(tharcmin, galaxy, rad_temp, hyp, ratio, regime='B', manual=False, **kwargs)`

Model-specific brightness halo/bulge function in the Regime “A”, “B” or “C” approximations

Parameters

- **tharcmin** – angular radius in arcmin
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and the half-light radius (default value = 1)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

brightness halo/bulge function

`diffsph.profiles.massmodels.Hem(r, galaxy, rad_temp, hyp, ratio, regime='B', manual=False, **kwargs)`

Model-specific emissivity halo/bulge function in the Regime “A”, “B” or “C” approximations

Parameters

- **r** – galactocentric distance in kpc

- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and the half-light radius (default value = 1)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the *diffsph.profiles.templates.hdz()* profile
- **beta** – exponent β in the *diffsph.profiles.templates.hdz()* profile
- **gamma** – exponent γ in the *diffsph.profiles.templates.hdz()* profile
- **alphaE** – parameter α_E in the *diffsph.profiles.templates.enst()* profile
- **rc** – core radius parameter r_c in the *diffsph.profiles.templates.cnfw()* profile
- **sigmav** – velocity dispersion parameter σ_v in the *diffsph.profiles.templates.sis()* profile

Returns

emissivity halo/bulge function

diffsph.profiles.massmodels.Hfd(*tharcmin*, *galaxy*, *rad_temp*, *hyp*, *ratio*, *regime='B'*, *manual=False*, ***kwargs*)

Model-specific flux-density halo/bulge function in the Regime "A", "B" or "C" approximations

Parameters

- **tharcmin** – angular radius in arcmin
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and the half-light radius (default value = 1)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

brightness halo/bulge function

`diffsph.profiles.massmodels.J(tharcmin, galaxy, rad_temp, manual=False, **kwargs)`

Model-specific J factor in Gev²/cm⁵

Parameters

- **tharcmin** – angular radius in arcmin
- **galaxy** (str) – name of the galaxy
- **rad_temp** (str) – radial template ('NFW', 'Einasto', etc.)
- **manual** (bool) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile

- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

J factor

`diffsph.profiles.massmodels.h(n, galaxy, rad_temp, hyp, ratio, manual=False, **kwargs)`

Model-specific n-th halo factor

Parameters

- **n** – order of the halo/bulge factor
- **rh** – diffusion halo/bulge radius
- **rad_temp** – radial template
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and the half-light radius
- **manual (bool)** – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual = 'False'**

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual = 'True'**

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

halo factor

`diffsph.profiles.massmodels.rho(r, rad_temp, manual=False, **kwargs)`

Dark matter density

Parameters

- **r** – galactocentric distance
- **rad_temp** – template ('NFW', 'Einasto', etc.)

- **manual** (*bool*) – manual input of parameter values in `rad_temp` (default value = 'False')

Keyword arguments

- `manual = 'False'`

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- `manual = 'True'`

Parameters

- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

dark matter density

diffsph.profiles.templates module

diffsph.profiles.templates.bkrt(*r, rs, rhos*)

Burkert dark-matter halo profile.

$$\rho(r) = \frac{\rho_s}{(1 + r/r_s)(1 + r^2/r_s^2)}$$

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – scale radius
- **rhos** – characteristic density

Returns

density at galactocentric distance *r*

diffsph.profiles.templates.cnfw(*r, rs, rhos, rc*)

Cored Navarro/Frenk/White dark-matter halo template.

$$\rho(r) = \frac{\rho_s}{(r/r_s + r_c/r_s)(1 + r/r_s)^2}$$

Parameters

- **r** – main variable (galactocentric distance)

- **rs** – scale radius
- **rhos** – characteristic density
- **rc** – core radius

Returnsdensity at galactocentric distance r `diffsph.profiles.templates.const(r, rs)`

Constant (top-hat) template

$$\rho(r) = \frac{3}{4\pi r_s^3} \Theta(r_s - r)$$

Parameters**rs** – characteristic radius**Returns**

constant density

`diffsph.profiles.templates.enst(r, rs, rhos, alphaE=0.17)`

Einasto dark-matter halo profile.

$$\rho(r) = \rho_s \exp \left[-\frac{2}{\alpha_E} \left(\frac{r^{\alpha_E}}{r_s^{\alpha_E}} - 1 \right) \right]$$

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – scale radius
- **rhos** – characteristic density
- **alphaE** – power-law slope of the Einasto profile, (default value = 0.17)

Returnsdensity at galactocentric distance r `diffsph.profiles.templates.hdz(r, rs, rhos, alpha, beta, gamma)`

Hernquist/Demand/Zhao dark-matter halo template.

$$\rho(r) = \frac{\rho_s}{(r/r_s)^\gamma (1 + (r/r_s)^\alpha)^{\frac{\beta-\gamma}{\alpha}}}$$

Using default values alpha = 1, beta = 3 and gamma = 1 results in the default NFW halo profile.

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – scale radius
- **rhos** – characteristic density
- **alpha** – inner exponent
- **beta** – large-r exponent
- **gamma** – small-r exponent

Returnsdensity at galactocentric distance r

diffsph.profiles.templates.nfw(*r, rs, rhos*)

Navarro/Frenk/White dark-matter halo template.

$$\rho(r) = \frac{\rho_s}{(r/r_s)(1+r/r_s)^2}$$

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – scale radius
- **rhos** – characteristic density

Returnsdensity at galactocentric distance *r***diffsph.profiles.templates.plmm(*r, rs*)**

Plummer template

$$\rho(r) = \frac{3}{4\pi r_s^3} \frac{1}{(1+r^2/r_s^2)^{5/2}}$$

Parameters

- **r** – main variable (distance to the center)
- **rs** – Plummer radius
- **rhoa** – central density

Returnsdensity of the Plummer sphere at distance *r***diffsph.profiles.templates.ps(*r, rs*)**

Point source template

$$\rho(r) = \frac{1}{4\pi r^2} \delta(r)$$

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – characteristic radius

Returnsdensity at galactocentric distance *r***diffsph.profiles.templates.ps_iso(*r, rs, rhos*)**

Pseudo-isothermal sphere dark-matter halo profile.

$$\rho(r) = \frac{\rho_s}{1+r^2/r_s^2}$$

Parameters

- **r** – main variable (galactocentric distance)
- **rs** – scale radius
- **rhos** – characteristic density

Returnsdensity at galactocentric distance *r*

diffsph.profiles.templates.sis(*r, sigmav*)

Singular isothermal sphere

$$\rho(r) = \frac{\sigma_v^2}{2\pi G r^2}$$

Parameters

- **r** – main variable (galactocentric distance)
- **sigmav** – velocity dispersion

Returns

density at galactocentric distance *r*

Module contents**diffsph.spectra package****Submodules****diffsph.spectra.analytics module****diffsph.spectra.analytics.Fav**(*x*)

Synchrotron-power function for randomly-oriented magnetic fields¹.

$$F(x) = x^2 \left(K_{4/3}(x)K_{1/3}(x) - \frac{3}{5}x[K_{4/3}^2(x) - K_{1/3}^2(x)] \right)$$

Returns

Pitch-angle averaged synchrotron function as a function of *x*

diffsph.spectra.analytics.M_C(*xi, eta, delta*)

Master function in the Regime-C limit

$$\mathcal{M}_C(\xi, \eta, \delta) = \frac{\xi^\delta}{(1-\delta)\eta} F(\xi^2)$$

diffsph.spectra.analytics.M_i(*xi, eta, delta*)

Master function in the large η limit

$$\mathcal{M}_i(\xi, \eta, \delta) = \frac{\Gamma^2(1/3)\eta^{-\frac{5}{3(1-\delta)}}}{5\sqrt[3]{2}(1-\delta)} \Gamma\left(\frac{5}{3(1-\delta)}, \eta\xi^{1-\delta}\right) \exp(\eta\xi^{1-\delta})$$

diffsph.spectra.analytics.M_raw(*xi, eta, delta*)

“Raw” master function

$$\mathcal{M}(\xi, \eta, \delta) = \int_\xi^\infty dx F(x^2) \exp(-\eta[x^{1-\delta} - \xi^{1-\delta}])$$

Returns

above integral

¹ Formula extracted from Ghisellini et al, 1988

diffsph.spectra.analytics.anltc_Mst(*xi, eta, delta*)

Master function

$$\mathcal{M}(\xi, \eta, \delta) = \int_{\xi}^{\infty} dx F(x^2) \exp(-\eta [x^{1-\delta} - \xi^{1-\delta}])$$

Note: Function evaluates the above integral only for those values where no numerical errors are present. Otherwise, it uses the approximate formulas `diffsph.spectra.analytics.M_C()` or `diffsph.spectra.analytics.M_i()`

diffsph.spectra.analytics.btot(*E, B*)

Total energy loss function in GeV/s

Parameters

- **E** – cosmic-ray energy in GeV
- **B** – magnitude of the magnetic field's smooth component in μG

Returns

energy-loss rate in GeV/s

diffsph.spectra.analytics.lam(*E, B, D0, delta=0.3333333333333333*)Syrovatskii variable in kpc^2 **Parameters**

- **E** – cosmic-ray energy in GeV
- **B** – magnitude of the magnetic field's smooth component in μG
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
(default value = 1/3)

ReturnsSyrovatskii variable in kpc^2 **diffsph.spectra.synchrotron module****diffsph.spectra.synchrotron.Enu(*B, nu*)**Typical particle energy in GeV for synchrotron radiation at the frequency *nu* in GHz and for a magnetic field *B* in μG **Parameters**

- **B** – magnitude of the magnetic field's smooth component in μG
- **nu** – frequency in GHz

Returns

Particle energy in GeV.

diffsph.spectra.synchrotron.Mst(*xi, eta, delta*)Interpolation function for the kernel function $\hat{\mathcal{M}}(\xi, \eta, \delta)$ **Parameters**

- **xi** – ξ

- **eta** – η
- **delta** – δ

Returns

Spectral-function kernel (as an interpolation function)

`diffsph.spectra.synchrotron.Mst_DM(xi, eta, m, delta, channel)`

Master function for dark-matter hypotheses

Parameters

- **xi** – ξ
- **eta** – η
- **delta** – δ
- **m** – WIMP mass in GeV
- **channel** – annihilation/decay channel

Returns

Master function (as an interpolation function) for DM hypotheses

`diffsph.spectra.synchrotron.Mst_pw(eta, Gamma, delta)`

Master function for the generic power-law hypothesis

Parameters

- **eta** – η
- **Gamma** – Γ
- **delta** – δ

Returns

Master function (as an interpolation function) for the generic power-law hypothesis

`diffsph.spectra.synchrotron.X(nu, tau, delta, B, hyp, **kwargs)`

Spectral function in erg/GHz for all hypotheses built in diffsp

Parameters

- **nu** – frequency in GHz
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
- **B** – magnitude of the magnetic field's smooth component in μG
- **hyp (str)** – hypothesis: 'wimp', 'decay' or 'generic'

Keyword arguments:

- If `hyp = 'wimp' or 'decay'`

Parameters

- **mchi** – mass of the DM particle in GeV/c^2
- **channel (str)** – annihilation/decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- If **hyp** = 'generic'

Parameters

Gamma – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)

Returns

spectral function in erg/GHz

`diffsph.spectra.synchrotron.X_DM(k, mchi, channel, nu, tau, delta, B)`

Spectral function in erg/GHz for all DM hypotheses built in `diffsph`

Parameters

- **k** – hypothesis index (k=1 for decay and k=2 for annihilation)
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** – annihilation/decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **nu** – frequency in GHz
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
- **B** – magnitude of the magnetic field's smooth component in μG

Returns

spectral function in erg/GHz

`diffsph.spectra.synchrotron.X_gen(Emin, Emax, S_func, nu, tau, delta, B)`

Spectral function in erg/GHz for generic CRE sources

$$X_{\text{gen}}(\nu) = \int_{E_m}^{E_M} dE' \hat{X}(\nu, E') S(E')$$

Parameters

- **Emin** – low-E cutoff energy in GeV of the CRE source '`S_func`'
- **Emax** – high-E cutoff energy in GeV of the CRE source '`S_func`'
- **S_func** – CRE source function
- **nu** – frequency in GHz
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
- **B** – magnitude of the magnetic field's smooth component in μG

Returns

spectral function in erg/GHz

`diffsph.spectra.synchrotron.X_pw(Gamma, nu, tau, delta, B)`

Spectral function in erg/GHz for the generic power-law hypothesis

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **nu** – frequency in GHz
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
- **B** – magnitude of the magnetic field's smooth component in μG

Returns

spectral function in erg/GHz

`diffsph.spectra.synchrotron.eta(E, B, tau, delta)`

η variable as a function of the CRE's energy, magnetic field, tau and delta parameters

Parameters

- **E** – CRE energy in GeV
- **B** – magnetic field strength in μG
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy

Returns

η variable

`diffsph.spectra.synchrotron.htX(E, nu, tau, delta, B, fast_comp=True)`

Spectral function kernel in erg/GHz \hat{X}

Parameters

- **E** – CRE energy in GeV
- **nu** – frequency in GHz
- **tau** – diffusion time-scale parameter for a 1 GeV CRE in s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy
- **B** – magnitude of the magnetic field's smooth component in μG
- **fast_comp** (`bool`) – if 'True', employs the interpolating method (default value = 'True')

Returns

spectral kernel in erg/GHz

`diffsph.spectra.synchrotron.lMst(Lxi, Leta, delta)`

Interpolation function for (kernel) $\log(\hat{\mathcal{M}})$

Parameters

- **Lxi** – $\log(\xi)$
- **Leta** – $\log(\eta)$
- **delta** – δ

Returns

$\log(\hat{\mathcal{M}})$ as a function of $\log(\xi)$, $\log(\eta)$ and δ

`diffsph.spectra.synchrotron.lMst_DM(Lxi, Leta, Lm, delta, channel)`

Interpolation function $\log(\mathcal{M})$ for DM hypotheses

Parameters

- **Lxi** – $\log(\xi)$
- **Leta** – $\log(\eta)$
- **Lm** – $\log(m/\text{GeV})$ (m is the WIMP mass)
- **delta** – δ
- **channel** – annihilation/decay channel

Returns

$\log(\mathcal{M})$ as a function of $\log(\xi)$, $\log(\eta)$, $\log(m)$ and δ

`diffsph.spectra.synchrotron.lMst_pw(Leta, Gamma, delta)`

Interpolation function $\log(\mathcal{M})$ for the generic power-law hypothesis

Parameters

- **Leta** – $\log(\eta)$
- **Gamma** – Γ
- **delta** – δ

Returns

$\log(\mathcal{M}_{\text{gen}})$ as a function of $\log(\eta)$, Γ and δ

Module contents

diffsph.utils package

Submodules

diffsph.utils.consts module

diffsph.utils.dictionaries module

diffsph.utils.tools module

`diffsph.utils.tools.TB(brightness, theta, nu, *args, **kwargs)`

Brightness temperature conversion

$$T_B = \frac{c^2}{2 k \nu^2} I_\nu$$

Parameters

- **brightness** – generic brightness function in Jy/sr
- **theta** – angular radius (as the first argument of the generic brightness function)
- **nu** – frequency (as the second argument of the generic brightness function)

Returns

brightness temperature in mK

`diffsph.utils.tools.approxhalo_fd(n, theta, dist, rh)`

Partial (θ -dependent) flux-density halo/bulge factor (approximate formula):

$$\mathcal{H}_n(\theta) = \mathcal{H}_n(r_h, R) - 2 \int_{R \sin(\theta)}^{r_h} dr r \kappa_1(r, R, \theta) \frac{\sin\left(\frac{n\pi r}{r_h}\right)}{r}$$

where R , rh and n are, respectively the distance, halo radius and Fourier index

`diffsph.utils.tools.approxhalo_fd_tot(n, dist, rh)`

Total flux-density halo/bulge factor (approximate formula):

$$\mathcal{H}_n(r_h, R) \simeq 4\pi \int_0^{r_h} dr r^2 \frac{\sin\left(\frac{n\pi r}{r_h}\right)}{r} ,$$

where R , rh and n are, respectively the distance, halo radius and Fourier index

`diffsph.utils.tools.check_cache()`

Function checks whether the `/.diffsph_cache/` folder exists. If it does not exists, it creates it

Returns

folder directory name

Return type

str

`diffsph.utils.tools.delta_float(inp)`

Float number for variable 'delta'

Parameters

`inp` – variable 'delta' as `str` ('kol', 'kra', etc.) or `float`

Returns

float number associated with 'inp'

Return type

float

`diffsph.utils.tools.df(func, **kwargs)`

`diffsph.utils.tools.evaluate(f, x, **kwargs)`

Function converts string into a python function's name and evaluates it

Parameters

- `f` – function to be evaluated

- `x` – first argument of `f`

Returns

$f(x)$

`diffsph.utils.tools.f(n, x)`

Basis function in Fourier-expanded brightness formula

$$f_n(x) = 2 \int_x^1 \frac{\sin(n\pi y) dy}{\sqrt{y^2 - x^2}}$$

Returns

f_n as a function of x

`diffsph.utils.tools.fwhm(brightness, thmax, *args, **kwargs)`

Full width at half maximum

Parameters

- **brightness** – generic brightness function
- **thmax** – signal's angular radius

Returns

Full width at half maximum in arcmin

`diffsph.utils.tools.g(n, x)`

Basis function in Fourier-expanded flux density formula

$$g_n(x) = 2 \int_x^1 \sqrt{y^2 - x^2} \sin(n\pi y) dy$$

Returns

g_n as a function of x

`diffsph.utils.tools.halo_fd(n, theta, dist, rh)`

Partial (θ -dependent) flux-density halo/bulge factor:

$$\mathcal{H}_n(\theta) = \mathcal{H}_n(r_h, R) - 2 \int_{R \sin(\theta)}^{r_h} dr r \kappa_1(r, R, \theta) \frac{\sin\left(\frac{n\pi r}{r_h}\right)}{r},$$

where R , rh and n are, respectively the distance, halo radius and Fourier index

`diffsph.utils.tools.halo_fd_tot(n, dist, rh)`

Total flux-density halo/bulge factor:

$$\mathcal{H}_n(r_h, R) = 2 \int_0^{r_h} dr r \kappa_0(r, R) \frac{\sin\left(\frac{n\pi r}{r_h}\right)}{r},$$

where R , rh and n are, respectively the distance, halo radius and Fourier index

Returns

Halo flux-density factor

`diffsph.utils.tools.hfd(fluxdens, thmax, *args, **kwargs)`

Half-flux diameter

Parameters

- **brightness** – generic brightness function
- **thmax** – signal's angular radius

Returns

Half-flux diameter in arcmin

`diffsph.utils.tools.hypothesis_index(hyp)`

Index of the hypothesis (1 for decaying DM or generic scenario, 2 for WIMP self-annihilation).

Parameters

`hyp (str)` – hypothesis: 'wimp', 'decay' or 'generic')

Returns

hypothesis index

Return type

int

`diffsph.utils.tools.ker_0(r, dist)`

$$\kappa_0(r, R) = \frac{1}{R} \log \sqrt{\frac{R+r}{R-r}}$$

`diffsph.utils.tools.ker_1(r, theta, dist)`

$$\kappa_1(\theta, r, R) = \frac{1}{R} \log \frac{R \cos \theta + \sqrt{r^2 - R^2 \sin^2 \theta}}{\sqrt{R^2 - r^2}}$$

`diffsph.utils.tools.load_data(folder)`

Function loads data from folder

Returns

data organized in form of a python dictionary

Return type

dict

`diffsph.utils.tools.sort_kwargs(**kwargs)`

Function sorts keyword arguments alphabetically

Returns

sorted keywords with corresponding entries

Return type

dict

`diffsph.utils.tools.var_to_str(inp)`

Dictionary for variables 'delta', 'hyp', 'galaxy', 'ref' and 'rad_temp'

Parameters

`inp` – input string or number

Returns

default variable name

Return type

str

Module contents

1.1.2 Submodules

1.1.3 `diffsph.limits` module

`diffsph.limits.decay_rate_gausslim(nu, a_fit, sigma_fit, beam_size, galaxy, rad_temp, D0=3e+28, delta='kol', B=2, mchi=50, channel='mumu', manual=False, **kwargs)`

Maximum dark matter decay rate allowed by the exclusion of a Gaussian-shaped signal

$$a_{\text{fit}} \exp \left(-\frac{\theta^2}{2\sigma_{\text{fit}}^2} \right)$$

Parameters

- **nu** – frequency in GHz
- **a_fit** – fitted gaussian amplitude in μ Jy / beam
- **sigma_fit** – width parameter of the Gaussian template in arcmin
- **beam_size** – beam size in arcseconds
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – dark matter halo model ('NFW', 'Einasto', etc.)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in $\mu \text{ G}$ (default value = $2\mu \text{ G}$)
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **sigmav** – velocity dispersion in km/s for the isothermal sphere `diffsph.profiles.templates.sis()`

Returns

upper limit on the DM decay rate in 1/s

Return type

float

```
diffsph.limits.decay_rate_limest(nu, rms_noise, beam_size, galaxy, rad_temp, ratio=1, D0=3e+28,
                                 delta='kol', B=2, mchi=50, channel='mumu', manual=False,
                                 high_res=False, accuracy=1, **kwargs)
```

(Estimated) maximum dark matter decay rate given the rms noise level of an observation

Parameters

- **nu** – frequency in GHz
- **rms_noise** – RMS noise level of the observation in μ Jy / beam
- **beam_size** – beam size in arcseconds
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – dark matter halo model ('NFW', 'Einasto', etc.)
- **ratio** – ratio between the diffusion halo and half-light radii
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **manual** (*bool*) – manual input of parameter values in `rad_temp` (default value = 'False')
- **high_res** (*bool*) – spatial resolution. If 'True', `synch emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **sigmav** – velocity dispersion in km/s for the isothermal sphere `diffsph.profiles.templates.sis()`

Returns

Estimated upper limit on the DM decay rate in 1/s

Return type

float

```
diffsph.limits.generic_rate_gausslim(nu, a_fit, sigma_fit, beam_size, galaxy, rad_temp, D0=3e+28,  
                                     delta='kol', B=2, Gamma=2, **kwargs)
```

Maximum CRE production rate (generic power-law hypothesis) allowed by the exclusion of a Gaussian-shaped signal

$$a_{\text{fit}} \exp\left(-\frac{\theta^2}{2\sigma_{\text{fit}}^2}\right)$$

Parameters

- **nu** – frequency in GHz
- **a_fit** – fitted gaussian amplitude in μ Jy / beam
- **sigma_fit** – width parameter of the Gaussian template in arcmin
- **beam_size** – beam size in arcseconds
- **galaxy** (str) – name of the galaxy
- **rad_temp** (str) – dark matter halo model ('NFW', 'Einasto', etc.)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = 3×10^{28} cm^2/s)
- **delta** (float, str) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$, default value = 2)
- **manual** (bool) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **sigmav** – velocity dispersion in km/s for the isothermal sphere *diffsph.profiles.templates.sis()*

Returns

upper limit on the generic CRE production rate in 1/s

Return type

float

```
diffsph.limits.generic_rate_limest(nu, rms_noise, beam_size, galaxy, rad_temp, ratio=1, D0=3e+28,
                                    delta='kol', B=2, Gamma=2, high_res=False, accuracy=1, **kwargs)
```

(Estimated) maximum CRE production rate (generic power-law hypothesis) given the rms noise level of an observation

Parameters

- **nu** – frequency in GHz
- **rms_noise** – RMS noise level of the observation in μ Jy / beam
- **beam_size** – beam size in arcseconds
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – dark matter halo model ('NFW', 'Einasto', etc.)
- **ratio** – ratio between the diffusion halo and half-light radii
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$, default value = 2)
- **manual** (*bool*) – manual input of parameter values in `rad_temp` (default value = 'False')
- **high_res** (*bool*) – spatial resolution. If 'True', `synch_emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **sigmav** – velocity dispersion in km/s for the isothermal sphere `diffsph.profiles.templates.sis()`

Returns

Estimated upper limit on the generic CRE production rate in 1/s

Return type

float

```
diffsph.limits.sigmav_gausslim(nu, a_fit, sigma_fit, beam_size, galaxy, rad_temp, D0=3e+28, delta='kol',
                                 B=2, mchi=50, channel='mumu', self_conjugate=True, manual=False,
                                 **kwargs)
```

Maximum WIMP self-annihilation cross-section allowed by the exclusion of a Gaussian-shaped signal

$$a_{\text{fit}} \exp\left(-\frac{\theta^2}{2\sigma_{\text{fit}}^2}\right)$$

Parameters

- **nu** – frequency in GHz
- **a_fit** – fitted gaussian amplitude in μ Jy / beam
- **sigma_fit** – width parameter of the Gaussian template in arcmin
- **beam_size** – beam size in arcseconds
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – dark matter halo model ('NFW', 'Einasto', etc.)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in $\mu \text{ G}$ (default value = $2\mu \text{ G}$)
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile

Returns

upper limit for the WIMP self-annihilation cross-section in cm^3/s

Return type

float

```
diffsph.limits.sigmax_limest(nu, rms_noise, beam_size, galaxy, rad_temp, ratio=1, D0=3e+28, delta='kol',
                             B=2, mchi=50, channel='mumu', self_conjugate=True, manual=False,
                             high_res=False, accuracy=1, **kwargs)
```

(Estimated) maximum WIMP self-annihilation cross-section given the rms noise level of an observation

Parameters

- **nu** – frequency in GHz
- **rms_noise** – RMS noise level of the observation in μ Jy / beam
- **beam_size** – beam size in arcseconds
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – dark matter halo model ('NFW', 'Einasto', etc.)
- **ratio** – ratio between the diffusion halo and half-light radii
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **manual** (*bool*) – manual input of parameter values in `rad_temp` (default value = 'False')
- **high_res** (*bool*) – spatial resolution. If 'True', `synch emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- `manual = 'False'`

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- `manual = 'True'`

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile

Returns

Estimated upper limit on WIMP self-annihilation cross-section in cm^{-3}/s

Return type
float

1.1.4 `diffsph.pyflux` module

`diffsph.pyflux.Dec_rad(galaxy)`

`diffsph.pyflux.RA_rad(galaxy)`

`diffsph.pyflux.coeff(n, nu, galaxy, rad_temp, hyp, ratio, D0, delta, B, manual=False, **kwargs)`

n-th coefficient participating in the Fourier-expanded Green's function solution of the CRE transport equation

$$s_n = h_n \times X_n$$

Parameters

- **n** – order of the halo/bulge factor
- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²

- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s
- **manual** = 'False'

Parameters

- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)
- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the *diffsph.profiles.templates.hdz()* profile
- **beta** – exponent β in the *diffsph.profiles.templates.hdz()* profile
- **gamma** – exponent γ in the *diffsph.profiles.templates.hdz()* profile
- **alphaE** – parameter α_E in the *diffsph.profiles.templates.enst()* profile
- **rc** – core radius parameter r_c in the *diffsph.profiles.templates.cnfw()* profile
- **sigmav** – velocity dispersion parameter σ_v in the *diffsph.profiles.templates.sis()* profile

Returns

n-th coefficient in the *which_N* function

```
diffsph.pyflux.synch_TB(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28, delta='kol', B=2,
                         manual=False, high_res=False, accuracy=1, **kwargs)
```

Model-specific brightness temperature from synchrotron radiation

Parameters

- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')

- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **manual** (*bool*) – manual input of parameter values in `rad_temp` (default value = 'False')
- **high_res** (*bool*) – spatial resolution. If 'True', `synch_emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- `hyp = 'wimp'` (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm^{-3}/s (default value = $3 \times 10^{-26} \text{ cm}^{-3}/\text{s}$)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- `hyp = 'decay'`

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- `hyp = 'generic'`

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s
- `manual = 'False'`

Parameters

- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)
- `manual = 'True'`

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile

- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Brightness temperature in mK

```
diffsph.pyflux.synch_TB_approx(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28, delta='kol',  
B=2, regime='B', manual=False, **kwargs)
```

Model-specific brightness temperature in the Regime “A”, “B” or “C” approximations

Parameters

- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy (str)** – name of the galaxy
- **rad_temp (str)** – radial template ('NFW', 'Einasto', etc.)
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta (float, str)** – power-law exponent of the diffusion coefficient as a function of the CRE’s energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field’s smooth component in μ G (default value = 2μ G)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual (bool)** – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
 - **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
 - **mchi** – mass of the DM particle in GeV/c²
 - **channel (str)** – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
 - **mchi** – mass of the DM particle in GeV/c²
 - **channel (str)** – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s
- **manual** = 'False'

Parameters

- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)
- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Brightness temperature in mK

```
diffsph.pyflux.synch_brightness(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28, delta='kol',  
B=2, manual=False, high_res=False, accuracy=1, **kwargs)
```

Model-specific brightness from synchrotron radiation

Parameters

- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy** (str) – name of the galaxy
- **rad_temp** (str) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (str) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta** (float, str) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **manual** (bool) – manual input of parameter values in rad_temp (default value = 'False')

- **high_res** (*bool*) – spatial resolution. If 'True', `synch emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- `hyp = 'wimp'` (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm^3/s (default value = $3 \times 10^{-26} \text{ cm}^3/\text{s}$)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- `hyp = 'decay'`

Parameters

- **width** – decay width of the DM particle in $1/\text{s}$
- **mchi** – mass of the DM particle in GeV/c^2
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- `hyp = 'generic'`

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in $1/\text{s}$

- `manual = 'False'`

Parameters

`ref` – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- `manual = 'True'`

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm^3
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Brightness in Jy/sr

Return type

float

```
diffsph.pyflux.synch_brightness_approx(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28,
                                         delta='kol', B=2, regime='B', manual=False, **kwargs)
```

Model-specific brightness from synchrotron radiation in the Regime “A”, “B” or “C” approximations

Parameters

- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy (str)** – name of the galaxy
- **rad_temp (str)** – radial template ('NFW', 'Einasto', etc.)
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta (float, str)** – power-law exponent of the diffusion coefficient as a function of the CRE’s energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field’s smooth component in μ G (default value = 2μ G)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual (bool)** – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **hyp = 'wimp'** (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel (str)** – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp = 'decay'**

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²
- **channel (str)** – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp = 'generic'**

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
 - **rate** – CRE production rate in 1/s
- **manual** = 'False'
- Parameters**
- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)
- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Brightness in Jy/sr

```
diffsph.pyflux.synch_emissivity(r, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28, delta='kol',  
B=2, manual=False, high_res=False, accuracy=1, **kwargs)
```

Model-specific emissivity from synchrotron radiation

Parameters

- **r** – galactocentric distance in kpc
- **nu** – frequency in GHz
- **galaxy** (str) – name of the galaxy
- **rad_temp** (str) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (str) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- **delta** (float, str) – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- **manual** (bool) – manual input of parameter values in rad_temp (default value = 'False')
- **high_res** (bool) – spatial resolution. If 'True', `synch_emissivity()` computes as many terms as needed in order to converge at $r = 0$ (default value = 'False')

- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (str) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (str) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s
- **manual** = 'False'

Parameters

- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)
- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Emissivity in erg/cm³ /Hz/s/sr

Return type

float

```
diffsph.pyflux.synch_emissivity_approx(r, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28,
                                         delta='kol', B=2, regime='B', manual=False, **kwargs)
```

Model-specific emissivity from synchrotron radiation in the Regime “A”, “B” or “C” approximations

Parameters

- **r** – galactocentric distance in kpc
- **nu** – frequency in GHz
- **galaxy** (*str*) – name of the galaxy
- **rad_temp** (*str*) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (*str*) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm² /s)
- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE’s energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field’s smooth component in μ G (default value = 2μ G)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³ /s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s

- `manual = 'False'`

Parameters

`ref` – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- `manual = 'True'`

Parameters

- `rs` – scale radius in kpc
- `rhos` – characteristic density in GeV/cm³
- `alpha` – exponent α in the `diffsph.profiles.templates.hdz()` profile
- `beta` – exponent β in the `diffsph.profiles.templates.hdz()` profile
- `gamma` – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- `alphaE` – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- `rc` – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- `sigmav` – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Emissivity in erg/cm³ /Hz/s/sr

```
diffsph.pyflux.synch_flux_density(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28,
                                    delta='kol', B=2, manual=False, high_res=False, accuracy=1,
                                    **kwargs)
```

Model-specific flux density from synchrotron radiation

Parameters

- `theta` – angular radius in arcmin
- `nu` – frequency in GHz
- `galaxy (str)` – name of the galaxy
- `rad_temp (str)` – radial template ('NFW', 'Einasto', etc.)
- `hyp (str)` – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- `ratio` – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- `D0` – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm²/s)
- `delta (float, str)` – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')
- `B` – magnitude of the magnetic field's smooth component in μ G (default value = 2μ G)
- `manual (bool)` – manual input of parameter values in rad_temp (default value = 'False')
- `high_res (bool)` – spatial resolution. If 'True', `synch_emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- `accuracy` – theoretical accuracy in % (default value = 1%)

Keyword arguments

- `hyp = 'wimp'` (default)

Parameters

- `sv` – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
- `self_conjugate` – if set 'True' (default value) the DM particle is its own antiparticle
- `mchi` – mass of the DM particle in GeV/c²
- `channel(str)` – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- `hyp = 'decay'`

Parameters

- `width` – decay width of the DM particle in 1/s
- `mchi` – mass of the DM particle in GeV/c²
- `channel(str)` – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- `hyp = 'generic'`

Parameters

- `Gamma` – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- `rate` – CRE production rate in 1/s

- `manual = 'False'`

Parameters

`ref` – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- `manual = 'True'`

Parameters

- `rs` – scale radius in kpc
- `rhos` – characteristic density in GeV/cm³
- `alpha` – exponent α in the `diffsph.profiles.templates.hdz()` profile
- `beta` – exponent β in the `diffsph.profiles.templates.hdz()` profile
- `gamma` – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- `alphaE` – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- `rc` – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- `sigmav` – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Flux density in μJy

```
diffsph.pyflux.synch_flux_density_approx(theta, nu, galaxy, rad_temp, hyp='wimp', ratio=1, D0=3e+28,  
                                         delta='kol', B=2, regime='B', manual=False, **kwargs)
```

Model-specific flux density from synchrotron radiation in the Regime “A”, “B” or “C” approximations

Parameters

- **theta** – angular radius in arcmin
- **nu** – frequency in GHz
- **galaxy (str)** – name of the galaxy
- **rad_temp (str)** – radial template ('NFW', 'Einasto', etc.)
- **hyp (str)** – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm²/s (default value = 3×10^{28} cm² /s)
- **delta (float, str)** – power-law exponent of the diffusion coefficient as a function of the CRE’s energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field’s smooth component in μ G (default value = 2μ G)
- **regime** – regime of the approximation. Must be either upper or lower case a, b, c or I/II/III.
- **manual (bool)** – manual input of parameter values in rad_temp (default value = 'False')

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³ /s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel (str)** – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²
- **channel (str)** – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
 - **rate** – CRE production rate in 1/s
- **manual** = 'False'

Parameters

- **ref** – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- manual = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile
- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

Flux density in μJy

```
class diffsh.pyflux.transport(rh=None, B=None, D0=None, tau0=None, delta=None)
```

Bases: object

property D0**Dcoeff(E)**

Diffusion coefficient in cm^2/s

Parameters

- **E** – cosmic-ray energy in GeV
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3 or 'kol')

Returns

Diffusion coefficient for CRE with energy E (GeV) in cm^2/s

Elosses(E)

Total energy loss function in GeV/s

Parameters

- **E** – cosmic-ray energy in GeV
- **B** – magnitude of the magnetic field's smooth component in μG

Returns

energy-loss rate in GeV/s

Syrovatskii_var(E)

Syrovatskii variable in kpc^2

Parameters

- **E** – cosmic-ray energy in GeV

- **B** – magnitude of the magnetic field's smooth component in μG
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy (default value = 1/3)

Returns

Syrovatskii variable in kpc^2

eta_var(E)

η variable as a function of the CRE's energy, magnetic field, tau and delta parameters

Parameters

- **E** – CRE energy in GeV
- **B** – magnetic field strength in μG
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy

Returns

η variable

hatXne(E, E0)

CRE number-density function kernel in $\text{s}/\text{GeV } \hat{X}_n$

Parameters

- **E** – CRE energy in GeV
- **E0** – injected CRE's energy in GeV
- **B** – magnetic field strength in μG
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s
- **delta** – power-law exponent of the diffusion coefficient as a function of the CRE's energy

Returns

Electron number density kernel in s/GeV

property rh

property tau0

```
diffsph.pyflux.which_N(nu, galaxy, rad_temp, hyp, ratio, D0, delta, B, manual=False, high_res=False,
accuracy=1, **kwargs)
```

Determines at which order should the Fourier-expanded Green's function solution be truncated and stores the associated $s_n = h_n \times X_n$ coefficients as an array in the /cache folder

Parameters

- **nu** – frequency in GHz
- **galaxy** (str) – name of the galaxy
- **rad_temp** (str) – radial template ('NFW', 'Einasto', etc.)
- **hyp** (str) – hypothesis: 'wimp' (**default**), 'decay' or 'generic'
- **ratio** – ratio between the diffusion halo/bulge and half-light radii (default value = 1)
- **D0** – magnitude of the diffusion coefficient for a 1 GeV CRE in cm^2/s (default value = $3 \times 10^{28} \text{ cm}^2/\text{s}$)

- **delta** (*float, str*) – power-law exponent of the diffusion coefficient as a function of the CRE’s energy (default value = 1/3 or 'kol')
- **B** – magnitude of the magnetic field’s smooth component in μ G (default value = 2μ G)
- **manual** (*bool*) – manual input of parameter values in rad_temp (default value = 'False')
- **high_res** (*bool*) – spatial resolution. If 'True', `synch_emissivity()` computes as many terms as needed in order to converge at $r = 0$. (default value = 'False')
- **accuracy** – theoretical accuracy in % (default value = 1%)

Keyword arguments

- **hyp** = 'wimp' (default)

Parameters

- **sv** – annihilation rate (annihilation cross section times relative velocity) σv in cm³/s (default value = 3×10^{-26} cm³/s)
- **self_conjugate** – if set 'True' (default value) the DM particle is its own antiparticle
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (*str*) – annihilation channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.
- **hyp** = 'decay'

Parameters

- **width** – decay width of the DM particle in 1/s
- **mchi** – mass of the DM particle in GeV/c²
- **channel** (*str*) – decay channel: $b\bar{b}$ ('bb'), $\mu^+\mu^-$ ('mumu'), W^+W^- ('WW'), etc.

- **hyp** = 'generic'

Parameters

- **Gamma** – power-law exponent of the generic CRE source ($1.1 < \Gamma < 3$)
- **rate** – CRE production rate in 1/s

- **manual** = 'False'

Parameters

ref – reference used ('Martinez' or '1309.2641', 'Geringer-Sameth' or '1408.0002', etc.)

- **manual** = 'True'

Parameters

- **rs** – scale radius in kpc
- **rhos** – characteristic density in GeV/cm³
- **alpha** – exponent α in the `diffsph.profiles.templates.hdz()` profile
- **beta** – exponent β in the `diffsph.profiles.templates.hdz()` profile
- **gamma** – exponent γ in the `diffsph.profiles.templates.hdz()` profile

- **alphaE** – parameter α_E in the `diffsph.profiles.templates.enst()` profile
- **rc** – core radius parameter r_c in the `diffsph.profiles.templates.cnfw()` profile
- **sigmav** – velocity dispersion parameter σ_v in the `diffsph.profiles.templates.sis()` profile

Returns

series truncation order N

1.1.5 Module contents

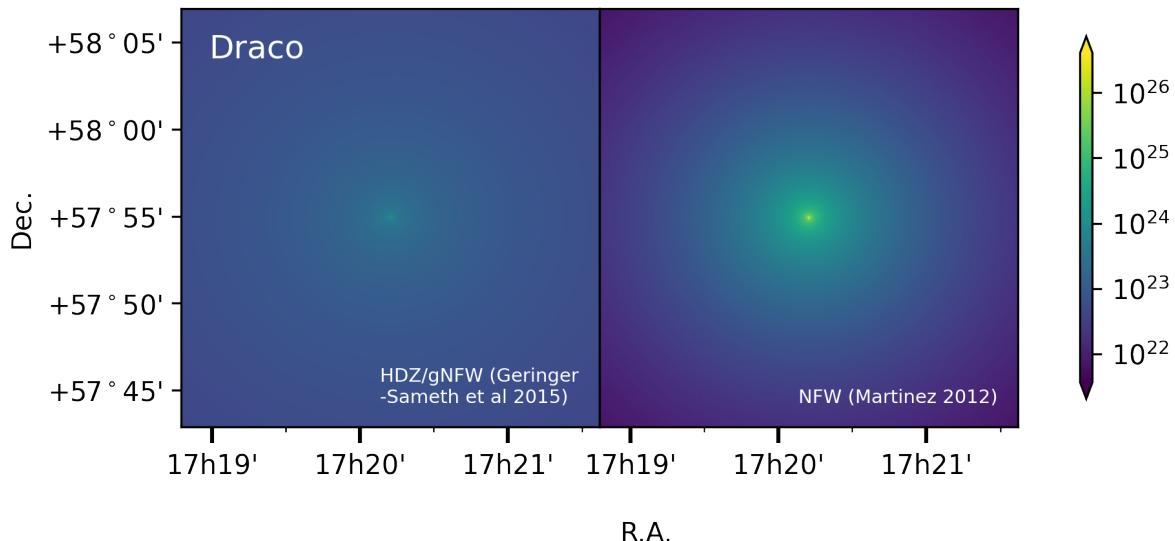
INDICES AND TABLES

- genindex
- modindex
- search

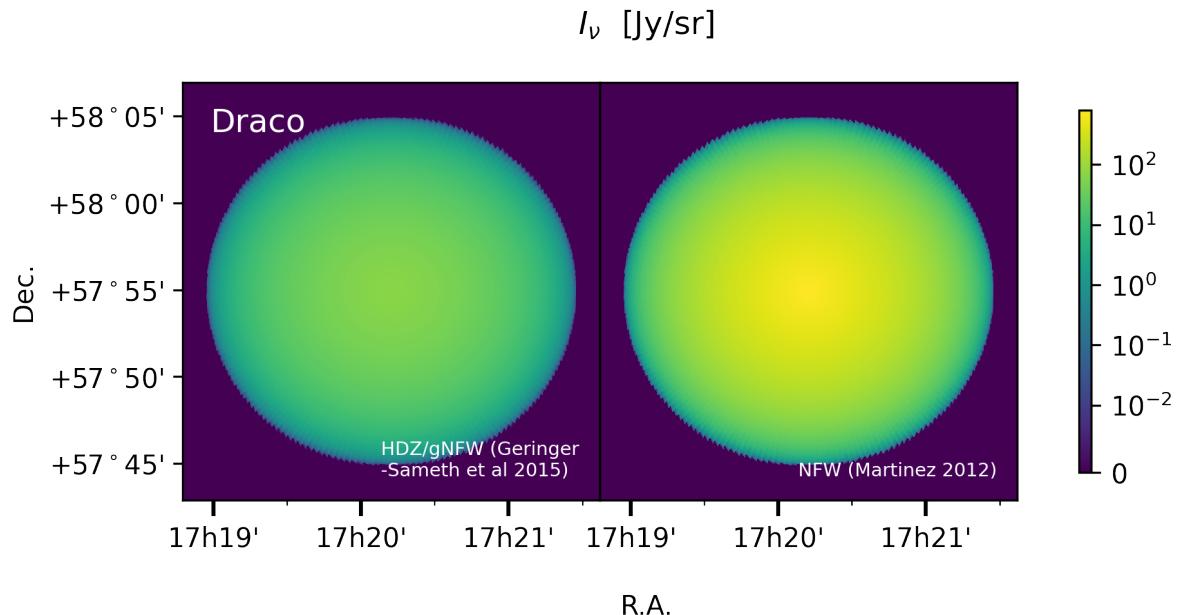
`diffsph` is a Python package that computes diffuse fluxes from Milky-Way satellite dwarf spheroidal (*dSph*) galaxies. It allows users to obtain

- J factor maps (relevant for gamma-ray astronomy)

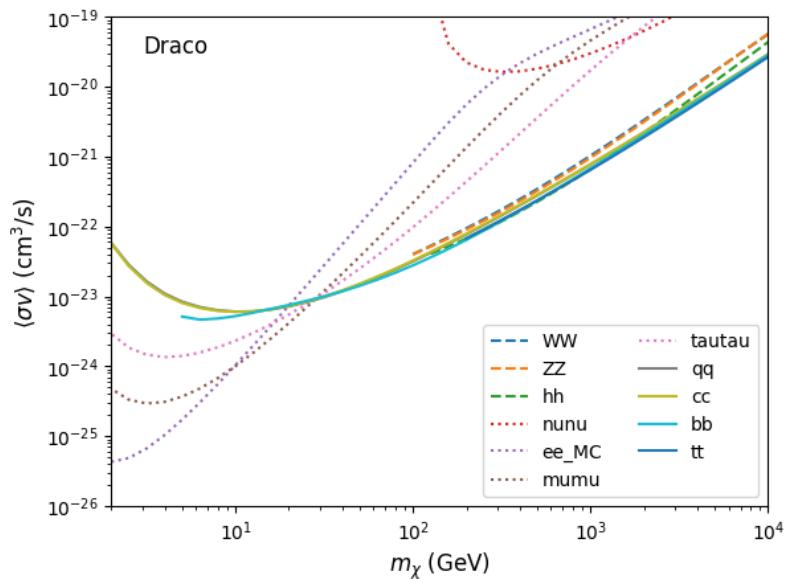
$$dJ/d\Omega \text{ [GeV}^2 \text{ cm}^{-5} \text{ sr}^{-1}\text{]}$$



- (radio frequency) synchrotron-radiation emission profiles



- bounds on e.~g. Dark Matter annihilation cross sections from radio astronomical observations



**CHAPTER
THREE**

INSTALLATION

Use Git or checkout with SVN using the web URL <https://github.com/mertio1/diffsph.git> , e. g.:

```
git clone https://github.com/mertio1/diffsph.git
```

or:

```
svn co https://github.com/mertio1/diffsph.git
```

Otherwise download the zip file from the repository <https://github.com/mertio1/diffsph>

For global installations, while in the `diffsph`'s main folder type:

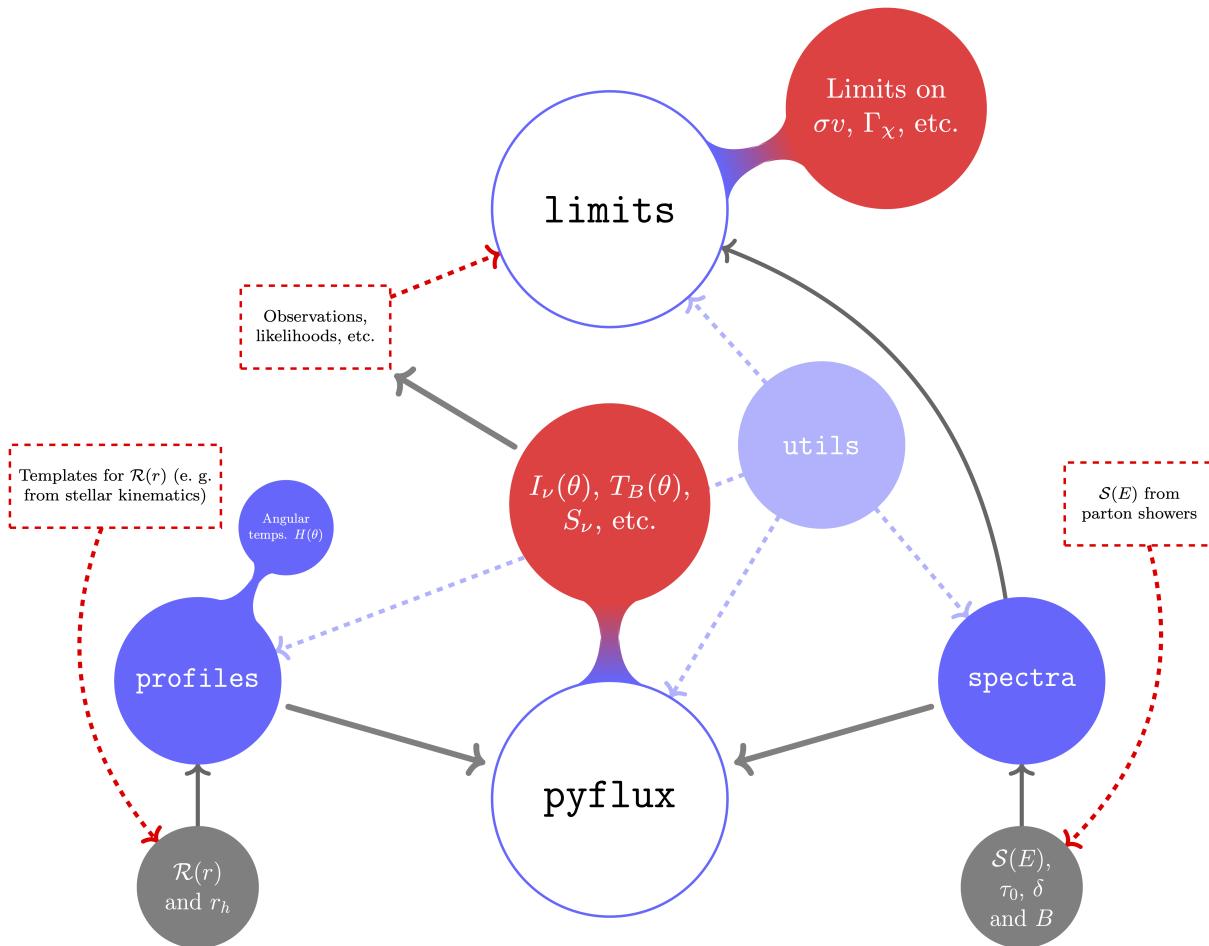
```
python setup.py bdist_wheel
```

and:

```
pip install .
```


ARCHITECTURE

The main functionalities and algorithmic structure of the code are captured by the diagram below



Users can both compute diffuse emission *fluxes* with the `pyflux` (`diffsph.pyflux`) module and 2σ *limits* on e. g. annihilation cross sections or decay rates of dark matter particles by using the `limits` (`diffsph.limits`) module. Details about the methods used to perform these computations are given in Ref.¹.

¹ M. Vollmann, “Universal profiles for radio searches of dark matter in dwarf galaxies”, doi:10.1088/1475-7516/2021/04/068 [arXiv:2011.11947 [astro-ph.HE]].

EXAMPLES

5.1 pyflux module

In order to get familiar with the code, use the following set of commands to generate the figure below:

```
from diffsth import pyflux as pf
import matplotlib.pyplot as plt
%matplotlib inline

# Angle grid in arcmin

theta_grid = [15 * i / 50 for i in range(0, 50)]

# List of satellite galaxies

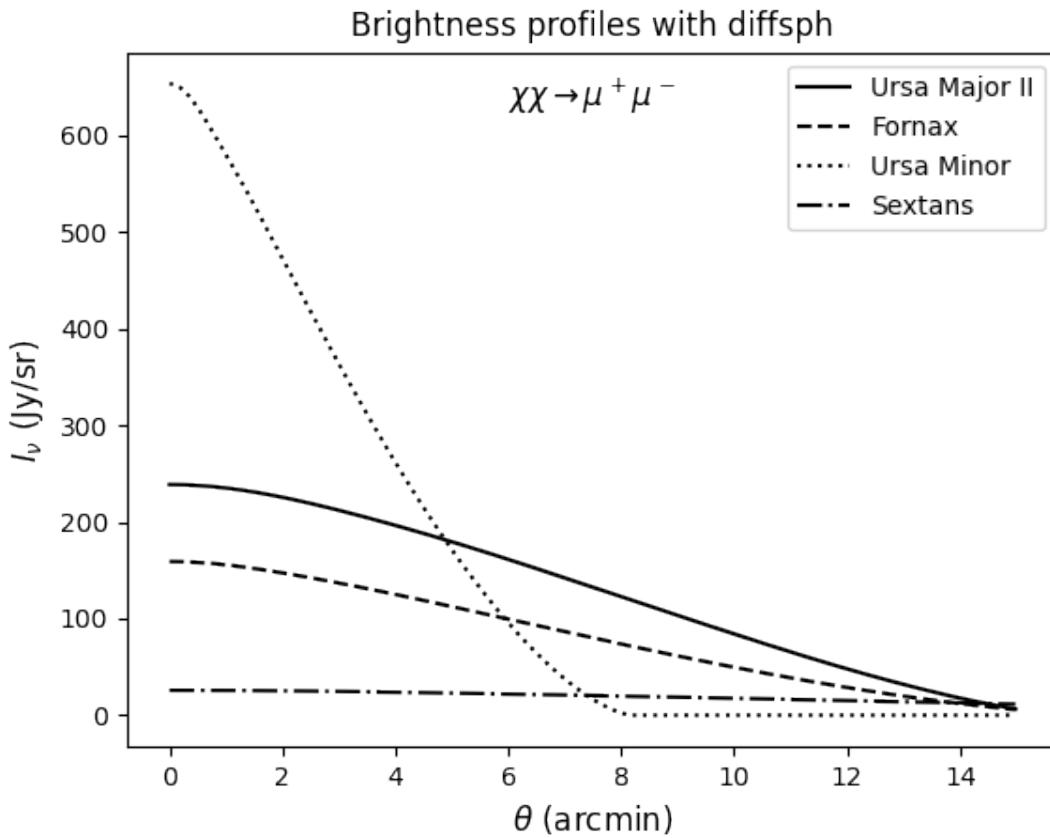
dsph_list = ['Ursa Major II', 'Fornax', 'Ursa Minor', 'Sextans']

# diffsth's computations at nu = 150 MHz and for the given model

Inu = [[pf.synch_brightness(th, nu = .150, galaxy = gal, rad_temp = 'HDZ',
                           hyp = 'wimp', ref = '1408.0002', sv = 3e-26,
                           mchi = 10, channel = 'mumu', high_res = True,
                           accuracy = .1)
        for th in theta_grid]
       for gal in dsph_list]

# Plots

plt.plot(theta_grid, Inu[0], "k", label = dsph_list[0])
plt.plot(theta_grid, Inu[1], "--k", label = dsph_list[1])
plt.plot(theta_grid, Inu[2], ":k", label = dsph_list[2])
plt.plot(theta_grid, Inu[3], "-.k", label = dsph_list[3])
plt.legend()
plt.xlabel('$\theta$ (arcmin)', size = 'large');
plt.ylabel('$I_\nu$ (Jy/sr)', size = 'large');
plt.title('Brightness profiles with diffsth');
plt.text(7.5, 630, '$\chi\chi \rightarrow \mu^+\mu^-$', horizontalalignment = 'center', size = 'large');
```



5.2 limits module

The following example shows how to obtain limits on the decay rate of dark matter particles using non-detection (noise level) in the field of Draco. It can take just a few minutes to compute them all in a modern laptop:

```
from diffsp import limits as lims
import matplotlib.pyplot as plt
%matplotlib inline

# DM mass grid in GeV
mass_grid = [10 ** (5 * i / 50) for i in range(0, 50)]

# List of decay channels
ch_list = ['WW', 'ZZ', 'hh', 'nunu', 'ee_MC', 'mumu', 'tautau', 'qq', 'cc', 'bb', 'tt']

# diffsp's computations at nu = 150 MHz and for the given image

rates = [[lims.decay_rate_limest(nu = .15, rms_noise = 100, beam_size = 20,
                                 galaxy = 'Draco', rad_temp = 'HDZ', mchi = mch,
                                 channel = ch, high_res = True, accuracy = .1,
```

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```

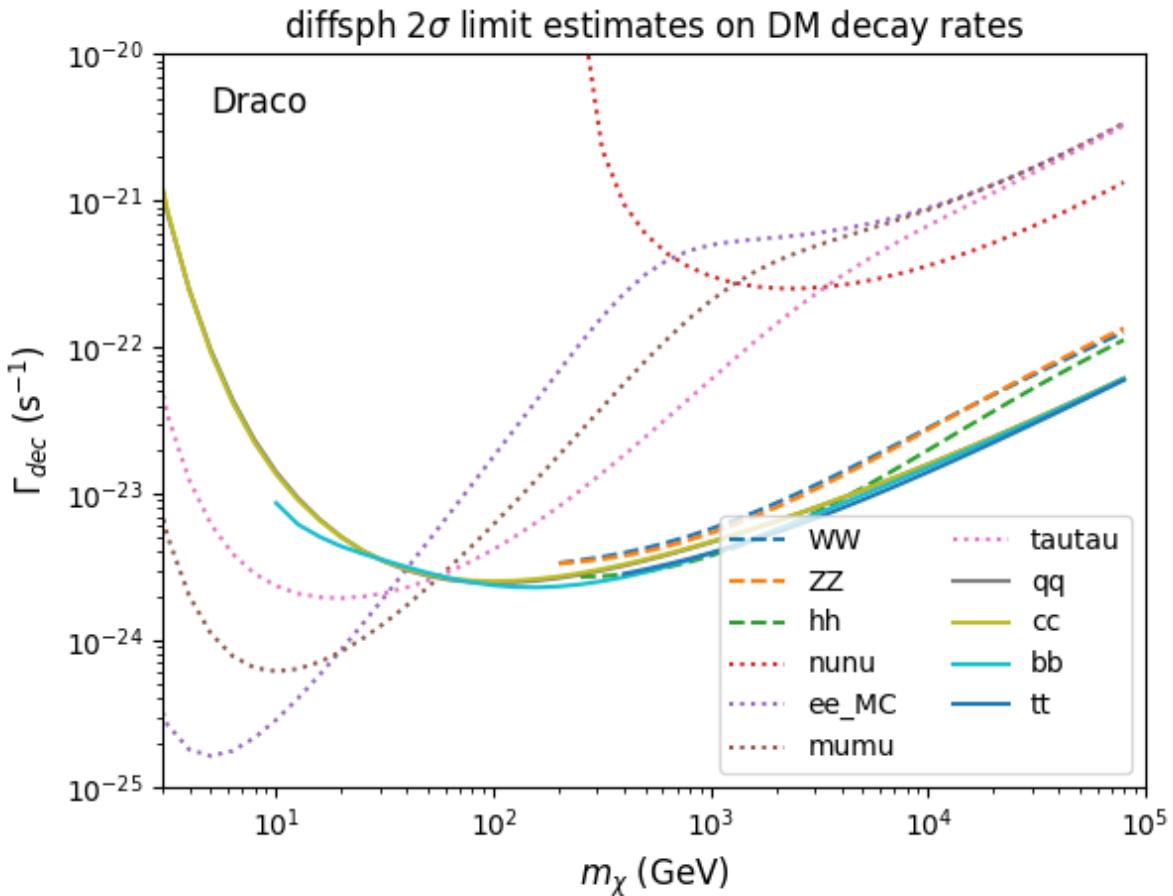
ref = '1408.0002')

for mch in mass_grid]
for ch in ch_list]

# Plots

[plt.loglog(mass_grid, rates[i], label = ch_list[i], ls = '--') for i in range(0, 3)]
[plt.loglog(mass_grid, rates[i], label = ch_list[i], ls = ':') for i in range(3, 7)]
[plt.loglog(mass_grid, rates[i], label = ch_list[i]) for i in range(7, len(ch_list))]
plt.ylim([1e-25, 1e-20]);
plt.xlim([3, 1e5]);
plt.legend(loc = 'lower right', ncols = 2)
plt.xlabel('$m_\chi$ (GeV)', size = 'large');
plt.ylabel('$\Gamma_{dec}$ ($s^{-1}$)', size = 'large');
plt.title('diffsph 2$\sigma$ limit estimates on DM decay rates');
plt.text(5, 4e-21, 'Draco', size = 'large');

```



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