# Premise Order Matters in Reasoning with Large Language Models

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# Abstract

Large language models (LLMs) have accomplished remarkable reasoning performance in various domains. However, in the domain of reasoning tasks, we discover a frailty: LLMs are surprisingly brittle to the ordering of the premises, despite the fact that such ordering does not alter the underlying task. In particular, we observe that LLMs achieve the best performance when the premise order aligns with the context required in intermediate reasoning steps. For example, in deductive reasoning tasks, presenting the premises in the same order as the ground-truth proof in the prompt (as opposed to random ordering) drastically increases the model's accuracy. We first examine the effect of premise ordering on deductive reasoning on a variety of LLMs, and our evaluation shows that even if the model performance is decent on the optimal order, permuting the premise order can cause a performance drop of over 30%. In addition, we release the benchmark R-GSM, based on GSM8K, to examine the ordering effect for mathematical problem-solving, and we again observe a significant drop in accuracy, relative to the original GSM8K benchmark.

# 1. Introduction

Large language models (LLMs) have demonstrated impressive performance across a variety of reasoning tasks (Wei et al., 2022; Cobbe et al., 2021; Hendrycks et al., 2021; Chen et al., 2021; Austin et al., 2021). In particular, recent state-of-the-art LLMs have reached or even surpassed human performance on multiple reasoning benchmarks, including STEM problem-solving and code generation (Bubeck et al., 2023; Gemini, 2023; Li et al., 2022). However, recent works show that LLMs exhibit failure modes that align with human-like cognitive biases (Berglund et al., 2023; Shi et al., 2023; Hagendorff et al., 2023; Jones & Steinhardt, 2022; McCoy et al., 2023). For example, Berglund et al. (2023) revealed the *Reversal Curse*; i.e., LLMs trained on "A is B" tend to fail to infer that "B is A." Distractibility is another failure mode (Shi et al., 2023; Jones & Steinhardt, 2022), in which LLM performance drastically decreases when irrelevant context is included in the task description.

In this work, we investigate the effect that premise order has on LLM reasoning. Specifically, in deductive reasoning, changing the order of premises alone does not change the conclusion. Consider the following illustrative example:

- 1. If A then B.
- 2. If B then C.
- 3. A is True.

We can derive that C is True regardless of the order of these 3 premises. While some studies show that humans have a preference on the premise order to facilitate their reasoning (Dekeyser et al., 2000; Girotto et al., 1997), the premise order does not drastically affect human performance, especially for problems that only involve *modus ponens* (if P then Q; P; therefore Q), which are relatively straightforward for humans.

In contrast to humans, we observe that for LLMs, the premise order has a significant impact on reasoning performance. In particular, LLMs reach the best performance when the premises are arranged **in the same order** as they appear in the ground-truth proof. Taking the illustrative problem above as an example, we observe two phenomena:

- 1. Presenting "If A then B" before "If B then C" in the prompt generally achieves a higher accuracy compared to the reverse order.
- 2. The performance gap is more significant when the number of premises increases.

Intuitively, such a preference on the premise order aligns with human preference (Dekeyser et al., 2000) because in the preferred order, each derivation step can be done on-thefly while looking at premises one by one, without needing to look back and forth across all premises at each step.

We conduct a systematic study on the premise order effect using a variety of LLMs, including GPT-4-turbo, GPT-3.5-

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#### × Shuffled → incorrect **✓ Sorted** → correct Rules: If duve, then dax. If kere and riff, then Rules: If nup, then hepe. If kere and riff, then ss. If feg and tess, then rabe. If wozz, then tess. If feg and tess, then rabe. If wozz, then riff. If rabe, then thoxe. If ag and riff and kere, riff. If tess and vepe, then nup.If ag and riff then hepe. If thoxe, then vepe. If nife and hume and ag, then dax. If feg and thoxe, then and kere, then hepe. If feg and thoxe, then ire. If nife and hume and ag, then dax. If ire and ire. If rebe and ene and heff, then kone. If ire dax, then wope. If rebe and ene and heff, then and dax, then wope. If tess and vepe, then nup. If rabe and vide and nife, then ag. If nup and rabe, then thoxe. If rabe and vide and nife, ag and vide, then duve. If zeck and hepe and dax, then riff. If nup, then hepe. If sene, then then ag. If fum, then wozz. If zeck and hepe and dax, then riff. If kere and wope, then fum. If sene, then hume. If thoxe, then vepe. If fum, hume. If hepe and tess and ag, then kere. If fum, then vide. If kere and wope, then fum. If then vide. If duve, then dax. If jag and kone, jag and kone, then thoxe. If fum, then wozz. then thoxe. If nup and ag and vide, then duve. Facts: Alice is cote. Alice is kone. Alice is duve. Facts: Alice is cote. Alice is kone. Alice is duve. Alice is ag. Alice is jag. Alice is tess. Alice is riff. Alice is feg. Alice is vide. Alice is riff. Alice is feq. Alice is vide. **Query:** Is Alice wozz? In each step, indicate Query: Is Alice wozz? In each step, indicate whether you are using a fact, or a rule. whether you are using a fact, or a rule. ... we haven't established a clear path to "fum" ... since Alice is fum, by the rule "If fum, then wozz," Alice is wozz. Therefore, based on the based on the given facts and rules... based on given facts and the application of the rules, the provided facts and the logical steps followed, Alice is indeed wozz. we cannot conclude that Alice is wozz.

Figure 1. Premise order affects the reasoning performance: a failure case for logical reasoning. Left: rules are sorted in the same order as the ground-truth proof (forward order with  $\tau = 1$  as defined in Section 2.1). Right: the wrong prediction with GPT-4-turbo after shuffling the rule set ( $\tau = 0$ ). Distracting rules are bold and in light blue.

turbo (OpenAI, 2023), PaLM 2-L (Google, 2023), and Gemini 1.0 Pro (Gemini, 2023). Our primary focus is deductive reasoning, and we benchmark all LLMs on problems that only involve *modus ponens* (if P then Q; P; therefore Q), where all LLMs in our evaluation at least achieve decent performance with a small number of premises. We show that the accuracy decrease caused by different ordering can be more than 30%. The ordering effect is further amplified when irrelevant premises (i.e., premises that are not needed to derive a conclusion) are presented in the prompt. Figure 1 illustrates a failure case, where all LLMs fail to generate the proof after changing the order of relevant rules. Interestingly, while all LLMs perform best when the premise order follows the ground-truth proof, they reveal different preferences on other alternative orderings. Specifically, compared to randomly ordering the premises, GPT-4-turbo and GPT-3.5-turbo generally achieve better performance when the premise order is exactly the reverse of the ground-truth proof. On the other hand, PaLM 2-L generally achieves the worst performance with such a reversed order.

Besides logical reasoning, we construct R-GSM to further investigate the ordering effect on mathematical reasoning. Specifically, we build R-GSM on top of a subset of the GSM8K benchmark (Cobbe et al., 2021), where we change the order of sentences in the problem description and manually verify that the ground-truth answer remains the same. Despite the fact that multiple LLMs have achieved very high accuracies on the original GSM8K benchmark, our experiments again show that even on such relatively simple reasoning problems, changing the premise order could still cause a notable performance drop for all LLMs, especially on longer problems that require more reasoning steps.

Our evaluation highlights that even in reasoning domains where the premise order **does not matter**, premise order **does matter in LLM reasoning**. In particular, starting from tasks where LLMs achieve decent performance with the forward order, the performance can significantly degrade with alternative premise orderings. The premise ordering effect indicates that LLMs are more comfortable reasoning via reading left-to-right instead of back-and-forth, which can be attributed to the auto-regressive model design or the reasoning bias learned from the training corpus. We leave proposing new training and modeling techniques to mitigate the premise order effect as future work.

#### 2. Benchmarks

#### 2.1. Logical Reasoning

Prior work has revealed the weaknesses of LLMs in logical reasoning (Han et al., 2022; Xu et al., 2023; Saparov



*Figure 2.* R-GSM example where the original problem can be correctly solved by all LLMs in our evaluation, but all of them failed on the reordered one. Different calculation steps and their corresponding problem statements are annotated in light blue. Specifically, the reasoning steps of the original problem follows the ordering of problem statements, while the reordered problem does not.

et al., 2023; Saparov & He, 2022; Wan et al., 2024), especially when the proof is long and requires the knowledge of multiple deduction theorems. To isolate the effect of premise orders, we focus on a confined problem space adapted from SimpleLogic (Zhang et al., 2022), which only includes propositional logic problems with definite clauses. Specifically, each problem includes: (1) a set of facts  $A_1, \ldots$ ,  $A_n$  that hold true; (2) a set of rules of the form "If X, then Y", "If  $X_0$  and  $X_1$ , then Y", or "If  $X_0$  and  $X_1$  and  $X_2$ , then Y"; and (3) a conclusion "C is True" to be proved. As opposed to SimpleLogic — which formulates the problem as a binary classification task (i.e., indicate whether the conclusion is True or False) — in our benchmark, every problem has a ground-truth label of True, and we consider the prediction to be correct only when the generated proof is completely valid. With these strict criteria, the LLM is required to produce the step-by-step deduction that leads to the conclusion, and any hallucination of nonexistent facts and rules is considered erroneous. In addition, differently from SimpleLogic, which uses English words as predicates (e.g., an example rule is "If Alice is fast and smart, then Alice is bad"), all predicates are randomly generated pseudowords in our benchmark. This design choice is motivated by our observation that when presented with rules of randomly selected English words, LLMs often question the validity of various rules and tend not to generate a proof. Using pseudowords eliminates this issue; additionally, this design also forces the LLM to generate the proof solely based on the problem statement, without relying on its internal knowledge.

The key characteristic of our benchmark is that for each logical reasoning problem, we synthetically generate variants with different premise orders. Specifically, we denote the order that conforms to the ground-truth proof with forward chaining as the *forward* order, where the rule applied in each derivation step is sequentially presented in the problem description. Intuitively, presenting premises in the forward order simplifies the problem for humans, as this allows us to write the proof on-the-fly while reading the premises. Conversely, a premise ordering that is more random increases the task difficulty, since carrying out the derivation requires us to repetitively look for premises for each reasoning step. Motivated by this intuition, we categorize different premise orders based on their Kendall tau distance  $\tau$  (Cicirello, 2019; Sen, 1968) to the forward order, normalized into the range [-1, 1]. Specifically,  $\tau = 1$  is the *forward* order, and we denote the order with  $\tau = -1$  as the *backward* order, which is the reverse of the forward order and aligns with the proof via backward chaining.  $\tau \approx 0$  suggests that there is no strong correlation between the premise order in the problem description and the proof. To thoroughly investigate the LLM preference on different premise orders, we evaluate the model performance on  $\tau = 0.5, 0$  and -0.5, in addition

to the forward ( $\tau = 1$ ) and backward ( $\tau = -1$ ) orders. We present examples with  $\tau = 1$  and 0 in Figure 1, and defer examples with other  $\tau$  values to Figure 11 in Appendix B.

We measure the premise order effect by varying the following two factors:

- Number of rules required in the proof. It is expected that the premise order effect is more significant for a proof with more rules. For our benchmark, we generate problems whose numbers of rules in the proof range from 4 to 12.
- Number of distracting rules (i.e., rules that are not useful for the proof) presented in the problem. The presence of distracting rules also complicates the problem, as premise selection itself is challenging (Wang et al., 2017; Ferreira & Freitas, 2020; Irving et al., 2016), and LLMs are shown to be easily distracted by irrelevant context (Shi et al., 2023). We include problem variants with 0, 5 and 10 distracting rules.

We generate 200 problems for each number of required rules. Considering different premise orders and numbers of distracting rules, each problem includes 15 variants, resulting in a total of 27K problems in our benchmark.

#### 2.2. R-GSM for Mathematical Reasoning

To further assess the effect of premise orders beyond logical reasoning, we construct the R-GSM dataset based on GSM8K (Cobbe et al., 2021), which is a popular benchmark of grade school math word problems. Specifically, we first select GSM8K test problems with at least 5 sentences in the problem description. Afterward, we filter out those problems where there is no alternative ordering that does not change the ground truth answer. An example of such problems is those with sentences that follow the causal order of an event series. For each of the remaining problem, we keep the last sentence untouched and rewrite the problem description with a different ordering of other sentences. Minor editing on words is allowed to ensure the grammatical correctness of the problem description. To facilitate the annotation process, for each problem, we write a simple function to enumerate all alternative orderings of problem statements until an ordering that causes the LLM prediction failure is discovered. Such enumeration is able to find failure cases on more than 70% problems for GPT-4-turbo and PaLM 2-L. However, as opposed to logical reasoning tasks, simply shuffling sentences in GSM8K problems often results in different ground truth answers or renders the problem invalid. Therefore, a manual rewriting process is done to ensure that the rewritten problems preserve the same ground truth answer and are grammatically correct. In total, our R-GSM benchmark contains 220 pairs of problems, including both the original GSM8K problem description and the manually rewritten one with a different ordering of problem statements.

Despite that over 60% of problems in R-GSM only have 5 sentences, and all problems have at most 8 sentences and less than 200 tokens, our evaluation shows that all LLMs still perform considerably worse on rewritten problems. Figure 2 presents an example in R-GSM where all LLMs correctly solve the original problem but not the rewritten one. Specifically, the reasoning steps for the original problem follows the ordering of problem statements, while for the rewritten problem, the second calculation step in the correct solution should refer to the second-to-last sentence instead of the second sentence in the problem description. We provide a more detailed case study in Section 3.3, and present the full dataset statistics in Appendix A.

#### **3. Experiments**

#### 3.1. Experimental Setup

We evaluate the premise ordering effect on GPT-4-turbo, GPT-3.5-turbo, PaLM 2-L and Gemini 1.0 Pro. We perform the greedy decoding with the temperature 0, and apply the zero-shot prompting in all experiments unless otherwise specified. On R-GSM, the model input only contains the problem description without additional instructions. For logical reasoning, as shown in Figure 1, we add an instruction in the prompt to ask for a derivation that specifies which premise is used in each step.

#### 3.2. Logical Reasoning

Figure 3 presents the results with different numbers of relevant rules included in ground-truth proofs, where the problem does not contain distracting rules, and the shuffled accuracy is the aggregation of results with  $\tau = 0.5$ , 0, and -0.5. Across different LLMs, the forward order consistently achieves the best performance, which aligns with the human preference. The performance drop caused by alternative orderings becomes more significant when the number of rules increases. Meanwhile, models with weaker reasoning capabilities are also more sensitive to different premise orders. Specifically, while the accuracy decrease of GPT-4-turbo and PaLM 2-L is up to 20 - 30%, with Gemini 1.0 Pro and GPT-3.5-turbo, changing the premise order from the forward order can degrade the accuracy from over 65% to below 25%, with an accuracy decrease of more than 40%.

**Breakdown on different premise orders.** We present the results of fine-grained breakdown on premise ordering in Figure 5, where the orders are categorized based on Kendall tau distance  $\tau$  as described in Section 2.1. Interestingly, while the top preference of all LLMs is the forward order, their preferences on other orders are not alike. Specifically,



Figure 3. Results on logical reasoning without distracting rules. See Table 7 in Appendix E for accuracy numbers.



Figure 4. Results on logical reasoning with distracting rules. See Tables 8 and 9 in Appendix E for accuracy numbers.



Figure 5. Fine-grained results on different  $\tau$  without distracting rules. See Table 10 in Appendix E for accuracy numbers.



Figure 6. Fine-grained results on different  $\tau$  with distracting rules. See Tables 11 and 12 in Appendix E for accuracy numbers.

GPT-4-turbo generally prefers the backward order over other orders, and the overall performance decreases with a smaller absolute value of  $\tau$ . This observation is also consistent with human reasoning patterns, as backward chaining is another well-established inference method. On the other hand, PaLM 2-L generally performs the worst with the backward order. With the decrease of  $\tau$  (i.e., the premise order deviates more from the forward order), the accuracy drops. The preferences of Gemini 1.0 Pro and GPT-3.5turbo are less consistent; still, they prefer the backward order more often than other non-forward premise orders.

Effect of distracting rules. We assess the effect of distracting rules of GPT-4-turbo and PaLM 2-L, which reach a decent performance without the presence of distracting rules. Figures 4 and 6 show that adding distracting rules further decreases the reasoning performance and magnifies the effect of different premise orders. Still, the overall preferences of both LLMs remain the same as the scenario without distracting rules. Specifically, both LLMs again achieve the best performance with the forward order, and GPT-4-turbo prefers the backward order over other non-forward orders, while PaLM 2-L performance decreases with a smaller  $\tau$ .

**Error analysis.** In Table 1, we present a breakdown on prediction errors across different premise orders. We consider the following error categories:

- 1. *wrong refutation*: the LLM wrongly claims that the conclusion can not be proved;
- 2. *rule hallucination*: the LLM generates rules that do not exist in the problem;
- 3. *fact hallucination*: the LLM generates facts that do not exist in the problem, or are not proved yet.

We observe that for all LLMs, fact hallucination is typically the most common error pattern, and this error type escalates dramatically with the decrease of  $\tau$ . The main reason is that LLMs are inclined to use the rules in the sequential order as they present in the problem, so when the next rule in the problem is not yet applicable, LLMs might still hallucinate facts to complete the proof step. Simultaneously, we observe that the percentage of wrong refutation is generally lower for  $\tau = -1$  than for  $|\tau| < 1$ . We present an example of wrong refutation in Figure 1, and we include more examples of rule and fact hallucination in Figure 10 of Appendix B.

#### 3.3. R-GSM for Mathematical Reasoning

Table 2 demonstrates the overall results on R-GSM. Again, all LLMs achieve a lower performance on R-GSM, as compared to GSM8K. Note that the original GSM8K problems are not necessarily written in the most preferable way, and thus sometimes the manual rewriting facilitates the reasoning and allows the model to correctly solve the reordered

	$\tau$	Correct	Wrong	Halluc	ination
			Refutation	Rule	Fact
	1	96.5%	0.5%	1.5%	1.5%
	0.5	76.0%	10.5%	2.0%	11.5%
GPT-4-turbo	0	82.0%	4.5%	3.5%	10.0%
	-0.5	84.5%	1.0%	4.5%	10.0%
	-1	84.0%	0.0%	3.5%	12.5%
	1	30.0%	24.5%	9.5%	35.5%
	0.5	1.0%	54.5%	9.5%	33.0%
GPT-3.5-turbo	0	0.5%	55.0%	7.5%	34.5%
	-0.5	2.0%	50.0%	8.5%	37.5%
	-1	1.5%	34.5%	14.5%	47.0%
	1	88.0%	0.5%	3.0%	8.5%
	0.5	74.5%	1.5%	9.5%	14.5%
PaLM 2-L	0	65.5%	2.0%	11.0%	21.5%
	-0.5	59.5%	1.5%	10.0%	29.0%
	-1	57.5%	1.0%	11.5%	30.0%
	1	16.5%	28.0%	5.0%	50.5%
	0.5	0.0%	59.0%	3.5%	37.5%
Gemini 1.0 Pro	0	0.0%	34.0%	9.0%	57.0%
	-0.5	0.5%	24.5%	9.5%	65.5%
	-1	0.5%	27.5%	11.5%	60.5%

*Table 1.* Breakdown on error types for logical reasoning with 12 relevant rules and no distracting rules.

	Init Acc	Reorder Acc
GPT-4-turbo	94.1%	85.0%
PaLM 2-L	86.4%	79.5%
Gemini 1.0 Pro	80.5%	69.1%
GPT-3.5-turbo	67.3%	51.8%

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	Init Acc	Reorder Acc
GPT-4-turbo	100%	89.9%
PaLM 2-L	100%	87.9%
Gemini 1.0 Pro	100%	74.6%
GPT-3.5-turbo	100%	64.9%

*Table 3.* For each model, the accuracies on the R-GSM subset where the original problems are correctly solved, thus the initial accuracy is 100% for all models.

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Figure 7. R-GSM results with different numbers of reasoning steps in the ground truth. See Table 13 in Appendix F for accuracy numbers.



Figure 8. R-GSM results with different problem lengths. See Table 14 in Appendix F for accuracy numbers.

	Temporal	Unknown	Others
GPT-4-turbo	45.0%	15.0%	40.0%
GPT-3.5-turbo	21.6%	19.6%	58.8%
PaLM 2-L	34.8%	4.3%	60.9%
Gemini 1.0 Pro	29.5%	18.2%	52.3%

*Table 4.* Error analysis on R-GSM. "Temporal" refers to the temporal order, and "Unknown" refers to the unknown variables.

version of a problem that it fails on the original one. Therefore, in Table 3, for each LLM, we also present the accuracy on those problems with their original descriptions solved by the model. We show that all LLMs fail on at least 10% of reordered problems that they are initially able to solve, and this performance degradation is more than 35% with GPT-3.5-turbo.

Given the performance degradation with zero-shot prompting, one potential mitigation is to apply few-shot chain-ofthought prompting and include demonstrations of solving reordered problems in the prompt. However, we observe that the few-shot results are mostly similar to or even worse than zero-shot ones. The only improvement we have seen is with GPT-3.5-turbo: using 5 exemplars of reordered problems annotated with ground truth solutions, the accuracy on original problems becomes 79.1%, and the accuracy on reordered problems becomes 66.4%. Despite the performance improvement, there is still a 13% accuracy drop after reordering. These results show that using few-shot demonstrations alone is insufficient for addressing the effect of premise orders.

**Breakdown of problem complexity.** Figures 7 and 8 present the breakdown results on different number of reasoning steps and different number of problem sentences, respectively. Unsurprisingly, across all LLMs, the proof accuracy suffers on problems that require more reasoning steps and contain a greater number of sentences. Overall, the gap between the accuracies on initial and rewritten problems is more significant with more reasoning steps and longer problems for both GPT-4-turbo and Gemini 1.0 Pro, while the gap remains similar across different numbers of reasoning steps and problem lengths for PaLM 2-L and GPT-3.5-turbo.

**Error analysis.** To further understand the failure modes, for each LLM, we analyze those error cases where the original problems can be correctly solved but not the reordered ones, and we categorize the common error types in Table 4. Similar to our observation in logical reasoning experiments, the prediction errors in R-GSM are primarily due to the LLMs blindly using numbers in the sequential order of their appearances in the problem. Specifically, the most common error case for all LLMs is their tendency to overlook temporal order. Figure 2 presents such an example, where the prediction failure is because some earlier events are described in the later part of the problem. Another category of errors occurs when some quantities are not specified while

<b>✓ Original →</b> correct	$\mathbf{X}$ Reordered $\rightarrow$ incorrect
Larry loves taking care of animals. He has 3 cats. He has 3 times as many dogs as cats. He has 2 fewer rabbits than dogs. He has a fish tank with three times the number of fish as rabbits. <b>He also has a collection of gerbils</b> <b>that's 1/3 the number of fish he has.</b> How many pets does Larry have?	Larry loves taking care of animals. He has 3 cats. He has 3 times as many dogs as cats. He has 2 fewer rabbits than dogs. <b>He also has a</b> <b>collection of gerbils that's 1/3 the number of</b> <b>fish he has.</b> He has a fish tank with three times the number of fish as rabbits. How many pets does Larry have?
Larry has 3 cats and 3 times as many dogs as cats so he has 3*3 = 9 dogs He has 2 fewer rabbits than dogs so he has 9-2 = 7 rabbits His fish tank has 3 times the number of rabbits so it has 3*7 = 21 fish His gerbil collection is 1/3 the number of fish	Larry has 3 cats and 3 times as many dogs as cats so he has 3*3 = 9 dogs He has 2 fewer rabbits than dogs so he has 9-2 = 7 rabbits He has 1/3 the number of gerbils as fish so he has 7/3 = 2 gerbils
<ul> <li>His gerbil collector is 1/3 the humber of hish</li> <li>he has so he has 21/3 =7 gerbils</li> <li>He has 3 cats, 9 dogs, 7 rabbits, 21 fish and</li> <li>7 gerbils for a total of 3+9+7+21+7 = 47</li> <li>pets. Answer: 47.</li> </ul>	He has 3 times the number of fish as rabbits so he has 3 * 7 = 21 fish All total he has 3 cats + 9 dogs + 7 rabbits + 2 gerbils + 21 fish = 42 pets. Answer: <b>42</b> .

*Figure 9.* R-GSM example where the original problem can be correctly solved by all LLMs, but GPT-3.5-Turbo fails on the reordered version while all the other LLMs still solve it correctly.

processing the problem in the sequential order, which introduces unknown variables for calculation. Take, for example, the problem in Figure 9. In the original problem, the number of each animal can be directly calculated based on its preceding sentence. However, in the reordered problem, the number of gerbils cannot directly be computed based on the preceding sentences, since the number of fish remains unknown up to that point, and the LLM must read the remaining sentences and calculate the number of fish first. However, the prediction from GPT-3.5-turbo instead uses the number calculated in the previous step (i.e., the number of rabbits) to calculate the number of gerbils, resulting in an error. Such a failure mode is less common with PaLM 2-L, but still constitutes a non-negligible proportion of prediction errors for the other LLMs. We present more examples of model predictions in Appendix C.

### 4. Related Work

Failure modes of LLMs. The premise order effect in this work is connected to several failure modes of LLMs in the literature, including the reversal curse (Berglund et al., 2023), distractibility (Shi et al., 2023), position bias (Liu et al., 2024; Wang et al., 2023), and limited capability of logical reasoning (Han et al., 2022; Xu et al., 2023; Saparov et al., 2023; Saparov & He, 2022; Wan et al., 2024; Zhu et al., 2023; Yan et al., 2023). Specifically, Shi et al. (2023)

show that including irrelevant context in the problem statement leads to a considerable performance drop on GSM8K and other reasoning benchmarks, revealing that LLMs are distractible. This finding is in-line with our evaluation on logical reasoning, where we observe that adding irrelevant rules not only degrades the overall logical reasoning performance, but also escalates the premise order effect. Similarly, the Reversal Curse (Berglund et al., 2023) unveils another perspective of the order effect, where they show that an LLM that recognizes "A is B" does not necessarily learn that "B is A." While their work studies the order effect between two entities within a single factual statement, our work focuses on reasoning problems with multiple premises, without restrictions on the number of (or relationship between) entities. In particular, for logical reasoning, we demonstrate that random permutations of premises often result in worse accuracy than the purely backward order. Liu et al. (2024) discover the lost-in-the-middle phenomenon in the long-context scenario: the LLM performance is the best when the relevant information to solve the task is placed at the beginning or the end of the input context, while the performance is the worst when the LLM needs to utilize input context in the middle. In Appendix D, we show that lost-in-the-middle phenomenon does not affect the performance on our tasks, since the length of input problems does not exceed 300 tokens in our benchmark, which is relatively small compared to the context length limit of LLMs in our

evaluation. Yan et al. (2023) present an approach called Concise and Organized Perception for deductive reasoning, which first generates directed graphs by connecting facts and rules in the problem, then prune and reorder the context accordingly before calling the LLM to solve the problem. The improvement achieved by this approach again demonstrates the effect of premise ordering and irrelevant premises on logical reasoning. While such input preprocessing methods can mitigate the ordering effect on certain reasoning tasks, they require task-specific design and do not generalize across domains. We consider developing generic end-to-end reasoning techniques for LLMs to address the premise order effect as future work.

Order effect for human logical reasoning. Although the premise order does not matter in deductive reasoning, several studies show that the premise order can impact the human reasoning performance (Dekeyser et al., 2000; Girotto et al., 1997). Dekeyser et al. (2000) described co-reference as a human preference of premise order; i.e., humans prefer the premises to be presented in an order where they can draw immediate conclusions after seeing each one. In this work, we show that LLMs also have such a preference, and they achieve the best performance when the ordering of rules follows the ground-truth proof. Girotto et al. (1997) studied how the premise order affects logical reasoning for humans, and found that the premise order has a significant effect in solving modus tollens problems (i.e., if P, then Q; not Q; therefore, not P), but not modus ponens problems (i.e., if P, then Q; P; therefore, Q). However, differing from our work, they studied the influence of different ordering between rules and facts, e.g., their experiments on modus tollens problems show that presenting negation statements (not Q) before rules (if P, then Q) improves the performance over the reverse order. On the other hand, our work focuses on modus ponens problems that are easier for both humans and LLMs, and we show that the LLM performance is still quite sensitive to the ordering of the premises.

Order effect of language models. Some prior works show that language models are able to understand permuted texts to some extent, i.e., after a random permutation of words, models usually maintain reasonable performance (Abdou et al., 2022; Sinha et al., 2020). Moreover, Cao et al. (2023) show that even when a large fraction of words are scrambled, GPT-4 still achieves decent performance on several reasoning benchmarks. In contrast to permuted texts in these works that are typically unnatural and nonsensical, our premise order permutations do not alter the semantic meaning and remain syntactically valid (we manually verify this). Nevertheless, we demonstrate that LLM reasoning performance is highly brittle to the ordering of the premises. For long-digit addition, prior works demonstrate that reversing the input numbers is a key to achieve better length generalization performance (Lee et al., 2023; Zhou et al., 2023; 2024). Specifically, by reversing the input numbers so that the least significant digit is presented first, the Transformer learns a simpler way of performing addition, where the model only needs to perform computation with the corresponding digits of operands and the carry-on digit at each step, without the need of looking at other digits. This approach enables the Transformer to better perform addition when trained from scratch, which also aligns with our finding: after reversing the input numbers, the premise order (i.e., orders of digits) follows the right ordering of performing long-digit addition, thus enables Transformers to better learn the task.

#### 5. Conclusion

In this work, we show that the premise order significantly affects LLMs' performance on reasoning tasks, even when the premise order does not change the underlying task itself. Our comprehensive evaluation demonstrates that LLM tendencies resemble human preference w.r.t. premise order, i.e., LLMs achieve the best performance when the premise order follows the intermediate reasoning steps to solve the problem. Conversely, LLMs face difficulties when the reasoning problem requires the model to read the problem description back-and-forth, resulting in a performance drop of over 30%. We further extend the study to mathematical reasoning and present the R-GSM benchmark, and again experimentally confirm the ordering effect.

While humans also have a preference of premise orders for reasoning problems, LLMs are much more susceptible to such ordering effects. We can attempt to ascribe the premise order effect to several candidate factors, such as the autoregressive model design, training objectives, and training data mixture. However, we leave proposing theoretical explanations of this limitation and developing new techniques towards addressing the premise order effect as future work.

#### **Impact Statement**

Our work presents an empirical study on weaknesses of LLM reasoning. One limitation of our work is that we did not conduct a rigorous human study on our benchmarks, and thus the LLM performance is not directly comparable to humans. This work can inspire future studies on the comparison of human and LLM reasoning.

While our work has not yet proposed a solution to address the premise order effect of LLMs, this work helps the community better understand the capabilities of existing LLMs, and thus better use them in practice. It may also motivate the community to identify the root cause of these pitfalls and address them, leading to the development of LLMs with stronger reasoning abilities.

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# A. R-GSM Dataset Statistics

Table 5 presents the statistics of our R-GSM benchmark.

# Steps	# Problems
2	20
3	43
4	65
5	43
6	23
7	15
8	11
	(a)
# Sentence	es # Problems
5	133
6	65
7	19
_	
8	3

*Table 5.* Statistics of the R-GSM dataset, with 220 problems in total: (a) breakdown on the number of reasoning steps; (b) breakdown on the number of sentences in the questions.

# **B.** Logical Reasoning Examples

Figure 10 presents common classes of errors — hallucinated rules and facts — by LLMs while solving our logical reasoning benchmark.

Figure 11 presents a sample logical reasoning problem with premise orders of different  $\tau$  values. We can see that the rules become less ordered when the absolute value of  $\tau$  decreases.

# **C. R-GSM Examples**

In this section, we present more examples of LLM predictions on R-GSM problems.

Figure 12 presents a failure case of a probability problem, which falls into the "Others" category in the error analysis (Table 4). Specifically, in the reordered problem, after the LLM reads the sentence about the scenario with a normal teacher coming in, the LLM immediately attempts to compute the probability that Marcus has to turn in his homework, ignoring that the LLM needs to compute the probability that a normal teacher will come in using the next sentence.

Figures 13 shows another wrong prediction of GPT-4 Turbo, where the error pattern is analogous to rule hallucination in logical reasoning evaluation. Interestingly, when moving the sentence about yellow cars preceding to the sentence about quantities of blue and green cars, GPT-4 Turbo starts to hallucinate the relationship between the number of yellow cars and the number of blue cars, resulting in insufficient information to correctly solve the problem.

Figures 14 and 15 present examples where both the original and reordered problems are correctly solved by LLMs in our evaluation. In both original problems, the succeeding sentences do not strongly depend on the preceding sentences.

#### D. Discussion: Does Logical Reasoning Suffer from the Lost-in-the-middle Issue?

Liu et al. (2024) demonstrate that when the input context becomes long, LLMs might suffer from the lost-in-the-middle issue: the model performance significantly degrades when relevant information to solve the task is in the middle of the input, instead of at the beginning or the end. Therefore, when given distracting rules for logical reasoning, another potential factor that might affect the model performance is the position of relevant rules in the model input.



Figure 10. Examples of hallucinated rules (left) and facts (right) produced by GPT-3.5-Turbo while solving our logical reasoning benchmark.





To examine the effect of such position bias, we conduct ablations on PaLM 2-L with 10 distracting rules, and we compare the performance with relevant rules added in the beginning, middle or the end of the problem description. Table 6 shows that with the same order and number of rules, the variation in performance is very small, whereas changing the order significantly affects the results. Note that the longest inputs in our logical reasoning benchmark, i.e., problems with 12 relevant rules and 10 distracting rules, only contain no more than 300 tokens, which is relatively short compared to the context length limit of LLMs in our evaluation. These results confirm that for our tasks where the input problems (and thus input context) are short, the lost-in-the-middle phenomenon is not the primary cause of the performance difference. In our primary experiments, for all logical reasoning problems, we interleave distracting rules with relevant rules in the input context.

# E. Full Results for Logical Reasoning

Tables 7 and 10 present the accuracy numbers for Figures 3 and 5, which are results on different numbers of relevant rules without distracting rules.

Tables 8 and 11 present the accuracy numbers for Figures 4 and 6 with 5 distracting rules.

Tables 9 and 12 present the accuracy numbers for Figures 4 and 6 with 10 distracting rules.

Premise Order Matters in Reasoning with Large Language Models

# rules, position \order	Forward	Backward	Shuffled
8, beginning	68.0%	40.0%	45.5%
8, middle	67.0%	39.0%	44.5%
8, end	67.0%	40.0%	45.5%
12, beginning	36.5%	17.0%	16.0%
12, middle	36.5%	17.0%	18.5%
12, end	35.0%	16.0%	19.5%

Table 6. Logical reasoning results performance of PaLM 2-L, with relevant rules at different positions of the input context.

# F. Full Results on R-GSM

Tables 13 and 14 present the accuracy numbers for Figures 7 and 8, which are breakdown results on R-GSM problems with different numbers of reasoning steps and different numbers of sentences in the problem description respectively.

 $\mathbf{X}$  Reordered  $\rightarrow$  incorrect



	Marcus is trying to decide whether he really needs to do his homework. There's a 50% chance that tomorrow he'll have a substitute teacher who won't collect the homework. Even if the normal teacher comes in, there's a 40% chance she'll give everyone an extension. Even if the whole class doesn't get an extension, there's a 20% chance Marcus can convince the teacher his dog ate his assignment and get a personal extension. What is the percentage chance that Marcus will actually have to turn in his homework tomorrow?	Marcus is trying to decide whether he really needs to do his homework. If the normal teacher comes in, there's a 40% chance she'll give everyone an extension. There's a 50% chance that tomorrow he'll have a substitute teacher who won't collect the homework. Even if the whole class doesn't get an extension, there's a 20% chance Marcus can convince the teacher his dog ate his assignment and get a personal extension. What is the percentage chance that Marcus will actually have to turn in his homework tomorrow?
		 Let's break it down:
	Let's break down the events:	1. The normal teacher comes in and does not
	1. There's a 50% chance of a substitute	give an extension (60% chance of this
	teacher who won't collect the homework.	will give an extension).
	2 If the normal teacher comes in (which has	- In this case, Marcus has a 20% chance of
	a 50% chance of not happening), there's a	getting a personal extension if he claims his
	40% chance she'll give an extension to the	dog ate his homework. This means there's an
	whole class	80% chance he will not get the personal
		extension and will have to turn in his
	3. If there's no class extension (which has a	nomework.
	60% chance of happening if the normal	- The probability of this scenario (normal
	teacher comes in), there's a 20% chance	eucher, no class extension, no personal
	Marcus can get a personal extension by	2. The normal teacher comes in and gives an
	convincing the teacher his dog ate his	2. The hornal teacher comes in and gives an extension (40% chance of this happening)
	homework	- If the teacher gives an extension Marcus
		does not have to turn in his homework
	Now, we add up all the probabilities where	tomorrow, so this scenario does not
	Marcus does not have to turn in his	contribute to the probability of Marcus having
	homework: $P(no homework) = P(substitute) +$	to turn in his homework.
	P(normal teacher and extension) + P(normal	3. A substitute teacher comes in (50% chance
	teacher, no class extension, and personal	of this happening).
	P(10  normework) = 0.50 + 0.20 + 0.00 +	- If there's a substitute teacher, Marcus does
	0.00  P(10  Homework) = 0.78  Or  78%	not have to turn in his homework tomorrow,
	Finally, we subtract this from 100% to find	so this scenario does not contribute to the
	the probability that Marcus will have to turn	probability of Marcus having to turn in his
	in his homework: P(homework) = 1- P(no	homework.
(Ca)	homework) $P(homework) = 1 - 0.76$	Now, we add up the probabilities of the
	P(homework) = 0.24 or 24%	scenarios where Marcus has to turn in his
	So, there is a 24% chance that Marcus will	homework - Probability of raying to turn in
	actually have to turn in his homework	So, there is a <b>48% chance</b> that Marcus will
	tomorrow.	baye to turn in his homework tomorrow

Figure 12. R-GSM example where the original problem can be correctly solved by GPT-4 Turbo, but the model fails on the reordered one.



Figure 13. R-GSM example where the original problem can be correctly solved by all models, but GPT-4 Turbo and Gemini Pro failed on the reordered one.



6

Sheila charged \$85.00 worth of merchandise on her credit card. **She ended up returning one item that cost \$15.00**. After she returned **the** item, she bought a frying pan that was on sale for 20% off \$20.00 and a set of towels that was 10% off \$30.00. She put both of these purchases on her credit card. What is the new balance on her credit card? ✓ Reordered → correct

Sheila charged \$85.00 worth of merchandise on her credit card. After she returned **an** item, she bought a frying pan that was on sale for 20% off \$20.00 and a set of towels that was 10% off \$30.00. She put both of these purchases on her credit card. **The returned item cost \$15.00.** What is the new balance on her credit card?

The frying pan was on sale for 20% off \$20.00 so that's 20\*.01 = <<20\*.01=0.20>>0.20 off The frying pan was \$20.00 and it's 20% off so that's 20\*.20 = <<20\*.20=4.00>>4.00 off The frying pan is \$20.00 and it's \$4.00 off so it now costs 20-4 = <<20-4=16.00>>16.00The towels were 10% off \$30.00 so that's 10\*.01 = <<10\*.01=0.10>>0.10 off The towels were \$30.00 and they're 10% off so that's 30\*.10 = <<30\*.10=3.00>>3.00 off The towels are \$30.00 and they're \$3.00 off so they now cost 30-3 = <<30-3=27.00>>27.00The frying pan is \$16.00 and the towels are \$27.00 so together they cost 16+27 = \$<<16+27=43.00>>43.00Sheila charged \$85.00 worth of merchandise and returned an item for \$15.00 so her balance was 85-15 = \$<<85-15=70.00>>70.00

Figure 14. R-GSM example where both the original and the reordered problems were correctly solved by all LLMs in our evaluation.

	<b>Original</b> → correct	<b>▼ Reordered</b> → correct
	Tony is painting a room with four walls. The north and south walls are 10 x 8 feet. The east and west walls are 5 x 8 feet. <b>A gallon of paint</b> <b>can cover 20 square feet and cost \$12.</b> How much will it cost to paint the room?	A gallon of paint can cover 20 square feet and cost \$12. Tony is painting a room with four walls. The east and west walls are 5 x 8 feet. The north and south walls are 10 x 8 feet. How much will it cost to paint the room?
	First, let's calculate the total area of the walls that Tony is wide and 8 feet tall. So for each of these walls: Area = Wid	going to paint. The east and west walls are both 5 feet Ith x Height = 5 feet x 8 feet = 40 square feet
	Since there are two of these walls, we need to double that 80 square feet	: Total area for east and west walls = 2 x 40 square feet =
	The north and south walls are both 10 feet wide and 8 fee 10 feet x 8 feet = 80 square feet	t tall. So for each of these walls: Area = Width x Height =
	Again, since there are two of these walls, we need to doub Total area for north and south walls = 2 x 80 square feet =	le that: 160 square feet
	Now, let's add the total areas of all four walls to get the to Total area = Area of east and west walls + Area of north a Total area = 80 square feet + 160 square feet = 240 squar	tal area to be painted: nd south walls e feet
	Now we know that one gallon of paint covers 20 square fe needs, we divide the total area by the coverage of one gall Gallons needed = Total area / Coverage per gallon Gallons needed = 240 square feet / 20 square feet per gall Gallons needed = 12 gallons	eet and costs \$12. To find out how many gallons Tony on: on
6	Since paint is typically sold by the gallon, Tony will need to wallspace. Now, let's calculate the total cost for the paint: Total cost = Number of gallons x Cost per gallon Total cost = 12 gallons x \$12 per gallon	buy 12 gallons of paint to cover the 240 square feet of
	Total cost = \$144	

Therefore, it will cost Tony **\$144** to buy the paint needed to cover the walls of the room.



# Rules	Order	Acc
	Forward	99.0%
4	Backward	99.5%
	Shuffled	98.8%
	Forward	98.5%
5	Backward	99.5%
	Shumed	98.2%
(	Forward	100%
0	Backward Shuffled	100%
	Siluineu	90.5%
7	Forward	99.0%
/	Shuffled	98.0% 97.0%
	Economical	00.00
8	Forward	99.0% 95.5%
0	Shuffled	93.5%
	Forward	08 5%
9	Backward	95.5%
	Shuffled	93.5%
	Forward	99.0%
10	Backward	92.5%
	Shuffled	87.3%
	Forward	98.5%
11	Backward	91.0%
	Shuffled	87.5%
	Forward	96.5%
12	Backward	84.0%
	Shuffled	80.8%
(a) <b>(</b>	GPT-4-turl	50.
# Rules	Order	Acc
	Forward	93.0%
4	Forward Backward	93.0% 73.5%
4	Forward Backward Shuffled	93.0% 73.5% 77.0%
4	Forward Backward Shuffled Forward	93.0% 73.5% 77.0% 90.0%
4	Forward Backward Shuffled Forward Backward	93.0% 73.5% 77.0% 90.0% 58.0%
4	Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0%
4	Forward Backward Shuffled Forward Backward Shuffled Forward	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5%
4 5 6	Forward Backward Shuffled Forward Backward Shuffled Forward Backward	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 77.5%
4 5 6	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 72.0%
4 5 6	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 72.0% 65.5%
4 5 6 7	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 25.0% 22.5%
4 5 6 7	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 22.5%
4 5 6 7	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 22.5% 50.0%
4 5 6 7 8	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 25.0% 22.5% 50.0% 17.5%
4 5 6 7 8	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 25.0% 22.5% 50.0% 17.5% 12.5%
4 5 6 7 8	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 50.0% 17.5% 12.5% 47.5%
4 5 6 7 8 9	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 25.0% 22.5% 50.0% 17.5% 12.5% 47.5% 11.5% 8.7%
4 5 6 7 8 9	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 72.0% 25.0% 22.5% 50.0% 17.5% 12.5% 47.5% 11.5% 8.7%
4 5 6 7 8 9	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 72.0% 65.5% 22.5% 50.0% 17.5% 12.5% 47.5% 11.5% 8.7% 34.0%
4 5 6 7 8 9 10	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 77.5% 72.0% 65.5% 25.0% 22.5% 50.0% 17.5% 12.5% 47.5% 11.5% 8.7% 34.0% 4.5%
4 5 6 7 8 9 10	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 50.0% 17.5% 12.5% 47.5% 11.5% 8.7% 34.0% 4.5% 2.5%
4 5 6 7 8 9 10	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 22.5% 22.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 34.0% 4.5% 2.5% 33.0% 33.0%
4 5 6 7 8 9 10 11	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 22.5% 22.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 34.0% 4.5% 2.5% 33.0% 2.0%
4 5 6 7 8 9 10 11	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 22.5% 22.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 17.5% 34.0% 4.5% 2.5% 33.0% 2.0% 1.5%
4 5 6 7 8 9 10 11	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 25.0% 22.5% 50.0% 22.5% 17.5% 17.5% 17.5% 17.5% 17.5% 12.5% 34.0% 4.5% 2.5% 33.0% 2.0% 1.5%
4 5 6 7 8 9 10 11 12	Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Shuffled Shuffled	93.0% 73.5% 77.0% 90.0% 58.0% 57.0% 87.5% 72.0% 65.5% 22.5% 50.0% 22.5% 17.5% 12.5% 47.5% 11.5% 8.7% 34.0% 4.5% 2.5% 33.0% 2.0% 1.5% 0.3%

# Rules	Order	Acc
" itules	Econord	08 507
4	Forward	98.5%
4	Shuffled	98.3%
	Shumeu	98.3%
-	Forward	98.5%
5	Backward	98.5%
	Shumed	98.3%
	Forward	98.0%
6	Backward	93.5%
	Shuffled	95.3%
	Forward	96.5%
7	Backward	89.0%
	Shuffled	91.2%
	Forward	95.5%
8	Backward	77.0%
	Shuffled	87.7%
	Forward	94.0%
9	Backward	79.0%
-	Shuffled	85.7%
	Forward	05.00%
10	Backward	93.0% 75.5%
10	Shuffled	81.0%
	Shumed	01.0%
	Forward	94.0%
11	Backward	66.0%
	Snumed	18.1%
	Forward	88.0%
	D 1 1	
12	Backward	57.5%
12	Shuffled	57.5% 66.5%
12 (b)	Shuffled PaLM 2-I	57.5% 66.5%
12 (b) # Rules	Backward Shuffled PaLM 2-I Order	57.5% 66.5%
12 (b) # Rules	Backward Shuffled PaLM 2-I Order Forward	57.5% 66.5%
12 (b) # Rules 4	PaLM 2-I Order Forward Backward	57.5% 66.5% 2. Acc 88.5% 70.0%
12 (b) # Rules 4	PaLM 2-I Order Forward Backward Shuffled	57.5% 66.5% 2. <u>Acc</u> 88.5% 70.0% 71.8%
12 (b) # Rules 4	Backward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward	57.5% 66.5% 2. Acc 88.5% 70.0% 71.8% 84.0%
12 (b) # Rules 4 5	PaLM 2-I Order Forward Backward Shuffled Forward Backward	57.5% 66.5% <u>Acc</u> 88.5% 70.0% 71.8% 84.0% 55.0%
12 (b) # Rules 4 5	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7%
12 (b) # Rules 4 5	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5%
12 (b) # Rules 4 5	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0%
12 (b) # Rules 4 5 6	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0%
12 (b) # Rules 4 5 6	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Eagward	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0%
12 (b) # Rules 4 5 6	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0%
12 (b) # Rules 4 5 6 7	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0%
12 (b) # Rules 4 5 6 7	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2%
12 (b) # Rules 4 5 6 7	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	51.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5%
12 (b) # Rules 4 5 6 7 8	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5% 15.5%
12 (b) # Rules 4 5 6 7 8	PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5% 15.5% 13.0%
12 (b) # Rules 4 5 6 7 8	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5% 15.5% 13.0% 50.5%
12 (b) # Rules 4 5 6 7 7 8 8 9	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 56.5% 13.0% 50.5% 9.5%
12 (b) # Rules 4 5 6 7 8 8 9	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5% 13.0% 50.5% 9.5% 8.7%
12 (b) # Rules 4 5 6 7 8 8 9	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 20.2% 64.0% 20.2% 56.5% 15.5% 13.0% 50.5% 9.5% 8.7% 37.0%
12 (b) # Rules 4 5 6 7 8 8 9 10	Packward Shuffled PaLM 2-I Order Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled Forward Backward Shuffled	57.5% 66.5% Acc 88.5% 70.0% 71.8% 84.0% 55.0% 51.7% 87.5% 67.0% 62.0% 64.0% 23.0% 20.2% 56.5% 15.5% 13.0% 50.5% 8.7% 37.0% 3.5%

(c) Gemini 1.0 Pro.

(d) GPT-3.5-turbo.

Forward Backward Shuffled

Forward Backward Shuffled

11

12

36.0% 1.0% 2.8%

30.0% 1.0% 1.2%

*Table 7.* Result table corresponding to Figure 3.

# Rules	Order	Acc	# Rules	Order	A
	Forward	98.0%		Forward	98.
4	Backward	99.5%	4	Backward	95.
	Shuffled	99.0%		Shuffled	94.
	Forward	99.5%		Forward	97.
5	Backward	98.5%	5	Backward	93.
	Shuffled	98.0%		Shuffled	94.
	Forward	97.5%		Forward	88.
6	Backward	97.0%	6	Backward	85.
	Shuffled	96.7%		Shuffled	88.
	Forward	93.5%		Forward	87.
7	Backward	92.0%	7	Backward	68.
	Shuffled	90.2%		Shuffled	75.
	Forward	89.5%		Forward	84.
8	Backward	85.5%	8	Backward	63.
	Shuffled	82.2%		Shuffled	66.
	Forward	88.0%		Forward	81.
9	Backward	84.0%	9	Backward	56.
	Shuffled	82.7%		Shuffled	60.
	Forward	89.0%		Forward	79.
10	Backward	77.0%	10	Backward	46.
	Shuffled	74.2%		Shuffled	55.
	Forward	84.5%		Forward	73.
11	Backward	75.5%	11	Backward	43.
	Shuffled	71.5%		Shuffled	42.
	Forward	80.5%		Forward	64.
12	Backward	72.5%	12	Backward	32.
	Shuffled	57.2%		Shuffled	38.

(a) GPT-4-turbo.

(b) PaLM 2-L.

Table 8. Results corresponding to Figure 4 with 5 distracting rules.

# Rules	Order	Acc		# Rules	Order	Acc
	Forward	97.0%			Forward	97.5%
4	Backward	98.0%		4	Backward	95.0%
	Shuffled	97.7%	6		Shuffled	96.3%
	Forward	98.0%			Forward	94.0%
5	Backward	96.0%		5	Backward	91.0%
	Shuffled	96.5%			Shuffled	92.5%
	Forward	92.5%			Forward	89.0%
6	Backward	88.5%		6	Backward	77.0%
	Shuffled	90.3%			Shuffled	79.7%
	Forward	84.5%			Forward	71.5%
7	Backward	80.0%		7	Backward	55.0%
	Shuffled	76.0%			Shuffled	60.7%
	Forward	81.5%			Forward	68.5%
8	Backward	76.5%		8	Backward	39.5%
	Shuffled	70.5%			Shuffled	46.7%
	Forward	73.0%			Forward	61.5%
9	Backward	65.0%		9	Backward	38.0%
	Shuffled	62.8%			Shuffled	42.7%
	Forward	64.5%			Forward	47.0%
10	Backward	59.0%		10	Backward	29.5%
	Shuffled	53.7%			Shuffled	30.7%
	Forward	58.5%			Forward	46.5%
11	Backward	53.0%		11	Backward	15.5%
	Shuffled	48.7%			Shuffled	25.0%
	Forward	57.5%			Forward	36.5%
12	Backward	46.5%		12	Backward	15.5%
	Shuffled	40.0%			Shuffled	18.2%

(a) GPT-4-turbo.

(b) PaLM 2-L.

Table 9. Results corresponding to Figure 4 with 10 distracting rules.

au	A
99.0%	-
95.0%	
91.0%	
94.5%	
95.5%	
99.0%	
91.0%	
82.5%	
88.5%	
92.5%	
98.5%	
90.0%	
84.5%	
88.0%	
91.0%	
96.5%	
76.0%	
82.0%	
84.5%	
84.5% 84.0%	
84.5% 84.0% turbo.	
84.5% 84.0% turbo. Acc	
84.5% 84.0% turbo. Acc 87.5%	
84.5% 84.0% turbo. Acc 87.5% 68.5%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 72.0%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 77.5%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 77.5% 50.0%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 77.5% 50.0% 10.5%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 77.5% 50.0% 10.5% 12.0%	
84.5% 84.0% turbo. Acc 87.5% 68.5% 75.5% 72.0% 77.5% 50.0% 10.5% 12.0% 15.0% 17.5%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         17.5%         34.0%         2.0%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         35%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         34.0%         2.0%         3.5%         2.0%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         3.5%         2.0%         4.5%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         3.5%         2.0%         4.5%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         3.5%         2.0%         4.5%         16.5%         0.0%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         3.5%         2.0%         4.5%         16.5%         0.0%	
84.5%         84.0%         turbo.         Acc         87.5%         68.5%         75.5%         72.0%         77.5%         50.0%         10.5%         12.0%         15.0%         17.5%         34.0%         2.0%         3.5%         2.0%         4.5%         16.5%         0.0%         0.0%         0.5%	

(c) Gemini 1.0 Pro.

(d) GPT-3.5-turbo.

Table 10. Result table corresponding to Figure 5.

Premise	Order	Matters	in	Reasoning	with	Large	Language	Models

# Rules	au	Acc	# Rules	au	
	1.0	89.5%		1.0	
	0.5	86.5%		0.5	
8	0.0	78.0%	8	0.0	
	-0.5	82.0%		-0.5	
	-1.0	85.5%		-1.0	
	1.0	89.0%		1.0	
	0.5	75.5%		0.5	
10	0.0	70.5%	10	0.0	
	-0.5	76.5%		-0.5	
	-1.0	77.0%		-1.0	
	1.0	84.5%		1.0	
	0.5	68.5%		0.5	
11	0.0	67.5%	11	0.0	
	-0.5	78.5%		-0.5	
	-1.0	75.5%		-1.0	
	1.0	80.5%		1.0	
	0.5	49.5%		0.5	
12	0.0	61.5%	12	0.0	
	-0.5	60.5%		-0.5	
	-1.0	72.5%		-1.0	

(a) GPT-4-turbo.

(b) PaLM 2-L.

Table 11. Results corresponding to Figure 6 with 5 distracting rules.

# Rules	au	Acc	# Rules	au	Acc
	1.0	81.5%		1.0	68.5%
	0.5	73.0%		0.5	48.5%
8	0.0	65.5%	8	0.0	45.5%
	-0.5	73.0%		-0.5	46.0%
	-1.0	76.5%		-1.0	39.5%
	1.0	64.5%		1.0	47.0%
	0.5	48.5%		0.5	35.0%
10	0.0	50.5%	10	0.0	30.0%
	-0.5	62.0%		-0.5	27.0%
	-1.0	59.0%		-1.0	29.5%
	1.0	58.5%		1.0	46.5%
	0.5	54.0%		0.5	30.0%
11	0.0	41.0%	11	0.0	24.5%
	-0.5	51.0%		-0.5	20.5%
	-1.0	53.0%		-1.0	15.5%
	1.0	57.5%		1.0	36.5%
	0.5	33.0%		0.5	18.0%
12	0.0	42.0%	12	0.0	19.0%
	-0.5	45.0%		-0.5	17.5%
	-1.0	46.5%		-1.0	15.5%
(a) G	PT-4-tu	rbo.	(b) ]	PaLM 2	-L.

Table 12. Results corresponding to Figure 6 with 10 distracting rules.

# Steps	Init Acc	Reorder Acc
>= 2	94.1%	85.0%
>=3	94.0%	84.0%
>=4	94.3%	82.8%
>=5	92.4%	79.3%
>=6	89.8%	73.5%
	(a) GPT-4-t	urbo.
# Steps	Init Acc	Reorder Acc
>= 2	80.5%	69.1%
>= 3	79.0%	68.0%
>=4	80.3%	66.2%
>= 5	80.4%	59.8%
>=6	71.4%	55.1%

# Steps	Init Acc	Reorder Acc
>=2	86.4%	79.5%
>= 3	85.5%	78.5%
>=4	84.1%	77.7%
>= 5	80.4%	71.7%
>=6	69.4%	63.3%
	(b) PaLM	2-L.
# Steps	(b) PaLM Init Acc	2-L. Reorder Acc
$\frac{\text{\# Steps}}{>= 2}$	(b) PaLM Init Acc 67.3%	2-L. Reorder Acc 51.8%
# Steps >= 2 >= 3	(b) PaLM Init Acc 67.3% 66.5%	2-L. Reorder Acc 51.8% 51.0%
# Steps >= 2 >= 3 >= 4	(b) PaLM Init Acc 67.3% 66.5% 63.1%	2-L. Reorder Acc 51.8% 51.0% 47.8%
# Steps >= 2 >= 3 >= 4 >= 5	(b) PaLM Init Acc 67.3% 66.5% 63.1% 58.7%	2-L. Reorder Acc 51.8% 51.0% 47.8% 39.1%

(c) Gemini 1.0 Pro.

(d) GPT-3.5-turbo.

Table 13. Results corresponding to Figure 7.

# Sentences	Init Acc	Reorder Acc		# Sentences	Init Acc	Reorder
>= 5	94.1%	85.0%	-	>= 5	86.4%	79.5%
>=6	89.7%	81.6%		>= 6	78.2%	69.0%
>=7	86.4%	68.2%		>=7	77.3%	72.7%
(8	(a) GPT-4-turbo.				(b) PaLM 2-1	L.
# Sentences	Init Acc	Reorder Acc	-	# Sentences	Init Acc	Reorder .
>= 5	80.5%	69.1%	-	>= 5	67.3%	51.8%
>=6	80.5%	60.9%		>= 6	62.1%	46.0%
>=7	72.7%	54.5%		>=7	54.5%	36.4%
(c)	Gemini 1.0	Pro.	(d)	) GPT-3.5-tu	rbo.	

Table 14. Results corresponding to Figure 8.