

# Unicycle: numerical simulations of seismic cycles in a viscoelastic half space with the integral method

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## Summary

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The deformation of the Earth's crust and upper mantle spans widely different length scales, from extreme localization within fault zones, to broadly distributed viscoelastic strain in the asthenosphere. The Unicycle software, which stands for Unified Cycle of Earthquakes, provides an efficient representation of these deformation mechanisms by combining surface and volume elements. Numerical simulations of seismic cycles in a viscoelastic half-space are conducted using the integral method whereby the elastic interactions are computed semi-analytically using closed-form expressions of Green's functions (Barbot et al., 2017; Barbot, 2018). The method only requires meshing of the regions that undergo thermo-dynamically irreversible deformation, 13 resulting in relatively small meshes that can be assembled easily. In strictly brittle models, the technique simplifies to the boundary integral method.

The approach accommodates complex structural settings with faults discretized with rectangle or triangle surface elements and ductile domains meshed with cuboid or tetrahedron volume elements. Forward models of seismic cycles with viscoelastic relaxation are obtained using 18 the fifth-order Runge-Kutta method with adaptive time steps. The calculation is particularly 19 efficient, requiring just a few matrix-vector multiplication per time step, which is parallelized 20 for a distributed-memory architecture. 21

Crustal dynamics is computed based on a physical model of rate- and state-dependent friction 22 (Barbot, 2019) and a nonlinear rheology for transient creep and steady-state creep of bulk 23 rocks (Masuti et al., 2016; Masuti & Barbot, 2021). Applications range from two-dimensional 24 models of the lithosphere-asthenosphere system (Barbot, 2020; Lambert & Barbot, 2016; Q. 25 Shi et al., 2020) to three-dimensional models of faults interacting with a ductile asthenosphere 26 (P. Shi et al., 2022). 27

## Statement of need

Unicycle is a series of Fortran90 standalone numerical modeling tools for simulations of 29 crustal dynamics in a two-dimensional or three-dimensional half-space. The input file allows 30 complex frictional, rheological, and structural settings and the automatic exploration of the 31 parameter space. The simulation requires the initial time-consuming calculation of large 32 matrices that capture the stress interactions among surface and volume elements. This matrix 33 can be automatically saved and re-used in subsequent calculations that use different material 34 properties but the same geometry. Meshing of the brittle faults and ductile regions is relatively 35 straightforward and can be done with standard tools. The simulation output is provided in 36 ASCII tables and netcdf binary files compatible with the General Mapping Tools version 5 and 37 above (Wessel et al., 2019). Additional output files enable three-dimensional visualization with 38 the Paraview software (Ahrens et al., 2005). 39

Unicycle is designed for scientists conducting research in lithosphere dynamics. Applications 40

#### DOI: 10.xxxxx/draft

#### Software

- Review C
- Repository I<sup>A</sup> Archive 🗗

Editor: ☑

Submitted: 24 June 2023 Published: unpublished

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- include fault dynamics, e.g., the initiation, propagation, and arrest of ruptures, lower-crustal
- <sup>42</sup> and asthenosphere dymamics with nonlinear rheology, e.g., power-law constitutive laws with
- 43 transient creep, and the mechanical coupling between localized and distributed deformation in
- 44 various tectonic environments. Successful simulation benchmarks for fault dynamics based on
- <sup>45</sup> comparison with other software can be found in Jiang et al. (2022).

## **Acknowledgements**

This study is supported in part by the National Science Foundation under award number EAR-1848192.

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