




1 ShOpt.jl: A Julia Package for Empirical Point Spread 2 Function Characterization of JWST NIRCам Data

3 Edward Berman ^{1¶} and Jacqueline McCleary ^{1¶}

4 ¹ Northeastern University, USA ¶ Corresponding author

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5 Summary

6 When astronomers capture images of the night sky, several factors – ranging from diffraction
7 and optical aberrations to atmospheric turbulence and telescope jitter – affect the incoming
8 light. The resulting distortion and blurring are summarized in the image’s point spread function
9 (PSF), the response of an optical system to an idealized point source. The PSF can obscure or
10 even mimic the astronomical signal of interest, making its accurate characterization essential.
11 By effectively modeling the PSF, we can predict image distortions at any location and proceed
12 to deconvolve the PSF, ultimately reconstructing distortion-free images.

13 The PSF characterization methods used by astronomers fall into two main classes: forward-
14 modeling approaches, which use physical optics propagation based on models of the optics, and
15 empirical approaches, which use stars as fixed points to model and interpolate the PSF across
16 the rest of the image. (Stars are essentially point sources before their light passes through the
17 atmosphere (when observing from the ground) and telescope, so the shape and size of their
18 surface brightness profiles define the PSF at that location.) Empirical PSF characterization
19 proceeds by first cataloging the observed stars, separating the catalog into validation and
20 training samples, and interpolating the training stars across the field of view of the camera.
21 After training, the PSF model can be validated by comparing the reserved stars to the PSF
22 model’s prediction.

23 Shear Optimization with ShOpt.jl introduces modern techniques, tailored to James Webb
24 Space Telescope (JWST) NIRCам imaging, for empirical PSF characterization across the field
25 of view. ShOpt has two modes of operation: approximating stars with analytic profiles, and
26 a more realistic pixel-level representation. Both modes take as input a catalog with image
27 cutouts – or “vignettes” – of the stars targeted for analysis.

28 Statement of need

29 Empirical PSF characterization tools like Point Spread Function Extractor (PSFex, [Bertin,](#)
30 [2011](#)) and Point Spread Functions in the Full Field of View (PIFF, [Jarvis et al., 2020](#)) are widely
31 popular in astrophysics. However, the quality of PIFF and PSFex models tends to be quite
32 sensitive to the parameter values used to run the software, with optimization sometimes relying
33 on brute-force guess-and-check runs. PIFF is also notably inefficient for large, well-sampled
34 images, taking hours in the worst cases. The JWST’s Near Infrared Camera (NIRCам) offers
35 vast scientific opportunities (e.g. [Casey, Kartaltepe, et al., 2023](#)); at the same time, this
36 unprecedented data brings new challenges for PSF modeling:

- 37 (1) Analytic functions like Gaussians are incomplete descriptions of the NIRCам PSF, as
38 evident from Figures 1 and 2. Figure 1 shows that to get a good PSF model we need to
39 model a large dynamic range over a large box size. Figure 2 illustrates that the residuals
40 between an idealized forward model and a Gaussian approximation can be quite severe.

41 This calls for well-thought-out, non-parametric modeling and diagnostic tools that can
 42 capture the full dynamic range of the NIRCcam PSF. ShOpt provides these models and
 43 diagnostics out of the box.

44 (2) The NIRCcam detectors have pixel scales of 0.03 (short wavelength channel) and 0.06
 45 (long wavelength channel) arcseconds per pixel (Beichman et al., 2012; Rieke et al.,
 46 2003, 2005). At these pixel scales, star vignettes need to be at least 131 by 131 pixels
 47 across to fully capture the wings of the PSFs (4-5 arcseconds). These vignette sizes are
 48 3-5 times larger than the ones used in surveys such as DES (Jarvis et al., 2020) and
 49 SuperBIT (McCleary et al., 2023) and force us to evaluate how well existing PSF
 50 fitters scale to this size. ShOpt has been designed for computational efficiency and aims to
 51 meet the requirements of detectors like NIRCcam.

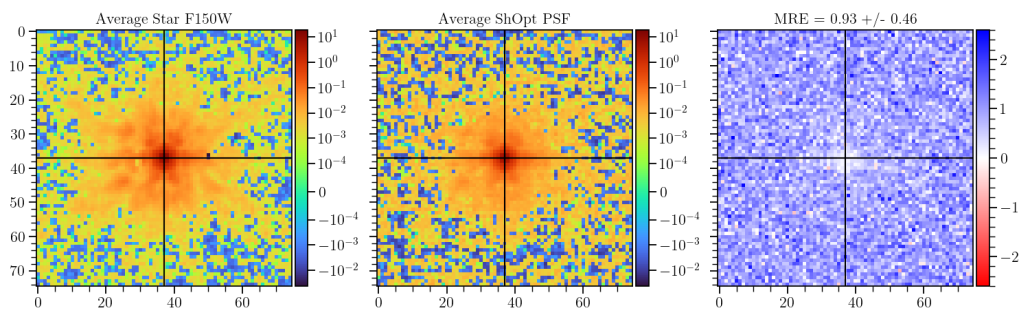


Figure 1: The plot on the left shows the average cutout of all stars in a supplied catalog. The plot in the middle shows the average point spread function model for each star. The plot on the right shows the average normalized error between the observed star cutouts and the point spread function model.

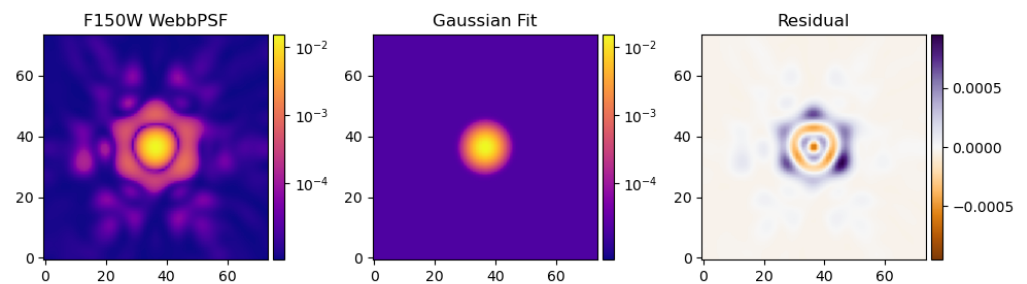


Figure 2: The plot on the left shows an idealized forward model of the NIRCcam F150W PSF made using WebbPSF. The middle shows a Gaussian approximation to the PSF. The right shows the residual between the WebbPSF model and the Gaussian approximation.

52 ShOpt bridges the speed of PSFex with the features of PIFF using fewer configurable hyperpa-

53 rameters. Sh0pt employs a number of techniques to optimize the speed of the program. First
54 and foremost, Sh0pt is equipped with support for multithreading. Polynomial interpolation
55 is used for handling PSF variations across the field of view. The polynomials given to each
56 basis element of the PSF are independent of one another and therefore can be distributed to
57 different CPU threads to be run in parallel. Sh0pt also introduces new methods for fitting
58 both analytic profiles and pixel based profiles. If an analytic profile is used to model the
59 PSF, then there are 3 basis elements parameterizing the model. We choose 2D elliptical
60 Gaussians for these analytic profiles because they are cheap to compute. Moreover, we use
61 the Limited Memory Broyden–Fletcher–Goldfarb–Shanno algorithm (LBFGS) to find these
62 paramters. This is faster but more memory intensive than Conjugate Gradient, the algorithm
63 used in PIFF. Moreover, the 3 basis elements are constrained to the manifold $B_2(r) \times \mathbb{R}_+$,
64 where $B_2(r) = \{(x, y) : x^2 + y^2 < 1\}$ and $\mathbb{R}_+ = \{x : x > 0\}$. We constructed a function
65 that maps any point in \mathbb{R}^3 into $B_2(r) \times \mathbb{R}_+$. The LBFGS algorithm uses successive iterations
66 to converge to a solution for the 3 basis elements, and so we use this function to ensure that
67 our update steps in LBFGS do not leave the constraint. For the pixel basis, both PIFF and
68 PSFex approximate the PSF by minimizing the reduced χ^2 between a grid of pixels and a
69 star vignette. PCA can quickly achieve the same purpose of approximating the input vignette
70 without overfitting to background noise. We also provide an autoencoder mode, which uses
71 deep learning to reconstruct the image. The weights and biases are not reset between stars, so
72 the knowledge of how to reconstruct one star is transferred to the next. This in turn leads to
73 fewer training iterations. Finally, Sh0pt is written in Julia. Julia uses a just in time compiler
74 which makes it faster than intepreted languages such as Python and has shown to be a good
75 choice for performance critical code (Stanitzki & Strube, 2021).

76 State of the Field

77 The JWST captures images at high resolution and at wavelengths of light that have been
78 previously unexplored (Gardner et al., 2006). With these images we are seeing farther into
79 the early universe than we ever have before. The complex optics of JWST coupled with our
80 desire to get the most out of the incredible data have presented the community with new set
81 of challenges that current software does not address: the need to create high-fidelity models
82 of the point spread function for diffraction-limited images across a wide range of wavelengths.
83 Sh0pt.jl is one attempt to solve this challenge and other teams are approaching the issue in
84 complementary ways, as described below.

85 A number of JWST PSF libraries already exist, using both empirical and forward-modeling
86 approaches. We describe them here and draw attention to their strengths and weaknesses to
87 further motivate the development of Sh0pt.jl. As described in the statement of need, PSFex
88 was one of the first precise and general purpose tools used for empirical PSF fitting. However,
89 the Dark Energy Survey collaboration reported small but noticeable discrepancies between the
90 sizes of PSFex models and the sizes of observed stars. They also reported ripple-like patterns
91 in the spatial variation of star-PSF residuals across the field of view (Jarvis et al., 2020), which
92 they attributed to the astrometric distortion solutions for the Dark Energy Camera.

93 These findings motivated the Dark Energy Survey's development of PIFF (Point Spread
94 Functions in the Full Field of View). PIFF works in sky coordinates on the focal plane, as
95 opposed to image pixel coordinates used in PSFex, which minimized the ripple patterns in
96 the star-PSF residuals and the PSF model size bias. (Based on the DES findings, Sh0pt
97 also works directly in sky coordinates.) PIFF is written in Python, a language with a large
98 infrastructure for astronomical data analysis, for example Astropy (Astropy Collaboration et
99 al., 2022) and Galsim (Rowe et al., 2015). The choice of language makes PIFF software more
100 accessible to programmers in the astrophysics community than PSFex, which was first written
101 in C in 2007 and much less approachable for a community of open source developers. One of
102 the motivations of Sh0pt was to write astrophysics specific software in Julia, because Julia
103 provides a good balance of readability and speed with its high-level functional paradigm and

104 just-in-time compiler (Stanitzki & Strube, 2021). Julia ranks behind Python, IDL, Matlab,
105 and Fortran in full-text mentions in astronomical literature (Collaboration et al., 2022). We
106 are optimistic that ShOpt will demonstrate that Julia is an appealing choice for programming
107 in astronomy despite its low adoption to date. There is also recent work on using PSFr for
108 PSF reconstructions that has been applied to JWST data (Ding et al., 2022; Merlin et al.,
109 2022; Santini et al., 2023; Yang et al., 2022). Similar to ShOpt, PSFr begins its PSF modeling
110 by stacking stars to form an initial guess. However, rather than using polynomial interpolation
111 to address spatial variations, PSFr employs an iterative process of shifting the pixels in its PSF
112 model. This process continues until the model can adequately represent all of the stars in
113 the catalog. Finally, the PSF fitter STARRED (Michalewicz et al., 2023) has been shown to
114 produce PSF models competitive with PSFr and PSFex. Like ShOpt, STARRED puts an emphasis
115 on computational efficiency and uses the JAX package to achieve just-in-time compilation.
116 There is future work to be done to benchmarking all of these empirical approaches on JWST
117 NIRCam data.

118 While WebbPSF provides highly precise forward models of the JWST PSF, these models
119 are defined for single-epoch exposures (Perrin et al., 2012, 2014). Much of the NIRCam
120 science is accomplished with image mosaics – essentially, the combination of single exposure
121 detector images into a larger, deeper image. The rotation of the camera between exposures,
122 the astrometric transformations and resampling of images before their combination into a
123 mosaic, and the mosaic's large area all make the application of WebbPSF models to mosaics a
124 non-trivial procedure. This has been done quite effectively (Ji et al., 2023), however, it is not
125 as easy to reproduce compared to running an empirical characterization tool like ShOpt.

126 As outlined in the state of the field, ShOpt is a tool built with the user experience in mind
127 that attempts to bridge the strengths of existing PSF fitters. ShOpt's combination of speed,
128 user friendliness, and accuracy enable the science goals of the COSMOS-Web survey, detailed
129 below.

130 The COMOS-Web survey is the largest cycle 1 JWST extragalactic survey according to area
131 and prime time allocation (Casey, Kartaltepe, et al., 2023), and covers 0.54 deg^2 (Beichman
132 et al., 2012; Rieke et al., 2023). Among other science goals, the COMOS-Web survey will
133 use the JWST to detect thousands of galaxies in the Epoch of Reionization ($6 \sim z \sim 11$) to
134 create one of the highest resolution large scale structure maps of the early universe (Casey,
135 Kartaltepe, et al., 2023). JWST data has also been used to pick out active galactic nuclei from
136 host galaxies (Zhuang & Shen, 2023) and identify 15 candidate galaxies whose luminosities
137 push the limits of our Λ CDM galaxy formation models (Casey, Akins, et al., 2023). These
138 science cases all rely upon good PSF modeling and underscore the importance of ShOpt.

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