




1 movement_primitives: Imitation Learning of Cartesian 2 Motion with Movement Primitives

3 Alexander Fabisch ¹

4 ¹ Robotics Innovation Center, German Research Center for Artificial Intelligence (DFKI GmbH), Bremen,
5 Germany

DOI: [10.xxxxxx/draft](https://doi.org/10.xxxxxx/draft)

Software

- [Review](#) 
- [Repository](#) 
- [Archive](#) 

Editor: Yasmin Mzayek 

Reviewers:

- [@ishaanamahajan](#)
- [@gautam-sharma1](#)

Submitted: 22 March 2024

Published: unpublished

License

Authors of papers retain copyright
and release the work under a
Creative Commons Attribution 4.0
International License ([CC BY 4.0](#)).

6 Summary

7 Movement primitives are a common representation of movements in robotics ([Maeda et al.,
8 2017](#)) for imitation learning, reinforcement learning, and black-box optimization of behaviors.
9 There are many types and variations. The Python library *movement_primitives* focuses on
10 imitation learning, generalization, and adaptation of movement primitives in Cartesian space.
11 It implements dynamical movement primitives, probabilistic movement primitives, as well as
12 Cartesian and dual Cartesian movement primitives with coupling terms to constrain relative
13 movements in bimanual manipulation. They are implemented in Cython to speed up online
14 execution and batch processing in an offline setting. In addition, the library provides tools for
15 data analysis and movement evaluation.

16 Statement of Need

17 Movement primitives are a common group of policy representations in robotics. Although
18 movement primitives are limited in their capacity to represent behavior that takes into account
19 complex sensor data during execution in comparison to general function approximators such
20 as neural networks, several instances (e.g., dynamical movement primitives) have proven to
21 be a reliable and effective tool in robot learning. A reliable tool deserves a similarly reliable
22 implementation. However, there are only a few actively maintained, documented, and easy to
23 use implementations. One of these is *movement_primitives*, which we present in this article.

24 Movement Primitives

25 Dynamical Movement Primitives (DMPs) are the most prominent example of movement
26 primitives ([Ijspeert et al., 2002, 2013](#)). From a high-level perspective ([Fabisch & Metzen,
27 2014](#)), a DMP is a policy

$$x_{t+1} = \pi_{w,v}(x_t, t),$$

28 where x_t is the state of an agent (position, velocity, and acceleration) at time t , w are the
29 weights (parameters) that define the shape of the movement, and v are meta-parameters. The
30 exact definition of the meta-parameters v depends on the DMP type, but most types allow
31 to set the initial state x_0 , the final state g , and the duration of the movement τ . A DMP
32 generates a trajectory in state space so that a controller that translates states x_t, x_{t+1} to
33 control commands is required.

34 DMPs have been used for imitation learning, in which one demonstration is enough to learn
35 a DMP. DMPs can also be used in a reinforcement learning setting, in which the weights of
36 the DMP or the meta-parameters can be learned. Saveriano et al. ([2023](#)) provide a survey of
37 DMPs and how they can be used.

38 In the *movement_primitives* library, we implement several types that are important for Cartesian
 39 movement generation: an extension that includes the final velocity as a meta-parameter (Mülling
 40 et al., 2013), DMPs for Cartesian poses in three dimensions with unit quaternions (Ude et
 41 al., 2014), and DMPs that define bimanual movements by introducing a coupling term that
 42 controls the relative motion of two arms (Gams et al., 2013).

43 Another type of movement primitives implemented in this library are Probabilistic Movement
 44 Primitives (ProMPs) (Paraschos et al., 2013) that capture the distribution of multiple demon-
 45 strations. Their probabilistic formulation allows to modify movements by conditioning, for
 46 instance, on viapoints.

47 Implementations of Movement Primitives

48 The *movement_primitives* library is a reimplementaion and extension of the movement
 49 primitive features of BOLeRo (Fabisch et al., 2020). BOLeRo is a C++/Python framework for
 50 behavior learning and optimization. However, the focus is very broad and more on reinforcement
 51 learning and behavior parameter optimization than on imitation learning.

52 Another similar library is dmpbbo (Stulp & Raiola, 2019), which has a general DMP imple-
 53 mentation and additional components to optimize the parameters of DMPs in reinforcement
 54 learning settings. The library is designed to train DMPs in Python and execute them in C++.
 55 Both implementations are not well-suited for imitation learning because additional tooling
 56 for data analysis and deployment is required. Switching between C++ and Python is also
 57 not convenient for various reasons: building and installing these packages is complicated,
 58 continuous integration is hard to set up, code maintenance is complicated, and it does not
 59 integrate easily with the Python scientific ecosystem.

60 There are more implementations listed by Saveriano et al. (2023) (available at [https://git-
 61 lab.com/dmp-codes-collection/third-party-dmp](https://git-lab.com/dmp-codes-collection/third-party-dmp)). A lot of these are exemplary Matlab scripts
 62 and not maintained anymore, or only implementations of specific papers. Other libraries
 63 do not support Cartesian movement primitives, which are only available in BOLeRo and
 64 *movement_primitives*. The latter also supports bimanual movements through dual Cartesian
 65 DMPs.

66 Design and Features

67 The main contributions of *movement_primitives* are (1) a fast Python-only library for movement
 68 primitives, and (2) robust implementations of several types of movement primitives (see Table 1).
 69 Our focus is on Cartesian movement primitives that are used to control one or two robotic arms
 70 and offer exemplary implementations of coupling terms for Cartesian (bimanual) DMPs. These
 71 can be used for obstacle avoidance and to constrain dual arm motions to relative positions
 72 and/or orientations.

Table 1: Overview of implemented movement primitives.

Class	Description	Publication
DMP	Standard DMP	Ijspeert et al. (2013)
DMP	Smooth spatial scaling	Pastor et al. (2009)
DMPWithFinalVelocity	Allows final velocity	Mülling et al. (2013)
CartesianDMP	DMP of Cartesian poses	Ude et al. (2014)
DualCartesianDMP	DMP of two Cartesian poses	Gams et al. (2013)
ProMP	Standard ProMP	Paraschos et al. (2013)

73 Furthermore, *movement_primitives* supports the whole imitation learning pipeline, including

74 data analysis through plotting and visualization (based on pytransform3d (Fabisch, 2019) and
75 Open3D (Zhou et al., 2018)), data preprocessing for imitation learning, good integration with
76 the scientific ecosystem in Python, simulation of learned movement primitives (in PyBullet
77 (Coumans & Bai, 2016–2021)), export to permanent data formats (pickle, JSON, YAML), and
78 analysis of kinematic feasibility. Although it has several dependencies and requires compilation
79 because of its Cython (Dalcin et al., 2011) components, it is possible to simply install it with
80 pip from PyPI.

81 **Example: Rotating a Compact Solar Panel with a Humanoid**

82 [Figure 1](#) and [Figure 2](#) show a humanoid robot rotating an object with two hands. The movement
83 is generated by a dual Cartesian DMP trained on a demonstrated rotation movement. The
84 width of the object is known. Hence, it can easily be adapted for similar objects with a different
85 size through a coupling term defined by (Gams et al., 2013).

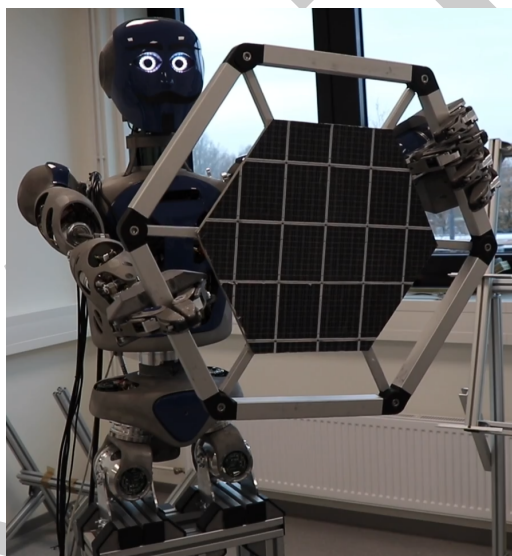


Figure 1: RH5 Manus (Boukheddimi et al., 2022) rotating a compact solar panel.

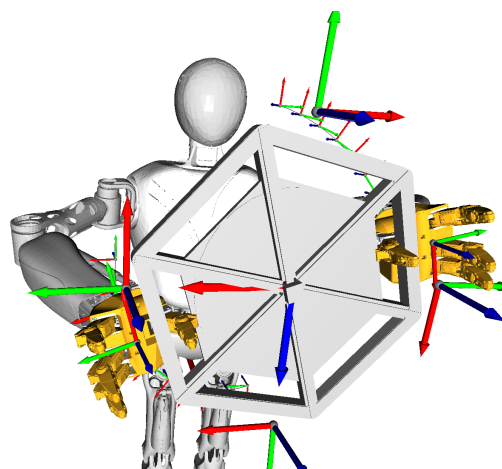


Figure 2: Visualization of similar rotation trajectory with another humanoid robot.

86 A similar task has been solved by Mronga & Kirchner (2021) with two Kuka iiwa arms. They

87 record a dataset for different panel sizes via kinesthetic teaching and use Gaussian mixture
 88 regression to represent the distribution of solutions and condition it on the object width to
 89 generalize. This is easier with ProMPs: for each demonstration, we compute ProMP weights,
 90 concatenate them with the task parameters over which we want to generalize, and learn a
 91 Gaussian mixture model, which we can condition on task parameters to generate ProMPs that
 92 define trajectory distributions to solve these tasks (Figure 3 and Figure 4).

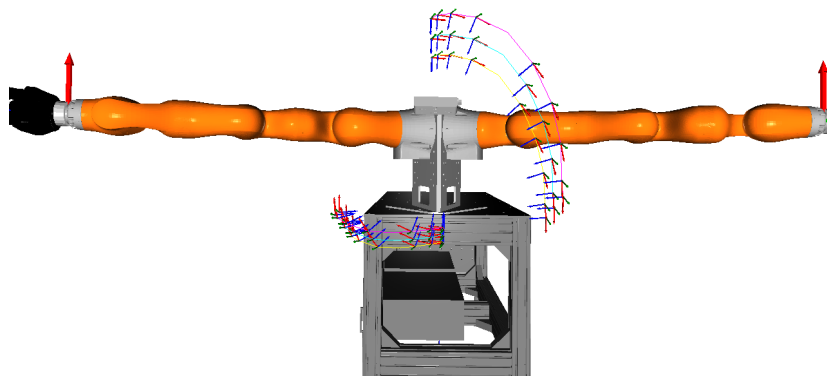


Figure 3: Mean trajectories for conditional ProMPs and panel widths 30/40/50 cm.

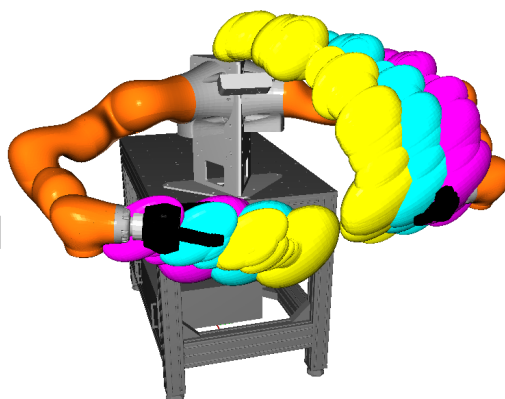


Figure 4: At each step, the position distribution defined by the conditioned ProMP is indicated by an equiprobable ellipsoid. The arms are at the mean start position for width 50 cm.

93 Benchmark of DMP Implementations

94 Since execution speed of DMPs is relevant in robotics, we compare several DMP implementa-
 95 tions from *dmpbbo* and *movement_primitives*. For this purpose, we create a minimum jerk
 96 trajectory of N dimensions that moves from $0 \in \mathbb{R}^N$ to $1 \in \mathbb{R}^N$ in one second, train a DMP
 97 on it, and execute the DMP step by step. We use M weights per dimension, and step through
 98 the DMP with $\Delta t = 0.001s$. The concept of *dmpbbo* is to train in Python and run DMPs
 99 in C++. We still analyze the Python version and the C++ version of *dmpbbo* as well as
 100 *movement_primitives* with various implementations of the integration (Euler integration with
 101 $h = 0.1 \cdot \Delta t$ and RK4 integration, both in Python and Cython). The default integration
 102 method of *dmpbbo* is RK4. Results for varying configurations of N and M are summarized
 103 in Figure 5, Figure 6 and Table 2. While the number of weights per dimension and the

104 number of dimensions have a considerable influence on the runtime of `dmpbbo`, the influence
 105 on the runtime of `movement_primitives` is negligible because NumPy (Harris et al., 2020)
 106 vectorization is used. More specifically, computing all steps of a DMP with 1 s duration
 107 at 1 kHz ($\Delta t = 0.001s$) with $N = 50$ dimensions and $M = 60$ weights per dimension
 108 takes $0.0822 \pm 0.0015s$ with the `movement_primitives` library and RK4 integration in Cython,
 109 which means 8.51% of the DMP's runtime is spent on computing steps. This allows online
 110 adaptation of the trajectory. `dmpbbo`'s C++ implementation is the best candidate for a low
 111 number of dimensions and weights per dimension. In this domain it outperforms all other
 112 implementations by a considerable margin. However, it scales linearly with these numbers.
 113 Hence, it is considerably slower for $N = 50$ and $M = 60$ than any RK4 implementation of
 114 `movement_primitives`. The Python version of `dmpbbo` is not able to run some configurations
 115 in real time. For example, $N = 6, M = 30$ needs $5.9292 \pm 0.0955s$ to compute.

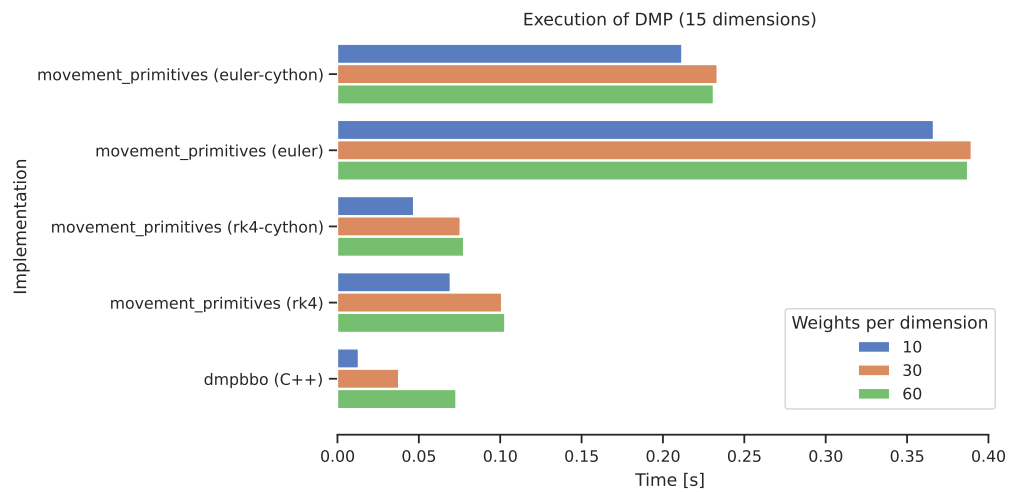


Figure 5: Benchmark of execution speed for various DMP implementations and configurations. Each bar shows an average over 100 stepwise executions of a DMP. Varying number of weights per dimension M , number of dimensions $N = 6$.

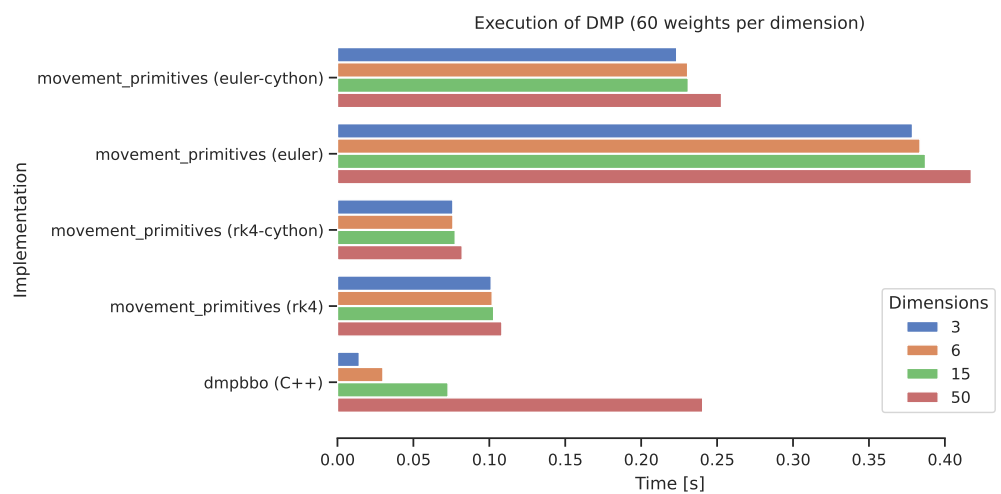


Figure 6: Benchmark of execution speed for various DMP implementations and configurations. Each bar shows an average over 100 stepwise executions of a DMP. Varying number of dimensions N , number of weights per dimension $M = 30$.

Table 2: Benchmark results for DMP execution. Best performance per setup in **bold**.

Library	Implementation	N	M	Time $\mu \pm \sigma$ [s]		
dmpbbo	C++	3	10	0.0027 \pm 0.0001		
			30	0.0077 \pm 0.0001		
			60	0.0144 \pm 0.0004		
		6	10	0.0049 \pm 0.0001		
			30	0.0146 \pm 0.0002		
			60	0.0300 \pm 0.0052		
		15	10	0.0129 \pm 0.0028		
			30	0.0376 \pm 0.0059		
			60	0.0729 \pm 0.0103		
		50	10	0.0401 \pm 0.0068		
			30	0.1236 \pm 0.0174		
			60	0.2405 \pm 0.0308		
		dmpbbo	Python	3	10	0.8137 \pm 0.0164
					30	1.6986 \pm 0.0319
					60	3.0244 \pm 0.0454
				6	10	1.3946 \pm 0.0228
					30	3.1676 \pm 0.0746
					60	5.9292 \pm 0.0955
15	10			3.2079 \pm 0.0593		
	30			7.4972 \pm 0.1366		
	60			14.2590 \pm 0.2811		
50	10			9.7134 \pm 0.0448		
	30			24.6018 \pm 2.0579		
	60			47.4420 \pm 2.0075		
movement_primitives	euler-cython			3	10	0.1946 \pm 0.0019
					30	0.2223 \pm 0.0070
					60	0.2234 \pm 0.0031
				6	10	0.1912 \pm 0.0033
					30	0.2301 \pm 0.0043
					60	0.2306 \pm 0.0060
		15	10	0.2117 \pm 0.0067		
			30	0.2334 \pm 0.0041		
			60	0.2310 \pm 0.0013		
		50	10	0.2260 \pm 0.0009		
			30	0.2547 \pm 0.0273		
			60	0.2529 \pm 0.0044		
		movement_primitives	rk4-cython	3	10	0.0447 \pm 0.0006
					30	0.0737 \pm 0.0018
					60	0.0760 \pm 0.0003
				6	10	0.0471 \pm 0.0036
					30	0.0733 \pm 0.0003
					60	0.0761 \pm 0.0003
15	10			0.0468 \pm 0.0022		
	30			0.0754 \pm 0.0005		
	60			0.0776 \pm 0.0002		
50	10			0.0752 \pm 0.0002		
	30			0.0794 \pm 0.0063		
	60			0.0822 \pm 0.0015		

116 Conclusion

117 Although movement primitives are a popular tool in robot learning, there is a lack of well
118 maintained implementations in particular for bimanual and Cartesian movements. *move-*
119 *ment_primitives* provides a well-tested, robust implementation of various movement primitives
120 with the goal of generating Cartesian robot movements. It integrates well with the existing
121 Python scientific ecosystem.

122 Acknowledgements

123 This work was supported by a grant of the German Federal Ministry of Economic Affairs and
124 Energy (BMW, FKZ 50 RA 1701) and by the European Commission under the Horizon 2020
125 framework program for Research and Innovation (project acronym: APRIL, project number:
126 870142).

127 References

- 128 Boukheddimi, M., Kumar, S., Peters, H., Mronga, D., Budhiraja, R., & Kirchner, F. (2022).
129 Introducing RH5 manus: A powerful humanoid upper body design for dynamic movements.
130 *2022 International Conference on Robotics and Automation (ICRA)*, 01–07. <https://doi.org/10.1109/ICRA46639.2022.9811843>
131
- 132 Coumans, E., & Bai, Y. (2016–2021). *PyBullet, a python module for physics simulation for*
133 *games, robotics and machine learning*. <http://pybullet.org>.
- 134 Dalcin, L., Bradshaw, R., Smith, K., Citro, C., Behnel, S., & Seljebotn, D. (2011). Cython:
135 The best of both worlds. *Computing in Science & Engineering*, 13(02), 31–39. <https://doi.org/10.1109/MCSE.2010.118>
136
- 137 Fabisch, A. (2019). pytransform3d: 3D transformations for python. *Journal of Open Source*
138 *Software*, 4(33), 1159. <https://doi.org/10.21105/joss.01159>
- 139 Fabisch, A., Langosz, M., & Kirchner, F. (2020). BOLeRo: Behavior optimization and
140 learning for robots. *International Journal of Advanced Robotic Systems*, 17(3). <https://doi.org/10.1177/1729881420913741>
141
- 142 Fabisch, A., & Metzen, J. H. (2014). Active contextual policy search. *Journal of Machine*
143 *Learning Research*, 15(97), 3371–3399. <http://jmlr.org/papers/v15/fabisch14a.html>
- 144 Gams, A., Nemec, B., Zlajpah, L., Wächter, M., Ijspeert, A., Asfour, T., & Ude, A. (2013).
145 Modulation of motor primitives using force feedback: Interaction with the environment
146 and bimanual tasks. *2013 IEEE/RSJ International Conference on Intelligent Robots and*
147 *Systems*, 5629–5635. <https://doi.org/10.1109/IROS.2013.6697172>
- 148 Harris, C. R., Millman, K. J., Walt, S. J. van der, Gommers, R., Virtanen, P., Cournapeau, D.,
149 Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., Kerkwijk,
150 M. H. van, Brett, M., Haldane, A., Río, J. F. del, Wiebe, M., Peterson, P., ... Oliphant,
151 T. E. (2020). Array programming with NumPy. *Nature*, 585(7825), 357–362. <https://doi.org/10.1038/s41586-020-2649-2>
152
- 153 Ijspeert, A. J., Nakanishi, J., Hoffmann, H., Pastor, P., & Schaal, S. (2013). Dynamical
154 movement primitives: Learning attractor models for motor behaviors. *Neural Computation*,
155 25(2), 328–373. https://doi.org/10.1162/NECO_a_00393
- 156 Ijspeert, A. J., Nakanishi, J., & Schaal, S. (2002). Movement imitation with nonlinear dynamical
157 systems in humanoid robots. *Proceedings 2002 IEEE International Conference on Robotics*
158 *and Automation*, 2, 1398–1403. <https://doi.org/10.1109/ROBOT.2002.1014739>

- 159 Maeda, G. J., Neumann, G., Ewerton, M., Lioutikov, R., Kroemer, O., & Peters, J. (2017).
160 Probabilistic movement primitives for coordination of multiple human–robot collaborative
161 tasks. *Autonomous Robots*, 41, 593–612. <https://doi.org/10.1007/s10514-016-9556-2>
- 162 Mronga, D., & Kirchner, F. (2021). Learning context-adaptive task constraints for robotic
163 manipulation. *Robotics and Autonomous Systems*, 141, 103779. [https://doi.org/10.1016/](https://doi.org/10.1016/j.robot.2021.103779)
164 [j.robot.2021.103779](https://doi.org/10.1016/j.robot.2021.103779)
- 165 Mülling, K., Kober, J., Kroemer, O., & Peters, J. (2013). Learning to select and generalize
166 striking movements in robot table tennis. *The International Journal of Robotics Research*,
167 32(3), 263–279. <https://doi.org/10.1177/0278364912472380>
- 168 Paraschos, A., Daniel, C., Peters, J. R., & Neumann, G. (2013). Probabilistic move-
169 ment primitives. In C. J. Burges, L. Bottou, M. Welling, Z. Ghahramani, & K. Q.
170 Weinberger (Eds.), *Advances in neural information processing systems* (Vol. 26).
171 Curran Associates, Inc. [https://proceedings.neurips.cc/paper_files/paper/2013/file/](https://proceedings.neurips.cc/paper_files/paper/2013/file/e53a0a2978c28872a4505bdb51db06dc-Paper.pdf)
172 [e53a0a2978c28872a4505bdb51db06dc-Paper.pdf](https://proceedings.neurips.cc/paper_files/paper/2013/file/e53a0a2978c28872a4505bdb51db06dc-Paper.pdf)
- 173 Pastor, P., Hoffmann, H., Asfour, T., & Schaal, S. (2009). Learning and generalization
174 of motor skills by learning from demonstration. *2009 IEEE International Conference on*
175 *Robotics and Automation*, 763–768. <https://doi.org/10.1109/ROBOT.2009.5152385>
- 176 Saveriano, M., Abu-Dakka, F. J., Kramberger, A., & Peternel, L. (2023). Dynamic movement
177 primitives in robotics: A tutorial survey. *The International Journal of Robotics Research*,
178 02783649231201196. <https://doi.org/10.1177/02783649231201196>
- 179 Stulp, F., & Raiola, G. (2019). DmpBbo: A versatile python/c++ library for function
180 approximation, dynamical movement primitives, and black-box optimization. *Journal of*
181 *Open Source Software*, 4(37), 1225. <https://doi.org/10.21105/joss.01225>
- 182 Ude, A., Nemeč, B., Petrić, T., & Morimoto, J. (2014). Orientation in cartesian space dynamic
183 movement primitives. *2014 IEEE International Conference on Robotics and Automation*
184 *(ICRA)*, 2997–3004. <https://doi.org/10.1109/ICRA.2014.6907291>
- 185 Zhou, Q.-Y., Park, J., & Koltun, V. (2018). Open3D: A modern library for 3D data processing.
186 *arXiv:1801.09847*.