

MACE: a Machine-learning Approach to Chemistry ² Emulation

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Software

- [Review](https://github.com/openjournals/joss-reviews/issues/7148) &
- [Repository](https://github.com/silkemaes/MACE) &
- [Archive](https://doi.org/)₁₇

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2 Observatory, Leiden University FO Beso 18 ¹⁰ Astrochemistry is the study of chemical species in astrophysical objects. By combining 11 observations and theoretical predictions, the physical conditions of the object can be analysed as well as its chemical composition and yields, since chemistry is closely coupled to the dynamics 13 of the environment. Most often, such astrophysical environments are known to be complex ¹⁴ and out of thermodynamic equilibrium. For that reason, the chemical evolution is usually ¹⁵ modelled using the chemical kinetics approach, in which a set of non-linear coupled ordinary 16 different equations (ODEs) is solved for a given network of chemical species and reactions. 17 For large chemical networks, however, this method is computationally slow. Therefore, we 18 developed MACE, a Machine-learning Approach to Chemistry Emulation, inspired on similar ¹⁹ work in the literature (e.g., Holdship et al. (2021); Grassi et al. (2022); Sulzer & Buck [\(2023\)](#page-3-2)). ²⁰ MACE is a PyTorch module that offers a trainable surrogate model that is able to emulate $_{21}$ chemical kinetics in a shorter computation time than its classical analogue. More specifically, ²² it provides a machine learning architecture, consisting of an autoencoder and a trainable ODE, implemented in PyTorch and torchode (Lienen & Günnemann, 2022). Mathematically, MACE is give by

$$
\hat{\mathbf{n}}(t) = \mathcal{D}\Big(G(\mathcal{E}(\mathbf{n}, \mathbf{p}), t)\Big),\tag{1}
$$

²⁵ where $\hat{\boldsymbol{n}}(t)$ represents the predicted chemical abundances at time t, more details can be found in Maes et al. (2024) and in Fig. 1, which shows a schematic representation of the architecture and flow of the emulator. MACE is developed in the context of circumstellar envelopes (CSEs) of evolved stars, but is flexible to be retrained on data of other astrophysical environments.

⁹ **Summary**

Figure 1: Schematic representation of the architecture of MACE. The symbols **n** and **p** represent the chemical abundances and physical parameters, respectively. The autoencoder (in blue) consists of an encoder \mathcal{E} , able to map **n** and **p** to a latent space representation **z**, and decoder \mathcal{D} , working the other way around. The function g represents the trainable ODE, which needs to be solved for a time step Δt . (Adapted from Maes et al. (2024).)

²⁹ **Statement of need**

Figure 1: Schematic representation of the architecture of MACE. The symbols *a* and *p* representation denotes the architecture of MACE. The subcencoder (in blue) consists envote C, able to map *n* and *p* to a latent spa ³⁰ Astrophysical objects or environments entail 3D dynamical processes, as well as chemical 31 and radiation processes. Thus, in order to properly model such an environment, these three ³² constituents all need to be included in a single simulation. However, modelling each constituents 33 separately already poses a computational challenge for a modest parameter space, let alone 34 running a simulation with the three constituents integrated, and on an extended parameter 35 space. Specifically on the chemistry side, it is generally established that, from a mathematical ³⁶ point of view, chemical kinetics is a stiff problem. When working with an extended chemical 37 network ($\gtrsim 100$ species, connected by $\gtrsim 1000$ reactions), the system becomes computationally ³⁸ very slow to solve. Therefore, it is essential to speed up the solver in an alternative way, ³⁹ also because the solver is applied multiple times when calculating the chemical evolution of ⁴⁰ a certain environment. A fast and accurate chemistry solver would make it computationally 41 feasible to run it alongside a 3D hydrodynamical and/or radiation model.

⁴² **Example case**

43 In the context of circumstellar envelopes, we aim to build a comprehensive model, consisting of ⁴⁴ 3D hydrodynamics, chemistry, and radiation. This is needed since recently, complex structure ⁴⁵ (such as spiral, arcs, and bipolarity) are observed in CSEs around evolved, low- and intermediate mass stars, currently attributed to the presence of (sub-)stellar companions [\(Decin et al., 2020;](#page-2-0) Gottlieb et al., 2022; Nordhaus & Blackman, 2006). In order to study these stars and their CSEs, taking into account companions, accurate 3-dimensional models are needed. Currently, only hydrodynamical modelling is done for these systems in $3D$ (e.g., Maes et al. [\(2021\)](#page-3-7); 50 Malfait et al. (2021)), though the aim is to include chemistry as well as radiation [\(Maes et al.,](#page-3-9) 51 [2022\)](#page-3-9). Starting with integrating chemistry and 3D hydrodynamics, this coupling will only be ⁵² computationally feasible when a faster alternative to chemical kinetics exists.

 53 The development of MACE is a first step towards this coupling. Using the MACE architecture,

 54 we are able to reproduce the 1D abundance profiles of 468 chemical species with an accuracy

⁵⁵ between 10 and 18, averaged over 3000 tests, for MACE models with different sets of

⁵⁶ hyperparameters, for the following error metric:

$$
error = \frac{\log_{10} \mathbf{n} - \log_{10} \hat{\mathbf{n}}}{\log_{10} \mathbf{n}},
$$
\n(2)

- which is executed element-wise and subsequently summed over the different chemical species.
- More details on the accuracy of the MACE models can be found in Maes et al. [\(2024\)](#page-3-4). Fig.
- [2](#page-2-1) shows the abundance profiles of seven chemical species, where the full curves indicate the
- 60 MACE test of model int4 from Maes et al. [\(2024\)](#page-3-4), and the dashed curves give the result for
- the classical model. On average, the MACE routine provides a speed-up of a factor 26, not
- taking into account the potential extra speed-up factor due to efficient vectorisation when
- coupling MACE with an SPH hydrodynamical model.

Code availability

The code of MACE is publicly available in a GitHub repository: [https://github.com/silkemaes/](https://github.com/silkemaes/MACE) MACE.

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