

Class 9 Computer Science Chapter 1: Introduction to Computational Systems Notes

Posted in **9 Computer Science**



These lecture notes are prepared by **Salman Ahmad**, who is both a **teacher** and a **web developer**. The purpose of this material is to make the topic clear and useful for students of Class 9 Computer Science.

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What is a System?

A **system** is a group of **connected parts that work together to perform a specific task or achieve a specific purpose**.

Example: A laptop is a computer system. Its **processor, RAM, storage, operating system, applications, and other components** work together to allow us to perform different tasks.

Information system

It is a **combination of people, technology, data, and procedures that work together to collect and turn data into useful information**.

Example

A **school information system** can collect student information such as names, marks, attendance, and fees. It processes this data and provides useful information such as **result cards, attendance reports, and student records**.

Objective of a System

The **objective of a system** is the **main purpose or goal that the system is designed to achieve**. A system is created to perform specific tasks and produce useful results.

Examples of System Objectives

Different systems are designed for different purposes. For example:

- **School Information System** → To manage student records, marks, attendance, and fees.
- **Banking System** → To manage customer accounts, deposits, withdrawals, and transactions.
- **Hospital Management System** → To manage patient records, appointments, treatments, and billing.
- **Library Management System** → To manage books, members, borrowing, and returning of books.
- **Online Shopping System** → To allow customers to search, order, and pay for products online.

Components of a System

The **components of a system** are the different parts that work together to achieve the system's objective. A system normally has the following main components:

1. **Input** → The data or resources entered into the system.
 - **Example:** Student names and marks entered into a school system.
2. **Processing** → The activities performed on the input to produce a useful result.
 - **Example:** Calculating a student's total and percentage.
3. **Output** → The useful information or result produced by the system.
 - **Example:** A student's result card.
4. **Feedback** → Information about the output that helps improve or control the system.
 - **Example:** A teacher checks the result and corrects an incorrect mark.

System Environment

The **system environment** includes everything **outside the system that interacts with or affects it**. These external factors can influence **how the system works and operates**.

Simple Example: Online Shopping System

An **online shopping system** interacts with:

- **Customers** – Buy products.
- **Delivery services** – Deliver orders.
- **Banks** – Process payments.
- **Internet** – Allows users to access the system.

Note: These things are **outside the system but interact with it**, so they are part of its **environment**.

Communication also called System Communication

Communication between the different parts of a system is important for the system to work properly. It allows the components to **share information and work together smoothly** to achieve the system's goal.

Examples

- **Computing System:** The **CPU communicates with memory** to get and store data.
- **Biological System:** The **brain sends signals to muscles** to make the body move.

Software

Software is a set of **programs and instructions** that tells a computer **what to do and how to perform different tasks**. Unlike hardware, software cannot be physically touched.

Types of Software

There are two main types of software:

1. System Software

System software controls and manages the computer's hardware and provides a platform for other software to run.

Examples of System Software

- **Operating System (OS)** – Manages the computer's hardware and provides an interface for users and applications.
Examples: Windows, Linux, macOS.
- **Device Drivers (DD)** – Help the operating system communicate with and control hardware devices.
Examples: Printer driver, graphics driver, keyboard driver.
- **Utility Programs (UP)** – Help maintain, protect, and manage the computer.
Examples: Disk Cleanup, antivirus software, backup tools.

2. Application Software

Application software is designed to help users **perform specific tasks**.

Examples of Application Software

- **Microsoft Word** → Writing documents
- **Microsoft Excel** → Working with data and calculations
- **Web Browsers** → Browsing the internet
- **Media Players** → Playing audio and video
- **Graphic Design Software** → Creating and editing images

Note: **System software** manages the computer and its hardware, while **application software** helps users perform specific tasks.

System Software vs Application Software

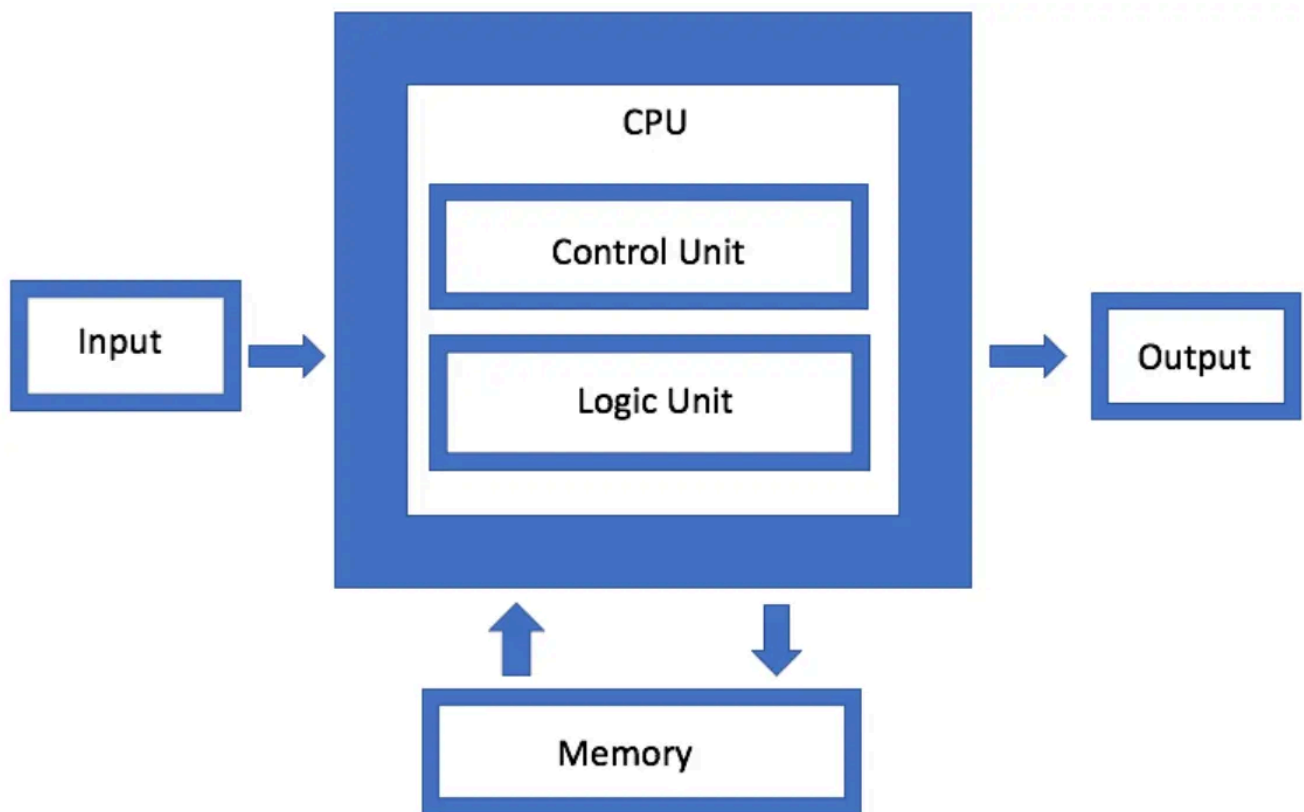
System Software	Application Software
It manages and controls the computer's hardware .	It helps users perform specific tasks .
It provides a platform for application software to run.	It runs on the system software.
It usually works in the background .	Users directly interact with it.
It is generally pre-installed with the computer or installed as part of the operating system.	It usually needs to be installed by the user according to their needs.
It is necessary for the basic operation of a computer.	It is used for specific user tasks.
Examples: Operating System, Device Drivers, Utility Programs.	Examples: MS Word, Excel, Web Browsers, Media Players.

The Architecture of von Neumann Computers

Introduction

The **von Neumann architecture** is a basic design or model of a computer. It explains how the main parts of a computer **work together to process data and instructions**. This model was developed in the **1940s** and is named after **John von Neumann**, a mathematician and physicist who contributed to its development.

Diagram or Struture



Main Components

A von Neumann computer mainly consists of:

- **Memory**
- **Central Processing Unit (CPU)**
- **Input Devices**
- **Output Devices**
- **System Bus**

1. Memory

Memory stores the **data and instructions** that the CPU needs to perform tasks. For example, when you open a program on your computer, it is loaded from the storage device into **RAM (Random Access Memory)**. The CPU can access the program and its data from RAM quickly, allowing the program to run efficiently.

2. Central Processing Unit (CPU)

The **CPU** is the main processing part of the computer. It **processes data and executes instructions** stored in memory.

The CPU has two important components:

Arithmetic Logic Unit (ALU)

The **ALU** performs:

- Mathematical calculations, such as **addition and subtraction**.
- Logical operations, such as **comparing values**.

Example: When you calculate **2 + 2** in a calculator application, the ALU performs the calculation.

Control Unit (CU)

The **Control Unit** controls and coordinates the activities of the computer. It tells other components **what to do and when to do it** according to the instructions of the program.

Example: When calculating **2 + 2**, the CU controls the process and makes sure the required data is obtained from memory and the ALU performs the calculation.

Note: ALU → Performs calculations and logical operations.

CU → Controls and coordinates the activities of the CPU.

3. Input Devices

Input devices allow users to **enter data and instructions into the computer**.

Examples include:

- **Keyboard**
- **Mouse**
- **Microphone**
- **Scanner**

Example: When you type your name using a keyboard, the keyboard sends the input to the computer for processing.

4. Output Devices

Output devices show or provide the **results produced by the computer**.

Examples include:

- **Monitor**
- **Printer**
- **Speakers**

Example: When the computer finishes processing some information, the result can be displayed on the monitor.

5. System Bus

A **system bus** is a communication pathway that allows the different components of a computer to **exchange data, addresses, and control signals**.

The system bus has three main parts:

Data Bus

The **Data Bus** carries the **actual data** between the CPU, memory, and other components.

Address Bus

The **Address Bus** carries information about **where the data should be sent or where it should be retrieved from**.

Control Bus

The **Control Bus** carries **control signals** that tell different components what actions to perform.

Note: The **system bus** acts like a **communication pathway** that allows different parts of the computer to communicate with each other.

Working of von Neumann Architecture

The **von Neumann architecture** executes instructions using a step-by-step process called the **Fetch-Decode-Execute-Store cycle**.

The CPU mainly performs **four stages**:

1. **Fetching** → Gets the instruction from memory.
2. **Decoding** → Understands what the instruction means.
3. **Execution** → Performs the required operation.
4. **Storing** → Stores or displays the result.

Example: Adding Two Numbers

Suppose we use a calculator to calculate **2 + 2**. The computer follows the four stages to produce the answer.

1. Fetching

Fetching means getting the next instruction from **memory**.

The **Program Counter (PC)** contains the address of the next instruction. The CPU uses this address to get the instruction from memory and places it in the **Instruction Register (IR)**.

2. Decoding

Decoding means **understanding the instruction** that was fetched.

The **Control Unit (CU)** examines the instruction and determines what operation needs to be performed.

For example, the CPU understands that an **addition** operation is required.

3. Execution

Execution means **performing the required operation**.

The **Arithmetic Logic Unit (ALU)** performs mathematical and logical operations.

For example:

$$2 + 2 = 4$$

The ALU performs the addition and produces the result **4**.

4. Storing

After execution, the result is **stored in memory or sent to an output device**.

For example, the result **4** can be displayed on the calculator screen.

Complete Process

Fetch → Decode → Execute → Store

Stage	What Happens?
Fetch	Get the instruction from memory
Decode	Understand the instruction
Execute	Perform the required operation
Store	Store or display the result

Example: 2 + 2

Fetch: Get the addition instruction

↓

Decode: Understand that addition is required

↓

Execute: ALU calculates $2 + 2 = 4$

↓

Store: Result **4** is stored or displayed

Number System

A **number system** is a method of **representing numbers using a specific set of digits or symbols**. Different number systems use different numbers of digits, called the **base** or **radix**.

In computer science, the following four number systems are commonly used:

1. Decimal Number System

The **Decimal Number System** has a **base of 10**. It uses **10 digits from 0 to 9**.

This is the number system that we normally use in our daily life.

Example: 25, 100, 458

2. Binary Number System

The **Binary Number System** has a **base of 2**. It uses only **two digits: 0 and 1**.

Computers use binary because electronic circuits can represent two basic states, such as **ON and OFF**. **0 means OFF** and **1 means ON**.

Example: 1010, 1101, 10001

3. Octal Number System

The **Octal Number System** has a **base of 8**. It uses **eight digits from 0 to 7**.

Example: 25, 147, 706

4. Hexadecimal Number System

The **Hexadecimal Number System** has a **base of 16**. It uses **16 symbols: 0–9 and A–F**.

Here:

- **A = 10**
- **B = 11**
- **C = 12**
- **D = 13**
- **E = 14**
- **F = 15**

Hexadecimal is used in areas such as **memory addresses, color codes, MAC addresses, and IPv6 addresses**.

Example: 2A, FF, 1B

Note: 1 octal digit is equal to 3 binary bits, while 1 hexadecimal digit is equal to 4 binary bits.

For example:

- **Octal:** 0 = 000, 1 = 001, 2 = 010, 3 = 011
- **Hexadecimal:** 0 = 0000, 1 = 0001, 2 = 0010, 3 = 0011

This makes it easier to convert binary numbers into **octal and hexadecimal** forms.

Decimal to Binary Conversion and Vice Versa

To convert a decimal number into binary, we repeatedly **divide the number by 2** and record the remainders. The binary answer is obtained by reading the remainders **from bottom to top**.

Example: Convert 8_{10} to Binary

Divide **8 by 2** repeatedly and write the remainders on the right:

```
2 | 8
2 | 4 - 0
2 | 2 - 0
2 | 1 - 0
```

Now read the remainders from **bottom to top**:

Therefore: $8_{10} = 1000_2$

Binary to Decimal

Now convert 1000_2 back to decimal:

1000_2

$$= (1 \times 2^3) + (0 \times 2^2) + (0 \times 2^1) + (0 \times 2^0)$$

$$= 8 + 0 + 0 + 0$$

$$= 8_{10}$$

Therefore:

$$1000_2 = 8_{10} \quad \checkmark$$

Note: When converting **decimal to binary**, divide by **2** repeatedly and read the remainders **from bottom to top**.

Decimal to Binary Conversion Practice Questions

Basic Questions

1. $5_{10} = ?_2$
2. $8_{10} = ?_2$
3. $10_{10} = ?_2$
4. $15_{10} = ?_2$
5. $20_{10} = ?_2$
6. $25_{10} = ?_2$

4-Digit Decimal Numbers

7. $1024_{10} = ?_2$
8. $1200_{10} = ?_2$
9. $1260_{10} = ?_2$
10. $1500_{10} = ?_2$
11. $2000_{10} = ?_2$
12. $4095_{10} = ?_2$

Challenge Questions

13. $345_{10} = ?_2$
14. $512_{10} = ?_2$
15. $999_{10} = ?_2$
16. $2048_{10} = ?_2$

Note: You can do **1 to 2 examples** from each section. The extra examples are added only for **better understanding and extra practice**.

Octal to Binary and Binary to Octal

The **Octal Number System** has a base of **8** and uses the digits **0 to 7**.

The **Binary Number System** has a base of **2** and uses only **0 and 1**.

The conversion between octal and binary is easy because:

Note: 1 octal digit = 3 binary bits.

To convert an octal number into binary, **replace each octal digit with its 3-bit binary equivalent**.

Octal	Binary
0	000
1	001
2	010
3	011
4	100
5	101
6	110
7	111

Example: Convert 5_8 to Binary

From the table:

$$5_8 = 101_2$$

2		5
2		2 - 1
		1 - 0

Example: Convert 25_8 to Binary

Convert each octal digit separately:

2	→	010
5	→	101

Therefore:

$$25_8 = 010101_2$$

Leading zeros can be removed:

$$25_8 = 10101_2$$

2		2
2		1 - 0

But because **1 octal digit = 3 binary bits**, we add a **leading zero**:

$$2_8 = 010_2$$

Note: The extra zero is added **only to make the binary representation 3 bits**, because each octal digit corresponds to exactly **3 binary bits**.

2		5
2		2 - 1
		1 - 0

Convert 010101_2 to Octal

$$010_2$$

$$= (0 \times 2^2) + (1 \times 2^1) + (0 \times 2^0)$$

$$= (0 \times 4) + (1 \times 2) + (0 \times 1)$$

$$= 0 + 2 + 0$$

$$= 2_8$$

So:

$$010_2 = 2_{10}$$

Since 2 is already an octal digit:

$$010_2 = 2_8 \quad \checkmark$$

Note: For binary-to-octal conversion, remember that **1 octal digit = 3 binary bits**.
Therefore, **010**₂ represents the single octal digit **2**₈.

$$101_2$$

$$= (1 \times 2^2) + (0 \times 2^1) + (1 \times 2^0)$$

$$= (1 \times 4) + (0 \times 2) + (1 \times 1)$$

$$= 4 + 0 + 1$$

$$= 5_8$$

Since 5 is already an octal digit:

$$101_2 = 5_8 \quad \checkmark$$

$$\text{Therefore: } 010101_2 = 25_8 \quad \checkmark$$

Practice Questions: Octal ↔ Binary

A. Convert Octal to Binary

Convert the following **octal numbers into binary**:

1. $3_8 = ?_2$
2. $5_8 = ?_2$
3. $7_8 = ?_2$
4. $12_8 = ?_2$
5. $25_8 = ?_2$
6. $34_8 = ?_2$
7. $47_8 = ?_2$
8. $105_8 = ?_2$
9. $246_8 = ?_2$
10. $725_8 = ?_2$

B. Convert Binary to Octal

Convert the following **binary numbers into octal**:

1. $011_2 = ?_8$
2. $101_2 = ?_8$
3. $110_2 = ?_8$
4. $010101_2 = ?_8$
5. $011100_2 = ?_8$
6. $100111_2 = ?_8$
7. $101010_2 = ?_8$
8. $001101011_2 = ?_8$
9. $010100110_2 = ?_8$
10. $111101101_2 = ?_8$

More Practice

11. $11_2 = ?_8$
12. $1001_2 = ?_8$
13. $10110_2 = ?_8$
14. $110101_2 = ?_8$
15. $1000111_2 = ?_8$
16. $10100110_2 = ?_8$
17. $111010011_2 = ?_8$

Note: Always start grouping the binary digits **from the right**. If the first group has only **1 or 2 bits**, add leading zeros to make a group of **3 bits**.

Examples

$1101_2 \rightarrow 1 \mid 101 \rightarrow 001 \mid 101$

$10101_2 \rightarrow 10 \mid 101 \rightarrow 010 \mid 101$

Hexadecimal to Binary and Binary to Hexadecimal

The **Hexadecimal Number System** has a base of **16** and uses the digits **0–9** and the letters **A–F**.

The **Binary Number System** has a base of **2** and uses only **0 and 1**.

The conversion between hexadecimal and binary is easy because:

Note: 1 hexadecimal digit = 4 binary bits. Therefore, each hexadecimal digit can be directly replaced by its **4-bit binary equivalent**.

Hexadecimal to Binary

To convert a hexadecimal number into binary, **replace each hexadecimal digit with its 4-bit binary equivalent**.

Hexadecimal	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101

Hexadecimal	Binary
6	0110
7	0111
8	1000
9	1001
A	1010
B	1011
C	1100
D	1101
E	1110
F	1111

Example: Convert 5_{16} to Binary

From the conversion table:

$$5_{16} = 0101_2$$

We can also verify this by converting 5 into decimal and then binary:

$$\begin{array}{r|l}
 2 & 5 \\
 2 & 2 - 1 \\
 & 1 - 0
 \end{array}$$

Reading the remainders from bottom to top:

$$5_{16} = 101_2$$

But because **1 hexadecimal digit = 4 binary bits**, we add a leading zero:

$$5_{16} = 0101_2$$

Note: The extra leading zero is added **only to make the binary representation 4 bits**, because each hexadecimal digit corresponds to exactly **4 binary bits**.

Example: Convert $2A_{16}$ to Binary

Convert each hexadecimal digit separately:

$2 \rightarrow 0010$

$A \rightarrow 1010$

Therefore:

$$2A_{16} = 00101010_2$$

Leading zeros can be removed when they are not required:

$$2A_{16} = 101010_2$$

Binary to Hexadecimal

To convert a binary number into hexadecimal, **group the binary digits into groups of 4 bits from the right**. Then replace each 4-bit group with its hexadecimal equivalent.

Note: Always start grouping the binary digits **from the right**. If the first group has only **1, 2, or 3 bits**, add leading zeros to make a group of **4 bits**.

Convert 1010_2 to Hexadecimal

$$1010_2$$

$$= (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (0 \times 2^0)$$

$$= (1 \times 8) + (0 \times 4) + (1 \times 2) + (0 \times 1)$$

$$= 8 + 0 + 2 + 0$$

$$= 10_{16}$$

Since 10 in hexadecimal is represented by A:

$$1010_2 = A_{16} \quad \checkmark$$

Convert 0010_2 to Hexadecimal

$$0010_2$$

$$= (0 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (0 \times 2^0)$$

$$= (0 \times 8) + (0 \times 4) + (1 \times 2) + (0 \times 1)$$

$$= 0 + 0 + 2 + 0$$

$$= 2_{16}$$

$$0010_2 = 2_{16} \quad \checkmark$$

Convert 00101010_2 to Hexadecimal

First, group the binary digits into groups of 4 from the right:

$$00101010_2$$

$$0010 \mid 1010$$

Now convert each group:

$$0010 \rightarrow 2$$

$$1010 \rightarrow A$$

Therefore:

$$00101010_2 = 2A_{16} \quad \checkmark$$

Note: For binary-to-hexadecimal conversion, **1 hexadecimal digit = 4 binary bits**.
Therefore, every group of 4 binary bits represents exactly one hexadecimal digit.

More Grouping Examples

$1101_2 \rightarrow 1101 \rightarrow D$

Therefore: $1101_2 = D_{16}$

$10101_2 \rightarrow 1 \mid 0101 \rightarrow 0001 \mid 0101$

Therefore: $10101_2 = 15_{16}$

$110101_2 \rightarrow 1101 \mid 0101$

Therefore: $110101_2 = D5_{16}$

Practice Questions: Hexadecimal ↔ Binary

A. Convert Hexadecimal to Binary

Convert the following **hexadecimal numbers into binary**:

1. $3_{16} = ?_2$
2. $5_{16} = ?_2$
3. $A_{16} = ?_2$
4. $F_{16} = ?_2$
5. $12_{16} = ?_2$
6. $2A_{16} = ?_2$
7. $3F_{16} = ?_2$
8. $4B_{16} = ?_2$
9. $7C_{16} = ?_2$
10. $AF_{16} = ?_2$

B. Convert Binary to Hexadecimal

Convert the following **binary numbers into hexadecimal**:

1. $0011_2 = ?_{16}$
2. $0101_2 = ?_{16}$
3. $1010_2 = ?_{16}$
4. $1111_2 = ?_{16}$

5. $00101010_2 = ?_{16}$
6. $00111111_2 = ?_{16}$
7. $01001011_2 = ?_{16}$
8. $01111100_2 = ?_{16}$
9. $10101111_2 = ?_{16}$
10. $11011010_2 = ?_{16}$

More Practice

11. $1101_2 = ?_{16}$
12. $10101_2 = ?_{16}$
13. $110101_2 = ?_{16}$
14. $1000111_2 = ?_{16}$
15. $10100110_2 = ?_{16}$
16. $111010011_2 = ?_{16}$
17. $1011010110_2 = ?_{16}$

Note: Always start grouping the binary digits **from the right**. If the first group has only **1, 2, or 3 bits**, add leading zeros to make a group of **4 bits**.

Examples of Binary Grouping

$1101_2 \rightarrow 1101 \rightarrow D$

$10101_2 \rightarrow 1 \mid 0101 \rightarrow 0001 \mid 0101$

$110101_2 \rightarrow 1101 \mid 0101$

$1000111_2 \rightarrow 1 \mid 0001 \mid 11 \rightarrow 0001 \mid 0001 \mid 11$

Decimal to Octal Conversion and Vice versa

To convert a **decimal number into octal**, divide the decimal number repeatedly by **8**. Write the remainders and read them **from bottom to top**.

Example: Convert 25_{10} to Octal

```
8 | 25
8 | 3 - 1
  | 0 - 3
```

Now read the remainders **from bottom to top**:

3 1

Therefore:

$$25_{10} = 31_8 \quad \checkmark$$

Note: Do not add a leading zero unless it is specifically needed to show a fixed number of digits. Therefore, $25_{10} = 31_8$, not 031_8 .

Convert 31_8 to Decimal

Multiply each octal digit by its corresponding power of **8**, starting from the right with 8^0 :

$$\begin{aligned} &31_8 \\ &= (3 \times 8^1) + (1 \times 8^0) \\ &= (3 \times 8) + (1 \times 1) \\ &= 24 + 1 \\ &= 25_{10} \end{aligned}$$

Therefore:

$$31_8 = 25_{10} \quad \checkmark$$

Practice Questions: Decimal $\leftrightarrow$ Octal

A. Convert Decimal to Octal

Convert the following **decimal numbers into octal**:

1. $8_{10} = ?_8$
2. $15_{10} = ?_8$
3. $25_{10} = ?_8$
4. $40_{10} = ?_8$
5. $64_{10} = ?_8$
6. $100_{10} = ?_8$
7. $125_{10} = ?_8$
8. $250_{10} = ?_8$
9. $500_{10} = ?_8$
10. $1000_{10} = ?_8$

B. Convert Octal to Decimal

Convert the following **octal numbers into decimal** using the **multiplication method**:

1. $7_8 = ?_{10}$
2. $12_8 = ?_{10}$
3. $25_8 = ?_{10}$
4. $31_8 = ?_{10}$
5. $45_8 = ?_{10}$
6. $100_8 = ?_{10}$
7. $125_8 = ?_{10}$
8. $250_8 = ?_{10}$
9. $345_8 = ?_{10}$
10. $1000_8 = ?_{10}$

Note: For decimal-to-octal conversion, repeatedly **divide by 8** and read the remainders **from bottom to top**. For octal-to-decimal conversion, multiply each digit by its corresponding power of **8**, starting from the right with 8^0 .

Trick to Solve Bigger Questions

Example: Convert 4455_{10} to Octal

First divide **4455** by **8**:

$$4455 \div 8 = 556.875$$

The whole-number quotient is **556** and the decimal part is **0.875**.

Now find the remainder:

$$0.875 \times 8 = 7$$

So the remainder is **7**.

Then continue with **556**:

$$556 \div 8 = 69.5$$

$$0.5 \times 8 = 4$$

So the remainder is **4**.

Continue:

$$69 \div 8 = 8.625$$

$$0.625 \times 8 = 5$$

Remainder = **5**

Continue:

$$8 \div 8 = 1$$

Remainder = **0**

Finally:

$$1 \div 8 = 0.125$$

$$0.125 \times 8 = 1$$

Remainder = **1**

Now read the remainders **from bottom to top**:

$$1 \rightarrow 0 \rightarrow 5 \rightarrow 4 \rightarrow 7$$

Therefore:

$$4455_{10} = 10547_8 \quad \checkmark$$

Data Representation in Computing Systems

Computers can **store and process different types of information**. To store this information, computers represent data using **binary digits (0 and 1)**.

One important type of data is **numeric data**, which includes whole numbers and integers.

1. Whole Numbers (W)

Whole numbers are numbers that include **zero and all positive numbers**. They do not include negative numbers or fractions.

Mathematically:

$$W = \{0, 1, 2, 3, 4, \dots\}$$

Examples

- Number of students = **50**
- Age = **18**
- Number of books = **25**

These values cannot normally be negative.

Whole Number Storage

A **byte** consists of **8 bits**. The more bytes used, the more values a computer can store. For **n bits**, the maximum whole number is:

Maximum value = $2^n - 1$

Storage	Bits	Maximum Value
1 Byte	8 bits	$2^8 - 1 = 255$
2 Bytes	16 bits	$2^{16} - 1 = 65,535$
4 Bytes	32 bits	$2^{32} - 1 = 4,294,967,295$

For example, an 8-bit whole number can represent values from:

$00000000_2 = 0_{10}$

to

$11111111_2 = 255_{10}$

2. Integers (Z)

Integers include **positive numbers, negative numbers, and zero**.

Mathematically:

$Z = \{..., -3, -2, -1, 0, 1, 2, 3, ...\}$

In computing, these are called **signed integers** because they can represent both positive and negative values.

Sign Bit

To represent positive and negative numbers, one bit is used as the **sign bit**. It is usually the **most significant bit (MSB)**.

- **0** → Positive
- **1** → Negative

Note: MSB (Most Significant Bit) is the leftmost bit in a binary number and usually has the highest place value. **LSB (Least Significant Bit)** is the rightmost bit and has the lowest place value.

Example:

```
Binary Number:  1 0 1 1 0 1 0 1
                ↑          ↑
                MSB       LSB
                (leftmost) (rightmost)
```

In 10110101_2 :

- **MSB = 1** → the leftmost bit.
- **LSB = 1** → the rightmost bit.

For an **8-bit signed integer**, one bit is used for the sign, leaving **7 bits** for the value.

The maximum positive value is:

$$2^7 - 1 = 127$$

So, the maximum positive value is:

$$01111111_2 = 127_{10}$$

Negative values are commonly stored using **2's complement**.

1's Complement

1's complement is a method of representing signed binary numbers.

To find the **1's complement**, simply **invert every bit**:

- **0 → 1**
- **1 → 0**

Example

```
Original:        00000101
1's complement:  11111010
```

So, the 1's complement of 00000101_2 is 11111010_2 .

2's Complement

2's complement is the common method used by computers to represent **negative integers**.

To find the 2's complement:

1. **Invert all the bits** to get the 1's complement.
2. **Add 1** to the result.

Example: Represent -5 in 8 Bits

First, write **+5** in binary:

```
0000101
```

Step 1: Invert all bits

```
1111010
```

Step 2: Add 1

```
  1111010
+ 0000001
-----
  1111011
```

Therefore:

$-5_{10} = 1111011_2$ in 8-bit 2's complement.

5. Minimum Integer Value

For an **n-bit signed integer**, the minimum value is:

Minimum value = -2^{n-1}

For an **8-bit integer**:

$-2^7 = -128$

Therefore, an 8-bit signed integer can represent values from:

–128 to +127

Examples

Storage	Bits	Minimum Value	Maximum Value
1 Byte	8	–128	127
2 Bytes	16	–32,768	32,767
4 Bytes	32	–2,147,483,648	2,147,483,647

Note: Whole numbers can represent **0 and positive values**, while integers can represent **negative, zero, and positive values**. Computers commonly use **2's complement** to store negative integers.

Binary Arithmetic

Binary arithmetic is the process of performing **addition, subtraction, multiplication, and division** using only **0 and 1**.

1. Binary Addition

Rules

Operation	Result
0 + 0	0
0 + 1	1
1 + 0	1
1 + 1	10
1 + 1 + 1	11

Example 1

```
  101
+ 011
-----
 1000
```

$$101_2 + 011_2 = 1000_2$$

Example 2

```
  1101
+ 0011
-----
 10000
```

$$1101_2 + 0011_2 = 10000_2$$

Example 3

```
 10110
+ 01101
-----
100011
```

$$10110_2 + 01101_2 = 100011_2$$

2. Binary Subtraction

Rules

Operation	Result
$0 - 0$	0
$1 - 0$	1
$1 - 1$	0
$10 - 1$	1

When $0 - 1$ occurs, we borrow from the next position.

Example 1

```

  1010
- 0011
-----
  0111

```

$$1010_2 - 0011_2 = 0111_2$$

Example 2

```

  1101
- 0101
-----
  1000

```

$$1101_2 - 0101_2 = 1000_2$$

Example 3

```

  10000

```



```
- 00111
```

```
-----
```

```
01001
```

$$10000_2 - 00111_2 = 01001_2$$

3. Binary Multiplication

Rules

Operation	Result
0×0	0
0×1	0
1×0	0
1×1	1

Example 1

```
  101
```

```
×  10
```

```
-----
```

```
 000
```

```
+ 1010
```

```
-----
```

```
1010
```

$$101_2 \times 10_2 = 1010_2$$

Example 2

```

      101
    ×  11
    ----
      101
+   1010
    ----
     1111

```

$$101_2 \times 11_2 = 1111_2$$

Example 3

```

      110
    × 101
    ----
      110
     000
+  11000
    ----
   11110

```

$$110_2 \times 101_2 = 11110_2$$

4. Binary Division

Binary division follows the same basic process as **decimal long division**.

Example 1

```

      10
    ----
10 ) 100
    10
    --
     00

```

0
--
0

$$100_2 \div 10_2 = 10_2$$

Example 2

```
      11
    -----
10 ) 110
    10
    --
     10
     10
     --
      0
```

$$110_2 \div 10_2 = 11_2$$

Example 3

```
     101
    -----
10 ) 1010
    10
    --
     01
     0
     --
      10
      10
      --
       0
```

$$1010_2 \div 10_2 = 101_2$$

Binary Subtraction Using 2's Complement

In binary arithmetic, **subtraction** can also be performed by adding the **2's complement** of the subtrahend to the minuend.

Note: Minuend is the number from which another number is subtracted.

Subtrahend is the number that is subtracted from the minuend.

Example: In $9 - 6$, **9** is the **minuend** and **6** is the **subtrahend**.

Example: Subtract 6 from 9

Minuend = $9_{10} = 1001_2$

Subtrahend = $6_{10} = 0110_2$

Step 1: Find the 2's Complement of the Subtrahend

Subtrahend:

0110

Invert all the bits:

1001

Add 1:

```
  1001
+ 0001
-----
  1010
```

Therefore, the 2's complement of 0110_2 is 1010_2 .

Step 2: Add the Minuend and 2's Complement

```
  1001
+ 1010
-----
 10011
```

Step 3: Discard the Carry Bit

The result is:

```
 10011
   ↑
  Carry
```

Discard the leftmost carry:

```
0011
```

$$0011_2 = 3_{10}$$

Therefore:

$$9_{10} - 6_{10} = 3_{10} \quad \checkmark$$

or

$$1001_2 - 0110_2 = 0011_2 \quad \checkmark$$

Note: In 2's complement subtraction, first find the **2's complement of the subtrahend**, add it to the **minuend**, and **discard the final carry** if one is produced.

Common Text Encoding Schemes

Computers store text as **binary data (0s and 1s)**. Text encoding schemes convert **letters, numbers, and symbols** into a form that computers can understand and store.

1. ASCII

ASCII stands for **American Standard Code for Information Interchange**.

It uses **7 bits** and represents **128 characters**.

Example

When you type **A**, ASCII represents it as **65**.

A → 65

Note: ASCII uses **7 bits**, so it can represent $2^7 = 128$ characters.

2. Extended ASCII

Extended ASCII uses **8 bits** and can represent up to **256 characters**.

It includes additional symbols and **special characters** that are not included in standard ASCII.

Example

Some extended ASCII character sets can represent additional characters such as **β** (**Greek beta**) and other special symbols.

Note: Extended ASCII is not one single universal character set. Different systems may use different 8-bit character sets for the additional 128 characters.

3. Unicode

Unicode is a character standard used to represent characters from **different languages and writing systems**.

Example

Unicode can represent English **A**, Urdu **ا**, Arabic **ع**, Chinese **中**, and many other characters.

Common Unicode encoding formats are:

- **UTF-8**
- **UTF-16**
- **UTF-32**

UTF stands for **Unicode Transformation Format**.

4. UTF-8

UTF-8 is a variable-length encoding that uses **1 to 4 bytes** for a character. It is **backward compatible with ASCII**. This means that standard ASCII characters use the same byte values in UTF-8.

Examples

A → 01000001 → 1 byte

An Urdu character such as ا requires **2 bytes** in UTF-8.

Note: UTF-8 uses fewer bytes for many common characters, especially English characters, which makes it efficient for storing and transmitting text.

5. UTF-16

UTF-16 is a variable-length encoding that uses **2 or 4 bytes** for a character.

Example

A → 00000000 01000001 → 2 bytes

Most commonly used characters require **2 bytes**, while some characters require **4 bytes**.

6. UTF-32

UTF-32 is a fixed-length encoding that uses exactly **4 bytes** for every character.

Example

A → 00000000 00000000 00000000 01000001

Therefore, the character **A** takes **4 bytes** in UTF-32.

Comparison of Text Encoding Schemes

Encoding	Size	Characters / Purpose
ASCII	7 bits	128 characters

Encoding	Size	Characters / Purpose
Extended ASCII	8 bits	Up to 256 characters
Unicode	Character standard	Characters from many languages
UTF-8	1–4 bytes	Variable-length Unicode encoding
UTF-16	2–4 bytes	Variable-length Unicode encoding
UTF-32	4 bytes	Fixed-length Unicode encoding

How Computers Store Files

Computers store **all types of files**, such as **images, audio, videos, and documents**, as **binary data (0s and 1s)**.

Storage Devices

1. Hard Disk Drive (HDD)

A **Hard Disk Drive (HDD)** uses **spinning disks** to read and write data. It usually provides a **large storage capacity**.

2. Solid State Drive (SSD)

A **Solid State Drive (SSD)** uses **flash memory** to store data. It provides **faster access and better performance** than an HDD.

Example

When you save a photo on your laptop, the photo is converted into **binary data** and stored on the computer's **HDD or SSD**.

3. Cloud Storage

Cloud storage stores files on **remote servers** that can be accessed through the **internet**.

It is useful for **backup** and for accessing files from **different devices**.

Examples of Cloud Storage

- Google Drive
- OneDrive
- Dropbox
- iCloud
- Google Photos

Note: Regardless of the type of file, computers ultimately store and process digital data in the form of **0s and 1s**. Different file types use different formats to organize this binary data.

Multiple Choice Questions (MCQs) on Introduction To Computational Systems

1. What is a computational system?

- a. A system used only for entertainment
- b. A system that processes data to produce useful information
- c. A system used only for communication
- d. A system that only stores files

Answer: b. A system that processes data to produce useful information

2. What is the main purpose of a computational system?

- a. To process data
- b. To play games
- c. To display pictures only
- d. To print documents only

Answer: a. To process data

3. Which of the following is a component of a computational system?

- a. Furniture
- b. Electricity bill
- c. Hardware
- d. Office building