

SE 350  
Operating  
Systems



# Lecture 5: Uniprocessor Scheduling

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# Outline

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- History
- Definitions
  - Response time, throughput, scheduling policy, ...
- Uniprocessor scheduling policies
  - FCFS, SJF/SRTF, RR, ...

# A Bit of History on Scheduling

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- By year 2000, scheduling was considered a solved problem

*“And you have to realize that there are not very many things that have aged as well as the scheduler. Which is just another proof that scheduling is easy.”*

Linus Torvalds, 2001<sup>[1]</sup>

- End to Dennard scaling in 2004, led to multiprocessor era
  - Designing new (multiprocessor) schedulers gained traction
  - Energy efficiency became top concern
- In 2016, it was shown that bugs in Linux kernel scheduler could cause up to **138x slowdown** in some workloads with proportional energy waist<sup>[2]</sup>

[1] L. Torvalds. The Linux Kernel Mailing List. <http://tech-insider.org/linux/research/2001/1215.html>, Feb. 2001.

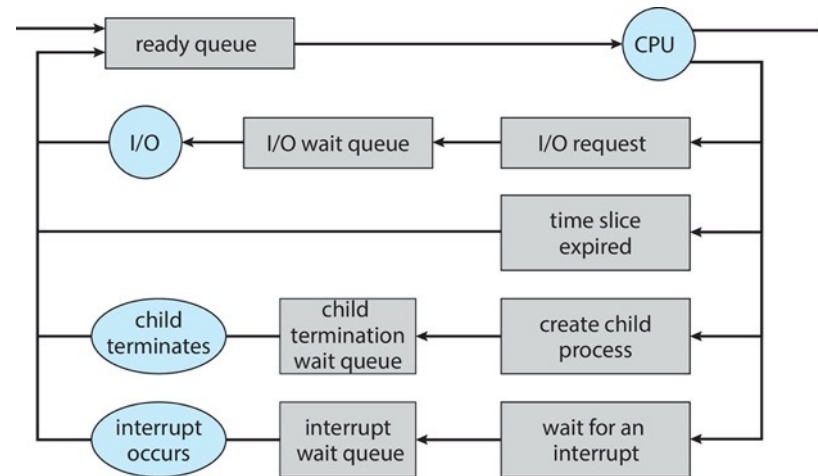
[2] Lozi, Jean-Pierre, et al. "The Linux scheduler: a decade of wasted cores." Proceedings of the Eleventh European Conference on Computer Systems. 2016.

# Definitions

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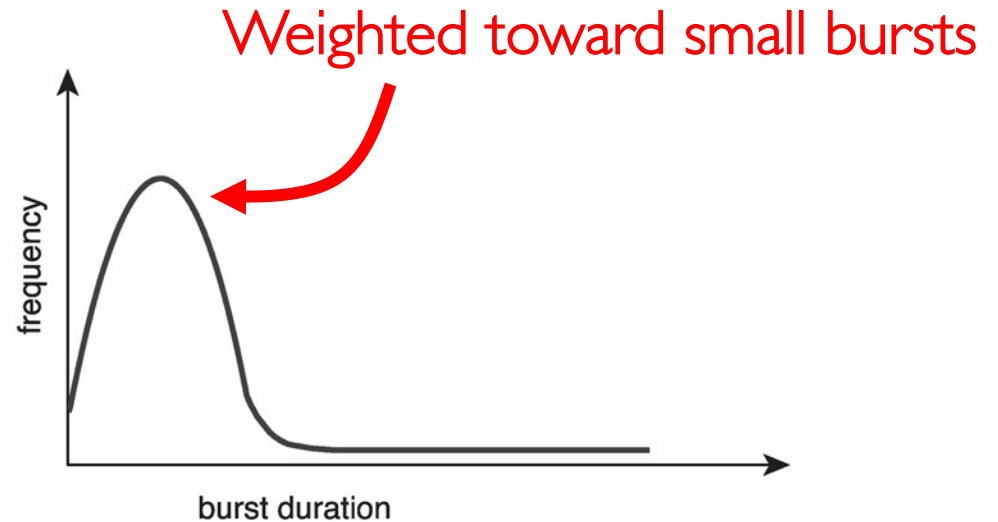
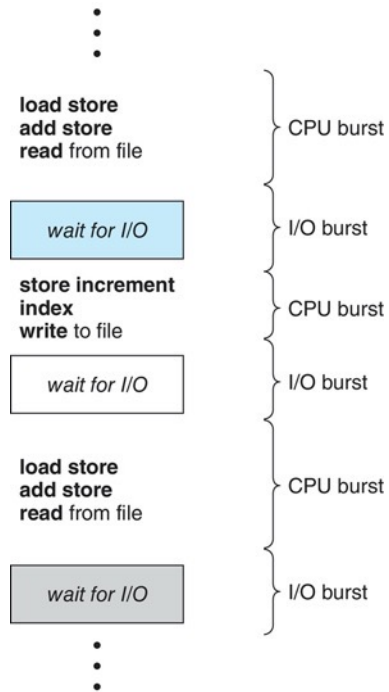
- **Task, thread, process, job**: unit of work
  - E.g., mouse click, web request, shell command, etc.)
- **Workload**: set of tasks
- **Scheduling algorithm**: takes workload as input, decides which tasks to do first
- **Overhead**: amount of extra work that is done by scheduler
- **Preemptive scheduler**: CPU can be taken away from a running task
- **Work-conserving scheduler**: CPUs won't be left idle if there are ready tasks to run
  - For non-preemptive schedulers, work-conserving is not always better (why?)
- **Only preemptive, work-conserving schedulers to be considered in this lecture!**

# Recall: CPU Scheduling



- Earlier, we talked about life-cycle of threads
  - Threads work their way from ready to running to various waiting queues
- **Question:** how does OS decide which thread to dequeue?
  - Obvious queue to worry about is ready queue
  - Others can be scheduled as well, however
- **Scheduling:** deciding which thread gets resource from moment to moment

# Execution Model



- Programs alternate between bursts of CPU and I/O
  - Use CPU for some period, then do I/O, then use CPU again, etc.
- CPU scheduling is about choosing thread which gets CPU for its next CPU burst
- With preemption, thread may be forced to give up CPU before finishing its burst

# CPU Scheduling Assumptions

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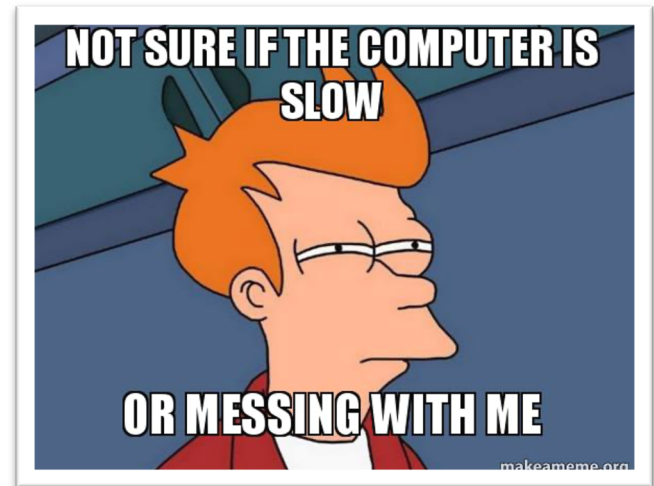
- There are many implicit assumptions for CPU scheduling
  - **One** program per user
  - **One** thread per program
  - Programs are **independent**
- These may not hold in all systems, but they simplify the problem
- High-level goal is to divide CPU time to optimize some desired properties



# Performance

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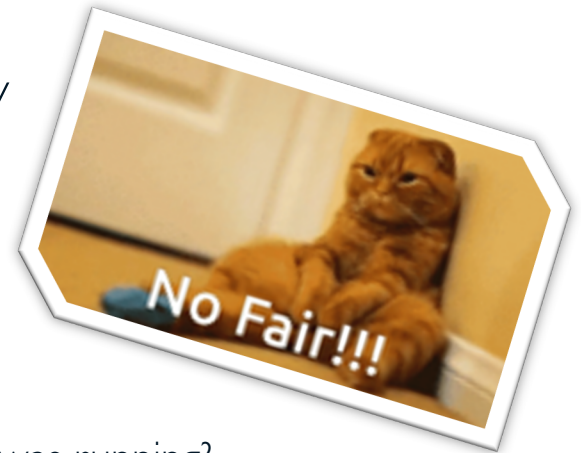
- Minimize **average response time**
  - Minimize avg. elapsed time to finish tasks
  - Response time is what users see
    - E.g., time to echo a keystroke in editor
    - E.g., time to compile a program
    - **Real-time tasks** must meet **deadlines** (more on this later)
- Maximize **throughput**
  - Maximize tasks per time unit (e.g., tasks per second)
  - Related to response time, but not identical
    - Minimizing response time could lead to more context switching which will than hurt throughput (more on this later)
  - Two parts to maximizing throughput
    - Minimize overhead (e.g., context-switching)
    - Efficient use of resources (e.g., CPU, disk, memory, etc.)



# Fairness

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- Share CPU time among *users* in some *equitable* way
- What does equitable mean?
  - Equal share of CPU time?
    - What if some tasks don't need their full share?
  - Minimize variance in worst case performance?
    - What if some tasks were running when no one else was running?
- Who are users? Actual users or programs?
  - If A runs one thread and B runs five, B could get five times as much CPU time on many OS's
- Fairness is not minimizing average response time
  - Improving average response time could make system less fair (more on this later)



# First-Come, First-Served (FCFS) Scheduling

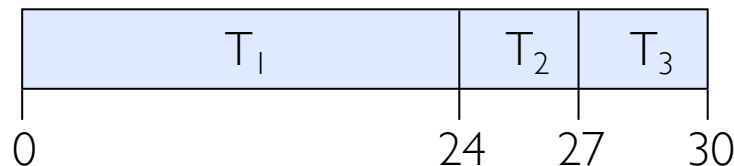
- First-come, first-served (FCFS)
  - Also “first-in, first-out” (FIFO)
  - In early systems, FCFS meant one program scheduled until done (including its I/O activities)
  - Now, it means that program keeps CPU until the end of its CPU burst



- Example

<u>Thread</u>	<u>CPU Burst Time</u>
$T_1$	24
$T_2$	3
$T_3$	3

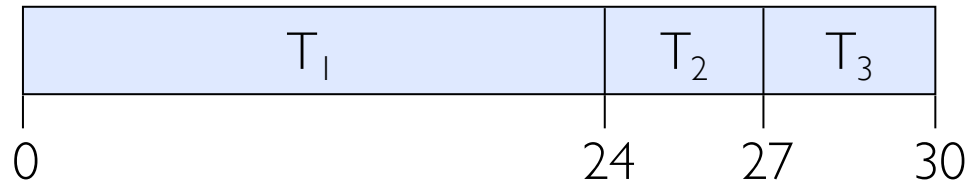
- Suppose threads arrive in order:  $T_1, T_2, T_3$



# FCFS Scheduling (cont.)

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- Example continued



- Wait time for  $T_1$  is 0, for  $T_2$  is 24, and for  $T_3$  is 27
- Average wait time is  $(0 + 24 + 27)/3 = 17$
- Average response time is  $(24 + 27 + 30)/3 = 27$

# FCFS Scheduling (cont.)

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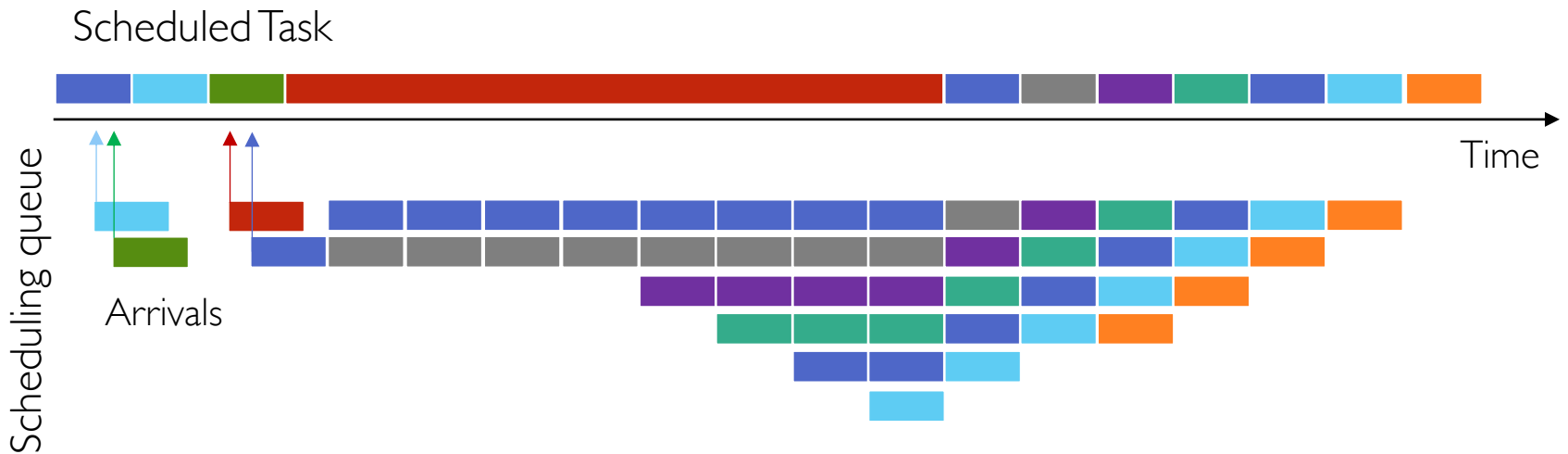
- If threads arrive in order:  $T_2, T_3, T_1$ , then we have



- Wait time for  $T_1$  is 6, for  $T_2$  is 0, and for  $T_3$  is 3
  - Average wait time is  $(6 + 0 + 3)/3 = 3$
  - Average response time is  $(3 + 6 + 30)/3 = 13$
  - Average wait time is much better (before it was 17)
  - Average response time is better (before it was 27)
- Pros and cons of FCFS
    - + Simple
    - - Short tasks get stuck behind long ones

# Convoy Effect

- With FCFS, convoys of small tasks tend to build up when a large one is running



# Round Robin (RR) Scheduling

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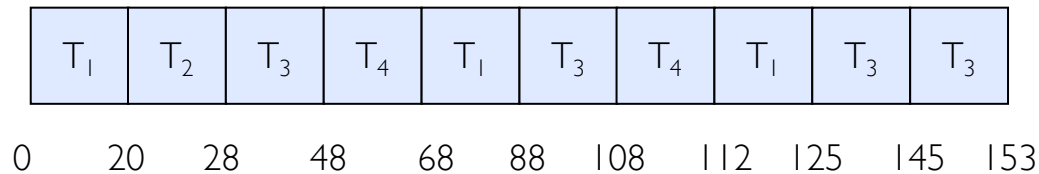
- FCFS is potentially bad for short tasks!
  - Depends on submit order
  - If you are first in line at supermarket with milk, you don't care who is behind you, on the other hand...
- Round robin
  - Each thread gets small unit of CPU time, called *time quantum* (usually 10-100 milliseconds)
  - Once quantum expires, thread is preempted and added to end of ready queue
  - $N$  threads in ready queue and time quantum is  $q \Rightarrow$ 
    - Each thread gets  $1/N$  of CPU time in chunks of **at most**  $q$  time units
    - **No thread waits more than  $(N-1)q$  time units**



# Example: RR with Time Quantum of 20

- Example

<u>Thread</u>	<u>Burst Time</u>
T <sub>1</sub>	53
T <sub>2</sub>	8
T <sub>3</sub>	68
T <sub>4</sub>	24



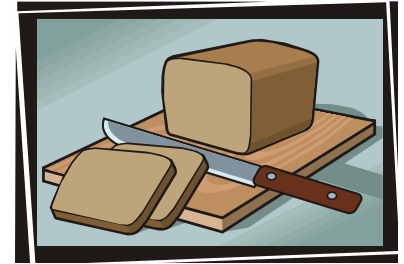
- Wait time for T<sub>1</sub> = (68 - 20) + (112 - 88) = 72  
T<sub>2</sub> = (20 - 0) = 20  
T<sub>3</sub> = (28 - 0) + (88 - 48) + (125 - 108) = 85  
T<sub>4</sub> = (48 - 0) + (108 - 68) = 88
- Average wait time is (72 + 20 + 85 + 88) / 4 = 66¼
- Average response time is (125 + 28 + 153 + 112) / 4 = 104½



# Round Robin Discussion

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- Pros and cons of RR
  - + Better for short tasks, fair
  - – Context-switching time adds up for long tasks
- How does performance change with time quantum?
  - What if it's too long?
    - Response time suffers!
  - What if it's too short?
    - Throughput suffers!
  - What if it's infinite ( $\infty$ )?
    - RR  $\Rightarrow$  FCFS
  - Time quantum must be long compared to context switching time, otherwise overhead will be too high



# Round Robin Time Quantum

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- Assume there is no context switching overhead
- What happens when we decrease  $Q$ ?
  1. Avg. response time always decreases or stays the same
  2. Avg. response time always increases or stays the same
  3. Avg. response time can increase, decrease, or stays the same

# Decrease Response Time

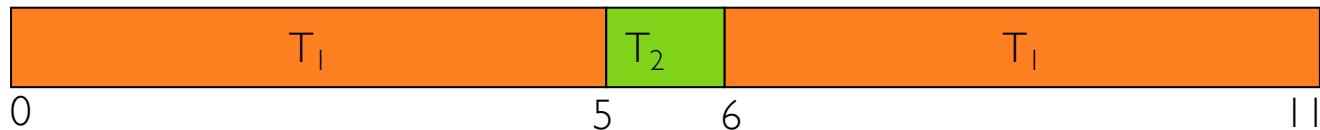
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- $T_1$ : burst time 10
- $T_2$ : burst time 1
- $Q = 10$



- Average response time =  $(10 + 11)/2 = 10.5$

- $Q = 5$

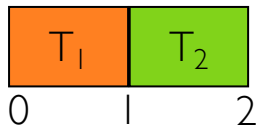


- Average response time =  $(6 + 11)/2 = 8.5$

# Same Response Time

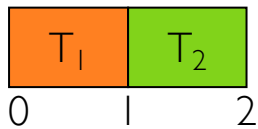
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- $T_1$ : burst time 1
- $T_2$ : burst time 1
- $Q = 10$



- Average response time =  $(1 + 2)/2 = 1.5$

- $Q = 1$

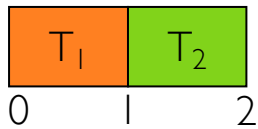


- Average response time =  $(1 + 2)/2 = 1.5$

# Increase Response Time

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- $T_1$ : burst time 1
- $T_2$ : burst time 1
- $Q = 1$



- Average response time =  $(1 + 2)/2 = 1.5$
- $Q = 0.5$



- Average response time =  $(1.5 + 2)/2 = 1.75$

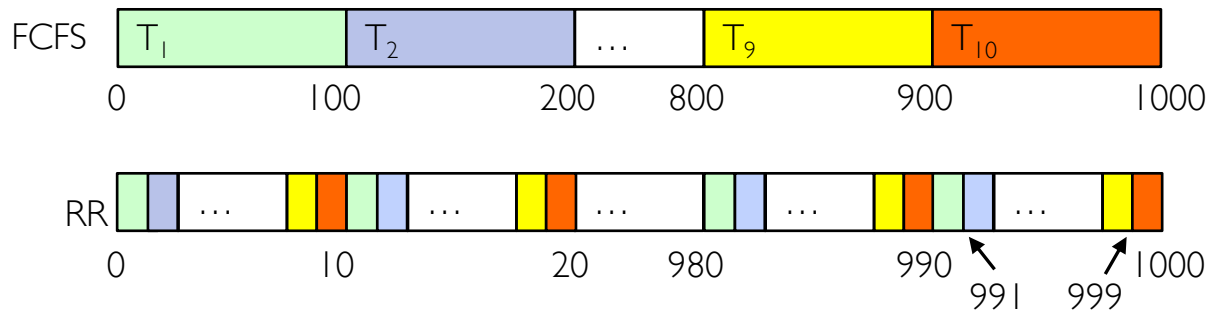
# Round Robin Discussion (cont.)

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- Actual choices of time quantum
  - Initially, UNIX time quantum was one second
    - Worked ok when UNIX was used by one or two users
    - What if you use text editor while there are three compilations going on?
      - It takes 3 seconds to echo each keystroke!
  - Need to balance short-task performance and long-task throughput
    - Typical time quantum today is between 10ms – 100ms
    - Typical context-switching overhead is 0.1ms – 1ms
    - Roughly 1% overhead due to context-switching

# FCFS vs. RR

- Assuming zero-cost context-switching time, is RR always better than FCFS?
- Suppose there are 10 tasks, each take 100s of CPU time, RR quantum is 1s



- Completion times

Task #	FCFS	RR
1	100	991
2	200	992
...	...	...
9	900	999
10	1000	1000

# FCFS vs. RR (cont.)

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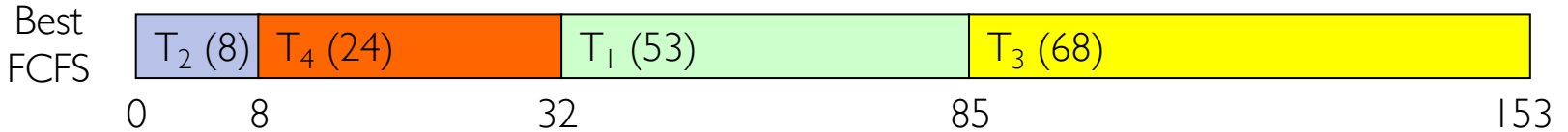
- Completion times

Task #	FCFS	RR
1	100	991
2	200	992
...	...	...
9	900	999
10	1000	1000

- Both RR and FCFS finish at the same time
- Average response time is much worse under RR!
  - Bad when all threads have the same length
- Also, cache must be shared between all tasks with RR but can be devoted to each task with FIFO
  - Total time for RR is longer even for zero-cost context switching!

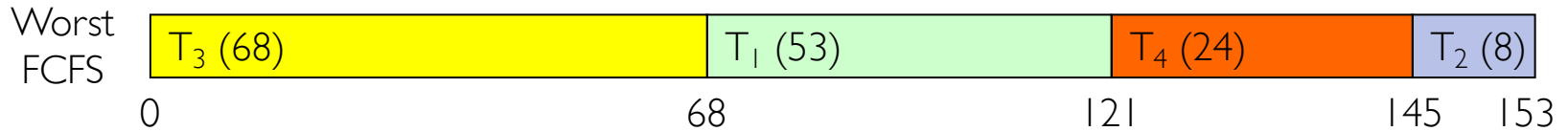


# Earlier Example: RR vs. FCFS, Effect of Different Time Quanta



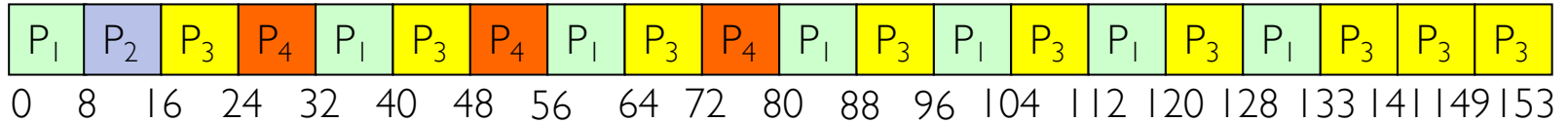
	Quantum	T1	T2	T3	T4	Average
Wait Time	Best FCFS	32	0	85	8	31¼
	1					
	5					
	8					
	10					
	20					
	Worst FCFS					
Response Time	Best FCFS	85	8	153	32	69½
	1					
	5					
	8					
	10					
	20					
	Worst FCFS					

# Earlier Example: RR vs. FCFS, Effect of Different Time Quanta (cont.)



	Quantum	T1	T2	T3	T5	Average
Wait Time	Best FCFS	32	0	85	8	31¼
	1					
	5					
	8					
	10					
	20					
	Worst FCFS	68	145	0	121	83½
	Response Time	Best FCFS	85	8	153	32
1						
5						
8						
10						
20						
Worst FCFS		121	153	68	145	121¾

# Earlier Example: RR vs. FCFS, Effect of Different Time Quanta (cont.)



	Quantum	T1	T2	T3	T5	Average
Wait Time	Best FCFS	32	0	85	8	31¼
	1	84	22	85	57	62
	5	82	20	85	58	61¼
	8	80	8	85	56	57¼
	10	82	10	85	68	61¼
	20	72	20	85	88	66¼
	Worst FCFS	68	145	0	121	83½
Response Time	Best FCFS	85	8	153	32	69½
	1	137	30	153	81	100½
	5	135	28	153	82	99½
	8	133	16	153	80	95½
	10	135	18	153	92	99½
	20	125	28	153	112	104½
	Worst FCFS	121	153	68	145	121¾

# Shortest Task First (SJF) Scheduling

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- Could we always mirror best FCFS?
- Shortest task first (SJF)
  - Run task that has least amount of computation to do
  - Sometimes called “Shortest Time to Completion First” (STCF)
- Shortest remaining time first (SRTF)
  - Preemptive version of SJF: if task arrives and has shorter time to completion than remaining time on current task, immediately preempt current task
  - Sometimes called “shortest remaining time to completion first” (SRTCF)
- These can be applied to whole program or current CPU burst
  - Key idea: get short tasks out of system
  - Big effect on short tasks, only small effect on long ones
  - Better average response time

# SJF/SRTF Optimality

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- SJF/SRTF minimize average response time! Why?
  - Consider alternative policy P (not SJF/SRTF) that is optimal
  - At some point, P chooses to run task that is not the shortest
  - Keep order of tasks the same, but run the shorter task first
  - This reduces average response time  $\Rightarrow$  contradiction!

# SJF/SRTF Discussion

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- SJF/SRTF are **best you can** do to minimize average response time
  - Provably optimal (SJF among non-preemptive, SRTF among preemptive)
  - Since SRTF is always at least as good as SJF, we can just focus on SRTF
- Comparison of SRTF with FCFS
  - What if all tasks are the same length?
    - SRTF  $\Rightarrow$  FCFS (i.e., **FCFS is best we can do if all tasks have the same length**)
  - What if tasks have varying length?
    - Unlike FCFS, with SRTF, short tasks do not get stuck behind long ones

# Mix of CPU and I/O Bound Tasks: FCFS vs. RR vs. SRTF

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- Example: suppose there are three tasks
  - A and B are both CPU bound with CPU bursts that last for a week
  - C is I/O bound with iterations of 1ms CPU burst followed by 9ms I/O burst
  - If A or B run by themselves, CPU utilization is 100% and I/O utilization is 0%
  - If C runs by itself, CPU utilization is 10% and I/O utilization is 90%
- What happens under FCFS scheduling policy?
  - Once A or B get in, keep CPU for two weeks  $\Rightarrow$  poor avg. response time
- What about RR or SRTF?
  - Easier to see with a timeline





# Problems with SRTF

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- **Starvation**: large tasks may never run if short ones keep coming
- **Overhead**: short tasks preempt long ones  $\Rightarrow$  too many context switches
- **Unfair**: large tasks are penalized, there is high variance in response time

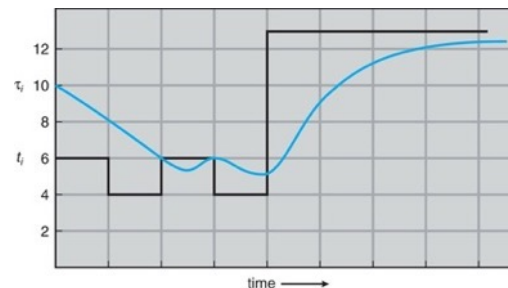
- **Impractical**: we need to somehow predict future

- Some systems ask users
  - When you submit your task, you have to say how long it will take
  - Users could maliciously misreport length of their task
  - E.g., would it work if a supermarket uses SJF?
    - Customers could game the system: come with one item at a time
    - To prevent cheating, systems may kill tasks if they take too long
- It's hard to predict task's runtime even for non-malicious users



# Predicting Length of Next CPU Burst

- **Adaptive**: dynamically make predictions based on past behavior
  - Works because programs have predictable behavior
    - If program was I/O bound in past, it'll likely be I/O bound in future
    - If behavior were random, this approach wouldn't help



- Example: use estimator function on previous bursts
  - Let  $t_{n-1}, t_{n-2}, t_{n-3}, \dots, t_1$  be previous CPU burst lengths
  - Estimate next burst  $\tau_n = f(t_{n-1}, t_{n-2}, t_{n-3}, \dots)$
  - Function  $f$  could be any time series estimator (e.g., Kalman filters, etc.)
  - For instance, exponential averaging  $\tau_n = \alpha t_{n-1} + (1-\alpha)\tau_{n-1}$  with  $(0 < \alpha \leq 1)$

# Aside: Application Types

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- Can we use past burst times to identify application types?
- Consider mix of *interactive* and *high-throughput* programs
  - How to best schedule them?
  - How to recognize one from the other?
    - Do you trust applications to say that they are “interactive”?
  - Should you schedule the set of applications identically on servers, workstations, pads, and cellphones?

# Aside: Application Types (cont.)

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- Assumptions encoded into many schedulers (e.g., *O(1) Scheduler*)
  - Applications that sleep a lot and have short bursts must be interactive
    - Give them high priority
  - Applications that compute a lot must be high-throughput apps
    - Give them lower priority, since they won't notice intermittent bursts from interactive apps
- In general, it is hard to characterize applications
  - What about apps that sleep for a long time, and compute for a long time?
  - What about applications that must run under all circumstances

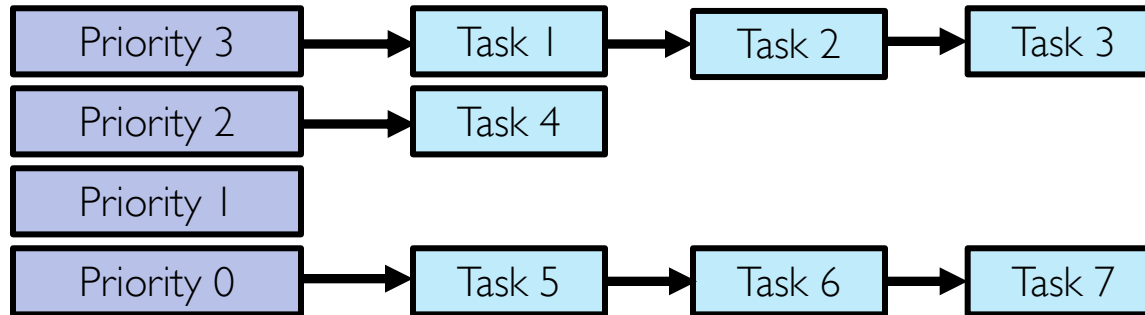
# SRTF Final Notes

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- Bottom line, we can't really know how long tasks will take
  - However, we can use SRTF as yardstick for measuring other policies
  - Optimal, so we can't do any better
  
- Pros & cons of SRTF
  - + Optimal (average response time)
  - – Hard to predict future
  - – Too many context switches
  - – Unfair

# Strict-priority Scheduling

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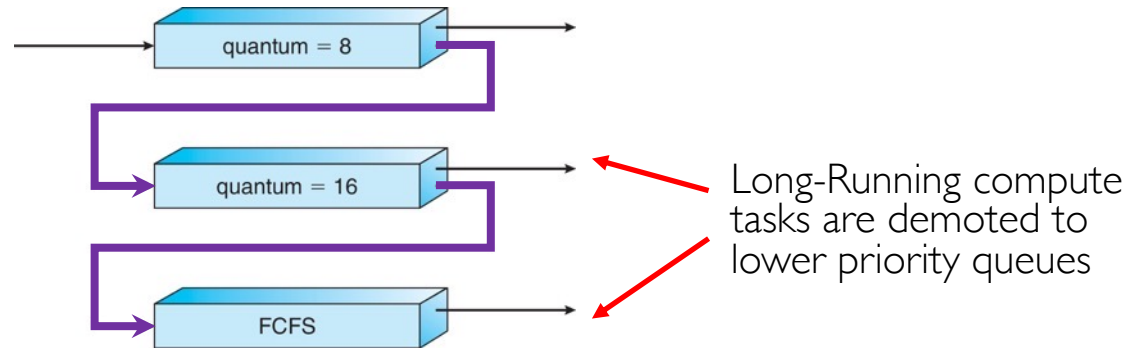
- Execution plan
  - Always execute highest-priority runnable tasks to completion
  - Each queue can be threaded in RR with some time-quantum
- Notice any problems?
  - **Starvation**
    - Lower-priority tasks may never run because of higher-priority tasks
  - **Priority inversion**
    - Low-priority task delays high-priority task by holding resources needed by high-priority task (more on this later)

# Fairness

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- Strict fixed-priority scheduling between queues is unfair (run highest, then next, etc.)
  - long running tasks may never get any CPU time
  - In Multics, shut down machine, found 10-year-old task
- One approach: give each queue some fraction of CPU
  - What if there are 100 short tasks and only one long task?
    - Like express lanes in a supermarket, sometimes express lanes get so long, get better service by going into one of other lines
- Another approach: increase priority of tasks that don't get service
  - What is done in some variants of UNIX
  - This is ad hoc; what rate should you increase priorities?
  - And, as system gets overloaded, no task gets CPU time, so everyone increases in priority  $\Rightarrow$  Interactive tasks suffer
- **Tradeoff: fairness is usually gained by hurting average response time!**

# Multi-level Feedback Queue

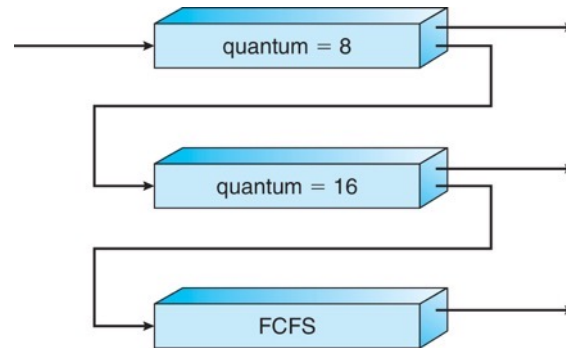


- Another method for exploiting past behavior (first use in CTSS)
  - Multiple queues, each with different priority
    - Higher priority queues often considered “foreground” tasks
  - Each queue has its own scheduling algorithm
    - E.g. foreground – RR, background – FCFS
    - Sometimes multiple RR priorities with quantum increasing exponentially (highest: 1ms, next: 2ms, next: 4ms, etc.)
- Adjust each task’s priority as follows (details vary)
  - Task starts in highest priority queue
  - If timeout expires, drop one level
  - If timeout doesn’t expire, push up one level (or to top)



# Multi-level Feedback Queue (cont.)

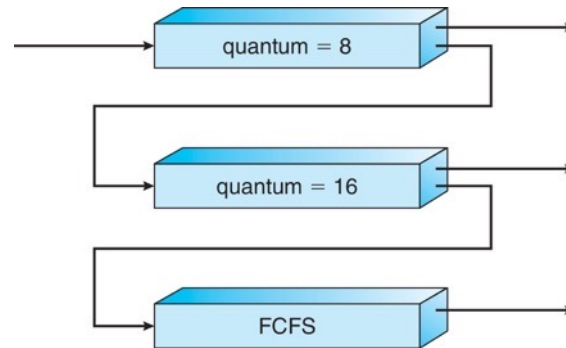
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- Result approximates SRTF
  - CPU bound tasks drop like a rock
  - Short-running I/O bound tasks stay near top
- Scheduling must be done between queues
  - **Fixed priority scheduling**
    - Serve all from highest priority, then next priority, etc.
  - **Time slicing**
    - Each queue gets fraction of CPU time
    - E.g., 70% to highest, 20% next, 10% lowest

# Multi-level Feedback Queue (cont.)

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- **Countermeasure**: user action that foil intent of OS designers
  - For multilevel feedback, put simple I/O's to keep task's priority high
  - Example of MIT Othello Contest
    - Cheater put `printf`'s, ran much faster than competitors!
    - Of course, if everyone did this, wouldn't work!

# Lottery Scheduling

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- Give each task  $i$  some number of lottery tickets  $N_i$
- On each time slice, randomly pick a winning ticket
- Lottery scheduling achieves **proportional-share allocations**
  - On average, CPU time is proportional to # of tickets given to task
- How to assign tickets?
  - Give tasks tickets proportional to their priorities
  - To approximate SRTF, give short tasks more and long tasks fewer
  - To avoid starvation, give every task at least one ticket (everyone makes progress)
- Compared to strict priority, lottery scheduling behaves gracefully as load changes
  - Adding or deleting one task affects all tasks proportionally, independent of how many tickets each task possesses



# Lottery Scheduling Example

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- Assume short tasks get 10 tickets, long tasks get 1 ticket

# short tasks/ # long tasks	% of CPU each short tasks gets	% of CPU each long tasks gets
1/1	91%	9%
0/2	N/A	50%
2/0	50%	N/A
10/1	9.9%	0.99%
1/10	50%	5%

- What if too many short tasks to give reasonable response time?
  - If load average is 100, hard to make progress
  - One approach is to log some users out

# Unfairness of Lottery Scheduling

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- Define unfairness for two tasks with the same burst time as
  - Unfairness = finish time of first one / finish time of last one
- As function of burst time

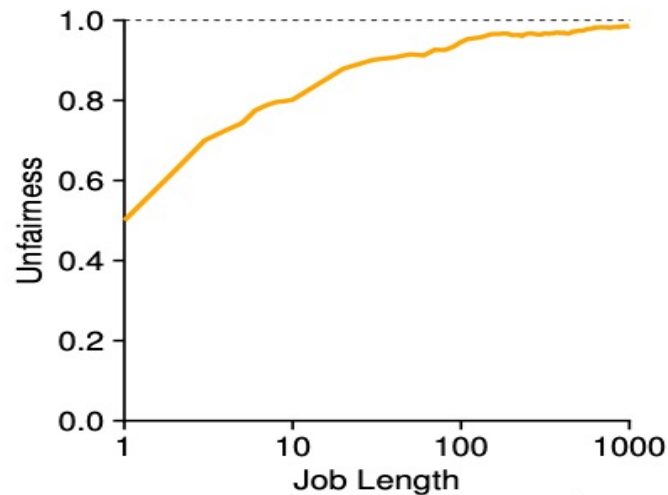


Figure 9.2: Lottery Fairness Study

# Stride Scheduling

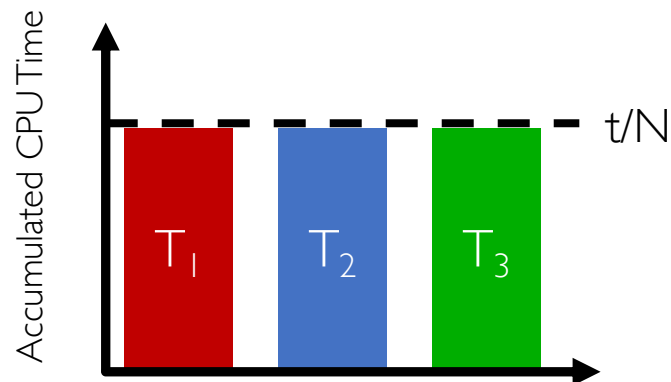
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- Achieves proportional-share scheduling without resorting to randomness
- Defines *stride* for each thread to be  $Big \# W / N_i$ 
  - The larger your share of tickets, the smaller your stride
  - E.g., with  $W = 10,000$ , and A, B, and C each having 100, 50, and 250 tickets, strides for A, B, and C are 100, 200, and 40, respectively
- Maintains *pass* counter for each thread
- Runs thread with lowest pass and adds its *stride* to its *pass*
  - Low-stride threads (lots of tickets) run more often
  - Thread with twice the tickets gets to run twice as often
  - Some messiness of counter wrap-around, new threads, ...

# Max-min Fair (MMF) Scheduling

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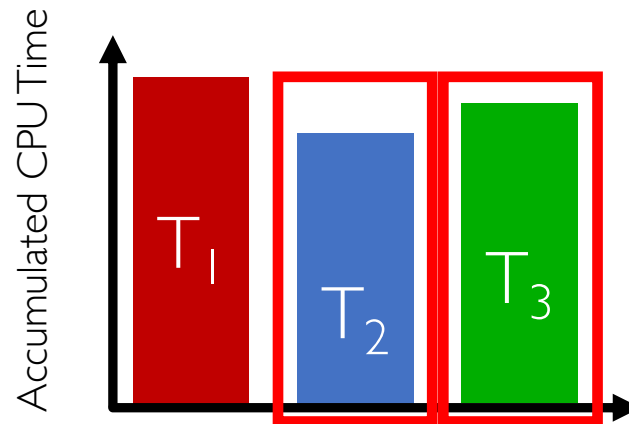
- Always choose thread with lowest accumulated CPU time
  - If chosen thread doesn't have CPU burst, schedule second lowest ...
  - Break ties randomly if multiple threads equally have lowest CPU time
- Goal is to give each thread equal share of CPU time
  - With  $N$  runnable threads, each thread should get  $1/N^{\text{th}}$  of CPU time
- At any time  $t$  we want to have



# MMF Scheduling (cont.)

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- Strict MMF causes too many context switches
  - It effectively turns to running one instruction of each thread
- Relaxed MMF runs thread with lowest accumulated CPU time for fixed time quantum before choosing next thread



- Notice any problem?
  - Fixed quantum leads to poor response time as # of threads increases



# MMF Scheduling (cont.)

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- Solution: dynamically change time quantum
- **Target latency**: interval during which all threads should run at least once
- Time quantum = Target latency / N
  - E.g., with 20ms target latency and 4 threads, time quantum is 5ms
- Notice any problem?
  - With 20ms target latency and 200 threads, time quantum becomes 0.1ms
  - Recall RR: large context switching overhead if time quantum gets to small
- **Minimum granularity**: minimum length of any time quantum
  - E.g., with target latency 20ms, 1ms minimum granularity, and 200 processes, time quantum is 1ms

# Weighted Max-min Fair Scheduling

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- What if we want to give more to some and less to others (proportional share)?
- **Key Idea:** assign weight  $w_i$  to each thread  $i$
- MMF uses single time quantum for all threads

$$Q = \frac{\text{Target latency}}{N}$$

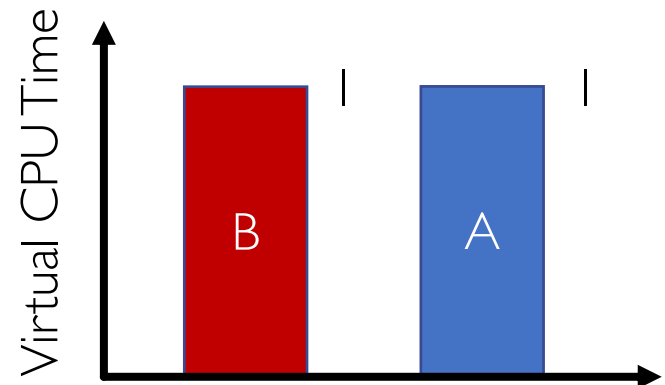
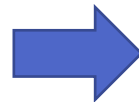
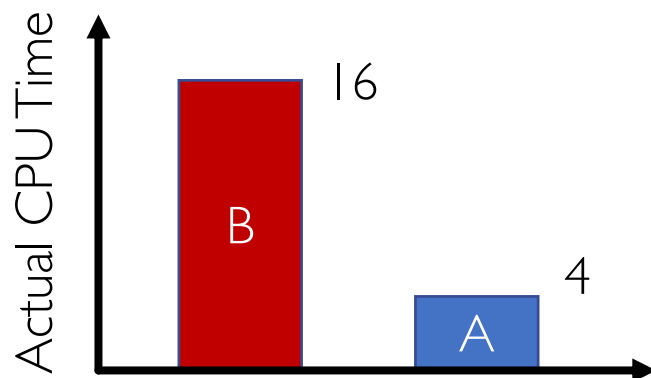
- Weighted MMF uses different time quanta for different threads

$$Q_i = \frac{w_i \times \text{Target latency}}{\sum_{j=1}^N w_j}$$

- E.g., with 20ms target latency, 1ms minimum granularity, and 2 threads: A with weight 1 and B with weight 4
  - Time quantum for A is 4 ms
  - Time quantum for B is 16 ms

# Weighted MMF Scheduling (cont.)

- Also track threads' *virtual runtime* rather than their true wall-clock runtime
- Higher weight: virtual runtime increases more slowly
- Lower weight: virtual runtime increases more quickly
- Linux *completely fair scheduler* deploys very similar ideas
  - Ready queue is implemented as red-black tree, in which threads are sorted in increasing order of their virtual runtime



# How to Evaluate Scheduling Algorithms?

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- **Deterministic modeling**
  - Pick workload and compute performance of each algorithm
- **Queueing models**
  - Mathematical approach for handling stochastic workloads (more on this later)
- **Simulations/Implementations**
  - Build system which allows actual algorithms to be run against actual data – most flexible/general

# Starvation and Sample Bias

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- Suppose you want to compare scheduling policies
  - Create some infinite sequence of arriving tasks
  - Start measuring
  - Stop at some point
  - Compute ART for finished tasks between start and stop
- Is this valid or invalid?
  - SJF and FCFS would complete different sets of tasks
    - Their ARTs are not directly comparable
    - E.g., suppose you stopped at any point in FCFS vs. SJF slide

# Solutions for Sample Bias

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- For both systems, measure for long enough that  
# of completed tasks  $\gg$  # of uncompleted tasks
- Start and stop system in idle periods
  - Idle period: no work to do
  - If algorithms are work-conserving, both will complete the same set of tasks

# Choosing Right Scheduling Algorithm

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If you care about	Then choose
CPU throughput	FCFS
Avg. response time	SRTF approximation
I/O throughput	SRTF approximation
Fairness (CPU time)	Linux CFS
Fairness – wait time to get CPU	RR
Favoring important threads	Priority
Proportional sharing	Lottery and stride scheduling

# Summary

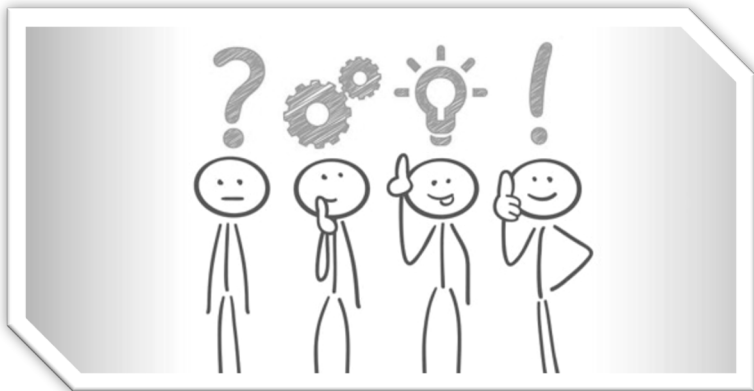
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- **First-come, first-served (FCFS)**
  - Threads are served in the order of their arrival
- **Round robin (RR)**
  - Give each thread a small amount of CPU time when it executes; cycle between all ready threads
- **Shortest task first (SJF) / shortest remaining time first (SRTF)**
  - Run whatever thread that has the least amount of computation to do/least remaining amount of computation to do
- **Multi-level feedback queue (MFQ)**
  - Multiple queues of different priorities and scheduling algorithms
- **Lottery and stride scheduling**
  - Give each thread a priority-dependent number of tickets
- **Max-min fair (MMF)**
  - Give each thread equal share of CPU time



# Questions?

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# Acknowledgment

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