# **A laboratory study of NMR relaxation times and pore coupling in heterogeneous media**

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# **ABSTRACT**

Nuclear magnetic resonance (NMR) relaxation times of geologic materials are closely related to pore geometry. In heterogeneous media, however, the details of this relationship are poorly understood because of a phenomenon known as pore coupling, which arises when diffusing protons sample multiple pores before relaxing. Laboratory experiments allow us to explore whether surface geochemistry can influence pore coupling and how this process affects the observed relaxation-time distribution. Measurements of the NMR response for microporous silica gel packs, treated with varying amounts of surface-coating iron, demonstrate that samples with less iron exhibit stronger pore coupling than those with abundant iron. When pore coupling is strong, the relaxationtime distribution grossly misrepresents the underlying bimodal pore-size distribution of micropores and macropores. Specifically, the bimodal relaxation-time distribution becomes merged and the relative amplitude of the peaks fails to reflect the true macropore and micropore volume. A reduction in pore coupling, observed with increasing iron content, is attributed to a decrease in the distance protons are able to diffuse before relaxing. Basic parameters describing the shape of the relaxation-time distributions for this range of samples are well-predicted by a 1D analytical model. Experimental results conclusively demonstrate that surface geochemistry is an important factor determining the degree to which pore coupling occurs and illustrate how this phenomenon can affect the interpretation of NMR relaxation measurements in heterogeneous porous media.

### **INTRODUCTION**

Nuclear magnetic resonance (NMR) relaxation measurements provide an unparalleled view into the pore space of geologic materials. The proton NMR method probes the time required for hydrogen nuclei in the pore water to relax to equilibrium through diffusion and interaction with the pore-scale physicochemical environment. NMR relaxation-time measurements have been used for decades in geophysical well logging to estimate hydrocarbon-reservoir properties such as porosity, pore-size distribution, and permeability ([Seevers,](#page-6-0) [1966;](#page-6-0) [Kenyon et al., 1988](#page-6-1)). Recent research has extended NMR geophysical techniques to near-surface environmental applications and has led to the development of a surface-based NMR method — magnetic resonance sounding (MRS) — to measure the NMR response of groundwater aquifers ([Legchenko and Valla, 2002;](#page-6-2) [Hertrich,](#page-6-3) [2008;](#page-6-3) [Walsh, 2008](#page-6-4)). Our current study seeks to improve the interpretation of near-surface NMR measurements by exploring the link between NMR relaxation times and pore-scale properties in heterogeneous porous media.

The analysis of NMR relaxation measurements in geologic materials requires an accurate model of the physical processes governing relaxation. Conventional interpretation of these data assumes a model of isolated pores in which each diffusing proton samples only one pore. Thus, it is assumed that each pore contributes independently to the NMR signal, with a characteristic relaxation time. In many nearsurface materials, however, pores are sufficiently connected that diffusing protons can readily sample multiple pores during NMR measurement. For materials in which pores are strongly coupled by diffusion, the resulting relaxation-time distribution reflects a complex averaging of the pore network that can be difficult to interpret.

Understanding the conditions in which pore coupling occurs and how this process can influence NMR relaxation measurement is fundamental to the successful use of NMR data in geophysical applications. Several studies have explored this issue theoretically, using models of idealized pore networks to determine how factors such as pore geometry ([Cohen and Mendelson, 1982;](#page-5-0) [McCall et al., 1991;](#page-6-5) [Zielinski et al., 2002](#page-6-6)) and surface geochemistry ([Ramakrishnan et](#page-6-7) [al., 1999;](#page-6-7) [Ramakrishnan et al., 2001](#page-6-8)) might control the extent of pore coupling. Despite the clear need to account for pore-coupling effects, relatively few laboratory studies have explored this phenome-non. [Toumelin et al.](#page-6-9) (2002) show that interpore diffusion can strong-

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ly influence NMR measurements in carbonates and note that the degree of coupling generally increases with temperature as pore-fluid diffusivity increases. [Anand and Hirasaki](#page-5-1) (2007) investigate geometric controls on pore coupling in microporous grain packs; they find that coupling between micropores and larger intergranular pores becomes more significant as grain diameter decreases. However, no laboratory study has explored the geochemical controls on pore cou-pling suggested by [Ramakrishan](#page-6-7) (1999).

The aim of our study is twofold:  $(1)$  to improve understanding of geochemical controls on pore coupling and (2) to determine how the coupling process affects the interpretation of NMR relaxation measurements. We first establish that surface geochemistry can, in fact, control the strength of pore coupling. In our laboratory approach, we study a well-characterized porous media, silica gel, and measure the NMR response of samples with varied geochemistry. Utilizing a demonstrated link between surface iron concentration and pore coupling strength, we are then able to identify specific effects of pore coupling on the relaxation-time distribution. Finally, we compare our experimental results with theoretical predictions from [Ra](#page-6-7)[makrishnan et al.](#page-6-7) (1999). Our study of NMR relaxation measurement in a controlled system contributes to our ultimate goal of improving the interpretation of NMR measurements in heterogeneous near-surface sediments.

#### **BACKGROUND**

In the standard NMR relaxation experiment, a static magnetic field is applied to a water-saturated sample, causing an equilibrium alignment of the magnetic moments associated with protons in the pore water. The system is then perturbed by a secondary radio-frequency pulse that excites the protons to a higher energy state, and we monitor the magnetization *M* over time as the system relaxes to equilibrium.

Two time constants describe NMR relaxation:  $T_1$  and  $T_2$ . The longitudinal relaxation rate  $T_1^{-1}$  is the rate at which the protons return to their equilibrium state. In the commonly assumed case of fast diffu-sion ([Senturia and Robinson, 1970](#page-6-10)), the net observed relaxation rate  $T_1^{-1}$  for a single pore is given by

$$
T_1^{-1} = T_{1B}^{-1} + \rho_1 \bigg(\frac{S}{V}\bigg),\tag{1}
$$

<span id="page-1-0"></span>where  $T_{1B}^{-1}$  is the relaxation rate of the bulk water, *S/V* is the surfacearea-to-volume ratio of the pore (inversely proportional to the pore radius  $r_{\text{pore}}$ ), and  $\rho_1$  is the longitudinal surface relaxivity ([Brownstein](#page-5-2) [and Tarr, 1979](#page-5-2)). Surface relaxivity is a geochemical property describing the capacity of the grain surface to enhance relaxation; it generally increases with the concentration of paramagnetic impurities on a surface (e.g., manganese(II)  $[Mn^{2+}]$  or iron(III)  $[Fe^{3+}]$ ) ([Foley et al., 1996;](#page-6-11) [Bryar et al., 2000](#page-5-3)). Together, the product  $\rho(S/V)$ is called the surface relaxation rate; it reflects the combined effect of geometry and geochemistry.

For practical reasons,  $T_1$  measurements are difficult to make with borehole or surface NMR instruments, so field applications of NMR typically involve measurements of  $T_2$ . The transverse relaxation rate  $T_2^{-1}$  is the rate at which protons dephase as they return to equilibrium. The expression for  $T_2^{-1}$  thus includes an additional term to account for internal magnetic field gradients *G* experienced by diffusing protons:

$$
T_2^{-1} = T_{2B}^{-1} + \rho_2 \left(\frac{S}{V}\right) + \frac{D}{12} (\gamma G t_E)^2.
$$
 (2)

<span id="page-1-1"></span>Here,  $\rho_2$  is the transverse surface relaxivity,  $T_{2B}^{-1}$  is the relaxation rate of the bulk water, *D* is the self-diffusion coefficient of the water,  $\gamma$  is the gyromagnetic ratio of the hydrogen nucleus, and  $t_E$  is the echo time, a timing parameter of the measurement. Relaxation in geologic materials with negligible magnetic susceptibility is dominated by surface relaxation, in which case the expression for  $T_2^{-1}$  is reduced to

$$
T_2^{-1} = \rho_2 \bigg(\frac{S}{V}\bigg). \tag{3}
$$

<span id="page-1-2"></span>If we consider the NMR relaxation response of a single waterfilled pore, the transverse magnetization signal is described by an exponential decay:

$$
M(t) = Ae^{-t/T_2},\tag{4}
$$

<span id="page-1-3"></span>where the initial signal amplitude *A* is proportional to the number of hydrogen nuclei (directly related to the pore volume). In a rock or sediment with a distribution of pore types, it conventionally is assumed that each pore contributes to the NMR signal in isolation and the net observed signal is modeled as multiexponential decay:

$$
M(t) = \sum_{i} A_i \exp\left(\frac{-t}{T_{2i}}\right),\tag{5}
$$

<span id="page-1-4"></span>where the amplitude  $A_i$  is proportional to the volume of water-filled porosity associated with a corresponding relaxation time  $T_{2i}$ . Using this model of isolated pores, the  $M(t)$  data are inverted to obtain a  $T_2$ distribution, which is scaled according to equation [3](#page-1-2) to estimate a pore-size distribution assuming uniform surface relaxivity and a simple pore shape (e.g.,  $S/V = 3/r_{\text{pore}}$  for spherical pores).

The simplest conceptualization of the isolated pore assumption is that each proton samples only one pore during the NMR measure-ment. [D'Orazio et al.](#page-6-12) (1989) explain more completely that the isolated pore model is valid as long as the distance over which a proton will diffuse is smaller than the scale over which dissimilar pores (with different  $T_2$ ) may be encountered. Although this condition generally is satisfied for NMR measurements in consolidated sandstones with tight pore throats and relatively uniform pore bodies ([Davies, 1990;](#page-6-13) [Borgia et al., 1996](#page-5-4)), the model often breaks down for materials with well-connected heterogeneous pores. [Hinedi et al.](#page-6-14) ([1993](#page-6-14)) and [Hinedi et al.](#page-6-15) (1997) study the NMR response of microporous near-surface materials, including soil aggregates and analogous synthetic silica gels, and note that the size of larger intergranular pores is grossly underestimated. Although not recognized by researchers, this error is most likely a consequence of pore coupling.

<span id="page-1-5"></span>During a given time period *T*, a proton will sample the pore network over an average diffusion length  $\ell$ , approximated as

$$
\ell = \sqrt{6DT},\tag{6}
$$

where *D* is the self-diffusion coefficient of water (at  $30^{\circ}$ C, *D*  $= 2.46 \times 10^{-9}$  m<sup>2</sup>/s; [Simpson and Carr, 1958](#page-6-16)). Considering the duration of NMR decay as represented by  $T_2$  (typically 10–1000 ms), a proton may diffuse more than  $100 \mu m$  during NMR measurement. As the diffusion length approaches the scale at which dissimilar pores are encountered, pore coupling will begin to complicate the NMR response. In the limiting case of infinite coupling when the diffusion length is unbounded, the resulting  $T_2$  distribution will exhibit a single peak representing  $\rho S/V$  of the entire pore network ([McCall](#page-6-5) [et al., 1991](#page-6-5)); however, the effect of pore coupling at intermediate strengths is poorly understood.

[Ramakrishnan et al.](#page-6-7) (1999) model diffusional coupling in microporous grains and argue that the degree to which pores are coupled may be highly dependent on surface relaxivity. When  $\rho_2$  is high, the diffusion length is reduced because enhanced relaxation limits the time and distance over which protons can travel before relaxing. [Bryar et al.](#page-5-3) (2000) and [Daughney et al.](#page-6-17) (2000) note consistent results for laboratory measurements of  $T_1$  in iron-coated silica gels. Surface coatings of paramagnetic iron(III) (Fe<sup>3+</sup>) increase  $\rho_1$  of the gels by more than two orders of magnitude and significantly alter the shape of the relaxation-time distributions. Our experiments here use a similar system of iron-coated silica gels to develop a range of samples between which the degree of pore coupling is expected to vary with iron concentration. The NMR  $T<sub>2</sub>$  relaxation measurements on these samples should thus allow us to directly investigate the effects of pore coupling and explore the link between  $T_2$  and pore geometry in heterogeneous materials.

# **METHODS AND MATERIALS**

# **Sample characterization and preparation**

The four samples used in this study are derived from a high-purity silica gel (Davisil<sup>®</sup> 150 Å 60–200 mesh, manufactured by Grace Davison) that has a bimodal pore-size distribution comprised of intragranular micropores (within the grains), reported to be approximately 15 nm in diameter, and larger intergranular macropores (between the grains). We first sieved the pure gel to achieve a narrower grain-size distribution of  $53-105 \mu m$ . The diameter of intragranular pores in a random packing is estimated to be about 20  $\mu$ m, as-suming a ratio of average pore size to grain size of 0.225 ([Barker and](#page-5-5) [Mehta, 1992](#page-5-5)). The micropore volume, expressed as milliliters/gram gel, was provided from manufacturer specifications as 1.2 ml/g.We measured the surface area of the gels  $(315.1 \pm 2.5 \text{ m}^2/\text{g})$  by the Brunauer-Emmett-Teller (BET) nitrogen adsorption method using a MicromeriticsASAP 2020 accelerated surface area and porosimetry system.

Our experimental approach was based on the assumption that increasing the amount of paramagnetic  $Fe<sup>3+</sup>$  on the gel surface would reduce pore coupling by increasing the surface relaxation rate; therefore, we closely controlled surface geochemistry. We rinsed the gel repeatedly with 10% hydrogen chloride (HCl) and distilled, deionized (DDI) water (18 M $\Omega$ cm) to remove paramagnetic impurities, and we retained a portion of the cleaned gel to be used as the highest purity sample for NMR analysis. We then synthesized three additional gels with varied amounts of paramagnetic Fe<sup>3+</sup> oxyhydroxide surface coating from the cleaned gel using methods of [Grantham et](#page-6-18) al. ([1997](#page-6-18)). Samples were placed under vacuum and saturated with aqueous solutions of ferrous sulfate (FeSO<sub>4</sub>). The mixtures were then oxidized by adding excess 30% hydrogen peroxide  $(H_2O_2)$  and were placed on an orbital shaker to equilibrate overnight. Following the iron coating treatment, the gels were rinsed with DDI water and oven dried overnight at 45°C.

We determined the amount of paramagnetic  $Fe<sup>3+</sup>$  sorbed to each gel from subsamples by atomic adsorption spectroscopy; concentrations of Fe<sup>3+</sup> by mass in the four samples ranged from  $0.00\%$  in the pure sample to 0.10% in the most heavily coated sample. Qualitative analysis by scanning electron microscopy (SEM) and energy disper-

sion spectrometry (EDS) confirmed that iron was effectively sorbed to the interior and exterior surfaces of the gels. Neither the porosity nor the surface area of the gels was changed, within experimental error, by the iron coating process.

#### **NMR measurements**

For NMR measurements, we packed dry samples of each gel in consistent weights and volumes into cylindrical Teflon™ sample holders with an interior diameter of 2.1 cm and height of 6 cm. In the first series of measurements, samples were completely saturated with DDI water. To ensure maximum saturation, we first evacuated each packed sample in a dry vacuum (75 mm mercury) for 30 min and then submerged the sample in a water bath before atmospheric pressure was restored. Samples were allowed to saturate for 2 hr while submerged. The volume of water held in micropores for each sample was calculated from the mass of dry sample (using manufacturer-specified  $1.2 \text{ ml/g}$  gel); the volume of water in macropores was determined gravimetrically as the difference between total water volume and micropore volume. We determined that of the total water volume, 58% was held in micropores and 42% was held in macropores.

We acquired a first series of NMR measurements directly after saturation. Following measurement at saturated conditions, we centrifuged the packed samples to drain water from the large intergranular pores. Centrifuging removed approximately 98% of the intergranular pore water (estimated gravimetrically); the intragranular porosity was left undrained by this process as a result of the extremely high capillary potential of the micropores.We then acquired a second series of NMR measurements, immediately after centrifuging, at which point the NMR signal was presumed to be primarily sensitive to water in the undrained intragranular micropores.

All NMR relaxation data were collected using a 2.2-MHz Maran Ultra NMR core analyzer (Resonance Instruments) with a CPMG pulse sequence. This instrument has a dead time of approximately 60  $\mu$ s. Data were acquired consistently at 30 $\degree$ C and were stacked 100 times to improve the signal-to-noise ratio (S/N). Measurements at varied echo-time  $t_F$  spacing indicated that magnetic gradient effects were negligible; therefore, the shortest available spacing,  $t_F$  $= 150 \mu s$ , was used to maximize data sampling at short times. Independent measurements on each sample were repeated three times to determine experimental variance.

We inverted each measured magnetization decay signal for a  $T_2$ relaxation-time distribution using a regularized nonnegative least-squares algorithm developed after [Whittall et al.](#page-6-19) (1991). In this approach, the data are fit to 200 logarithmically spaced  $T_2$  values, from 1 ms to 10 s, and the inverted model is regularized for smoothness. Regularization parameters were selected such that the data were fit to a tolerance equal to the measured noise level. This statistically robust approach limits inversion artifacts and is required in order to ascribe physical significance to observed differences in the smoothness of the  $T_2$  distribution.

### **RESULTS AND DISCUSSION**

## **Laboratory NMR results**

The four gels provide a group of samples with identical geometry and varied geochemistry, with  $\rho_2$  expected to increase as iron content increases. An increase in  $\rho_2$  is predicted to lead to a decrease in pore coupling as faster surface relaxation reduces the distance protons may diffuse before relaxing. Thus, analyzing these samples should allow us to assess (1) the extent to which pore coupling may be controlled by surface geochemistry and (2) how the coupling process affects NMR data interpretation.

The resulting  $T_2$  distributions for each of the gel samples are shown in Figure [1,](#page-3-0) with iron concentrations increasing from top  $(0.000\% \text{ Fe}^{3+})$  to bottom  $(0.010\% \text{ Fe}^{3+})$ . Solid curves show distributions for NMR measurements at fully saturated conditions; dashed curves are for measurements collected after centrifuging. Distributions for each sample are normalized by the total signal amplitude at full saturation, which is consistent between all samples to within experimental error.

We first consider the  $T_2$  distributions for all four samples obtained after centrifuging, when the NMR measurement is sensitive exclusively to the saturated micropores. The integrated amplitude of each distribution reflects 58% of the normalized signal; thus, the total volume of microporosity is captured accurately. Despite the reported uniform intragranular pore size, we observe slightly broad peaks. Regularization of the inverted distributions may result in some peak broadening; however, we have consistently found that inversions of data with high S/N (e.g.,  $\sim$ 130 here) can produce narrow peaks when warranted by the data.We therefore interpret the breadth of the peaks as indicating that the size and surface-iron concentration of the

<span id="page-3-0"></span>

Figure 1. NMR relaxation-time distributions for the four silica gel samples: (a) pure gel, (b)  $0.002\%$  Fe<sup>3+</sup>, (c)  $0.004\%$  Fe<sup>3+</sup>, and (d)  $0.010\%$  Fe<sup>3+</sup>. Iron concentrations increase from top to bottom. Solid curves are for measurements at full saturation; dashed curves are for measurements after centrifuging (signal exclusively from micropores). Curves for each sample are normalized by the initial signal amplitude for the fully saturated measurements.

micropores are not entirely uniform. For samples with increasing iron concentrations, we observe a shift of the centrifuged  $T_2$  peak to shorter times, reflecting an expected increase in  $\rho_2$ . We calculate  $\rho_2$ for each sample (Table  $1$ ) from equation [3,](#page-1-2) using the logarithmic mean relaxation time for each centrifuged distribution and independent measurements of *S*/*V*.

Analyzing the  $T_2$  distributions for measurements at full saturation allows us to investigate the extent to which coupling occurs between the macropores and micropores. We begin with the results for the low- $\rho_2$  pure gel, which we expect to exhibit the strongest degree of pore coupling. Given that the macropores and micropores differ in size by approximately three orders of magnitude, the isolated pore model should predict two distinct peaks in the relaxation-time distribution. Instead, we observe one broad peak with two marginally discernible modes separated by less than two orders of magnitude. This apparent averaging of the underlying pore-size distribution indicates that the two pore types are strongly coupled by diffusion. In the other three samples, as the concentration of iron coating the gel surface is increased, we observe a separation of the distribution into two clearly discernible modes or peaks, reflecting the anticipated decrease in pore coupling. However, even for the most heavily iron-treated gel, the distance separating these peaks is less than would be predicted by a purely isolated pore model.

Let us now explore the meaning of the relaxation-time distributions for these samples, spanning a range of coupling strengths. We refer to the two modes in each distribution as the fast relaxing signal (at lower  $T_2$  values) and the slow relaxing signal (at higher  $T_2$  values). For all samples, the fast relaxing signal corresponds directly to the signal from the microporosity, represented in the centrifuged measurements. Thus, the relaxation time of the micropores is reflected accurately despite the presence of pore coupling and could be used to estimate a pore size, assuming a given  $\rho_2$  value. On the other hand, the location of the slow relaxing signal, which should reflect the relative size of the macropores in the absence of pore coupling, overlaps the fast-relaxing micropore signal when pore coupling is strong and successively separates as the degree of pore coupling is reduced. Thus, when pore coupling is dominant, the relative size of the macropores would likely be dramatically underestimated.

In addition to this apparent shift in the position of the  $T_2$  distributions, we observe that pore coupling affects the relative amplitudes of the fast and slow relaxing signals.We estimate the relative volume of water relaxing at fast  $T_2$  ( $\theta_{w\text{-fast}}$ ) versus slow  $T_2$  ( $\theta_{w\text{-slow}}$ ) for each saturated sample by first splitting the distribution at the point of minimum slope and then integrating the distribution to the left and right, respectively. Values for the ratio  $\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$ , estimated in this manner for each sample, are listed in Table [1.](#page-3-1) In the absence of pore coupling, we would expect  $\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$  to reflect the true ratio of mi-

<span id="page-3-1"></span>**Table 1. Tabulated estimates of geochemical properties for** each sample and the estimated  $\bar{\theta}_{w\text{-fast}}/\theta_{w\text{-slow}}$  for laboratory **measurements and model data.**

$\%$ Fe <sup>3+</sup> by mass	$\rho_{2}$ $(\mu m/s)$	$\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$ laboratory	$\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$ modeled
0.000	$0.201 \pm 0.007$	$0.61 \pm 0.04$	0.64
0.002	$0.345 + 0.004$	$0.93 \pm 0.05$	1.00
0.004	$0.592 \pm 0.010$	$1.12 \pm 0.06$	1.21
0.010	$0.953 \pm 0.004$	$1.26 \pm 0.06$	1.34

cropore volume to macropore volume  $(1.37 \pm 0.04)$ . For the pure gel, which exhibits the greatest degree of pore coupling,  $\theta_{w\text{-fast}}/$  $\theta_{w\text{-slow}}$  underpredicts the true ratio by 55%, grossly misrepresenting the true pore geometry. As pore coupling weakens with increasing iron content, we see that the accuracy of this estimated ratio improves, eventually reaching 94% of the true value.

These laboratory observations are compatible with a conceptual model of pore coupling proposed by [Ramakrishnan et al.](#page-6-7) (1999), in which protons move freely between intragranular micropores and intergranular macropores before relaxing. The leftward merging of the slow relaxing peak for samples with low iron concentrations occurs because most protons that originate in macropores can diffuse freely into the microporous grains before relaxing. These protons thus relax at a much faster rate than would be predicted for isolated macropores and exhibit an averaging of rates for the two pore types. When surface relaxivity is high, fewer protons that originate in the macropores can efficiently sample the microporous region before relaxing, lessening the degree to which the slow relaxing peak is skewed leftward.

The relative amplitude of the two peaks is likewise affected by the relative number of protons that sample both pore types. When relaxation occurs slowly, many protons are able to diffuse out of the smaller intragranular pores before relaxing and so decay at an averaged rate. For samples with substantial iron surface coatings, relaxation occurs rapidly, so more protons originating in micropores relax before diffusing out of the grain. Thus, the amplitude of the fast relaxing  $T_2$  peak more accurately represents the true micropore volume in these samples. We anticipate that the presence of other paramagnetic ions such as  $Mn^{2+}$  on the grain surface would produce similar effects.

#### **Comparison to analytical models**

We can further compare our results quantitatively with the 1D model of pore coupling, presented and described by [Ramakrishnan](#page-6-7) et al. ([1999](#page-6-7)). This model applies the NMR diffusion-reaction equation in two separate domains, one representing a microporous grain and one representing a macropore. The microporous grain, with radius  $R_g$  and porosity  $\varphi_\mu$ , is treated as a continuum in which surface relaxation occurs at a specified rate  $T_{2S\mu}$ . To account for restricted diffusion occurring within the micropores, the self-diffusion coefficient of water *D* is scaled by the formation factor of the microporous grain  $F_{\mu}$ . The total porosity of the system  $\varphi_t$  determines the dimensions of the two domains. The magnetization in the macropore domain  $M_m$  is governed by the standard NMR diffusion equation:

$$
D\frac{d^2M_m}{dx^2} - M_m T_{2B}^{-1} = \frac{dM_m}{dt},\tag{7}
$$

<span id="page-4-0"></span>where  $T_{2B}$  is the bulk water relaxation rate.

<span id="page-4-1"></span>Equation [8](#page-4-1) describes  $M_{\mu}$ , the magnetization in the domain of the microporous grain:

$$
\frac{D}{F_{\mu}} \frac{d^2 M_{\mu}}{dx^2} - \phi_{\mu} M_{\mu} (T_{2S\mu}^{-1} + T_{2B}^{-1}) = \phi_{\mu} \frac{dM_{\mu}}{dt}.
$$
 (8)

<span id="page-4-2"></span>A boundary condition between domains,

$$
D\frac{d^2M_m}{dx^2} = \frac{D}{F_\mu}\frac{d^2M_\mu}{dx^2} + \rho_2 M_m (1 - \varphi_\mu),
$$
 (9)

matches flux into and out of the microporous grain and allows for relaxation at the grain wall with a surface relaxivity of  $\rho_2$ .

We fully parameterized four models to be representative of our measured samples. A value of  $T_{2B} = 3.05$  s, consistently measured for all centrifuged fluids, was used across all models. Values for  $(T_{2S\mu}^{-1} + T_{2B}^{-1})$  in equation [8](#page-4-1) are derived from the mean log relaxation time for the micropores in each sample, measured after centrifuging. Representative values of  $\rho_2$ , obtained as described previously, are listed in Table [1.](#page-3-1) Geometric parameters  $R_g = 30 \mu m$ ,  $\varphi_t = 0.83$ , and  $\varphi_{\mu}$  = 0.725 reflect manufacturer specifications confirmed by independent measurements. It was not possible to measure  $F_{\mu}$  directly, so we selected a value of 1.4  $(1/\varphi_\mu)$ , consistent with an open, weblike network of pores typical of silica gels. We used a standard value of  $D = 2.46 \times 10^{-9}$  m<sup>2</sup>/s for water at 30°C ([Simpson and Carr, 1958](#page-6-16)).

[Ramakrishnan](#page-6-7) (1999) explains that exact analytic solutions to the parameterized equations can be obtained using Laplace transforms; the solutions yield two principal exponential-decay modes (smoothing effects are not modeled). However, obtaining analytic solutions is very challenging, so we used Comsol Multiphysics® to obtain accurate numerical solutions. In Figure [2,](#page-4-3) we plot the position and magnitude of the resulting principal decay modes, superimposed

<span id="page-4-3"></span>

Figure 2. Comparison between laboratory measurements and the simulated relaxation response based on the [Ramakrishnan et al.](#page-6-7) ([1999](#page-6-7)) 1D model: (a) pure gel, (b)  $0.002\%$  Fe<sup>3+</sup>, (c)  $0.004\%$  Fe<sup>3+</sup>, and (d)  $0.010\%$  Fe<sup>3+</sup>. Solid curves are for laboratory measurements on gels at saturated conditions. Dashed bars show the position and amplitude of the primary exponential relaxation modes derived from the model. Mode amplitudes are all normalized such that, for the pure gel, the long-time peak is exactly matched by the long-time mode.

<span id="page-5-6"></span>

Figure 3. Comparison of  $\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$  derived from laboratory- and model-generated results. Estimates from laboratory measurements represent the ratio of integrated amplitude for the short-time peak to that of the long-time peak. Error bars show the standard deviation for this estimate from repeated measurements. Estimates from modeled data represent the ratio of the short-time mode amplitude to that of the long-time mode. The hollow black diamond (top right) represents the actual value of the micropore-to-macropore volume, which would be reflected by  $\theta_{w\text{-fast}}/\theta_{w\text{-slow}}$  in the absence of pore-coupling effects.

over the experimental  $T_2$  distributions for each sample. In general, modeled relaxation times closely predict the location of the  $T_2$  peaks for laboratory measurements. However, the relaxation time for the slow relaxing peak is slightly overestimated in models representing the 0.004% and 0.010% Fe<sup>3+</sup> gels.

Plotted in Figure [3](#page-5-6) and listed in Table [1](#page-3-1) is a comparison of  $\theta_{w-\text{fast}}$  /  $\theta_{w-\text{slow}}$ , determined for each of the laboratory and modeled distributions (direct comparison is not possible in Figure [2](#page-4-3) because the width of the experimental  $T_2$  peaks is not constant). We plot modeled and experimental values along a 1:1 line in Figure [3](#page-5-6) as filled circles with experimental error bars; the hollow diamond (top right) represents the true ratio value (1.37), which would be observed for zero pore coupling. The modeled and experimental data agree quite well; however, as iron concentrations increase, the modeled  $\theta_{w-fast} / \theta_{w-slow}$  increasingly exceeds the experimental result. These minor disparities between modeled and laboratory results at higher iron concentrations suggest that the model may slightly overpredict the extent to which increased surface relaxivity can reduce pore-coupling effects. Nonetheless, general agreement with our experimental results indicates that this relatively simple 1D model provides an accurate and extremely useful tool for predicting NMR relaxation behavior in this class of heterogeneous media.

#### **CONCLUSIONS**

The NMR relaxation times of porous geologic materials are closely linked to the volume and geometry of the water-saturated pore space. Thus, there is tremendous potential for using NMR relaxation measurements, acquired with borehole or surface-based instruments, in near-surface applications to estimate subsurface properties. It is clear, however, that substantial research is needed to fully understand the processes governing NMR relaxation in near-surface materials. This study has focused on the impact of pore coupling, a process that can significantly affect NMR relaxation measurements in systems with well-connected pores.

Our experimental results demonstrate conclusively that surface geochemistry can be a significant factor determining the strength of pore coupling and thus the relationship between pore geometry and NMR relaxation times. By controlling for surface geochemistry in well-characterized samples, we directly assessed the impact of pore coupling on the observed  $T_2$  distribution in samples representing a range of coupling strengths. For materials with intragranular microporosity and intergranular macroporosity, pore coupling reduces the slowest relaxation time associated with macropores and decreases the amplitude of the fast relaxing signal associated with the micropores. If unaccounted for in the interpretation of the NMR relaxation data, the presence of pore coupling would lead to an underestimation of the total micropore volume and the size of the largest pores. Good agreement between our laboratory results and an analytical model suggests that a theoretical approach may help predict the extent to which pore coupling will affect NMR measurements in other porous media.

Our study has only considered the behavior of silica gels, which have smaller pores and a lower  $\rho_2$  value than is typical for most geologic materials. The small pores tend to limit the extent of the diffusion, whereas the low  $\rho_2$  value tends to enhance the extent of diffusion. Although these properties of silica gel are different from those of a typical geologic material, the well-characterized geometry of the gel allows us to investigate the physics linking surface chemistry and pore coupling. Our findings lead us to anticipate that for a wide class of unconsolidated materials with well-connected pores, the NMR relaxation-time distribution will not accurately convey the underlying pore structure because of pore coupling effects. Additional research is required to explore the impact of pore coupling in a broader range of materials to improve the interpretation of NMR data and to advance the use of NMR methods in near-surface applications.

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