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Hybrid Variational/Ensemble Data Assimilation

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Outline

• Background

• Some results

• Introduction to hybrid practice

What is data assimilation?



Some data assimilation methods

- Three-dimensional variational (3DVAR)
 - Background error covariances (BECs) typically fixed/ time-invariant
 - May yield poor results when actual flow differs from that encapsulated within the fixed "climatology"
- Ensemble Kalman filter (EnKF)
 - Time-evolving, "flow-dependent" BECs estimated from a short-term ensemble forecast
 - Many different flavors (e.g., ETKF, EAKF)

Ensemble BECs (i.e., spread)

•Average ensemble spread of wind speed over \sim 3 weeks at 0000 UTC



Ensemble BECs (i.e., spread)

•General definition of covariance:

$$\frac{1}{n-1}\sum_{i=1}^{n}(x_i-\overline{x})(y_i-\overline{y})$$

•In vector matrix form (here, assume *n* is ensemble size):

$$= \frac{1}{n-1} \sum_{i=1}^{n} (\mathbf{x}_{i} - \overline{\mathbf{x}}) (\mathbf{x}_{i} - \overline{\mathbf{x}})^{\mathrm{T}}$$
$$= \frac{1}{n-1} \sum_{i=1}^{n} (\delta \mathbf{x}_{i}) (\delta \mathbf{x}_{i})^{\mathrm{T}}$$

"Hybrid" variational/ensemble DA

- "Hybrid" variational/ensemble
 - Incorporates ensemble background errors within a variational (e.g., 3DVAR) framework
 - Combination of fixed and timeevolving background errors
 - Main additional expense compared to 3DVAR is running an ensemble of forecasts



What is Hybrid DA?

- Deterministic background is analyzed by a variational algorithm (i.e., minimize a cost function)
 - It combines the 3DVAR "climatological" BECs and "errors of the day" from ensemble perturbations
- Traditionally generates a deterministic analysis (like 3DVAR)
- Need a separate system to update ensemble
 - Could be ensemble forecasts already available from operational centers
 - Could be an EnKF-based DA system
 - Could be a multiple model/physics ensemble
- Ensemble needs to be good to well-represent "errors of the day"





Hybrid formulation

(Hamill and Snyder, 2000)

• 3DVAR cost function

$$J(\mathbf{x}) = \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^{\mathrm{T}} \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \frac{1}{2} [H(\mathbf{x}) - \mathbf{y}]^{\mathrm{T}} \mathbf{R}^{-1} [H(\mathbf{x}) - \mathbf{y}]$$

• Idea: replace **B** by a weighted sum of static \mathbf{B}_{s} and the ensemble \mathbf{B}_{e}

$$\mathbf{B} = a_s \mathbf{B}_s + a_e \mathbf{B}_e \circ \mathbf{C}, \qquad a_s = 1 - a_e$$

- Term C is localization for the ensemble
- Terms a_s and a_e can be tuned to determine how much \mathbf{B}_s and \mathbf{B}_e are weighted
- This form is difficult to implement for a large NWP model
 - Most systems use "extended control variables"

Hybrid formulation used in WRFDA (Lorenc, 2003)

• Ensemble covariance is included in the 3DVAR cost function through augmentation of control variables $\alpha_i (M \times 1)$

$$J(\mathbf{x}, \alpha) = \beta_s \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^{\mathrm{T}} \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \beta_e \frac{1}{2} \sum_{i=1}^{\mathrm{N}} \alpha_i^{\mathrm{T}} \mathbf{C}^{-1} \alpha_i$$
$$+ \frac{1}{2} [\mathbf{y} - H(\mathbf{x} + \mathbf{x}_e)]^{\mathrm{T}} \mathbf{R}^{-1} [\mathbf{y} - H(\mathbf{x} + \mathbf{x}_e)]$$

 $\mathbf{x}_{e}^{'} = \sum_{i=1}^{N} \alpha_{i} \circ \mathbf{x}_{i}^{'}$, where $\mathbf{x}_{i}^{'}$ is the ensemble perturbation for the ensemble member i.

• denote element - wise product. α_i is in effect the ensemble weight.

C: correlation matrix (effectively loclization of ensemble perturbations)

• More simply: $J(\mathbf{x}, \alpha) = J_b + J_e + J_o$

• β_s and $\beta_e (1/\beta_s + 1/\beta_e = 1)$ can be tuned to have different weight between static and ensemble part

Single observation tests

• Potential temperature increment, 21st model level



Meaning of localization

- Localization defines the extent to which an observation can produce an analysis increment
- In this example, 100% of the BECs are from ensemble



Advantages of Hybrid DA

- Hybrid localization is in model space while EnKF localization is usually in observation space
- For some observation types (e.g., radiances), localization is not well defined in observation space
- Easier to make use of existing radiance VarBC in hybrid
- For small ensembles, use of static **B** could be beneficial to have a higher-rank covariance.

Sample results

- Example over North America at coarse grid spacing
- Similar results have been obtained by many studies



From Wang et al. (2008)

Hybrid vs. 3DVAR and EnKF

• Fractions skill scores for rainfall (higher is better)



Typhoon example

• Mean tropical cyclone track errors



Dual-Resolution hybrid (V3.6)

Schwartz et al. (2015; MWR)



Hybrid analysis on 15-km grid but with ensemble perturbation input from 45-km grid

Intermediate domain

• WRFDA directly reads in d01 ensembles, then cuts to d02 size (making use of WRF model nest namelist setting)





Impact of dual-resolution

• Mean tropical cyclone track errors



Impact of dual-resolution

(b) 98th percentile (a) 97th percentile (c) 99th percentile 0.60 0.60 0.60 SS 0.40 0.40 0.40 Fractions skill • score (FSS) 0.20 0.20 0.20 aggregated 5 25 50 75 100 125 150 over the first 12 25 75 100 125 150 50 5 25 50 75 100 125 150 5 forecast hours (d) 99.25th percentile (e) 99.5th percentile (f) 99.75th percentile and 55 4-km 0.60 0.60 0.60 forecasts SS 0.40 0.40 0.40 0.20 0.20 0.20 25 50 75 100 125 150 5 50 75 100 125 150 25 50 75 100 125 150 5 25 5 Radius of Influence (km) Radius of Influence (km) Radius of Influence (km) EnKF 3DVAR 20-km Hybrid 4-km GFS 3DVAR 4-km Hybrid 20-km

Hybrid practice

- Computation steps:
 - Compute ensemble mean (gen_be_ensmean.exe)
 - Extract ensemble perturbations (gen_be_ep2.exe)
 - Run WRFDA in "hybrid" mode (da_wrfvar.exe)
 - Display results for: ens_mean, std_dev, ensemble perturbations, hybrid increments, cost function
 - If time permits, play with different namelist settings: "je_factor" and "alpha_corr_scale"
- Scripts to use:
 - Some NCL scripts to display results
- Ensemble generation part not included in current practice

Namelist for WRFDA in hybrid mode

&wrfvar7 je_factor=2, # half/half for ensemble and static B weightings (tunable parameter) &wrfvar16 # ensemble part is in model space (u,v,t,q,ps)alphacv_method=2, ensdim_alpha=10, # ensemble size alpha_corr_type=3, # 1=Exponential; 2=SOAR; 3=Gaussian alpha_corr_scale=750., # correlation scale in km (tunable parameter) alpha_std_dev=1.,

alpha_vertloc=true, (use program "gen_be_vertloc.exe 42" to generate file)

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